
Deep content-based music recommendation

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Abstract

Automatic music recommendation has become an increasingly relevant problem in recent years, since a lot of music is now sold and consumed digitally. Most recommender systems rely on collaborative filtering. However, this approach suffers from the cold start problem: it fails when no usage data is available, so it is not effective for recommending new and unpopular songs. In this paper, we propose to use a latent factor model for recommendation, and predict the latent factors from music audio when they cannot be obtained from usage data. We compare a traditional approach using a bag-of-words representation of the audio signals with deep convolutional neural networks, and evaluate the predictions quantitatively and qualitatively on the Million Song Dataset. We show that using predicted latent factors produces sensible recommendations, despite the fact that there is a large semantic gap between the characteristics of a song that affect user preference and the corresponding audio signal. We also show that recent advances in deep learning translate very well to the music recommendation setting, with deep convolutional neural networks significantly outperforming the traditional approach.

1 Introduction

In recent years, the music industry has shifted more and more towards digital distribution through online music stores and streaming services such as iTunes, Spotify, Grooveshark and Google Play. As a result, automatic music recommendation has become an increasingly relevant problem: it allows listeners to discover new music that matches their tastes, and enables online music stores to target their wares to the right audience.

Although recommender systems have been studied extensively, the problem of music recommendation in particular is complicated by the sheer variety of different styles and genres, as well as social and geographic factors that influence listener preferences. The number of different items that can be recommended is very large, especially when recommending individual songs. This number can be reduced by recommending albums or artists instead, but this is not always compatible with the intended use of the system (e.g. automatic playlist generation), and it disregards the fact that the repertoire of an artist is rarely homogenous: listeners may enjoy particular songs more than others.

Many recommender systems rely on usage patterns: the combinations of items that users have consumed or rated provide information about the users' preferences, and how the items relate to each other. This is the *collaborative filtering* approach. Another approach is to predict user preferences from item content and metadata.

The consensus is that collaborative filtering will generally outperform content-based recommendation [1]. However, it is only applicable when usage data is available. Collaborative filtering suffers from the *cold start problem*: new items that have not been consumed before cannot be recommended. Additionally, items that are only of interest to a niche audience are more difficult to recommend because usage data is scarce. In many domains, and especially in music, they comprise the majority of

	Artists with positive values	Artists with negative values
1	Justin Bieber, Alicia Keys, Maroon 5, John Mayer, Michael Bublé	The Kills, Interpol, Man Man, Beirut, the bird and the bee
2	Bonobo, Flying Lotus, Cut Copy, Chromeo, Boys Noize	Shinedown, Rise Against, Avenged Sevenfold, Nickelback, Flyleaf
3	Phoenix, Crystal Castles, Muse, Röyksopp, Paramore	Traveling Wilburys, Cat Stevens, Creedence Clearwater Revival, Van Halen, The Police

Table 1: Artists whose tracks have very positive and very negative values for three latent factors. The factors seem to discriminate between different styles, such as indie rock, electronic music and classic rock.

the available items, because the users’ consumption patterns follow a power law [2]. Content-based recommendation is not affected by these issues.

1.1 Content-based music recommendation

Music can be recommended based on available metadata: information such as the artist, album and year of release is usually known. Unfortunately this will lead to predictable recommendations. For example, recommending songs by artists that the user is known to enjoy is not particularly useful.

One can also attempt to recommend music that is perceptually similar to what the user has previously listened to, by measuring the similarity between audio signals [3, 4]. This approach requires the definition of a suitable similarity metric. Such metrics are often defined ad hoc, based on prior knowledge about music audio, and as a result they are not necessarily optimal for the task of music recommendation. Because of this, some researchers have used user preference data to tune similarity metrics [5, 6].

1.2 Collaborative filtering

Collaborative filtering methods can be neighborhood-based or model-based [7]. The former methods rely on a similarity measure between users or items: they recommend items consumed by other users with similar preferences, or similar items to the ones that the user has already consumed. Model-based methods on the other hand attempt to model latent characteristics of the users and items, which are usually represented as vectors of latent factors. Latent factor models have been very popular ever since their effectiveness was demonstrated for movie recommendation in the Netflix Prize [8].

1.3 The semantic gap in music

Latent factor vectors form a compact description of the different facets of users’ tastes, and the corresponding characteristics of the items. To demonstrate this, we computed latent factors for a small set of usage data, and listed some artists whose songs have very positive and very negative values for each factor in Table 1. This representation is quite versatile and can be used for other applications besides recommendation, as we will show later (see Section 5.1). Since usage data is scarce for many songs, it is often impossible to reliably estimate these factor vectors. Therefore it would be useful to be able to predict them from music audio content.

There is a large *semantic gap* between the characteristics of a song that affect user preference, and the corresponding audio signal. Extracting high-level properties such as genre, mood, instrumentation and lyrical themes from audio signals requires powerful models that are capable of capturing the complex hierarchical structure of music. Additionally, some properties are impossible to obtain from audio signals alone, such as the popularity of the artist, their reputation and their location.

Researchers in the domain of *music information retrieval* (MIR) concern themselves with extracting these high-level properties from music. They have grown to rely on a particular set of engineered audio features, such as mel-frequency cepstral coefficients (MFCCs), which are used as input to simple classifiers or regressors, such as SVMs and linear regression [9]. Recently this traditional approach has been challenged by some authors who have applied deep neural networks to MIR problems [10, 11, 12].

In this paper, we strive to bridge the semantic gap in music by training deep convolutional neural networks to predict latent factors from music audio. We evaluate our approach on an industrial-scale dataset with audio excerpts of over 380,000 songs, and compare it with a more conventional approach using a bag-of-words feature representation for each song. We assess to what extent it is possible to extract characteristics that affect user preference directly from audio signals, and evaluate the predictions from our models in a music recommendation setting.

2 The dataset

The Million Song Dataset (MSD) [13] is a collection of metadata and precomputed audio features for one million contemporary songs. Several other datasets linked to the MSD are also available, featuring lyrics, cover songs, tags and user listening data. This makes the dataset suitable for a wide range of different music information retrieval tasks. Two linked datasets are of interest for our experiments:

- The Echo Nest Taste Profile Subset provides play counts for over 380,000 songs in the MSD, gathered from 1 million users. The dataset was used in the Million Song Dataset challenge [14] last year.
- The Last.fm dataset provides tags for over 500,000 songs.

Traditionally, research in music information retrieval (MIR) on large-scale datasets was limited to industry, because large collections of music audio cannot be published easily due to licensing issues. The authors of the MSD circumvented these issues by providing precomputed features instead of raw audio. Unfortunately, the audio features provided with the MSD are of limited use, and the process by which they were obtained is not very well documented. The feature set was extended by Rauber et al. [15], but the absence of raw audio data, or at least a mid-level representation, is still an issue. However, we were able to attain 29 second audio clips for over 99% of the dataset from 7digital.com.

Due to its size, the MSD allows for the music recommendation problem to be studied in a more realistic setting than was previously possible. It is also worth noting that the Taste Profile Subset is one of the largest collaborative filtering datasets that are publicly available today.

3 Weighted matrix factorization

The Taste Profile Subset contains play counts per song and per user, which is a form of *implicit feedback*. We know how many times the users have listened to each of the songs in the dataset, but they have not explicitly rated them. However, we can assume that users will probably listen to songs more often if they enjoy them. If a user has never listened to a song, this can have many causes: for example, they might not be aware of it, or they might expect not to enjoy it. This setting is not compatible with traditional matrix factorization algorithms, which are aimed at predicting ratings.

We used the *weighted matrix factorization* (WMF) algorithm, proposed by Hu et al. [16], to learn latent factor representations of all users and items in the Taste Profile Subset. This is a modified matrix factorization algorithm aimed at implicit feedback datasets. Let r_{ui} be the play count for user u and song i . For each user-item pair, we define a preference variable p_{ui} and a confidence variable c_{ui} ($I(x)$ is the indicator function, α and ϵ are hyperparameters):

$$p_{ui} = I(r_{ui} > 0), \quad (1)$$

$$c_{ui} = 1 + \alpha \log(1 + \epsilon^{-1} r_{ui}). \quad (2)$$

The preference variable indicates whether user u has ever listened to song i . If it is 1, we will assume the user enjoys the song. The confidence variable measures how certain we are about this particular preference. It is a function of the play count, because songs with higher play counts are more likely to be preferred. If the song has never been played, the confidence variable will have a low value, because this is the least informative case.

The WMF objective function is given by:

$$\min_{x_*, y_*} \sum_{u, i} c_{ui} (p_{ui} - x_u^T y_i)^2 + \lambda \left(\sum_u \|x_u\|^2 + \sum_i \|y_i\|^2 \right), \quad (3)$$

where λ is a regularization parameter, x_u is the latent factor vector for user u , and y_i is the latent factor vector for song i . It consists of a confidence-weighted mean squared error term and an L2 regularization term. Note that the first sum ranges over all users and all songs: contrary to matrix factorization for rating prediction, where terms corresponding to user-item combinations for which no rating is available can be discarded, we have to take all possible combinations into account. As a result, using stochastic gradient descent for optimization is not practical for a dataset of this size. Hu et al. propose an efficient alternating least squares (ALS) optimization method, which we used instead.

4 Predicting latent factors from music audio

Predicting latent factors for a given song from the corresponding audio signal is a regression problem. It requires learning a function that maps a time series to a vector of real numbers. We evaluate two methods to achieve this: one follows the conventional approach in MIR by extracting local features from audio signals and aggregating them into a bag-of-words (BoW) representation. Any traditional regression technique can then be used to map this feature representation to the factors. The other method is to use a deep convolutional network.

Latent factor vectors obtained by applying WMF to the available usage data are used as ground truth to train the prediction models. It should be noted that this approach is compatible with any type of latent factor model that is suitable for large implicit feedback datasets. We chose to use WMF because an efficient optimization procedure exists for it.

4.1 Bag-of-words representation

Many MIR systems rely on the following feature extraction pipeline to convert music audio signals into a fixed-size representation that can be used as input to a classifier or regressor [5, 17, 18, 19, 20]:

- **Extract MFCCs from the audio signals.** We computed 13 MFCCs from windows of 1024 audio frames, corresponding to 23 ms at a sampling rate of 22050 Hz, and a hop size of 512 samples. We also computed first and second order differences, yielding 39 coefficients in total.
- **Vector quantize the MFCCs.** We learned a dictionary of 4000 elements with the K-means algorithm and assigned all MFCC vectors to the closest mean.
- **Aggregate them into a bag-of-words representation.** For every song, we counted how many times each mean was selected. The resulting vector of counts is a bag-of-words feature representation of the song.

We then reduced the size of this representation using PCA (we kept enough components to retain 95% of the variance) and used linear regression and a multilayer perceptron with 1000 hidden units on top of this to predict latent factors. We also used it as input for the metric learning to rank (MLR) algorithm [21], to learn a similarity metric for content-based recommendation. This was used as a baseline for our music recommendation experiments, which are described in Section 5.2.

4.2 Convolutional neural networks

Convolutional neural networks (CNNs) have recently been used to improve on the state of the art in speech recognition and large-scale image classification by a large margin [22, 23]. Three ingredients seem to be central to the success of this approach:

- Using rectified linear units (ReLUs) [24] instead of sigmoid nonlinearities leads to faster convergence and reduces the vanishing gradient problem that plagues traditional neural networks with many layers.
- Parallelization is used to speed up training, so that larger models can be trained in a reasonable amount of time. We used the Theano library [25] to take advantage of GPU acceleration.

- A large amount of training data is required to be able to fit large models with many parameters. The MSD contains enough training data to be able to train large models effectively.

We have also evaluated the use of dropout regularization [26], but this did not yield any significant improvements.

We first extracted an intermediate time-frequency representation from the audio signals to use as input to the network. We used log-compressed mel-spectrograms with 128 components and the same window size and hop size that we used for the MFCCs (1024 and 512 audio frames respectively). The networks were trained on windows of 3 seconds sampled randomly from the audio clips. This was done primarily to speed up training. To predict the latent factors for an entire clip, we averaged over the predictions for consecutive windows.

Convolutional neural networks are especially suited for predicting latent factors from music audio, because they allow for intermediate features to be shared between different factors, and because their hierarchical structure consisting of alternating feature extraction layers and pooling layers allows them to operate on multiple timescales.

4.3 Objective functions

Latent factor vectors are real-valued, so the most straightforward objective is to minimize the mean squared error (MSE) of the predictions. Alternatively, we can also continue to minimize the weighted prediction error (WPE) from the WMF objective function. Let y_i be the latent factor vector for song i , obtained with WMF, and y'_i the corresponding prediction by the model. The objective functions are then (θ represents the model parameters):

$$\min_{\theta} \sum_i \|y_i - y'_i\|^2, \quad (4) \quad \min_{\theta} \sum_{u,i} c_{ui} (p_{ui} - x_u^T y'_i)^2. \quad (5)$$

5 Experiments

5.1 Versatility of the latent factor representation

To demonstrate the versatility of the latent factor vectors, we compared them with audio features in a tag prediction task. Tags can describe a wide range of different aspects of the songs, such as genre, instrumentation, tempo, mood and year of release.

We ran WMF to obtain 50-dimensional latent factor vectors for all 9,330 songs in the subset, and trained a logistic regression model to predict the 50 most popular tags from the Last.fm dataset for each song. We also trained a logistic regression model on a bag-of-words representation of the audio signals, which was first reduced in size using PCA (see Section 4.1). We used 10-fold cross-validation and computed the average area under the ROC curve (AUC) across all tags. This resulted in an average AUC of **0.69365** for audio-based prediction, and **0.86703** for prediction based on the latent factor vectors.

5.2 Latent factor prediction: quantitative evaluation

To assess quantitatively how well we can predict latent factors from music audio, we used the predictions from our models for music recommendation. For every user u and for every song i in the test set, we computed the score $x_u^T y_i$, and recommended the songs with the highest scores first. As mentioned before, we also learned a song similarity metric on the bag-of-words representation using metric learning to rank. In this case, scores for a given user are computed by averaging similarity scores across all the songs that the user has listened to.

The following models were used to predict latent factor vectors:

- Linear regression trained on the bag-of-words representation described in Section 4.1.
- A multi-layer perceptron (MLP) trained on the same bag-of-words representation.
- A convolutional neural network trained on log-scaled mel-spectrograms to minimize the mean squared error (MSE) of the predictions.

- The same convolutional neural network, trained to minimize the weighted prediction error (WPE) from the WMF objective instead.

For our initial experiments, we used a subset of the dataset containing only the 9,330 most popular songs, and listening data for only 20,000 users. We used 1,881 songs for testing. For the other experiments, we used all available data: we used all songs that we have usage data for and that we were able to download an audio clip for (382,410 songs and 1 million users in total, 46,728 songs were used for testing).

Model	mAP	AUC
MLR	0.01801	0.60608
linear regression	0.02389	0.63518
MLP	0.02536	0.64611
CNN with MSE	0.05016	0.70987
CNN with WPE	0.04323	0.70101

We report the mean average precision (mAP, cut off at 500 recommendations per user) and the area under the ROC curve (AUC) of the predictions. We evaluated all models on the subset, using latent factor vectors with 50 dimensions. We compared the convolutional neural network with linear regression on the bag-of-words representation on the full dataset as well, using latent factor vectors with 400 dimensions. Results are shown in Tables 2 and 3 respectively.

Table 2: Results for all considered models on a subset of the dataset containing only the 9,330 most popular songs, and listening data for 20,000 users.

On the subset, predicting the latent factors seems to outperform the metric learning approach. Using an MLP instead of linear regression results in a slight improvement, but the limitation here is clearly the bag-of-words feature representation. Using a convolutional neural network results in another large increase in performance. Most likely this is because the bag-of-words representation does not reflect any kind of temporal structure.

Interestingly, the WPE objective does not result in improved performance. Presumably this is because the weighting causes the importance of the songs to be proportional to their popularity. In other words, the model will be encouraged to predict latent factor vectors for popular songs from the training set very well, at the expense of all other songs.

On the full dataset, the difference between the bag-of-words approach and the convolutional neural network is much more pronounced. Note that we did not train an MLP on this dataset due to the small difference in performance with linear regression on the subset. We also included results for when the latent factor vectors are obtained from usage data. This is an upper bound to what is achievable when predicting them from content. There is a large gap between our best result and this theoretical maximum, but this is to be expected: as we mentioned before, many aspects of the songs that influence user preference cannot possibly be extracted from audio signals only. In particular, we are unable to predict the popularity of the songs, which considerably affects the AUC and mAP scores.

Model	mAP	AUC
random	0.00015	0.49935
linear regression	0.00101	0.64522
CNN with MSE	0.00672	0.77192
upper bound	0.23278	0.96070

Table 3: Results for linear regression on a bag-of-words representation of the audio signals, and a convolutional neural network trained with the MSE objective, on the full dataset (382,410 songs and 1 million users). Also shown are the scores achieved when the latent factor vectors are randomized, and when they are learned from usage data using WMF (upper bound).

5.3 Latent factor prediction: qualitative evaluation

Evaluating recommender systems is a complex matter, and accuracy metrics by themselves do not provide enough insight into whether the recommendations are sound. To establish this, we also performed some qualitative experiments on the subset. For each song, we searched for similar songs by measuring the cosine similarity between the predicted usage patterns. We compared the usage patterns predicted using the latent factors obtained with WMF (50 dimensions), with those using latent factors predicted with a convolutional neural network. A few songs and their closest matches according to both models are shown in Table 4. When the predicted latent factors are used, the matches are mostly different, but the results are quite reasonable in the sense that the matched songs are likely to appeal to the same audience. Furthermore, they seem to be a bit more varied, which is a useful property for recommender systems.

Wang et al. [28] extend probabilistic matrix factorization (PMF) [29] with a topic model prior on the latent factor vectors of the items, and apply this model to scientific article recommendation. Topic proportions obtained from the content of the articles are used instead of latent factors when no usage data is available. The entire system is trained jointly, allowing the topic model and the latent space learned by matrix factorization to adapt to each other. Our approach is sequential instead: we first obtain latent factor vectors for songs for which usage data is available, and use these to train a regression model. Because we reduce the incorporation of content information to a regression problem, we are able to use a deep convolutional network.

McFee et al. [5] define an artist-level content-based similarity measure for music learned from a sample of collaborative filter data using metric learning to rank [21]. They use a variation on the typical bag-of-words approach for audio feature extraction (see section 4.1). Their results corroborate that relying on usage data to train the model improves content-based recommendations. For audio data they used the CAL10K dataset, which consists of 10,832 songs, so it is comparable in size to the subset of the MSD that we used for our initial experiments.

Weston et al. [17] investigate the problem of recommending items to a user given another item as a query, which they call ‘collaborative retrieval’. They optimize an item scoring function using a ranking loss and describe a variant of their method that allows for content features to be incorporated. They also use the bag-of-words approach to extract audio features and evaluate this method on a large proprietary dataset. They find that combining collaborative filtering and content-based information does not improve the accuracy of the recommendations over collaborative filtering alone.

Both McFee et al. and Weston et al. optimized their models using a ranking loss. We have opted to use quadratic loss functions instead, because we found their optimization to be more easily scalable. Using a ranking loss instead is an interesting direction of future research, although we suspect that this approach may suffer from the same problems as the WPE objective (i.e. popular songs will have an unfair advantage).

7 Conclusion

In this paper, we have investigated the use of deep convolutional neural networks to predict latent factors from music audio when they cannot be obtained from usage data. We evaluated the predictions by using them for music recommendation on an industrial-scale dataset. Even though a lot of characteristics of songs that affect user preference cannot be predicted from audio signals, the resulting recommendations seem to be sensible. We can conclude that predicting latent factors from music audio is a viable method for recommending new and unpopular music.

We also showed that recent advances in deep learning translate very well to the music recommendation setting in combination with this approach, with deep convolutional neural networks significantly outperforming a more traditional approach using bag-of-words representations of audio signals. This bag-of-words representation is used very often in MIR, and our results indicate that a lot of research in this domain could benefit significantly from using deep neural networks.

References

- [1] M. Slaney. Web-scale multimedia analysis: Does content matter? *MultiMedia, IEEE*, 18(2):12–15, 2011.
- [2] Ò. Celma. *Music Recommendation and Discovery in the Long Tail*. PhD thesis, Universitat Pompeu Fabra, Barcelona, 2008.
- [3] Malcolm Slaney, Kilian Q. Weinberger, and William White. Learning a metric for music similarity. In *Proceedings of the 9th International Conference on Music Information Retrieval (ISMIR)*, 2008.
- [4] Jan Schlüter and Christian Osendorfer. Music Similarity Estimation with the Mean-Covariance Restricted Boltzmann Machine. In *Proceedings of the 10th International Conference on Machine Learning and Applications (ICMLA)*, 2011.
- [5] Brian McFee, Luke Barrington, and Gert R. G. Lanckriet. Learning content similarity for music recommendation. *IEEE Transactions on Audio, Speech & Language Processing*, 20(8), 2012.
- [6] Richard Stenzel and Thomas Kamps. Improving Content-Based Similarity Measures by Training a Collaborative Model. pages 264–271, London, UK, September 2005. University of London.

- [7] Francesco Ricci, Lior Rokach, Bracha Shapira, and Paul B. Kantor, editors. *Recommender Systems Handbook*. Springer, 2011.
- [8] James Bennett and Stan Lanning. The netflix prize. In *Proceedings of KDD cup and workshop*, volume 2007, page 35, 2007.
- [9] Eric J. Humphrey, Juan P. Bello, and Yann LeCun. Moving beyond feature design: Deep architectures and automatic feature learning in music informatics. In *Proceedings of the 13th International Conference on Music Information Retrieval (ISMIR)*, 2012.
- [10] Philippe Hamel and Douglas Eck. Learning features from music audio with deep belief networks. In *Proceedings of the 11th International Conference on Music Information Retrieval (ISMIR)*, 2010.
- [11] Honglak Lee, Peter Pham, Yan Largman, and Andrew Ng. Unsupervised feature learning for audio classification using convolutional deep belief networks. In *Advances in Neural Information Processing Systems 22*, 2009.
- [12] Sander Dieleman, Philémon Brakel, and Benjamin Schrauwen. Audio-based music classification with a pretrained convolutional network. In *Proceedings of the 12th International Conference on Music Information Retrieval (ISMIR)*, 2011.
- [13] Thierry Bertin-Mahieux, Daniel P.W. Ellis, Brian Whitman, and Paul Lamere. The million song dataset. In *Proceedings of the 11th International Conference on Music Information Retrieval (ISMIR)*, 2011.
- [14] Brian McFee, Thierry Bertin-Mahieux, Daniel P.W. Ellis, and Gert R.G. Lanckriet. The million song dataset challenge. In *Proceedings of the 21st international conference companion on World Wide Web*, 2012.
- [15] Andreas Rauber, Alexander Schindler, and Rudolf Mayer. Facilitating comprehensive benchmarking experiments on the million song dataset. In *Proceedings of the 13th International Conference on Music Information Retrieval (ISMIR)*, 2012.
- [16] Yifan Hu, Yehuda Koren, and Chris Volinsky. Collaborative filtering for implicit feedback datasets. In *Proceedings of the 2008 Eighth IEEE International Conference on Data Mining*, 2008.
- [17] Jason Weston, Chong Wang, Ron Weiss, and Adam Berenzweig. Latent collaborative retrieval. In *Proceedings of the 29th international conference on Machine learning*, 2012.
- [18] Jason Weston, Samy Bengio, and Philippe Hamel. Large-scale music annotation and retrieval: Learning to rank in joint semantic spaces. *Journal of New Music Research*, 2011.
- [19] Jonathan T Foote. Content-based retrieval of music and audio. In *Voice, Video, and Data Communications*, pages 138–147. International Society for Optics and Photonics, 1997.
- [20] Matthew Hoffman, David Blei, and Perry Cook. Easy As CBA: A Simple Probabilistic Model for Tagging Music. In *Proceedings of the 10th International Conference on Music Information Retrieval (ISMIR)*, 2009.
- [21] Brian McFee and Gert R. G. Lanckriet. Metric learning to rank. In *Proceedings of the 27th International Conference on Machine Learning*, 2010.
- [22] Geoffrey Hinton, Li Deng, Dong Yu, George E Dahl, Abdel-rahman Mohamed, Navdeep Jaitly, Andrew Senior, Vincent Vanhoucke, Patrick Nguyen, Tara N Sainath, et al. Deep neural networks for acoustic modeling in speech recognition: the shared views of four research groups. *Signal Processing Magazine, IEEE*, 29(6):82–97, 2012.
- [23] A. Krizhevsky, I. Sutskever, and G. E. Hinton. Imagenet classification with deep convolutional neural networks. In *Advances in Neural Information Processing Systems 25*, 2012.
- [24] Vinod Nair and Geoffrey E. Hinton. Rectified linear units improve restricted boltzmann machines. In *Proceedings of the 27th International Conference on Machine Learning (ICML-10)*, 2010.
- [25] James Bergstra, Olivier Breuleux, Frédéric Bastien, Pascal Lamblin, Razvan Pascanu, Guillaume Desjardins, Joseph Turian, David Warde-Farley, and Yoshua Bengio. Theano: a CPU and GPU math expression compiler. In *Proceedings of the Python for Scientific Computing Conference (SciPy)*, June 2010.
- [26] G. E. Hinton, N. Srivastava, A. Krizhevsky, I. Sutskever, and R. R. Salakhutdinov. Improving neural networks by preventing co-adaptation of feature detectors. Technical report, University of Toronto, 2012.
- [27] Laurens Van der Maaten and Geoffrey Hinton. Visualizing data using t-sne. *Journal of Machine Learning Research*, 9(2579-2605):85, 2008.
- [28] Chong Wang and David M. Blei. Collaborative topic modeling for recommending scientific articles. In *Proceedings of the 17th ACM SIGKDD international conference on Knowledge discovery and data mining*, 2011.
- [29] Ruslan Salakhutdinov and Andriy Mnih. Probabilistic matrix factorization. In *Advances in Neural Information Processing Systems*, volume 20, 2008.