



Lecture 4

Higher - order functions
Asserts



Some slides were borrowed from John DeNero

Midterm Date

A: Week 5, Thursday

B: Week 6, Tuesday

C: Does not matter

Overall idea

- **Want:** is the ability to build **abstractions** by assigning names to common patterns and then to work in terms of the names directly.
- **Need:** to construct functions that can *accept* other functions as arguments or *return* functions as values.
- Functions that manipulate functions are called *higher-order* functions.

Nested Definitions (demo)



```
def make_adder(n) :  
    def adder(k) :  
        return k + n  
    return adder
```

```
add3 = make_adder(3)  
print(add3(9))
```

What will be printed?

A: 3

B: 9

C: 12

D: It does not make sense

Locally defined functions

Functions defined *within other function* bodies are bound to names in a *local frame*.

A function that
returns a function

```
def make_adder(n):  
    """Return a function that takes one argument k and returns k + n.  
  
    >>> add_three = make_adder(3)  
    >>> add_three(4)  
    7  
    """  
    def adder(k):  
        return k + n  
    return adder
```

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    >>> add_three(4)  
    7  
    """  
    def adder(k):  
        return k + n  
    return adder
```

The name `add_three` is bound
to a function

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A function that
returns a function

```
def make_adder(n):  
    """Return a function that takes one argument k and returns k + n.
```

```
>>> add_three = make_adder(3)
```

```
>>> add_three(4)
```

```
7  
"""
```

The name `add_three` is bound
to a function

```
def adder(k):  
    return k + n  
return adder
```

A def statement within
another def statement

Locally defined functions

Functions defined *within other function* bodies are bound to names in a local frame.

A function that
returns a function

```
def make_adder(n):  
    """Return a function that takes one argument k and returns k + n.
```

```
>>> add_three = make_adder(3)  
>>> add_three(4)  
7  
"""
```

The name `add_three` is bound
to a function

```
def adder(k):  
    return k + n  
return adder
```

A `def` statement within
another `def` statement


Can refer to names in the
enclosing function

Call Expressions as Operator Expressions

```
make_adder(1) ( 2 )
```

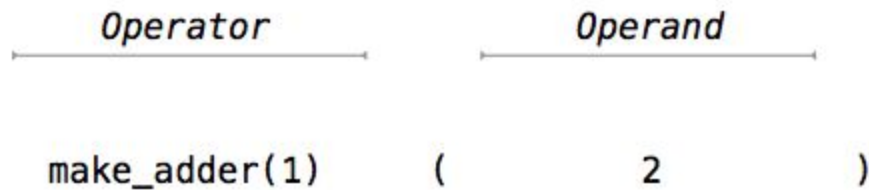
Call Expressions as Operator Expressions

Operator



`make_adder(1) (2)`

Call Expressions as Operator Expressions



Call Expressions as Operator Expressions

```
def make_adder(n):  
    def adder(k):  
        return k + n  
    return adder
```

An expression that
evaluates to a function

Operator

Operand

make_adder(1)

(

2

)

Call Expressions as Operator Expressions

```
def make_adder(n):  
    def adder(k):  
        return k + n  
    return adder
```

An expression that
evaluates to a function

Operator

An expression that
evaluates to its argument

Operand

make_adder(1)

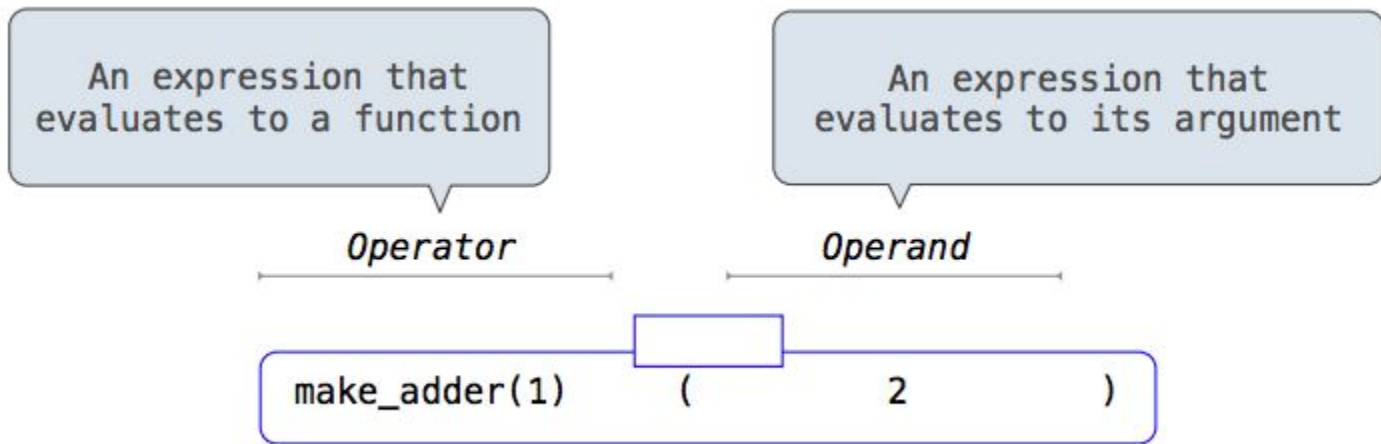
(

2

)

Call Expressions as Operator Expressions

```
def make_adder(n):  
    def adder(k):  
        return k + n  
    return adder
```



Call Expressions as Operator Expressions

```
def make_adder(n):  
    def adder(k):  
        return k + n  
    return adder
```

An expression that
evaluates to a function

An expression that
evaluates to its argument

Operator

Operand

make_adder(1)

(

2

)

make_adder(1)

Call Expressions as Operator Expressions

```
def make_adder(n):  
    def adder(k):  
        return k + n  
    return adder
```

An expression that
evaluates to a function

An expression that
evaluates to its argument

Operator

Operand

make_adder(1)

(

2

)

make_adder(1)

func make_adder(n)

Call Expressions as Operator Expressions

```
def make_adder(n):  
    def adder(k):  
        return k + n  
    return adder
```

An expression that
evaluates to a function

An expression that
evaluates to its argument

Operator

Operand

make_adder(1)

(

2

)

make_adder(1)

func make_adder(n)

1

Call Expressions as Operator Expressions

```
def make_adder(n):  
    def adder(k):  
        return k + n  
    return adder
```

An expression that
evaluates to a function

An expression that
evaluates to its argument

Operator

Operand

make_adder(1)

(

2

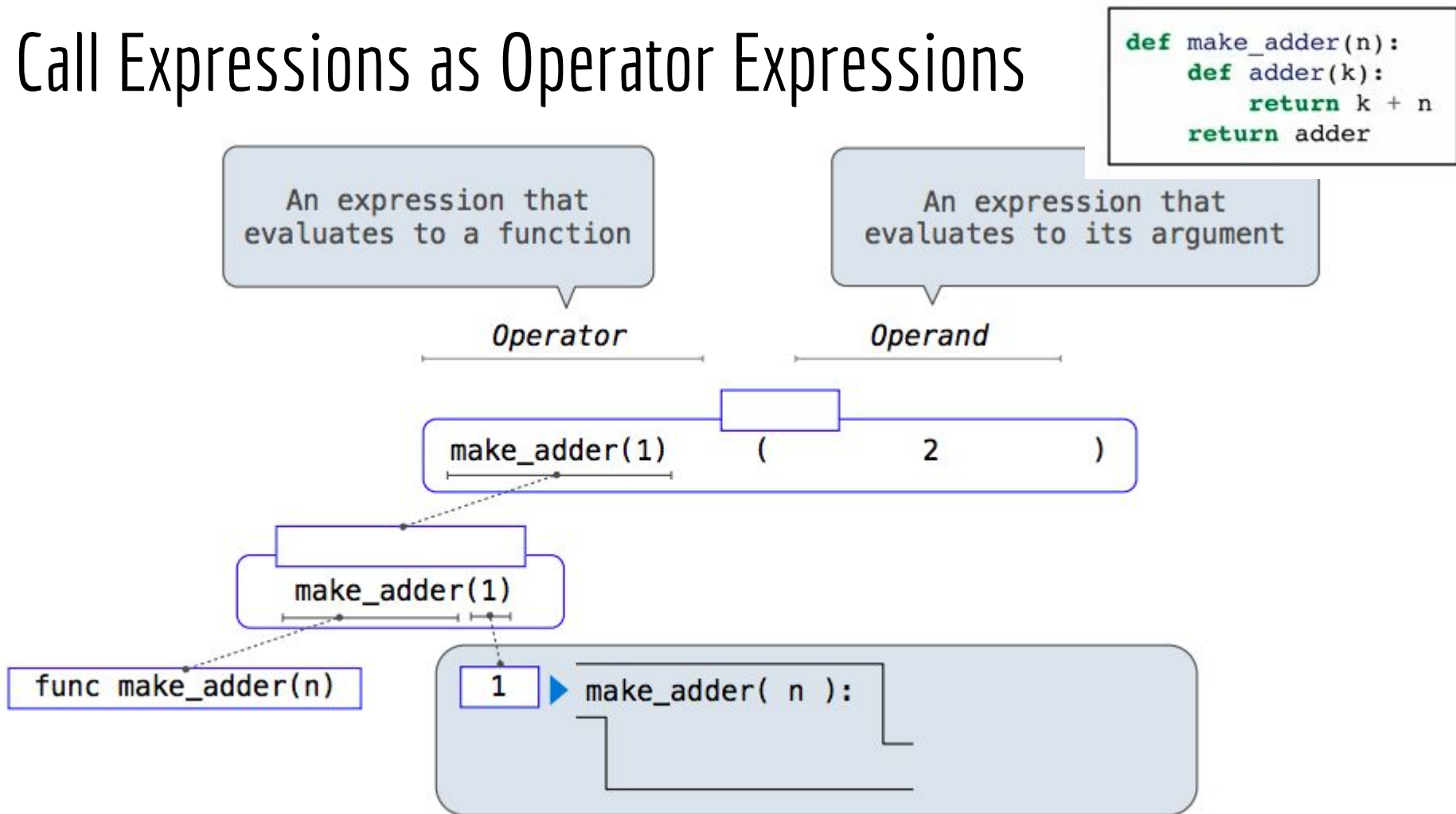
)

make_adder(1)

func make_adder(n)

1

▶ make_adder(n):



Call Expressions as Operator Expressions

```
def make_adder(n):  
    def adder(k):  
        return k + n  
    return adder
```

An expression that
evaluates to a function

An expression that
evaluates to its argument

Operator

Operand

make_adder(1)

(

2

)

make_adder(1)

func make_adder(n)

1

make_adder(n):

```
def adder(k):  
    return k + n  
return adder
```

Call Expressions as Operator Expressions

```
def make_adder(n):  
    def adder(k):  
        return k + n  
    return adder
```

An expression that
evaluates to a function

An expression that
evaluates to its argument

Operator

Operand

make_adder(1)

(

2

)

make_adder(1)

func make_adder(n)

1

▶ make_adder(n):

```
def adder(k):  
    return k + n  
return adder
```

▶ func adder(k)

Call Expressions as Operator Expressions

```
def make_adder(n):  
    def adder(k):  
        return k + n  
    return adder
```

An expression that
evaluates to a function

An expression that
evaluates to its argument

Operator

Operand

make_adder(1)

(

2

)

func adder(k)

make_adder(1)

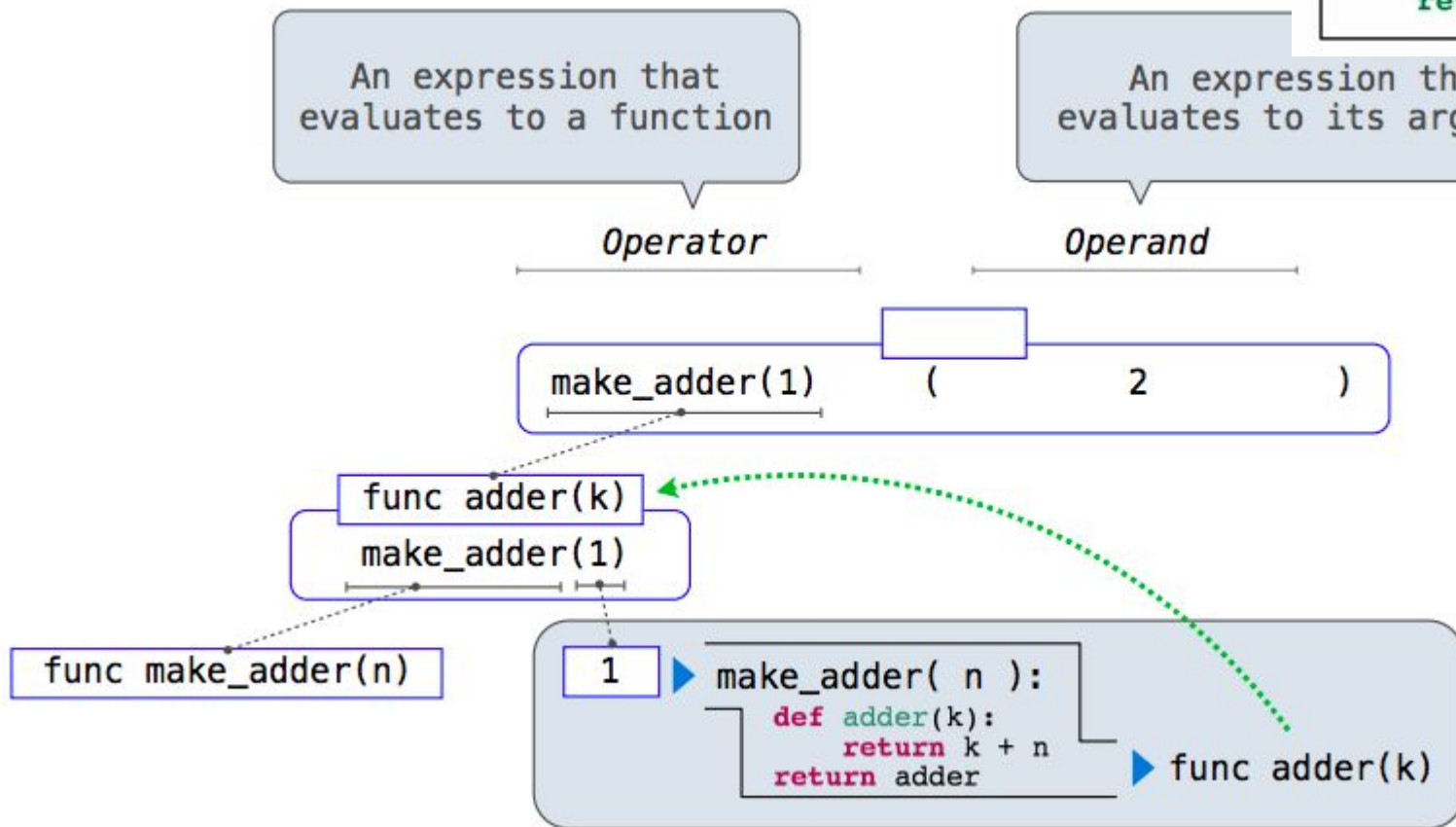
func make_adder(n)

1

make_adder(n):

```
def adder(k):  
    return k + n  
return adder
```

func adder(k)



Call Expressions as Operator Expressions

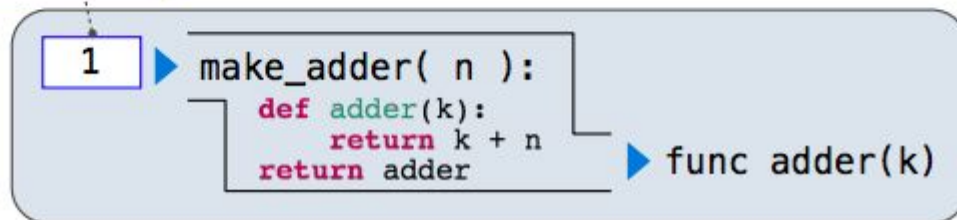
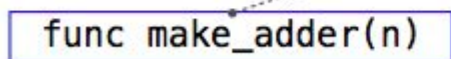
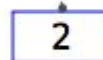
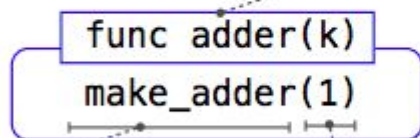
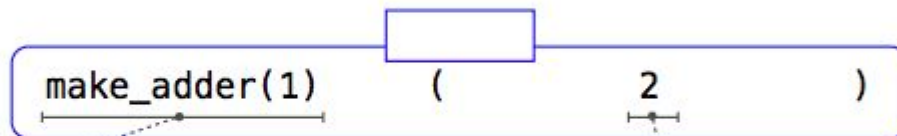
```
def make_adder(n):  
    def adder(k):  
        return k + n  
    return adder
```

An expression that
evaluates to a function

An expression that
evaluates to its argument

Operator

Operand



Call Expressions as Operator Expressions (Demo)

An expression that evaluates to a function

An expression that evaluates to its argument

Operator

Operand

```
def make_adder(n):  
    def adder(k):  
        return k + n  
    return adder
```

make_adder(1)

3

(

2

)

func adder(k)

make_adder(1)

2

func make_adder(n)

1

make_adder(n):

```
def adder(k):  
    return k + n  
return adder
```

func adder(k)

The purpose of higher-order functions

Higher-order function: A function that takes a function as an argument value or returns a function as a return value

Useful:

- Express general methods of computation
- Remove repetition from programs
- Each function has exactly one job

Environment diagrams describe how higher-order functions work!

Nested Definitions.

(Think before answering)



```
def make_multiplier_of(n):  
    def multiplier(x):  
        return x * n  
    return multiplier  
  
times3 = make_multiplier_of(3)  
print(multiplier(9))
```

What will be printed?

A: 3

B: 9

C: 27

D: It does not make sense

E: Error

Log function



```
def logger (msg) :  
  
    def log_message () :  
        print('Log: ', msg)  
  
    return log_message  
  
log_hi = logger("Hi")  
log_hi()
```

What will be printed?

A: Hi!

B: Log: Hi!

C: Log:

D: Still does not make sense

E: Error

Html_tags.

```
paragraph = html_tag('p')  
paragraph('This is long paragraph')
```

```
<p>This is long paragraph</p>
```

```
print_h1 = html_tag('h1')  
print_h1('Test Headline!')  
print_h1('Another headline!')
```

```
<h1>Test Headline!</h1>  
<h1>Another headline!</h1>
```

Html_tags. How would you write it?

```
paragraph = html_tag('p')  
paragraph('This is long paragraph')
```

```
<p>This is long paragraph</p>
```

```
print_h1 = html_tag('h1')  
print_h1('Test Headline!')  
print_h1('Another headline!')
```

```
<h1>Test Headline!</h1>  
<h1>Another headline!</h1>
```

```
>>> a = "Today"  
>>> b = "June"  
>>> print('{0} is not {1}, {1} is not {0}'.format(a,b))  
Today is not June, June is not Today
```

```
def html_tag(tag):  
    def wrap_text(msg):  
        print('<{0}>{1}</{0}>'.format(tag, msg))  
    return wrap_text
```

```
print_h1 = html_tag('h1')  
print_h1('Test Headline!')  
print_h1('Another headline!')
```

```
<h1>Test Headline!</h1>  
<h1>Another headline!</h1>
```

Question



```
def repeat(f, x):  
    while f(x) != x:  
        x = f(x)  
    return x
```

```
def g(y):  
    return (y+5)//3
```

```
result = repeat(g, 5)
```

What is the value of the *result*?

- A. 0
- B. Infinite loop
- C. 2
- D. 2.5
- E. 3



Local Names

(Local parameters of the functions have *local* scope)



Question (demo)



```
def f(x,y):  
    return g(x)
```

```
def g(a):  
    return a + y
```

```
f(1, 2)
```

What will be the output?

A: 3

B: 1

C: 2

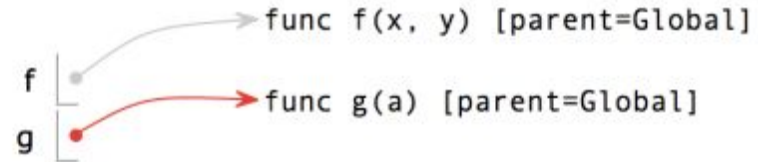
D: Error

E: None of the above

Local Names are not Visible to Other (Non-Nested) Functions

```
1 def f(x, y):  
2     return g(x)  
3  
4 def g(a):  
→ 5     return a + y  
6  
7 result = f(1, 2)
```

Global frame



f1: f [parent=Global]

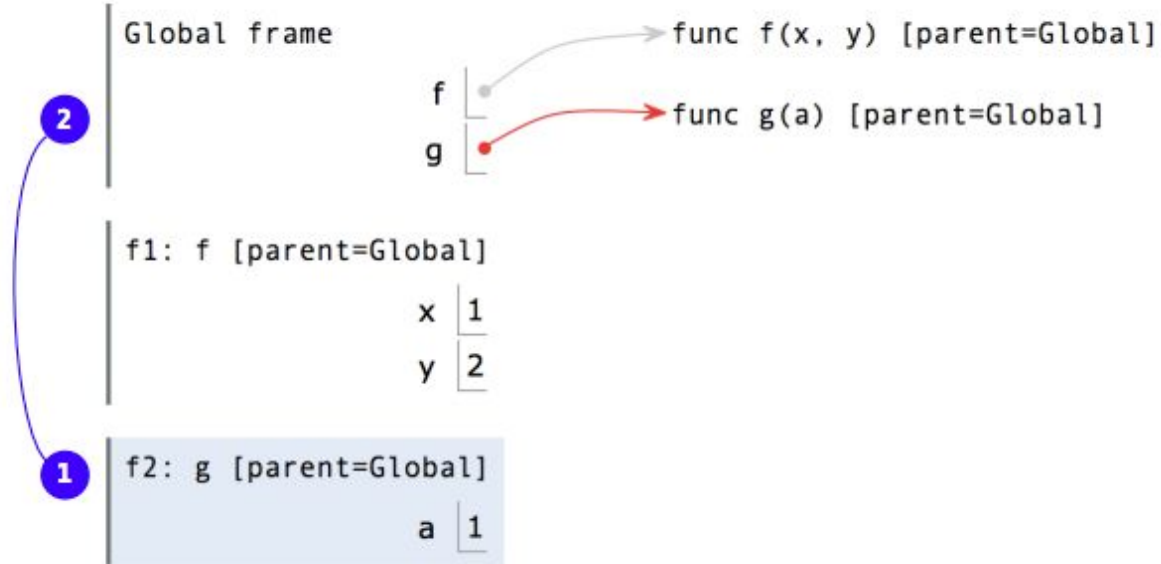
x | 1
y | 2

f2: g [parent=Global]

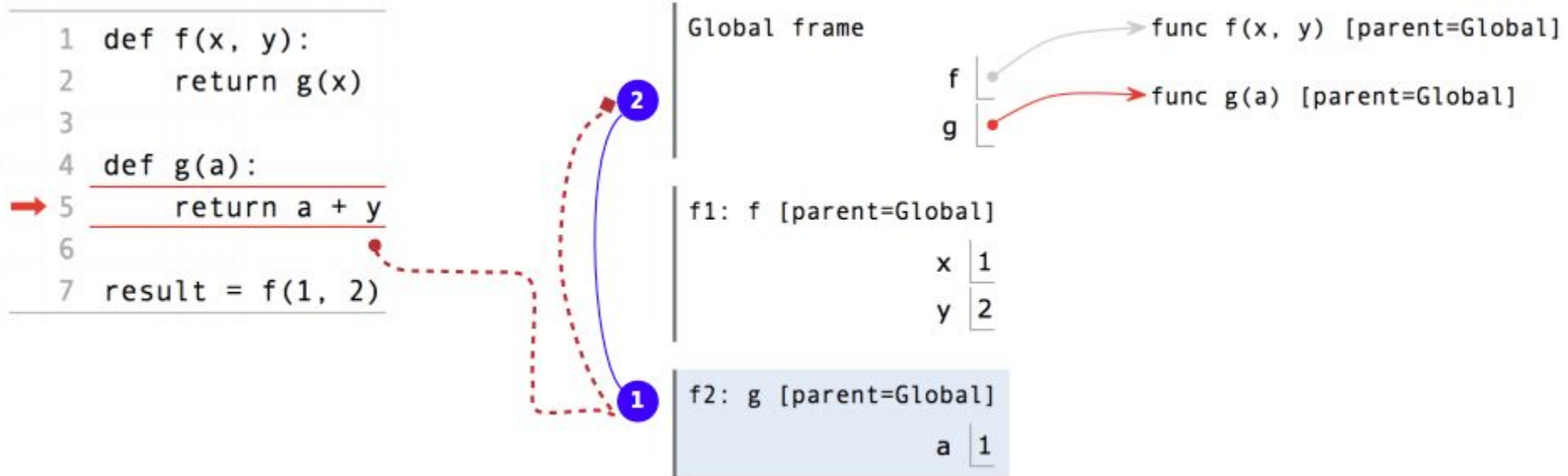
a | 1

Local Names are not Visible to Other (Non-Nested) Functions

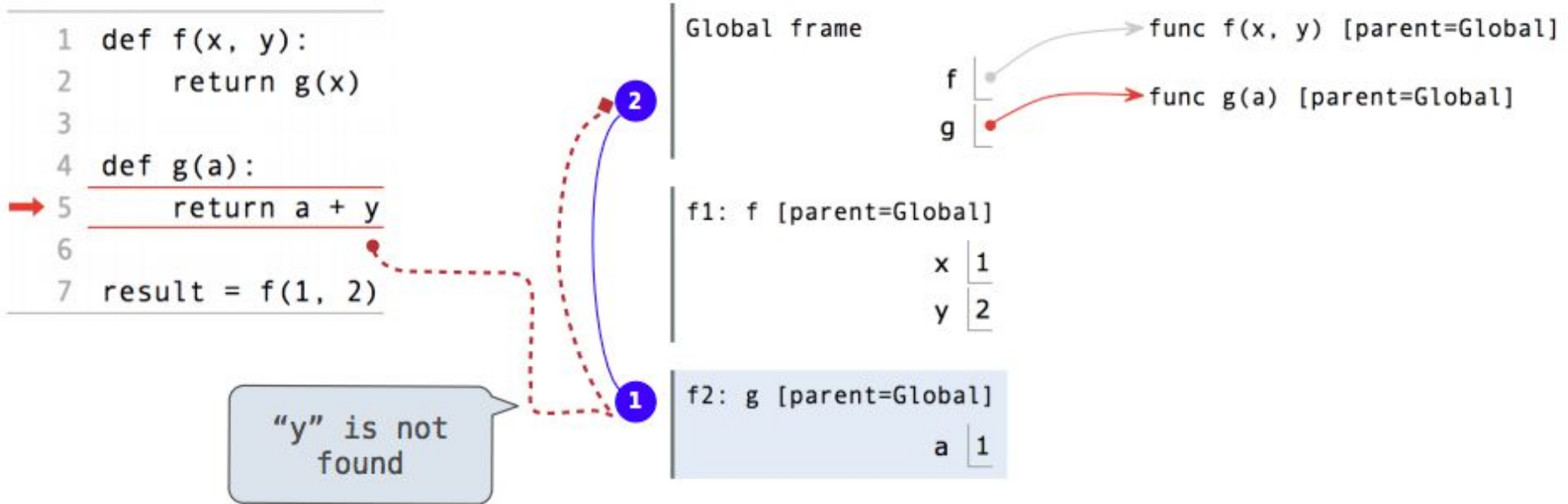
```
1 def f(x, y):  
2     return g(x)  
3  
4 def g(a):  
→ 5     return a + y  
6  
7 result = f(1, 2)
```



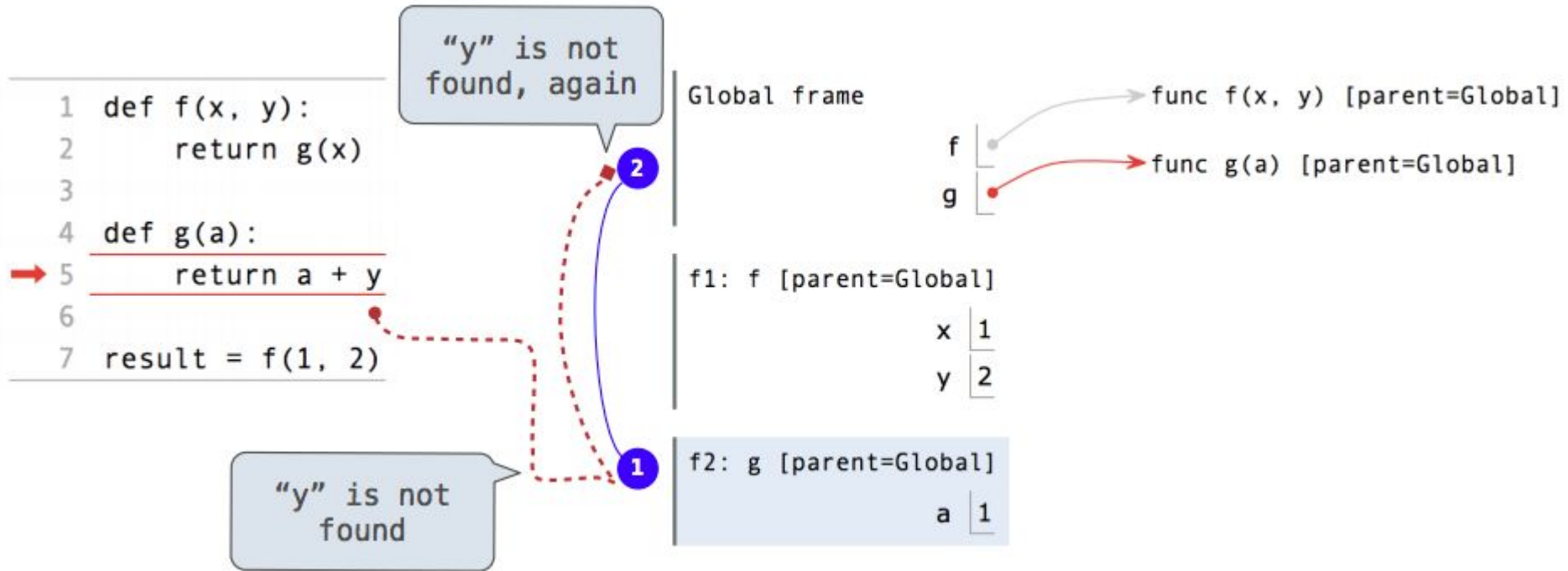
Local Names are not Visible to Other (Non-Nested) Functions



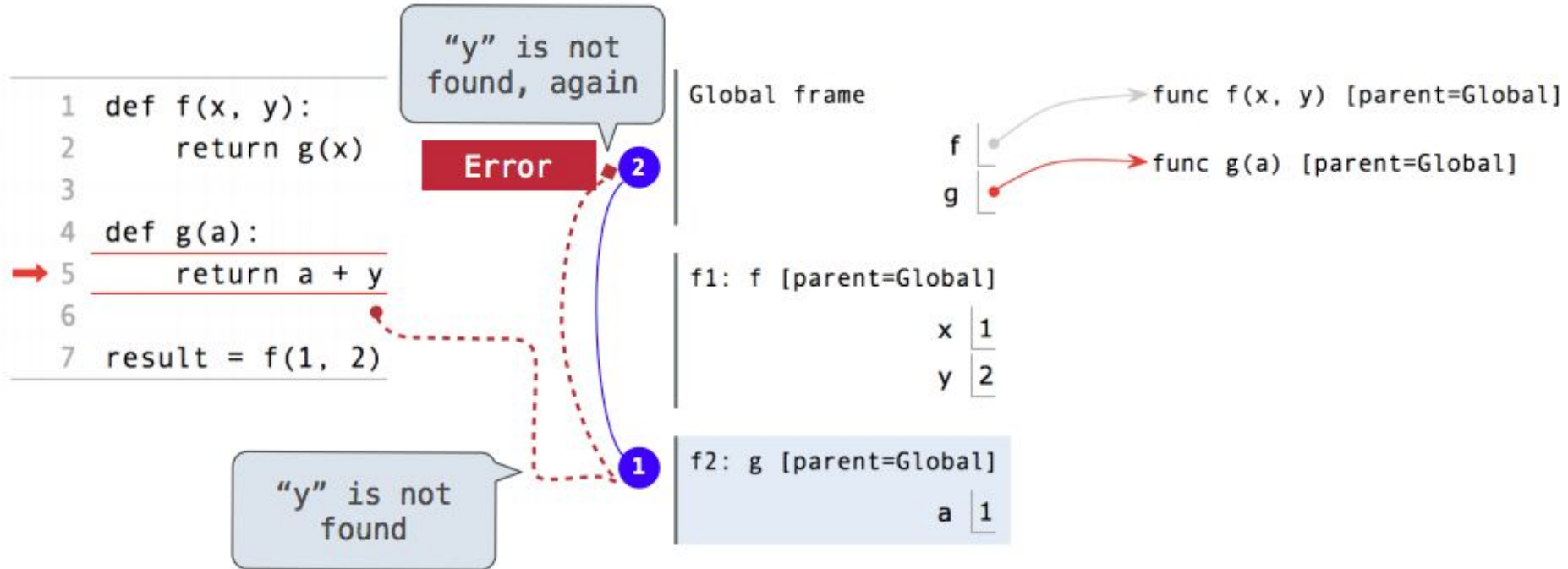
Local Names are not Visible to Other (Non-Nested) Functions



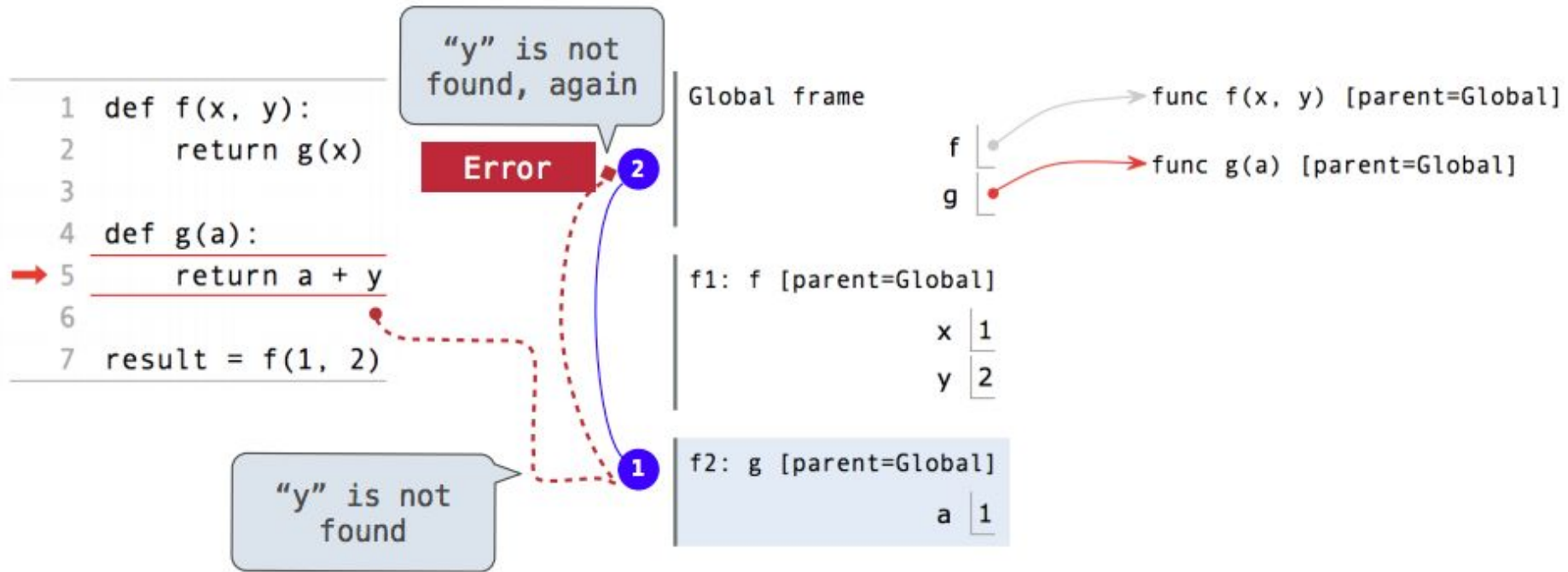
Local Names are not Visible to Other (Non-Nested) Functions



Local Names are not Visible to Other (Non-Nested) Functions

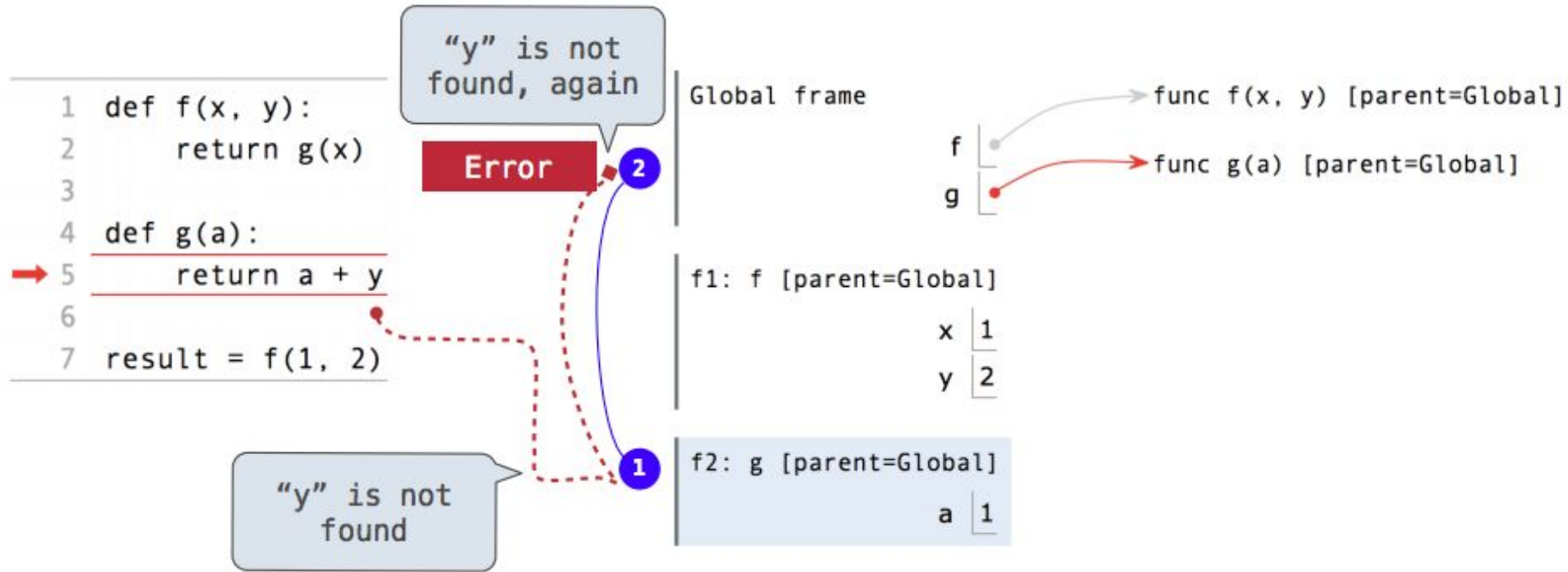


Local Names are not Visible to Other (Non-Nested) Functions



- An environment is a sequence of frames.

Local Names are not Visible to Other (Non-Nested) Functions



- An environment is a sequence of frames.
- The environment created by calling a top-level function (no def within def) consists of one local frame, followed by the global frame.

Check Point



```
def func1(a, b):  
    return 1 + func2(a + b)
```

```
def func2(c):  
    a = 3  
    return c + a
```

```
func1(1, 1)
```

Output?

A: Error

B: 5

C: 6

D: 7

E: Other

Practice with HOF. What is the output? (on your own)

```
def f(x, y):
```

```
    x, y = y, x
```

```
    def x(x):
```

```
        return y(x)
```

```
    return x
```

```
def y(x):
```

```
    return 6 + x
```

```
def z(y):
```

```
    return 4
```

```
g = f(y, z)
```

```
h = g(5)
```

ASSERT STATEMENTS IN PYTHON



Assertions and Exceptions

- Assertions should be used to check something *that should never happen*, while an exception should be used to check something *that might happen*.
 - Exceptions will be covered later.
- Assertions can be disabled at runtime using parameters, and are disabled by default, so don't count on them except for debugging purposes.
 - Using `-O`
- Assertions are used for **debugging** purposes only.

Assertions (demo)

- `assert`
 - Key word in Python

Syntax:

1. `assert <condition>`
2. `assert <condition>, (optional) <error message>`

If `<condition>` is `false` raise `AssertionError` exception

Assertion: * not the best way to use it

```
def double (x):  
    return x * 2
```

```
def triple(func, num):  
    assert isinstance(num, int), "Must be integer"  
  
    return func(num) * 3
```

```
>>> triple(double, 10.1)
```

```
File "/Users/marinalanglois/Desktop/test.py", line 26, in triple  
    assert isinstance(num, int), "Must be integer"  
AssertionError: Must be integer
```

Assertion: * not the best way to use it

```
def double (x):  
    return x * 2
```

```
def triple(func, num):  
    assert isinstance(num, int), "Must be integer"  
    assert callable(func), "Must be function"  
    return func(num) * 3
```

```
>>> doubl2 = 1000  
>>> triple(doubl2, 10)
```

```
File "/Users/marinalanglois/Desktop/test.py", line 27, in triple  
    assert callable(func), "Must be function"  
AssertionError: Must be function
```



Lambda Expressions (Functions)

An expression that evaluates to a function

(Demo)



Lambda Expressions

- *An expression that evaluates to a function*
- Known as:
 - Anonymous functions
- We use lambda functions when we require a (nameless) function for a short period of time.
- We generally use it as an argument to a higher-order function
- Lambda functions are used along with built-in functions like *filter()*, *map()* and *reduce()*
- *Used with apply when working with Pandas*

Lambda Expressions

An expression that evaluates to a function

```
>>> double = lambda x: 2 * x
```

A function

with formal parameter x

that returns the value of "2 * x"

Traditional way

```
def double x:  
    return 2 * x
```

Lambda Expressions

```
# add x and y
```

```
add = lambda x, y: x + y
```

```
def add (x, y):  
    return x + y
```

Lambda Expressions

```
# max of x and y
```

```
max = lambda x, y: x if x > y else y
```

*Return x, if x is greater than y,
otherwise return y*

```
def max(x, y):  
    if x > y:  
        return x  
  
    else:  
        return y
```

Lambda Expressions

- No “**return**” keyword
- **return**: Must be a single expression:
 - The **lambda**'s body is similar to what we'd put in a **def** body's **return** statement.
- Can not contain complex statements (like while or for loops)

```
>>> def f(x, y, z): return x + y + z
```

```
>>> f(2, 30, 400)
```

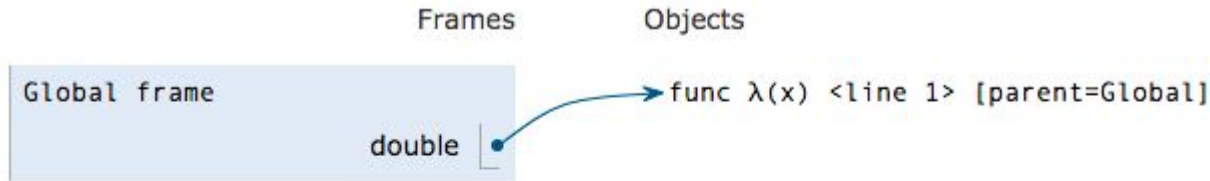
```
>>> f = lambda x, y, z: x + y + z
```

```
>>> f(2, 30, 400)
```

Intrinsic name

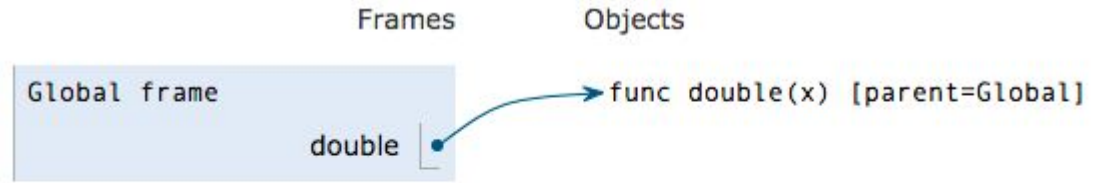
```
double = lambda x: 2*x
```

```
def double (x):  
    return 2 * x
```



```
f1: λ <line 1> [parent=Global]
```

x	4
Return value	8



```
f1: double [parent=Global]
```

x	4
Return value	8

Practice with lambdas. What is the output?

```
def writer():  
    title = 'Sir'  
    name = (lambda x:title + ' ' + x)  
    return name  
  
who = writer()  
print(who('Arthur Ignatius Conan Doyle'))
```

What is the output? (2 questions)

```
L = [lambda x: x ** 2,  
      lambda x: x ** 3,  
      lambda x: x ** 4]
```

```
for f in L:  
    print(f(3))
```

```
print(L[0](11))
```


Re-write it using def statements

```
L = [lambda x: x ** 2,  
      lambda x: x ** 3,  
      lambda x: x ** 4]  
for f in L:  
    print(f(3))  
  
print(L[0](11))
```

Rewrite it using def statements

```
L = [lambda x: x ** 2,  
     lambda x: x ** 3,  
     lambda x: x ** 4]  
for f in L:  
    print(f(3))  
  
print(L[0](11))
```

```
def f1(x): return x ** 2  
def f2(x): return x ** 3  
def f3(x): return x ** 4  
  
L = [f1, f2, f3]  
for f in L:  
    print(f(3))
```

TIME FOR A
BREAK

