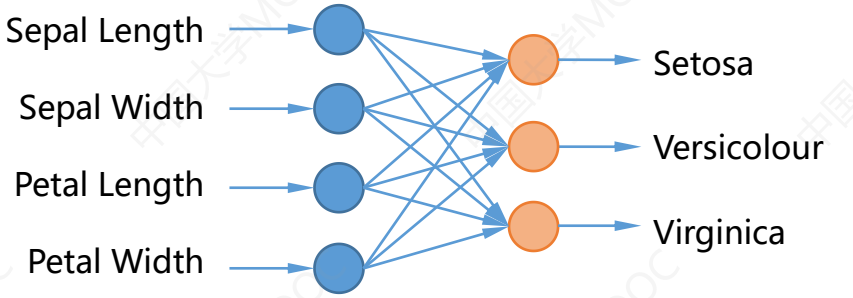
12.6 实例：实现多层神经网络

单层神经网络



- 激活函数 softmax函数
- 损失函数 交叉熵损失函数

$$Y = X\,W + B$$

输出 输入属性 权值矩阵 阈值

```
np.random.seed(612)
W = tf.Variable(np.random.randn(4,3),dtype=tf.float32)
B = tf.Variable(np.zeros([3]),dtype=tf.float32)
```

```
for i in range(0,iter+1):
    with tf.GradientTape() as tape:
        PRED_train=tf.nn.softmax(tf.matmul(X_train,W)+B)
        Loss_train=tf.reduce_mean(tf.keras.losses.categorical_crossentropy(y_true=Y_train,y_pred=PRED_train))

    PRED_test=tf.nn.softmax(tf.matmul(X_test,W)+B)
    Loss_test=tf.reduce_mean(tf.keras.losses.categorical_crossentropy(y_true=Y_test,y_pred=PRED_test))

    accuracy_train=tf.reduce_mean(tf.cast(tf.equal(tf.argmax(PRED_train.numpy(),axis=1),y_train),tf.float32))
    accuracy_test=tf.reduce_mean(tf.cast(tf.equal(tf.argmax(PRED_test.numpy(),axis=1),y_test),tf.float32))

    acc_train.append(accuracy_train)
    acc_test.append(accuracy_test)
    cce_train.append(Loss_train)
    cce_test.append(Loss_test)

    grads = tape.gradient(Loss_train,[W,B])
    W.assign_sub(learn_rate*grads[0])
    B.assign_sub(learn_rate*grads[1])

    if i % display_step == 0:
        print("i: %i, TrainAcc:%f, TrainLoss: %f ,TestAcc:%f, TestLoss: %f" % (i,accuracy_train,Loss_train,accuracy_test,Loss_test))
```

$Y = XW + B$

- 设置超参数

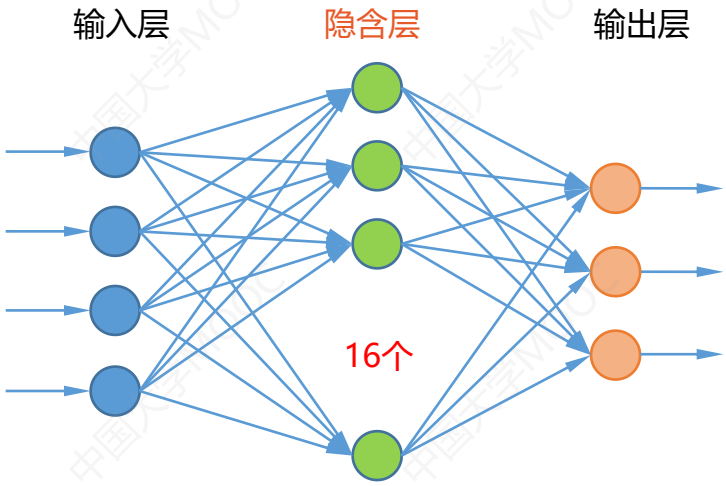
```
learn_rate = 0.5
iter = 50

display_step =10
```

- 训练结果

```
i: 0, TrainAcc:0.333333, TrainLoss: 2.066978 ,TestAcc:0.266667, TestLoss: 1.880856
i: 10, TrainAcc:0.875000, TrainLoss: 0.339410 ,TestAcc:0.866667, TestLoss: 0.461705
i: 20, TrainAcc:0.875000, TrainLoss: 0.279647 ,TestAcc:0.866667, TestLoss: 0.368414
i: 30, TrainAcc:0.916667, TrainLoss: 0.245924 ,TestAcc:0.933333, TestLoss: 0.314814
i: 40, TrainAcc:0.933333, TrainLoss: 0.222922 ,TestAcc:0.933333, TestLoss: 0.278643
i: 50, TrainAcc:0.933333, TrainLoss: 0.205636 ,TestAcc:0.966667 TestLoss: 0.251937
```

多层神经网络结构设计



W_1 (4,16)　B_1 (16,)　W_2 (16,3)　B_2 (3,)

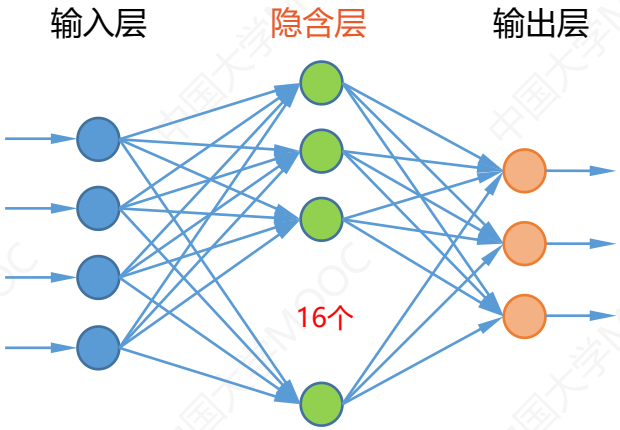
$H = X W_1 + B_1$　　$Y = H W_2 + B_2$

隐含层激活函数　relu函数

输出层激活函数　softmax函数

损失函数　交叉熵损失函数

多层神经网络的实现



W_1 (4,16)　B_1 (16,)　W_2 (16,3)　B_2 (3,)

$H = \mathrm{Relu}(XW_1 + B_1)$　$Y = Softmax(\mathrm{HW}_2 + B_2)$

设置模型参数

```
np.random.seed(612)
W1 = tf.Variable(np.random.randn(4,16),dtype=tf.float32)
B1= tf.Variable(tf.zeros([16]),dtype=tf.float32)
W2 = tf.Variable(np.random.randn(16,3),dtype=tf.float32)
B2= tf.Variable(tf.zeros([3]),dtype=tf.float32)
```

定义网络结构

```
Hidden_train=tf.nn.relu(tf.matmul(X_train,W1)+B1)
PRED_train=tf.nn.softmax(tf.matmul(Hidden_train,W2)+B2)
Loss_test=tf.reduce_mean(tf.keras.losses.categorical_crossentropy
                         (y_true=Y_test,y_pred=PRED_test))
```

$H = XW_1 + B_1$

$Y = HW_2 + B_2$

更新模型参数

```
grads = tape.gradient(Loss_train, [W1,B1,W2,B2])

W1.assign_sub(learn_rate*grads[0])
B1.assign_sub(learn_rate*grads[1])
W2.assign_sub(learn_rate*grads[2])
B2.assign_sub(learn_rate*grads[3])
```

完整程序：多层神经网络实现鸢尾花分类

- 导入库，设置GPU模式

```
In [1]: import tensorflow as tf
        print("TensorFlow version:", tf.__version__)

        TensorFlow version: 2.0.0

In [2]: import pandas as pd
        import numpy as np
        import matplotlib.pyplot as plt

In [3]: gpus = tf.config.experimental.list_physical_devices('GPU')
        tf.config.experimental.set_memory_growth(gpus[0], True)
```

- 加载数据，转换为NumPy数组

```
In [4]: TRAIN_URL = "http://download.tensorflow.org/data/iris_training.csv"
        train_path = tf.keras.utils.get_file(TRAIN_URL.split('/')[-1], TRAIN_URL)

        TEST_URL = "http://download.tensorflow.org/data/iris_test.csv"
        test_path = tf.keras.utils.get_file(TEST_URL.split('/')[-1], TEST_URL)

In [5]: df_iris_train = pd.read_csv(train_path, header=0)
        df_iris_test = pd.read_csv(test_path, header=0)

In [6]: iris_train=np.array(df_iris_train)
        iris_test=np.array(df_iris_test)

In [7]: iris_train.shape,iris_test.shape

Out[7]: ((120, 5), (30, 5))
```

- 数据预处理

```
In [8]: x_train=iris_train[:,0:4]
        y_train=iris_train[:,4]

        x_test=iris_test[:,0:4]
        y_test=iris_test[:,4]

In [9]: x_train.shape,y_train.shape
Out[9]: ((120, 4), (120,))

In [10]: x_test.shape,y_test.shape
Out[10]: ((30, 4), (30,))

In [11]: x_train=x_train-np.mean(x_train,axis=0)
         x_test=x_test-np.mean(x_test,axis=0)
```

```
In [12]: X_train=tf.cast(x_train, tf.float32)
         Y_train=tf.one_hot(tf.constant(y_train, dtype=tf.int32), 3)

         X_test=tf.cast(x_test, tf.float32)
         Y_test=tf.one_hot(tf.constant(y_test, dtype=tf.int32), 3)

In [13]: X_train.shape, Y_train.shape

Out[13]: (TensorShape([120, 4]), TensorShape([120, 3]))

In [14]: X_test.shape, Y_test.shape

Out[14]: (TensorShape([30, 4]), TensorShape([30, 3]))
```

- 设置超参数和显示间隔

```
In [15]: learn_rate = 0.5
         iter = 50
         display_step =10
```

- 设置模型参数初始值

```
In [16]: np.random.seed(612)
         W1 = tf.Variable(np.random.randn(4,16),dtype=tf.float32)
         B1= tf.Variable(tf.zeros([16]),dtype=tf.float32)
         W2 = tf.Variable(np.random.randn(16,3),dtype=tf.float32)
         B2= tf.Variable(tf.zeros([3]),dtype=tf.float32)
```

- 训练模型

```
In [17]: acc_train=[]
         acc_test=[]
         cce_train=[]
         cce_test=[]
```

```
for i in range(0,iter+1):
    with tf.GradientTape() as tape:
        Hidden_train=tf.nn.relu(tf.matmul(X_train,W1)+B1)
        PRED_train=tf.nn.softmax(tf.matmul(Hidden_train,W2)+B2)
        Loss_train=tf.reduce_mean(tf.keras.losses.categorical_crossentropy(y_true=Y_train,y_pred=PRED_train))

        Hidden_test=tf.nn.relu(tf.matmul(X_test,W1)+B1)
        PRED_test=tf.nn.softmax(tf.matmul(Hidden_test,W2)+B2)
        Loss_test=tf.reduce_mean(tf.keras.losses.categorical_crossentropy(y_true=Y_test,y_pred=PRED_test))

    accuracy_train=tf.reduce_mean(tf.cast(tf.equal(tf.argmax(PRED_train.numpy(),axis=1),y_train),tf.float32))
    accuracy_test=tf.reduce_mean(tf.cast(tf.equal(tf.argmax(PRED_test.numpy(),axis=1),y_test),tf.float32))

    acc_train.append(accuracy_train)
    acc_test.append(accuracy_test)
    cce_train.append(Loss_train)
    cce_test.append(Loss_test)

    grads = tape.gradient(Loss_train,[W1,B1,W2,B2])
    W1.assign_sub(learn_rate*grads[0])
    B1.assign_sub(learn_rate*grads[1])
    W2.assign_sub(learn_rate*grads[2])
    B2.assign_sub(learn_rate*grads[3])

    if i % display_step == 0:
        print("i: %i, TrainAcc:%f, TrainLoss: %f ,TestAcc:%f, TestLoss: %f" % (i,accuracy_train,Loss_train,accuracy_test,Loss_test))
```

- 训练结果

learn_rate=0.5，2层神经网络

```
i: 0,  TrainAcc:0.433333,  TrainLoss: 2.205641 ,TestAcc:0.400000,  TestLoss: 1.721138
i: 10,  TrainAcc:0.941667,  TrainLoss: 0.205314 ,TestAcc:0.966667,  TestLoss: 0.249661
i: 20,  TrainAcc:0.950000,  TrainLoss: 0.149540 ,TestAcc:1.000000,  TestLoss: 0.167103
i: 30,  TrainAcc:0.958333,  TrainLoss: 0.122346 ,TestAcc:1.000000,  TestLoss: 0.124693
i: 40,  TrainAcc:0.958333,  TrainLoss: 0.105099 ,TestAcc:1.000000,  TestLoss: 0.099869
i: 50,  TrainAcc:0.958333,  TrainLoss: 0.092934 ,TestAcc:1.000000,  TestLoss: 0.084885
```

learn_rate=0.5，单层神经网络

```
i: 0,  TrainAcc:0.333333,  TrainLoss: 2.066978 ,TestAcc:0.266667,  TestLoss: 1.880856
i: 10,  TrainAcc:0.875000,  TrainLoss: 0.339410 ,TestAcc:0.866667,  TestLoss: 0.461705
i: 20,  TrainAcc:0.875000,  TrainLoss: 0.279647 ,TestAcc:0.866667,  TestLoss: 0.368414
i: 30,  TrainAcc:0.916667,  TrainLoss: 0.245924 ,TestAcc:0.933333,  TestLoss: 0.314814
i: 40,  TrainAcc:0.933333,  TrainLoss: 0.222922 ,TestAcc:0.933333,  TestLoss: 0.278643
i: 50,  TrainAcc:0.933333,  TrainLoss: 0.205636 ,TestAcc:0.966667,  TestLoss: 0.251937
```

- 结果可视化

```
In [19]: plt.figure(figsize=(10,3))

         plt.subplot(121)
         plt.plot(cce_train,color="blue",label="train")
         plt.plot(cce_test,color="red",label="test")
         plt.xlabel("Iteration")
         plt.ylabel("Loss")
         plt.legend()

         plt.subplot(122)
         plt.plot(acc_train,color="blue",label="train")
         plt.plot(acc_test,color="red",label="test")
         plt.xlabel("Iteration")
         plt.ylabel("Accuracy")
         plt.legend()

         plt.show()
```