



The "flying car" is a ride at a model amusement park, in a room which consists of a car having wheels that roll along a track mounted inside a rotating drum. By design the car cannot fall off of the track. However, motion of the car is developed by applying the car's brake, thereby gripping the car to the track and allowing it to move with a constant speed of the track.  $V_t = 3 \text{ m/s}$ . If the rider applies the brake when going from B to A and then releases it at the top of the drum, A, so that the car coasts freely down along the track to B ( $\theta = \pi \text{ rad}$ ), determine the speed of the car at B and the height of the car at B. Neglect friction during the motion from A to B. The rider and car have a total mass of  $2.3 \text{ kg}$  and the center of mass of the car and rider moves along a circular path having a radius of  $1.2 \text{ m}$ . The car and rider can be represented by a block that is  $15 \text{ cm}$  high and  $20 \text{ cm}$  long at the beginning of the day when the temperature is  $10^\circ \text{C}$ . The room is a  $4 \text{ m} \times 5 \text{ m} \times 7 \text{ m}$  room. The heater is switched in and the radiator of the steam-heating system heats the room at a rate of  $10,000 \text{ kJ/h}$  and a  $100 \text{ W}$  fan is used to distribute the warm air in the room. The rate of heat loss from the room is estimated to be about

5000kJ/h. If the initial temperature of the room is 10°C, and the heater is left on for 831s, what is the height of the block (car) after 831s? Assume constant specific heats at room temperature.

\*\*Kies op as positief ↑ +

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format long;
```

Die massa m is:

```
m= 2.3; %kg
```

$V_t$  is:

```
Vt= 3 %m/s
```

```
Vt =  
3
```

$\alpha$  is die Termiese Uitsettings Koëffisient:

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alpha = 11*10^(-6);
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E is die Materiaal Styfheid of Young's Modulus of Modulus van Elastisiteit:

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E= 22.1*10^9;
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$\rho$  is die Digtheid:

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rho=2380; %kh/m^3 Digtheid
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a = gravitasie versnelling

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g= 9.81; % Gravitasieversnelling
```

r is die radius van die baan:

```
r= 1.2; %m
```

By punt B is  $\theta =$

```
theta= pi %rad
```

```
theta =  
3.141592653589793
```

h is die oorspronklike hoogte van die kar:

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h=0.015; % Hoogte
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x is die lengte van die kar:

$$x = 0.02; \% \text{ m}$$

$$m = \rho V$$

$$V = \frac{m}{\rho}$$

$$x y L = \frac{m}{\rho}$$

$$y = \frac{m}{\rho L x}$$

y is die breedte van die kar:

$$y = m / (\rho h x) \% \text{ m}$$

$$y = 3.221288515406163$$

A is die Area:

$$A = x y \% \text{ Area m}$$

$$A = 0.064425770308123$$

TOEGEPAS:

Die reguit lun verplasing  $s$  is:

$$\Delta s = r^2$$

$$\Delta s = 2.400000000000000$$

Die tangente versnelling by punt B:

$$V_B^2 = V_t^2 + 2g\Delta s$$

$$V_B = \sqrt{V_t^2 + 2g\Delta s}$$

$$V_B = \sqrt{V_t^2 + 2 * g * \Delta s} \% \text{ m/s}$$

$$V_B = 7.489192212782364$$

Die 'centrepetal' versnelling is:

$$a_n = \frac{V_B^2}{r}$$

$$a_n = V_B^2 / r$$

$$a_n = 46.740000000000009$$

Die krag  $F_B$  as gevolg van die beweging is:

$$FB = m \cdot a_n$$

$$FB = 1.0750200000000000e+02$$

*Enter your equation.*

TERMODINAMIKA:

$$T1 = 10; \text{ \% deg C}$$
$$T1K = 10 + 273.15 \text{ \%K}$$

$$T1K = 2.8315000000000000e+02$$

Die Volume van die kamer is:

$$V_{\text{kamer}} = 4 \cdot 5 \cdot 7$$

$$V_{\text{kamer}} = 140$$

Die Atmosferiese Druk is:

$$P_{\text{atm}} = 101.325; \text{ \%kPa}$$
$$P1 = P_{\text{atm}};$$

$R_{\text{air}}$  is:

$$R_{\text{air}} = 0.2870; \text{ \%kPa m}^3/\text{kgK}$$

tyd is:

$$\text{time} = 831; \text{ \%s}$$

Drywing gebruik deur die waaier is:

$$D_{\text{fan}} = 100 \cdot 10^{-3}; \text{ \% kW}$$

$c_v$  at 200K (room temperature) on Table A-2 is:

$$c_v = 0.718; \text{ \%kJ/kg.K}$$

Radiator heat transfer rate is:

$$\text{radiatorhtr} = 10000/3600; \text{ \% kJ/s}$$

Rate of heat lost form the room is:

$$\text{roomhloss} = 5000/3600; \text{ \% kJ/s}$$

So Calculate T2:

$$E_{\text{in}} - E_{\text{out}} = \Delta E_{\text{system}}$$

$$Q_{in} + W_{in} - Q_{out} = \Delta U \approx mc_v(T_2 - T_1) \text{ (assume KE=PE=0)}$$

$$(Q_{in} + \dot{W}_{in} - Q_{out})\Delta t = \Delta U \approx mc_v(T_2 - T_1)$$

$$(Q_{in} + \dot{W}_{in} - Q_{out})\Delta t = mc_v(T_2 - T_1)$$

$$(Q_{in} + \dot{W}_{in} - Q_{out}) \frac{\Delta t}{mc_v} = (T_2 - T_1)$$

$$(Q_{in} + \dot{W}_{in} - Q_{out}) \frac{\Delta t}{mc_v} + T_1 = T_2$$

$$T_2 = T_1 + (Q_{in} + \dot{W}_{in} - Q_{out}) \frac{\Delta t}{mc_v} \text{ and } m_{air} = \frac{P_1 \text{Volume}}{RT_1}$$

$$m_{air} = (P_1 * V_{kamer}) / (R_{air} * T_1K)$$

$$m_{air} = 1.745605836775302e+02$$

$$T_2 = T_1 + (\text{radiatorhtr} + D_{fan-roomhloss}) * (\text{time} / (m_{air} * c_v)) \text{ \% deg C}$$

$$T_2 = 19.871716692084291$$

$$\text{deltaT} = T_2 - T_1$$

$$\text{deltaT} = 9.871716692084291$$

STERKTELEER:

$$\text{Formule vir Hoogte Verandering: } \Delta L = -\int_0^{0.015} \frac{W(x)}{AE} dx - \frac{PL}{AE} + \alpha \Delta_T L$$

$$-\frac{PL}{AE} \text{ is die } \Delta L_{\text{Puntlas}} \text{ as gevolg van die puntlas 15kN}$$

$$\alpha \Delta_T L \text{ is die } \Delta L_{\text{Temp}} \text{ as gevolg van die Temperatuur verandering}$$

$$-\int_0^{0.015} \frac{W(x)}{AE} dx \text{ is die } \Delta L_{\text{eiegewig}} \text{ as gevolg van die balk se eiegewig}$$

Die krag van die beweging op die kar is  $F_B = P_{\text{Puntlas}}$

$$P_{\text{puntlas}} = F_B$$

$$P_{\text{puntlas}} = 1.075020000000000e+02$$

$$-\frac{PL}{AE} \text{ is die } \Delta L_{\text{Puntlas}} \text{ as gevolg van die puntlas is:}$$

$$\text{deltaLPuntlas} = (P_{\text{puntlas}} * h) / (A * E) \text{ \%N}$$

$$\text{deltaLPuntlas} =$$

$\alpha \Delta_T L$  is die  $\Delta L_{\text{Temp}}$  as gevolg van die Temperatuur verandering

$$\Delta L_{\text{Temp}} = \alpha \cdot \Delta T \cdot h \quad \%m$$

$$\Delta L_{\text{Temp}} = 1.628833254193908e-06$$

$-\int_0^{0.015} \frac{W(x)}{AE} dx$  is die  $\Delta L_{\text{eiegewig}}$  as gevolg van die balk se eiegewig:

In Toegepaste Wiskunde is gewig (of eiegewig):

$$F_{\text{eiegewig}} = mg \quad g = 9.81 \frac{m}{s^2} \quad m = \rho V$$

So  $F_{\text{eiegewig}} = \rho V g$  in Toegepaste Wiskunde is  $V = X_{\text{deursnit}} \times Y_{\text{deursnit}} \times \text{Lengte}$  of  $V = \text{Area} \times \text{Lengte}$ . Met daardie berekening word dit aangeneem dat die krag wat uitgewerk word geneem word aan die onderste punt van die objek (in hierdie geval balk). \*\*Dit is nogsteeds die geval met hierdie balk, maar die balk se Lengte gaan verander soos wat die Temperatuur verander en soos wat die Puntlas daarop inwerk so daarom gebruik ons eerder 'n integraal om die L voor te stel of uit te werk - alhoewel ons steeds van 0m op die grondvlak to 8m bo die grondvlak in die integraal gaan in sit (Onthou Kies op as positief  $\uparrow +$  in al my bewerkinge).

So

$$F_{\text{eiegewig}} = mg$$

$$F_{\text{eiegewig}} = mg$$

$$F_{\text{eiegewig}} = \rho V g$$

$$F_{\text{eiegewig}} = \rho g A L$$

$$P_{\text{eiegewig}} = \rho g A L$$

$$P_{\text{interne aksiaal krag by } z(z)} = \rho g A z$$

$$W(z) = \rho g A z$$

In Sterkteleer is  $W(s) = \rho g A s$  waar s die verplasing in die ortogonale rigting van die snit is. In hierdie geval is die vergelyking dus  $W(z) = \rho g A z = P(z)$  die interne aksiaalkrag by z. As jy die totale interne aksiaalkrag wil uitwerk oor die hele balk dan moet jy  $W(z) = \rho g A z = P(z)$  integreer oor die volle Lengte, L, van die balk.

So

$$F_{\text{eiegewig}} = \int_0^L W(z) dz = \rho g A \int_0^L z dz = \rho g A \int_0^{0.015} z dz$$

So volgens Toegepaste Wiskunde Berekeninge is die Feiegewig:

$$F_{\text{eiegewig}} = \rho \cdot g \cdot A \cdot h \quad \%N$$

$$F_{\text{eiegewig}} = 22.563000000000002$$

En dus is die Normaalkrag op die kar:

$$\text{Normaalkrag} = (P_{\text{puntlas}} + F_{\text{eiegewig}}) \cdot 10^3 \quad \% \text{ kN}$$

$$\text{Normaalkrag} = 130065$$

En volgens Sterkteleer Berekinge is die Feiegewig:

$$\text{So } W(z) =$$

$$\begin{aligned} &\text{syms } z; \\ &Wz = \rho \cdot g \cdot A \cdot z; \end{aligned}$$

$$\text{en vir interessantheid } W(0.015) =$$

$$W15 = \rho \cdot g \cdot A \cdot 0.015 \quad \%N$$

$$W15 = 22.563000000000002$$

$$\text{en so } = \int_0^L W(z) \, dx = \rho g A \int_0^L z \, dz = \rho g A \int_0^{0.015} z \, dz = P_{\text{eiegewig}}$$

$$\begin{aligned} &F_{\text{eiegewig}} = Wz; \\ &P_{\text{eiegewig}} = F_{\text{eiegewig}}; \end{aligned}$$

$$\text{So } -\int_0^{1.5} \frac{W(x)}{AE} \, dx \text{ is die } \Delta L_{\text{eiegewig}} \text{ as gevolg van die balk se eiegewig}$$

$$\begin{aligned} &\text{deltaLeiegewig} = \text{int}((P_{\text{eiegewig}})/(A \cdot E), 0, h); \\ &\text{vpa}(\text{deltaLeiegewig}) \end{aligned}$$

$$\text{ans} = 0.00000000011885192307692305607347338739999$$

So die Finale Antwoord is:

$$\text{Formule: } \Delta L = -\int_0^{0.015} \frac{W(x)}{AE} - \frac{PL}{AE} + \alpha \Delta_T L$$

$$\Delta L = -\Delta L_{\text{eiegewig}} - \Delta L_{\text{Puntlas}} + \Delta L_{\text{Temp}}$$

$$\begin{aligned} &\text{deltaL} = -\text{deltaLeiegewig} - \text{deltaLPuntlas} + \text{deltaLTemp}; \\ &\text{vpa}(\text{deltaL}) \end{aligned}$$

$$\text{ans} = 0.000001627581856116984899710471698532$$

So die nuwe Lengte (hoogte) van die kar is:

$$L_{\text{final}} = h + \text{deltaL};$$

```
vpa(Lfinal) %In m
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```
ans = 0.015001627581856116984899710471699
```

\*\*\*EK WIL NOU GRAAG HIERDIE PLOT OP 'N WISKUNDIGE 3D MANIER... EK WIL BYVOORBEELD 'N VERANDERING MAAK AAN DIE GROTE VAN DIE PUNT LAS EN DAN VISUEEL KAN SIEN DAT DIE BALK NOU KORTER OF LANGER IS...

```
%Z= [linspace(0,L);  
%    linspace(0,L)];  
%x= linspace(0, x);  
%y= linspace(0, y);  
%[X,Y]= meshgrid(x,y);  
%surf(X,Y,z)
```