

01.

$$A = \begin{bmatrix} x & 1 \\ 5 & 3 \end{bmatrix} \cdot B = \begin{bmatrix} 3 & -1 \\ y & 2 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$\begin{cases} 3x + y = 1 \\ 15 + 3y = 0 \end{cases}$$

$$\begin{cases} -x + 2 = 0 \\ -5 + 6 = 1 \end{cases}$$

$$15 + 3y = 0$$

$$3y = -15$$

$$y = \frac{-15}{3}$$

$$y = -5$$

$$-x + 2 = 0$$

$$2 = x$$

$$x + y$$

$$2 - 5$$

$$\hookrightarrow -3$$

(C)

data
fecha

D S T Q Q S S
D L M M J V S

02.

$$A = \begin{pmatrix} 1 & 0 & 1 \\ k & 1 & 3 \\ 1 & k & 3 \end{pmatrix}$$

a. $k=0$ e $k=3$

$$\begin{pmatrix} 1 & 0 & 1 \\ 0 & 1 & 3 \\ 1 & 0 & 3 \end{pmatrix} \begin{array}{l} 1 \ 0 \\ 0 \ 1 \\ 1 \ 3 \end{array}$$

$$3+0+0 - (1+0+0)$$

$$D=3-1$$

$$D=2, \quad \times$$

↳ admite inversão

b. $k=1$ e $k=-1$

$$\begin{pmatrix} 1 & 0 & 1 \\ 1 & 1 & 3 \\ 1 & 1 & 3 \end{pmatrix} \begin{array}{l} 1 \ 0 \\ 1 \ 1 \\ 1 \ 1 \end{array}$$

$$3+0+1 - (1+3+0)$$

$$4-4$$

$$0$$

$$\begin{pmatrix} 1 & 0 & 1 \\ -1 & 1 & 3 \\ 1 & -1 & 3 \end{pmatrix} \begin{array}{l} 1 \ 0 \\ -1 \ 1 \\ 1 \ -1 \end{array}$$

$$3+0+1 - (1-3+0)$$

$$4+2$$

$D=6 \rightarrow$ admite inversão

data
fecha

D S T Q Q S S
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C. $k=1$ e $k=2$

↳ não admite inversão

$$\begin{bmatrix} 1 & 0 & 1 \\ 2 & 1 & 3 \\ 1 & 2 & 3 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 2 & 1 \\ 1 & 2 \end{bmatrix}$$

$$3+0+4 - (1+6+0)$$
$$7 - 7$$

$$D=0$$

↳ não admite
inversão

(C)

data
fecha

D S T Q Q S S
D L M M J V S

03.

$$A = \begin{pmatrix} 3 & 5 \\ 2 & 4 \end{pmatrix}$$

$$DA = 3 \cdot 4 - (5 \cdot 2)$$

$$DA = 12 - 10$$

$$DA = 2$$

$$B = A^{-1}$$

$$\begin{pmatrix} 4 & -5 \\ -2 & 3 \end{pmatrix} \div 2 = \begin{pmatrix} 2 & -\frac{5}{2} \\ -1 & \frac{3}{2} \end{pmatrix}$$

(C)

$$04. \begin{bmatrix} x & 1 & 2 \\ 3 & 1 & 2 \\ 10 & 1 & x \end{bmatrix}$$

a. $x \neq 3$ e $x \neq 2$

9

$$\begin{bmatrix} 3 & 1 & 2 \\ 3 & 1 & 2 \\ 10 & 1 & 3 \end{bmatrix} \begin{bmatrix} 3 & 1 \\ 3 & 1 \\ 10 & 1 \end{bmatrix}$$

$$9 + 20 + 6 - (20 + 6 + 9) = 35 - 35 = 0$$

$$\begin{bmatrix} 2 & 1 & 2 \\ 3 & 1 & 2 \\ 10 & 1 & 2 \end{bmatrix} \begin{bmatrix} 2 & 1 \\ 3 & 1 \\ 10 & 1 \end{bmatrix}$$

$$4 + 20 + 6 - (20 + 4 + 6) = 30 - 30 = 0$$

data
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06.

$$\begin{pmatrix} -1 & -1 & 2 \\ 2 & 1 & -2 \\ 1 & 1 & -1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{matrix} \cdot (-1) \\ \cdot -2 \\ \end{matrix}$$

$$\begin{pmatrix} 1 & 1 & 0 \\ 0 & -1 & 2 \\ 1 & 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} -1 & -1 & 2 \\ 2 & 1 & -2 \\ 1 & 1 & -1 \end{pmatrix} + \begin{pmatrix} 1 & 1 & 0 \\ 0 & -1 & 2 \\ 1 & 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} -1+1 & -1+1 & 2+0 \\ 2+0 & 1+(-1) & -2+2 \\ 1+1 & 1+0 & -1+1 \end{pmatrix}$$

$$\begin{pmatrix} 0 & 0 & 0 \\ 2 & 0 & 0 \\ 2 & 1 & 0 \end{pmatrix} \quad (B)$$

data
fecha

D S T Q O S S
D L M M J V S

06.

$$(X \cdot A)^T = B$$

$$((X \cdot A)^T)^T = B^T = X \cdot A = B^T$$

$$X A A^{-1} = B^T A^{-1} \quad - X I = B^T A^{-1}$$

$$X = B^T A^{-1}$$

B

data
fecha

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D S T Q Q S S
D L M M J V S

07.

$$A \cdot \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 4x + 5y \\ 5x + 6y \end{bmatrix}$$

$$A = \begin{bmatrix} 4 & 5 \\ 5 & 6 \end{bmatrix}$$

$$\text{INVERSO} = \begin{bmatrix} -6 & 5 \\ 5 & -4 \end{bmatrix}$$

(D)

data
fecha

D S T Q Q S S
D L M M J V S

08.

$$A = \begin{pmatrix} 2 & k \\ -2 & 1 \end{pmatrix}$$

b.

$$k = -2$$

$$k = \frac{-8 \pm 0}{2 \cdot -4} = k = \frac{-8 \pm 0}{-8}$$

$$k_1 = \frac{-8}{-8}$$

$$k_2 = \frac{-8}{-8}$$

$$k_1 = -1$$

$$k_2 = -1$$

(B)

-1

data
fecha

D S T Q Q S S
D L M M J V S

09.

a.

$$(a+b) \cdot (a+b)$$

$$(a+b) \cdot (a+b)$$

$$a^2 - ab + ba - b^2$$

b.

$$(a+b)^2 = (a+b) \cdot (a+b)$$

$$ba + ab = a^2 + ab + ba + b^2$$

$$a^2 + 2ab + b^2$$

c.

$$\frac{\text{Det } a}{\text{Det } b}$$

$$\frac{\text{Det } a}{\text{Det } b}$$

$$\text{Det}(-a) = (-1)^2 \cdot \text{Det } a = \text{Det } a \neq 0$$

$$\frac{\text{Det } a}{\text{Det } b} = 1$$

$$\frac{\text{Det } a}{\text{Det } b}$$

d.

$$\text{Det}(ab) = 1$$

$$\text{Det}(b) \cdot \text{Det}(a) = 1$$

$$\text{Det}(b) = \frac{1}{\text{Det}(a)}$$