



Sheet#3 Normalized Cut and Kmeans Clustering

Submit a report and the codes used. Report is essential.
Normalized Cut

Kmeans Clustering

1. Use the k-means algorithm and Euclidean distance to cluster the following 8 examples into 3 clusters: A1=(2,10), A2=(2,5), A3=(8,4), A4=(5,8), A5=(7,5), A6=(6,4), A7=(1,2), A8=(4,9). The distance matrix based on the Euclidean distance is given below:

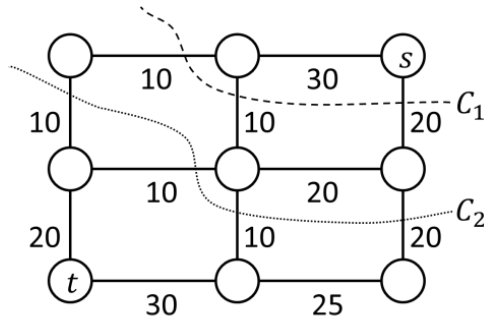
	A1	A2	A3	A4	A5	A6	A7	A8
A1	0	$\sqrt{25}$	$\sqrt{36}$	$\sqrt{13}$	$\sqrt{50}$	$\sqrt{52}$	$\sqrt{65}$	$\sqrt{5}$
A2		0	$\sqrt{37}$	$\sqrt{18}$	$\sqrt{25}$	$\sqrt{17}$	$\sqrt{10}$	$\sqrt{20}$
A3			0	$\sqrt{25}$	$\sqrt{2}$	$\sqrt{2}$	$\sqrt{53}$	$\sqrt{41}$
A4				0	$\sqrt{13}$	$\sqrt{17}$	$\sqrt{52}$	$\sqrt{2}$
A5					0	$\sqrt{2}$	$\sqrt{45}$	$\sqrt{25}$
A6						0	$\sqrt{29}$	$\sqrt{29}$
A7							0	$\sqrt{58}$
A8								0

Suppose that the initial seeds (centers of each cluster) are A1, A4 and A7. Run the k-means algorithm for 1 epoch only. At the end of this epoch show:

- a. The new clusters
- b. The centers of the new clusters
- c. Draw a 10 by 10 space with all the 8 points and show the clusters after the first epoch and the new centroids.
- d. How many more iterations are needed to converge? Draw the result for each epoch.

Normalized Cut

- Given the graph below. The weight on each edge is the affinity between two nodes. Consider the two cuts
- C_1 and C_2 in the graph. For each cut, compute the values of the graph cut and the normalized cut. Which cut will be favored by each algorithm? What is your explanation?



- Write your python code** to implement K ways normalized cut $k=3$
 - Use RBF kernel with $\gamma = \{0.01, 0.1, 1, 10\}$. Which of these γ values produces a connected graph? Plot the normalized eigenvectors using (Y vectors as in pseudo code) **scatter3d**
 - Use Similarity graph as the 3-NN graph. Where $\text{Sim}(x_i, x_j)=1$ iff x_j is one of the nearest three points to x_i (or vice versa). Plot the normalized eigenvectors using (Y vectors as in pseudo code) **scatter3d**

