

*Simple*_Xⁿ module

IN480 course [\[1\]](#)

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1 Introduction

The *Simplexⁿ* library, named **simplexn** within the Python version of the LARCC framework, provides combinatorial algorithms for some basic functions of geometric modelling with simplicial complexes. In particular, provides the efficient creation of simplicial complexes generated by simplicial complexes of lower dimension, the production of simplicial grids of any dimension, and the extraction of facets (i.e. of $(d - 1)$ -faces) of complexes of d -simplices. [2]

1.1 Requirements

There is no need to install extra packages to run the Julia code, it is sufficient loading the built-in package *Combinatorics.jl* (i.e. `using Combinatorics`); however, in order to be able to make the graphs it is necessary to install the package *Plots.jl* [5] (i.e. `Pkg.add("Plots")`) and load it (i.e. `using Plots`) with the preferred backend (for example `gr()`).

We used four processors (`addprocs(4)` at startup), five REPL included.

1.2 API

`larExtrude1(model::Tuple{Array{Array{Int64,1},1},Array{Array{Int64,1},1}}, pattern::Array{Int64,1})`

Description: this function generates the output model vertices in a multiple extrusion of a LAR model.

Input: `model` contains a pair (V, FV) , where V is the array of input vertices, and FV is the array of d -cells (given as arrays of vertex indices) providing the input representation of a LAR cellular complex. `pattern` is an array of integers, whose absolute values provide the sizes of the ordered set of 1D (in local coords) subintervals specified by the pattern itself.

Output: it is a model that contains a pair $(outV, triangles)$ representing the triangulation of the input `model`.

`larSimplexGrid1(shape::Array{Int64,1})`

Description: this function generates the simplicial grids of any dimension and shape.

Input: `shape` is an array of integers used to specify the shape of the created array.

Output: it is a model that contains a pair (V, FV) , where V is the array of input vertices, and FV is the array of d -cells (given as arrays of vertex indices) providing the input representation of a LAR cellular complex.

`larSimplexFacets(simplices::Array{Array{Int64,1},1})`

Description: this function provides the extraction of non-oriented $(d - 1)$ -facets of d -dimensional simplices.

Input: `simplices` is the array of d -cells (given as arrays of vertex indices) providing the input representation of a LAR cellular complex.

Output: it is an array of d -cells of integers, i.e. the input LAR representation of the topology of a cellular complex.

`quads2tria(model::Tuple{Array{Array{Int64,1},1},Array{Array{Int64,1},1}})`

Description: this function gives the conversion of a LAR boundary representation (B-Rep), i.e. a LAR model **V**, **FV** made of 2D faces, usually quads but also general polygons, into a LAR model **VERTS**, **TRIANGLES** made by triangles.

Input: `model` contains a pair (V, FV), where V is the array of input vertices, and FV is the array of *d*-cells (given as arrays of vertex indices) providing the input representation of a LAR cellular complex.

Output: it is a model that contains a pair (V, triangles) representing the triangulation of the input model.

2 Implementation

All the code in this section works with a simple copy and paste in Julia REPL; however, if a code block starts in a page and ends at the following one, it is required to pay attention at the numbers and headers of the pages.

Moreover, we left in the code some comments we think could be useful.

2.1 larExtrude1

This function generates the output model vertices in a multiple extrusion of a LAR model.

2.1.1 Python code

```
def larExtrude1(model,pattern):
    V, FV = model
    d, m = len(FV[0]), len(pattern)
    coords = list(cumsum([0]+(AA(ABS)(pattern))))
    offset, outcells, rangelimit = len(V), [], d*m
    for cell in FV:
        tube = [v + k*offset for k in range(m+1) for v in cell]
        cellTube = [tube[k:k+d+1] for k in range(rangelimit)]
        outcells += [reshape(cellTube, newshape=(m,d,d+1)).tolist()]

    outcells = AA(CAT)(TRANS(outcells))
    cellGroups = [group for k,group in enumerate(outcells) if pattern[k]>0]
    outVertices = [v+[z] for z in coords for v in V]
    outModel = outVertices, CAT(cellGroups)
    return outModel
```

2.1.2 Julia code - serial

```
# Generation of the output model vertices in a multiple extrusion of a LAR model
function larExtrude1(model::Tuple{Array{Array{Int64,1},1},Array{Array{Int64,1},1}},
    pattern::Array{Int64,1})
```

```

V, FV = model
d, m = length(FV[1]), length(pattern)
coords = cumsum(append!([0],abs.(pattern))) # built-in function cumsum
offset, outcells, rangelimit = length(V), Array{Int64}(m,0), d*m
for cell in FV
    tube = [v + k*offset for k in 0:m for v in cell]
    celltube = Int64[]
    for k in 1:rangelimit
        append!(celltube,tube[k:k+d])
    end
    outcells = hcat(outcells,permutedims(reshape(celltube,d*(d+1),m),[2,1]))
end
cellGroups = Int64[]
for k in 1:m
    if pattern[k]>0
        cellGroups = vcat(cellGroups,outcells[k,:])
    end
end
outVertices = [vcat(v,z) for z in coords for v in V]
outCellGroups = Array{Int64,1}[]
for k in 1:d+1:length(cellGroups)
    append!(outCellGroups,[cellGroups[k:k+d]])
end
return outVertices, outCellGroups
end

```

2.1.3 Parallel optimization

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2.1.4 Julia code - parallel

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2.1.5 Unit test code

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2.1.6 Script

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2.2 larSimplexGrid1

This function generates the simplicial grids of any dimension and shape.

2.2.1 Python code

```
def larSimplexGrid1(shape):
    model = VOID
    for item in shape:
        model = larExtrude1(model,item*[1])
    return model
```

2.2.2 Julia code - serial

```
# Generation of simplicial grids of any dimension and shape
function larSimplexGrid1(shape::Array{Int64,1})
    model = [Int64[],[[0]] # the empty simplicial model
    for item in shape
        model = larExtrude1(model,repmat([1],item))
    end
    return model
end
```

2.2.3 Parallel optimization

It is not possible to parallelize this function because every iteration of the loop requires the model that is computed in the previous one. The only difference here is the addition of `@everywhere`.

2.2.4 Julia code - parallel

```
# Generation of simplicial grids of any dimension and shape
@everywhere function larSimplexGrid1(shape::Array{Int64,1})
    model = [Int64[]],[[0]] # the empty simplicial model
    for item in shape # no parallelism
        model = larExtrude1(model, repmat([1],item))
    end
    return model
end
```

2.2.5 Unit test code

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2.2.6 Script

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2.3 larSimplexFacets

This function provides the extraction of non-oriented $(d - 1)$ -facets of d -dimensional simplices.

2.3.1 Python code

```
def larSimplexFacets(simplices):
    out = []
```

```

d = len(simplices[0])
for simplex in simplices:
    out += AA(sorted)([simplex[0:k]+simplex[k+1:d] for k in range(d)])
out = set(AA(tuple)(out))
return sorted(out)

```

2.3.2 Julia code - serial

Extraction of non-oriented (d-1)-facets of d-dimensional simplices
using Combinatorics # for combinations() function

```

function larSimplexFacets(simplices::Array{Array{Int64,1},1})
    out = Array{Int64,1}[]
    d = length(simplices[1])
    for simplex in simplices
        append!(out,collect(combinations(simplex,d-1)))
    end
    return sort!(unique(out),lt=lexless) # array of arrays, not of tuples
end
#map(x->tuple(x...),[[0, 1],[0, 4],[1, 2]])

```

2.3.3 Parallel optimization

Here, other than the classic addition of `@everywhere`, we used `@parallel` to split the computation of the for among multiple processors. The `return` automatically waits the end of the computation.

2.3.4 Julia code - parallel

Extraction of non-oriented (d-1)-facets of d-dimensional simplices
`@everywhere` using Combinatorics # for combinations() function

```

@everywhere function larSimplexFacets(simplices::Array{Array{Int64,1},1})
    out = Array{Int64,1}[]
    d = length(simplices[1])
    out = @parallel (append!) for simplex in simplices
        collect(combinations(simplex,d-1))
    end
    return sort!(unique(out),lt=lexless) # array of arrays, not of tuples
end
#map(x->tuple(x...),[[0, 1],[0, 4],[1, 2]])

```

2.3.5 Unit test code

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2.3.6 Script

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2.4 quads2tria

This function gives the conversion of a LAR boundary representation (B-Rep), i.e. a LAR model **V**, **FV** made of 2D faces, usually quads but also general polygons, into a LAR model **VERTS**, **TRIANGLES** made by triangles.

2.4.1 Python code

```
def quads2tria(model):
    V,FV = model
    out = []
    nverts = len(V)-1
    for face in FV:
        centroid = CCOMB([V[v] for v in face])
        V += [centroid]
        nverts += 1

        v1, v2 = DIFF([V[face[0]],centroid]), DIFF([V[face[1]],centroid])
        v3 = VECTPROD([v1,v2])
        if ABS(VECTNORM(v3)) < 10**3:
            v1, v2 = DIFF([V[face[0]],centroid]), DIFF([V[face[2]],centroid])
            v3 = VECTPROD([v1,v2])
        transf = mat(INV([v1,v2,v3]))
        verts = [(V[v]*transf).tolist()[0][:-1] for v in face]

        tcentroid = CCOMB(verts)
        tverts = [DIFF([v,tcentroid]) for v in verts]
        rverts = sorted([[ATAN2(vert),v] for vert,v in zip(tverts,face)])
        ord = [pair[1] for pair in rverts]
```

```

    ord = ord + [ord[0]]
    edges = [[n,ord[k+1]] for k,n in enumerate(ord[:-1])]
    triangles = [[nverts] + edge for edge in edges]
    out += triangles
return V,out

```

2.4.2 Julia code - serial

```

# Transformation to triangles by sorting circularly the vertices of faces
function quads2tria(model::Tuple{Array{Array{Float64,1},1},Array{Array{Int64,1},1}})
    V, FV = model
    out = Array{Int64,1}[]
    nverts = length(V)-1
    for face in FV
        arr = [V[v+1] for v in face]
        centroid = sum(arr)/length(arr)
        append!(V,[centroid])
        nverts += 1
        v1, v2 = V[face[1]+1]-centroid, V[face[2]+1]-centroid
        v3 = cross(v1,v2)
        if norm(v3) < 1/(10^3)
            v1, v2 = V[face[1]+1]-centroid, V[face[3]+1]-centroid
            v3 = cross(v1,v2)
        end
        transf = inv(hcat(v1,v2,v3)')
        verts = [(V[v+1]'*transf)'[1:end-1] for v in face]
        tcentroid = sum(verts)/length(verts)
        tverts = [v-tcentroid for v in verts]
        iterator = collect(zip(tverts, face))
        rverts = [[atan2(reverse(iterator[i][1])...),iterator[i][2]]
            for i in 1:length(iterator)]
        rvertss = sort(rverts,lt=(x,y)->isless(x[1],y[1]))
        ord = [pair[2] for pair in rvertss]
        append!(ord,ord[1])
        edges = [[i[2],ord[i[1]+1]] for i in enumerate(ord[1:end-1])]
        triangles = [prepend!(edge,nverts) for edge in edges]
        append!(out,triangles)
    end
    return V, out
end

```

2.4.3 Parallel optimization

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2.4.4 Julia code - parallel

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2.4.5 Unit test code

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2.4.6 Script

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3 Conclusions

The graphs have showed the parallel code is (significantly) slower than the serial one. A possible way to improve this problem could be to rewrite all the functions using different structures and procedures to handle the data, avoiding array of arrays and similar.

However, the complete lack of documentation online, official and non, for the correct use of the macros and how they specifically work makes the task quite difficult.

References

- [1] IN480 course [web page](#).
- [2] Python Simple_X^n module [pdf](#).
- [3] A. Paoluzzi, *Geometric Programming for Computer-Aided Design*, Wiley, 2003.
- [4] Official [Julia website](#).
- [5] Documentation of the [Plots package](#) for Julia.
- [6] M. Sherrington, *Mastering Julia*, Packt Publishing, 2015.