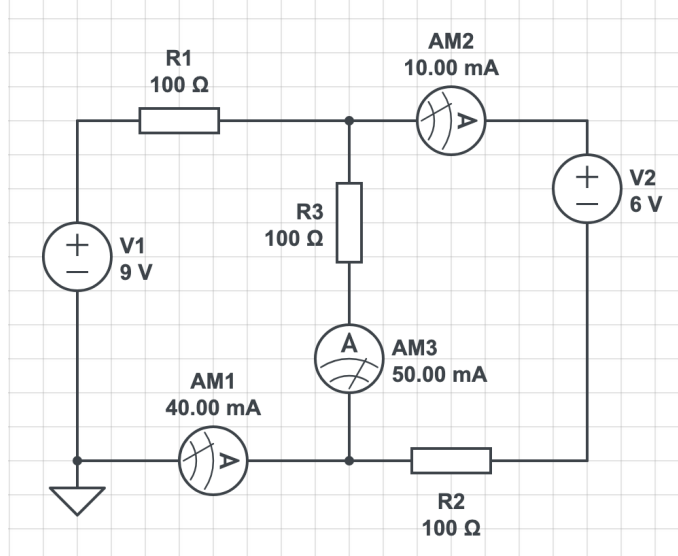


Write down a matrix-vector equation where the unknown is a vector of currents,  $I_1$ ,  $I_2$  and  $I_3$ . Verify that the ammeter values shown in this diagram are correct.



**Solving the above with Doolittle's method** Write down the system matrix,  $A$ , using Kirchhoff's Laws and find its LU Decomposition using Doolittle's method. What is the right-hand side?

$$\begin{bmatrix} A_{11} & A_{12} & A_{13} \\ A_{21} & A_{22} & A_{23} \\ A_{31} & A_{32} & A_{33} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix}$$

In the following decomposition, determine all the entries such as  $L_{21}$  and  $U_{12}$ .

$$A = \begin{bmatrix} 1 & 0 & 0 \\ L_{21} & 1 & 0 \\ L_{31} & L_{32} & 1 \end{bmatrix} \begin{bmatrix} U_{11} & U_{12} & U_{13} \\ 0 & U_{22} & U_{23} \\ 0 & 0 & U_{33} \end{bmatrix}$$

Use  $L$  and  $U$  to calculate the value of the currents in the circuit.

Calculate the currents when (a)  $V_1 = 5$  and  $V_2 = 4$  Volts, and (b)  $V_1 = 100$  and  $V_2 = 1$  Volts. Use the LU decomposition each time.