```
QUESTION 1

This definition of sumlist/2 is not tail recursive:

sumlist([], 0).
sumlist([N|Ns], Sum):-
sumlist(Ns, Sum0),
Sum is N + Sum0.

Rewrite it to be tail recursive.

QUESTION 2

Given a binary tree defined to satisfy the predicate tree/1

tree(empty).
tree(node(Left,_,Right)):-
tree(Left),
tree(Right).
```

write a predicate tree_list(Tree, List) that holds when List is a list of all the elements of Tree, in left-to-right order. This code need only work in the mode where the tree is input.

OUESTION 3

Revise the definition from the previous question not to use append/3 to construct the list. That is, ensure the cost of the operation is proportional to the number of elements in the tree.

Hint: look at the approach taken to write a tail recursive reverse predicate for inspiration.

OUESTION 4

Write a predicate list_tree(List, Tree) that holds when Tree is a balanced tree whose elements are the elements of List, in the order they appear in List. This need only work in the mode where List is a proper list.

Hint: first divide the list into the first half, the middle element, and the last half, then recursively construct a tree from the first half and second half, and assemble these into the resulting tree.