

**Data Structures**  
**Lab 2 – Red Black Tree**

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## ➤ Problem Statement:

- Implementing Red Black Tree with the following methods:
  1. **getRoot:** return the root of the given Red black tree.
  2. **isEmpty:** return whether the given tree is empty or not.
  3. **clear:** Clear all keys in the given tree.
  4. **search:** return the value associated with the given key or null if no value is found.
  5. **contains:** return true if the tree contains the given key and false otherwise.
  6. **insert:** Insert the given key in the tree while maintaining the red black tree properties. If the key is already present in the tree, update its value.
  7. **delete:** Delete the node associated with the given key. Return true in case of success and false otherwise.
- Implementing an interface similar to TreeMap java interface with the following functions:
  1. **ceilingEntry:** Returns a key-value mapping associated with the least key greater than or equal to the given key, or null if there is no such key.
  2. **ceilingKey:** Returns the least key greater than or equal to the given key, or null if there is no such key.
  3. **clear:** Removes all of the mappings from this map.
  4. **containsKey:** Returns true if this map contains a mapping for the specified key.
  5. **containsValue:** Returns true if this map maps one or more keys to the specified value.
  6. **entrySet:** Returns a Set view of the mappings contained in this map in ascending key order.
  7. **firstEntry:** Returns a key-value mapping associated with the least key in this map, or null if the map is empty.
  8. **firstKey:** Returns the first (lowest) key currently in this map, or null if the map is empty.
  9. **floorEntry:** Returns a key-value mapping associated with the greatest key less than or equal to the given key, or null if there is no such key.
  10. **floorKey:** Returns the greatest key less than or equal to the given key, or null if there is no such key.
  11. **get:** Returns the value to which the specified key is mapped, or null if this map contains no mapping for the key.
  12. **headMap:** Returns a view of the portion of this map whose keys are strictly less than toKey in ascending order.
  13. **headMap:** Returns a view of the portion of this map whose keys are less than (or equal to, if inclusive is true) toKey in ascending order.
  14. **keySet:** Returns a Set view of the keys contained in this map.
  15. **lastEntry:** Returns a key-value mapping associated with the greatest key in this map, or null if the map is empty.
  16. **lastKey:** Returns the last (highest) key currently in this map.
  17. **pollFirstElement:** Removes and returns a key-value mapping associated with the least key in this map, or null if the map is empty.
  18. **pollLastEntry:** Removes and returns a key-value mapping associated with the greatest key in this map, or null if the map is empty.
  19. **put:** Associates the specified value with the specified key in this map.

- 20. **putAll:** Copies all of the mappings from the specified map to this map.
- 21. **remove:** Removes the mapping for this key from this TreeMap if present.
- 22. **size:** Returns the number of key-value mappings in this map.
- 23. **values:** Returns a Collection view of the values contained in this map.

## ➤ Algorithms:

- **Insert:**

```
insert(key, value)
    t = root
    p = nullNode
    while (!t.isNull()) {
        p = t
        if (key == t.getKey)
            t.value=value
        else if (key < t.getKey)
            t = t.Left
        else
            t = t.Right
    }
    z.parent=p
    z.key=key
    z.value=value
    if (p == nullNode)
        root = z;
    else if (key < p.key)
        p.Left=z
    else
        p.Right=z
    z.right=nullNode
    z.left=nullNode
    z.color=RED
    insertFix(z);
```

```

insertFix(z)
    while (z.parent.color=RED) {
        if (z.parent == z.parent.parent.Left)
            y = z.parent.parent.Right
            if (y.color = RED)
                y.color=BLACK
                z.parent.color=BLACK
                z.parent.parent.color=RED
                z = z.getParent().getParent();
            else
                if (z == z.parent.Right)
                    z = z.parent
                    rotateLeft(z);
                z.parent.color=BLACK
                z.parent.parent.color=RED
                rotateRight(z.parent.parent)
        else if ((z.parent == z.parent.parent.right) {
            y = z.parent.parent.LeftChild
            if (y.color=RED)
                y.color=BLACK
                z.parent.color=BLACK
                z.parent.parent.color=RED
                z = z.parent.parent
            else
                if (z == z.parent.Left)
                    z = z.parent
                    rotateRight(z)
                z.parent.color=BLACK
                z.parent.parent.color=RED
                rotateLeft(z.parent.parent)
    }
    root.color=BLACK

```

- **Delete:**

**delete(T key)**

```
t = root
while (key != t.Key) {
    if (key > t.Key)
        t = t.Right
    }else
        t = t.Left
}
color = t.color
if (t. Left.isNull()) {
    x = t. Right
    transplant(t.Right, t)
else if (t.Right.isNull())
    x = t.LeftChild
    transplant(t.Left, t);
else
    min = minimum(t.Right);
    x = min.RightChild
    color = min.color
    if (min.parent != t)
        transplant(x, min)
        min.Right=t.Right
        min.Right.parent=min
    else
        x.parent=min
    transplant(min, t);
    min. Left=t.LeftChild
    t.Left.parent=min
    min.color=t.color
    t = min;
if (color=BLACK) {
    deleteFix(x);
}
```

**deleteFix(x)**

```
while (x != root && x.color=BLACK) {
    if (x == x.parent.Left)
        z = x.parent.RightChild
        if (z.color==RED)
            z.color=BLACK
            x.parent.color=RED
            rotateLeft(x.parent)
            z = x.parent.Right
        if (z.Left.color=BLACK && z.Right.color==BLACK)
            z.color=RED
            x = x.parent
        else
            if (z. Left.color=RED && z.Right.olor=BLACK)
                z.Left.color=BLACK
                z.color=RED
                rotateRight(z)
                z = x.parent.Right
                z.color=x.parent.color
                x.parent.color=BLACK
                z.Right.color=BLACK
                rotateLeft(x.parent)
                x = root
    else
        z = x.parent.RightChild
        if (z.color==RED) {
            z.color=BLACK
            x.parent.color=RED
            rotateRight(x.parent)
            z = x.parent.Left
        if (z.Left.color=BLACK && z.Right.color==BLACK)
            z.color=RED
            x = x.parent
        else
            if (z. Right.color=RED && z.Left.olor=BLACK)
                z.Right.color=BLACK
                z.color=RED
                rotateLeft(z)
                z = x.parent.Left
                z.color=x.parent.color
                x.parent.color=BLACK
                z.Left.color=BLACK
                rotateRight(x.parent)
                x = root
    }
    x.color=.BLACK
```