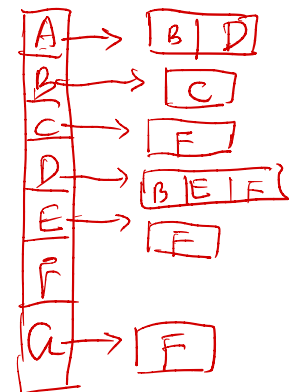
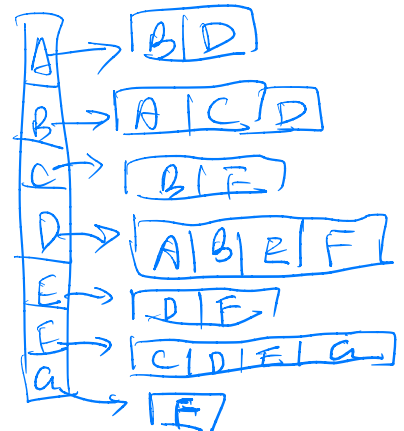
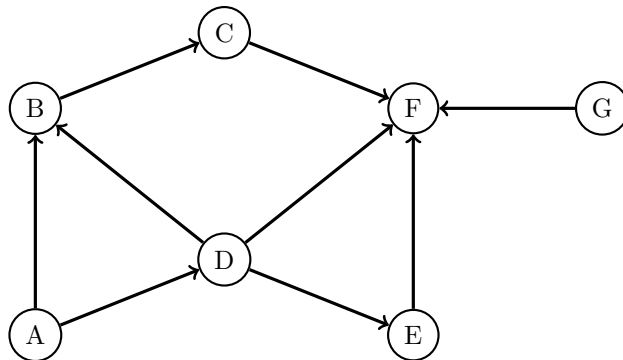


Graphs



- 1.1 Write the graph above as an adjacency matrix, then as an adjacency list. What would be different if the graph were undirected instead?

	A	B	C	D	E	F	G
A	0	1	0	1	0	0	0
B	0	0	1	0	0	0	0
C	0	1	0	0	0	1	0
D	1	1	0	0	1	1	0
E	0	0	0	0	1	1	0
F	0	0	0	0	0	1	1
G	0	0	0	0	0	1	0

	A	B	C	D	E	F	G
A	0	1	0	1	0	0	0
B	0	0	1	0	0	0	0
C	0	1	0	0	0	1	0
D	1	1	0	0	1	1	0
E	0	0	0	0	1	1	0
F	0	0	0	0	0	1	1
G	0	0	0	0	0	1	0

- 1.2 Give the DFS preorder, DFS postorder, and BFS order of the graph traversals starting from vertex A. Break ties alphabetically.

DFS preorder: ABCFDE

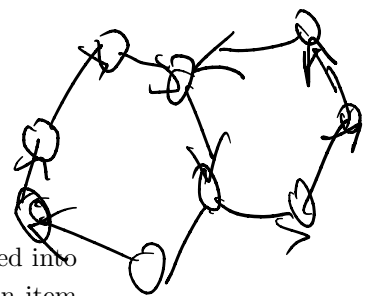
BFS: ABDCEF

DFS postorder: FCBEDA

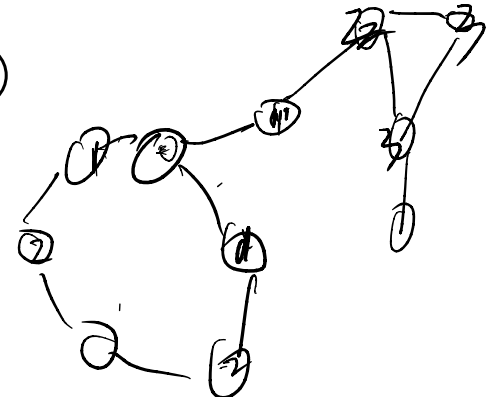
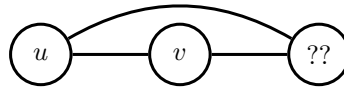
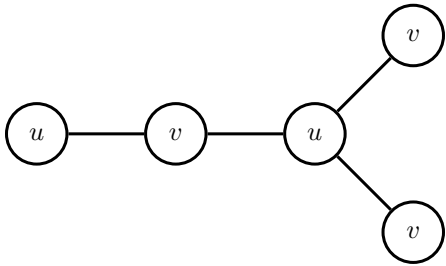
- 1.3 Give a valid topological sort of the graph. (Hint: Consider the reverse postorder of the whole graph.)



Graph Algorithm Design



- 2.1 An undirected graph is said to be bipartite if all of its vertices can be divided into two disjoint sets U and V such that every edge connects an item in U to an item in V . For example below, the graph on the left is bipartite, whereas on the right the graph is not. Provide an algorithm which determines whether or not a graph is bipartite. What is the runtime of your algorithm?



- 2.2 Provide an algorithm that finds the shortest cycle (in terms of the number of edges used) in a directed graph in $O(EV)$ time and $O(E)$ space, assuming $E > V$.

- 2.3 Consider the following implementation of DFS, which contains a crucial error:

```

create the fringe, which is an empty Stack
push the start vertex onto the fringe and mark it
while the fringe is not empty:
    pop a vertex off the fringe and visit it
    for each neighbor of the vertex:
        if neighbor not marked:
            push neighbor onto the fringe
            mark neighbor
  
```

Give an example of a graph where this algorithm may not traverse in DFS order.

