

S.T.F.

$$x(t) = a_0 + \sum_{n=1}^{\infty} \left[ a_n \cos \frac{n\pi t}{2} + b_n \sin \frac{n\pi t}{2} \right]$$

$$a_0 = \frac{1}{T} \int_{t_0}^{t_0+T} f(t) dt \quad b_n = \frac{1}{2} \int_{-2}^2 f(t) dt = \frac{1}{2} \int_{-1}^0 A(t+1) \sin \frac{n\pi}{2} t dt \dots$$

$$= \frac{1}{4} \int_{-2}^2 f(t) dt \quad \dots - \frac{1}{2} \int_0^1 A(t-1) \sin \frac{n\pi}{2} t dt = \frac{A}{2} \left[ \int_{-1}^0 (t+1) \sin \frac{n\pi}{2} t dt - \int_0^1 (t-1) \sin \frac{n\pi}{2} t dt \right]$$

$$= \frac{1}{4} \int_{-1}^0 A(t+1) dt - \frac{1}{4} \int_0^1 A(t-1) dt \quad \begin{matrix} u=t+1; t-1 & dv = \sin \frac{n\pi}{2} t dt \\ du = dt & v = -\frac{2}{\pi n} \cos \frac{n\pi}{2} t \end{matrix}$$

$$= \frac{A}{4} \left[ \frac{t^2}{2} + t \right]_{-1}^0 - \frac{A}{4} \left[ \frac{t^2}{2} - t \right]_{0}^1 - \frac{A}{2} \left[ -\frac{2(t+1)}{\pi n} \cos \frac{n\pi}{2} t \right]_{-1}^0 + \frac{2}{\pi n} \int_{-1}^0 \cos \frac{n\pi}{2} t dt$$

$$= \frac{A}{4} \left[ \frac{1}{2} \right] - \frac{A}{4} \left[ -\frac{1}{2} \right] = \frac{A}{2} \left[ \frac{4}{\pi^2 n^2} \sin \frac{n\pi}{2} \right]_{-1}^0 - \frac{A}{2} \left[ \frac{4}{\pi^2 n^2} \sin \frac{n\pi}{2} \right]_0^1$$

$$a_0 = \frac{A}{8} + \frac{A}{8} = \frac{A}{4} \quad = + \frac{A}{2\pi^2 n^2} \sin \frac{n\pi}{2} - \frac{A}{2\pi^2 n^2} \sin \frac{n\pi}{2} = 0$$

$$x(t) = \frac{A}{4} + \sum_{n=1}^{\infty} \left[ \frac{4A}{n^2 \pi^2} \left( 1 - \cos \frac{n\pi}{2} \right) \cdot \cos \frac{n\pi}{2} t \right]$$

