



Marketing Mix Optimization

Causal Inference in Marketing Science

The webinar will start at:

13:00:00

The current time is:

12:47:30

Central Daylight Time, UTC-5

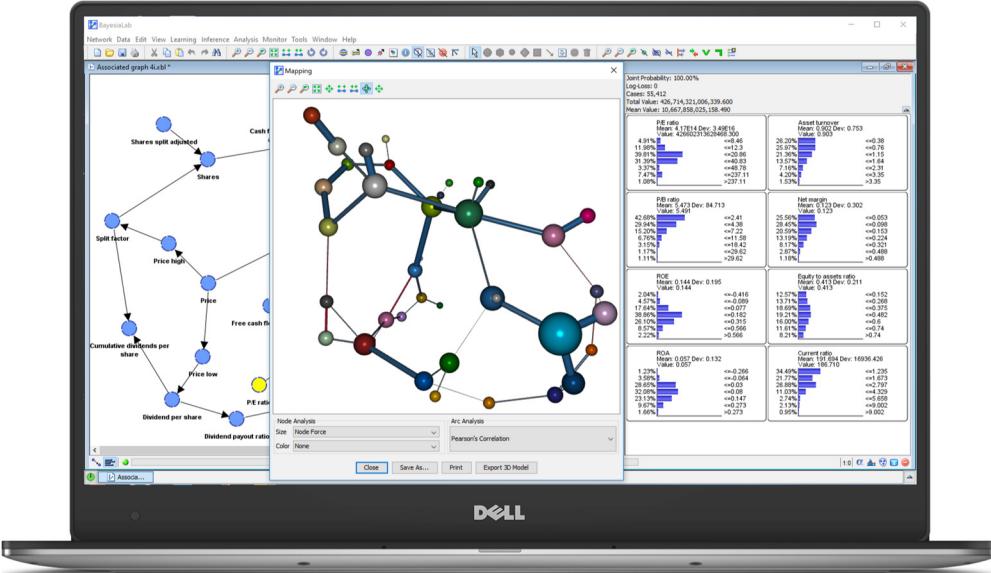


Stefan Conrady

stefan.conrady@bayesia.us



BAYESIALAB



A desktop software for:

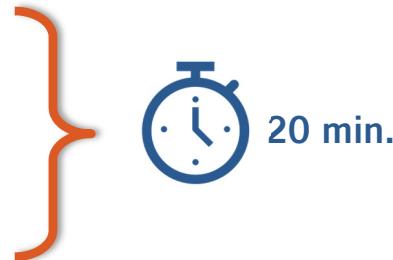
- encoding
- learning
- editing
- performing inference
- analyzing
- simulating
- optimizing

with Bayesian networks.

Today's Program

1. Motivation & Background

- Introductory Example:
The Generic 2000 Commercial
- Simpson's Paradox & Causality

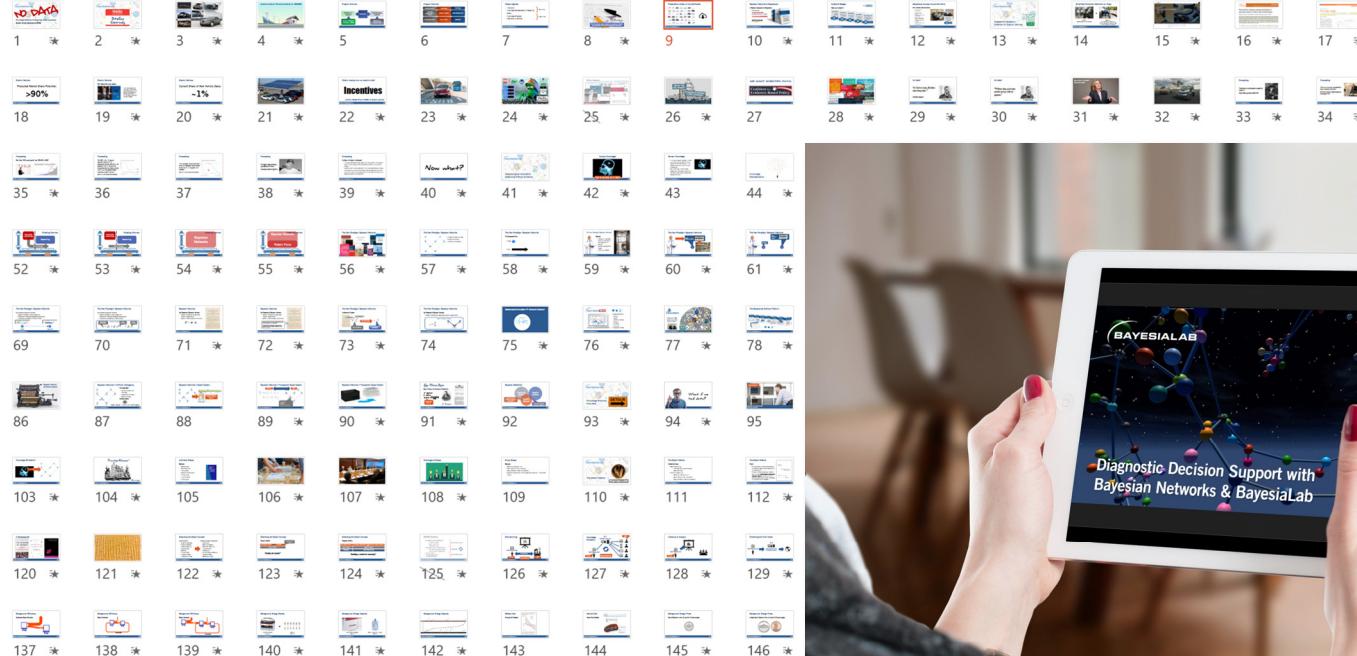


2. Marketing Mix Modeling Workflow

- Causal Assumptions?
- Disjunctive Cause Criterion
- Machine-Learning with BayesiaLab
- Causal Inference & Optimization



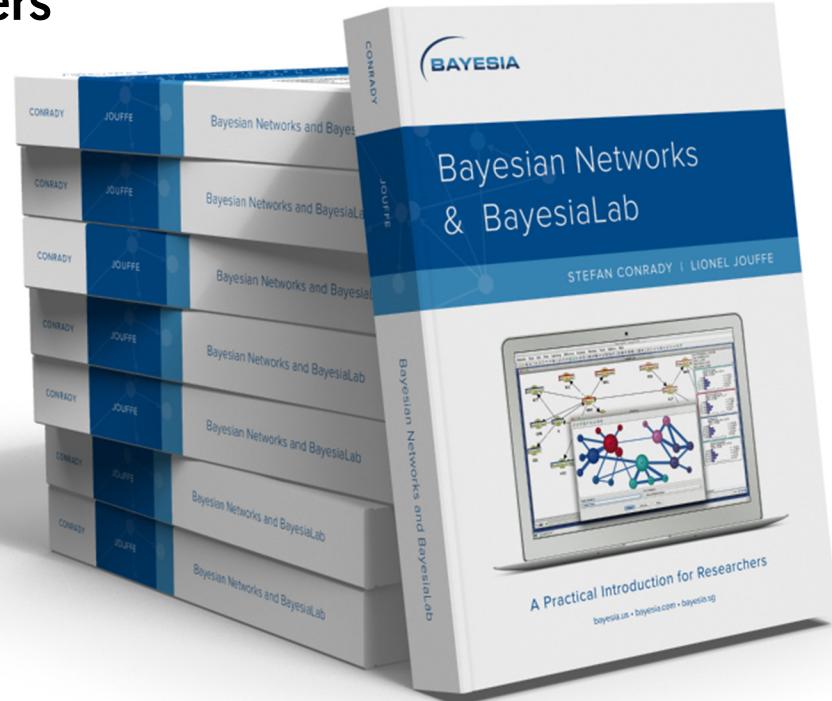
Webinar Slides, Data, and Recording Available



Bayesian Networks & BayesiaLab

A Practical Introduction for Researchers

- Free download:
www.bayesia.com/book
- Hardcopy available on Amazon:
<http://amzn.com/0996533303>



Introductory Example

GENERIC
2000



- The Generic Car Company runs a commercial at the Super Bowl for its new model, the Generic 2000.



- The Generic Car Company runs a commercial at the Super Bowl for its new model, the Generic 2000.



Introductory Example

Telephone Survey

- Afterwards, Generic conducts a telephone survey of 1,000 car shoppers to understand the effect of the Super Bowl commercial on shopping and purchase behavior.



Ad Exposure	Gender	Test Drive	Purchase
0	1	0	0
0	0	1	1
0	1	0	0
0	0	0	0
1	1	0	1
1	1	0	0
		1	1
		1	0
		1	1
		1	0



Introductory Example

Analyzing the survey with a cross-tab...

Ad Exposure	Gender	Test Drive	Purchase
0	1	0	0
0	0	1	1
0	1	0	0
0	0	0	0
1	1	0	1
1	1	0	0
1	0	1	1
0	1	1	0
⋮	⋮	⋮	⋮
0	1	1	0



Ad Exposure	Purchase
No	60%
Yes	45%



-15%

Introductory Example

However, grouping the survey data by Gender reveals:

Ad Exposure	Gender	Test Drive	Purchase
0	1	0	0
0	0	1	1
0	1	0	0
0	0	0	0
1	1	0	1
1	1	0	0
1	0	1	1
0	1	1	0
⋮	⋮	⋮	⋮
0	1	1	0



Gender	Ad Exposure	Purchase
Male	No	30%
	Yes	35%
Female	No	70%
	Yes	75%



Introductory Example

How is this possible?

Ad Exposure	Purchase
No	60%
Yes	45%



Gender	Ad Exposure	Purchase
Male	No	30%
	Yes	35%
Female	No	70%
	Yes	75%



Simpson's Paradox

Simpson's paradox is a phenomenon in probability and statistics, in which an effect appears in subgroups of data but disappears or reverses when these groups are combined.

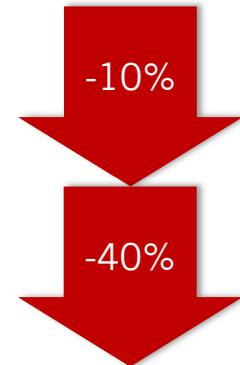
Introductory Example

Grouping the data by Test Drive shows:

Ad Exposure	Gender	Test Drive	Purchase
0	1	0	0
0	0	1	1
0	1	0	0
0	0	0	0
1	1	0	1
1	1	0	0
1	0	1	1
0	1	1	0
⋮	⋮	⋮	⋮
0	1	1	0



Test Drive	Ad Exposure	Purchase
No	No	60%
	Yes	50%
Yes	No	60%
	Yes	30%



Introductory Example

Finally, grouping the data by Gender and Test Drive reveals:

Ad Exposure	Gender	Test Drive	Purchase
0	1	0	0
0	0	1	1
0	1	0	0
0	0	0	0
1	1	0	1
1	1	0	0
1	0	1	1
0	1	1	0
⋮	⋮	⋮	⋮
0	1	1	0



Test Drive	Gender	Ad Exposure	Purchase
No	Male	No	30%
		Yes	40%
	Female	No	70%
		Yes	80%
Yes	Male	No	30%
		Yes	20%
	Female	No	70%
		Yes	60%



So, what's the advertising effect?

Test Drive	Gender	Ad Exposure	Purchase
No	Male	No	30%
		Yes	40%
	Female	No	70%
		Yes	80%
Yes	Male	No	30%
		Yes	20%
	Female	No	70%
		Yes	60%

≈ 0

Gender	Ad Exposure	Purchase
Male	No	30%
	Yes	35%
Female	No	70%
	Yes	75%

Ad Exposure	Purchase
No	-0.15
Yes	45%

Test Drive	Ad Exposure	Purchase
No	No	60%
	Yes	50%
Yes	No	60%
	Yes	30%

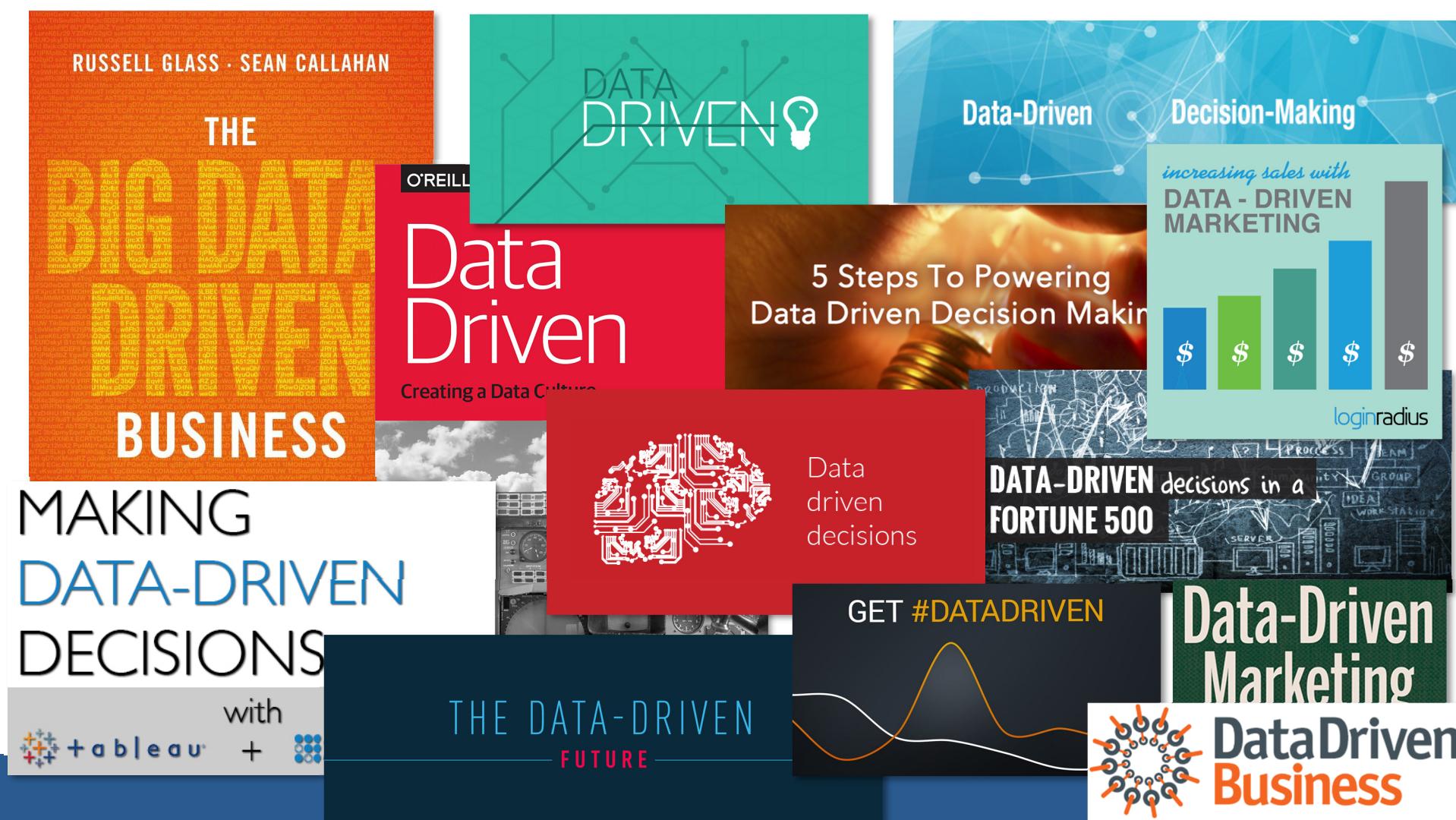
-0.2



Your Opinion?

Did this commercial have a positive or negative effect on purchase?





Introductory Example

$$\text{Purchase} = -0.15 \cdot \text{Ad Exposure} + 0.6 \quad (R^2 = 0.02)$$

-0.15

$$\text{Purchase} = 0.05 \cdot \text{Ad Exposure} + 0.4 \cdot \text{Gender} + 0.3 \quad (R^2 = 0.14)$$

+0.05

$$\text{Purchase} = -0.2 \cdot \text{Ad Exposure} - 0.1 \cdot \text{Test Drive} + 0.67 \quad (R^2 = 0.03)$$

-0.2

$$\text{Purchase} = 0.001 \cdot \text{Ad Exposure} + 0.4 \cdot \text{Gender} - 0.1 \cdot \text{Test Drive} + 0.37 \quad (R^2 = 0.15)$$

≈ 0

$$y=f(x)$$

Observational vs. Causal Inference

$$y=f(x)$$

ambiguous



Observational Inference (Prediction)

$$y=f(\text{see}(x))$$

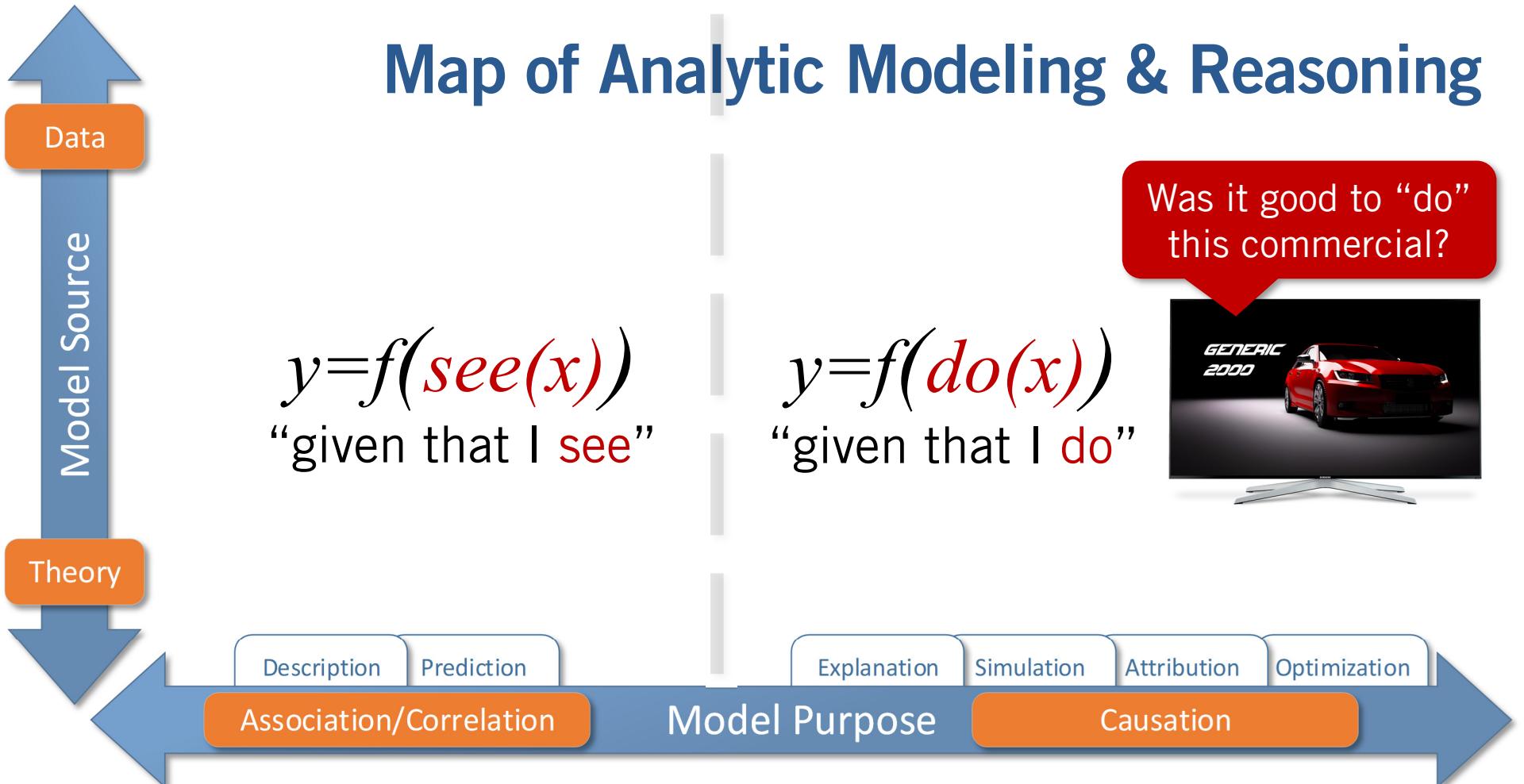
“given that I see”

Causal Inference (Intervention)

$$y=f(\text{do}(x))$$

“given that I do”

Map of Analytic Modeling & Reasoning



So, what's the additive effect?

“given that I see”

Test Drive	Gender	Ad Exposure	Purchase
No	Male	No	30%
		Yes	40%
	Female	No	70%
		Yes	80%
Yes	Male	No	30%
		Yes	20%
	Female	No	70%
		Yes	60%

≈ 0

“given that I see”

Test Drive	Gender	Ad Exposure	Purchase
No	Male	No	60%
		Yes	50%
Yes	Female	No	60%
		Yes	30%

-0.2

“given that I see”

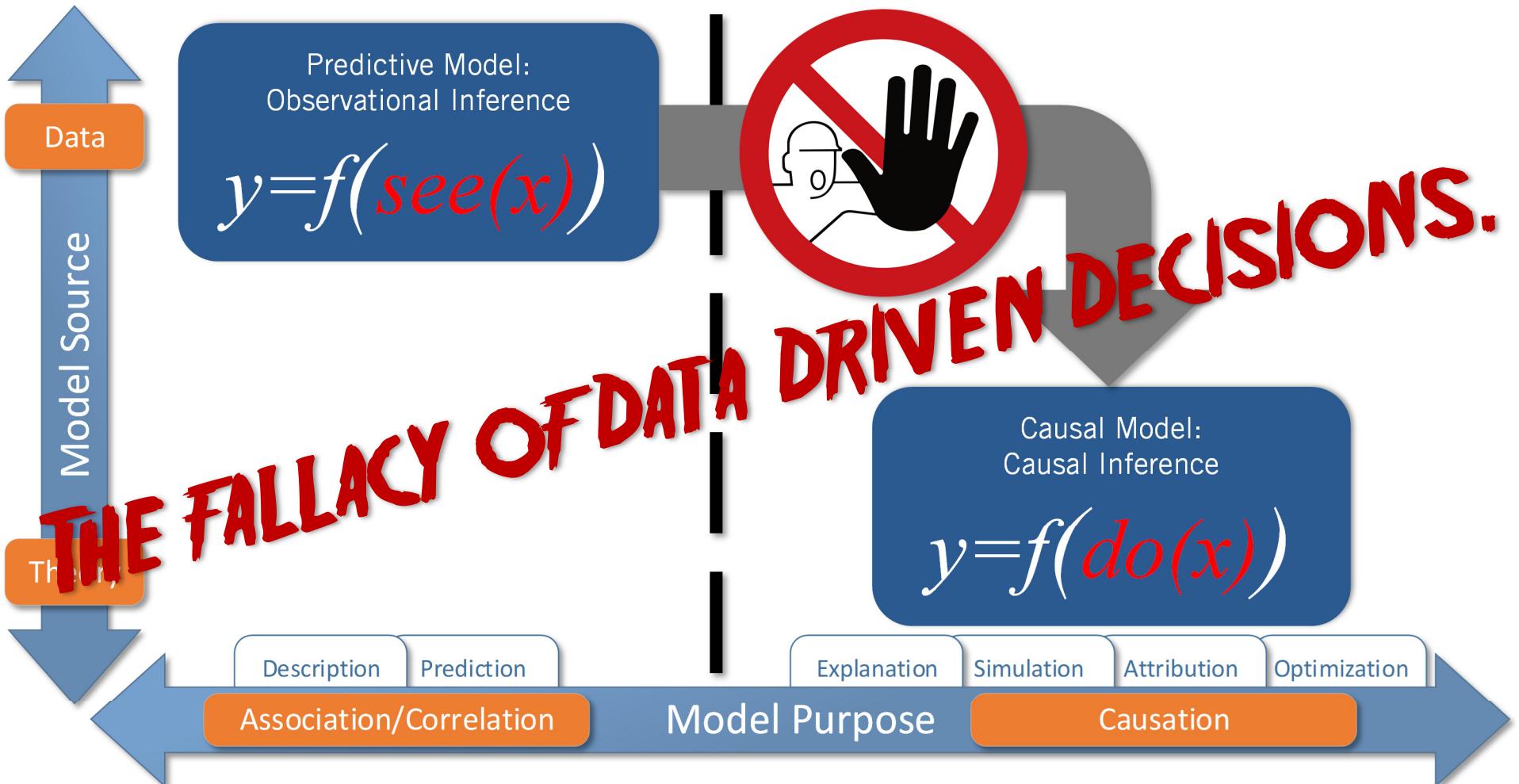
Gender	Ad Exposure	Purchase
Male	No	30%
	Yes	35%
Female	No	70%
	Yes	75%

+0.05

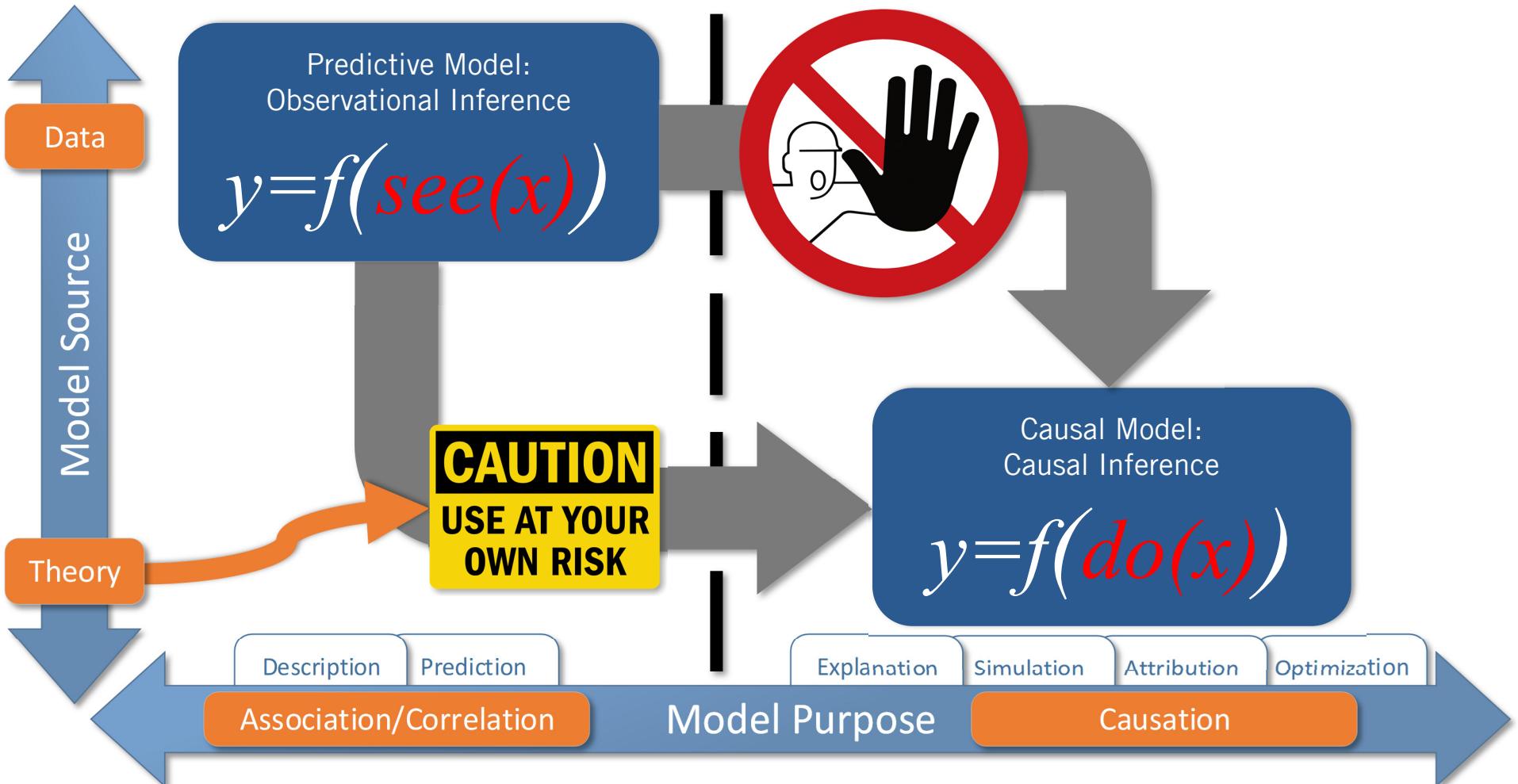
Ad Exposure	Purchase
No	60%
Yes	45%

-0.15

“given that I see”



Once upon a time. . .



Map of Analytic Modeling & Reasoning

Data

Model Source

Theory

Bayesian Networks

Description

Prediction

Explanation

Simulation

Attribution

Optimization

Association/Correlation

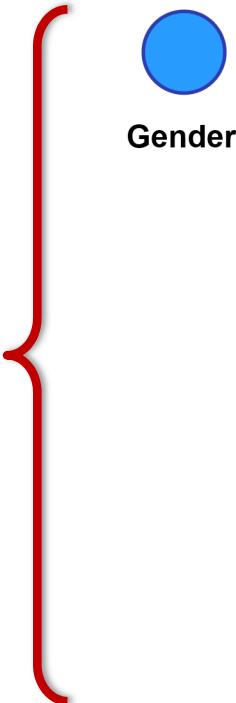
Model Purpose

Causation

Introductory Example

Develop Theory

What's the story here?



Gender



Ad Exposure



Test Drive



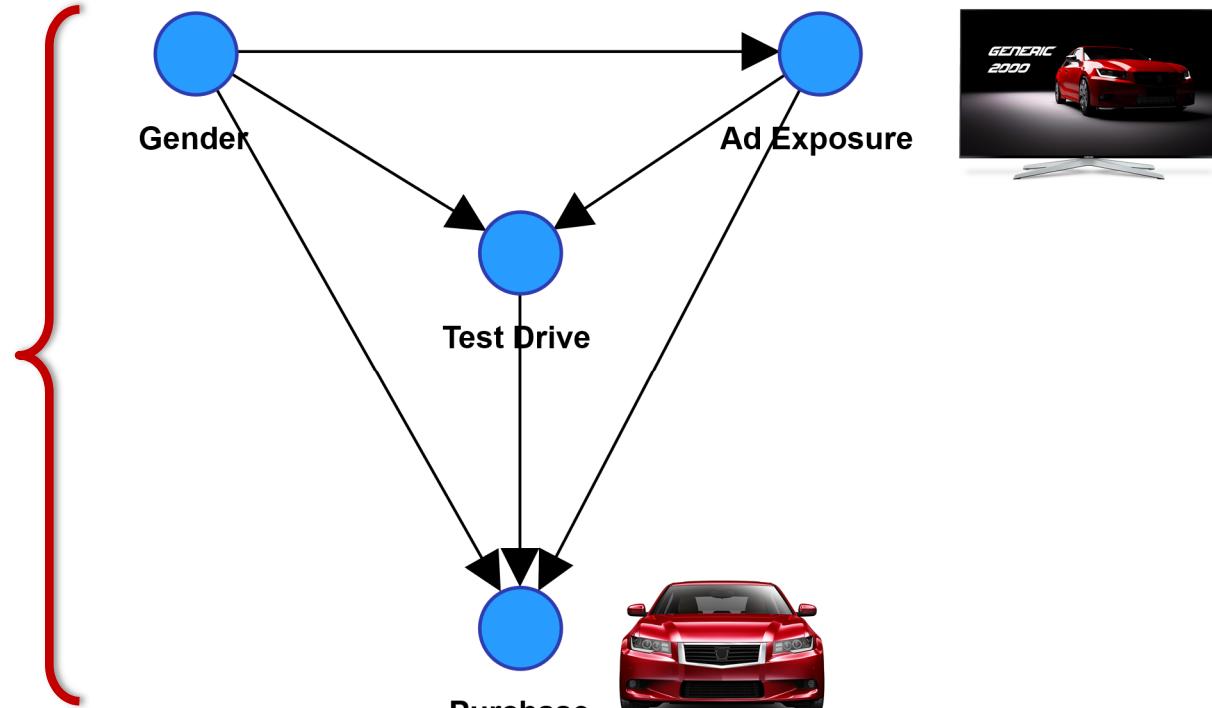
Purchase



Introductory Example

Our Theory!

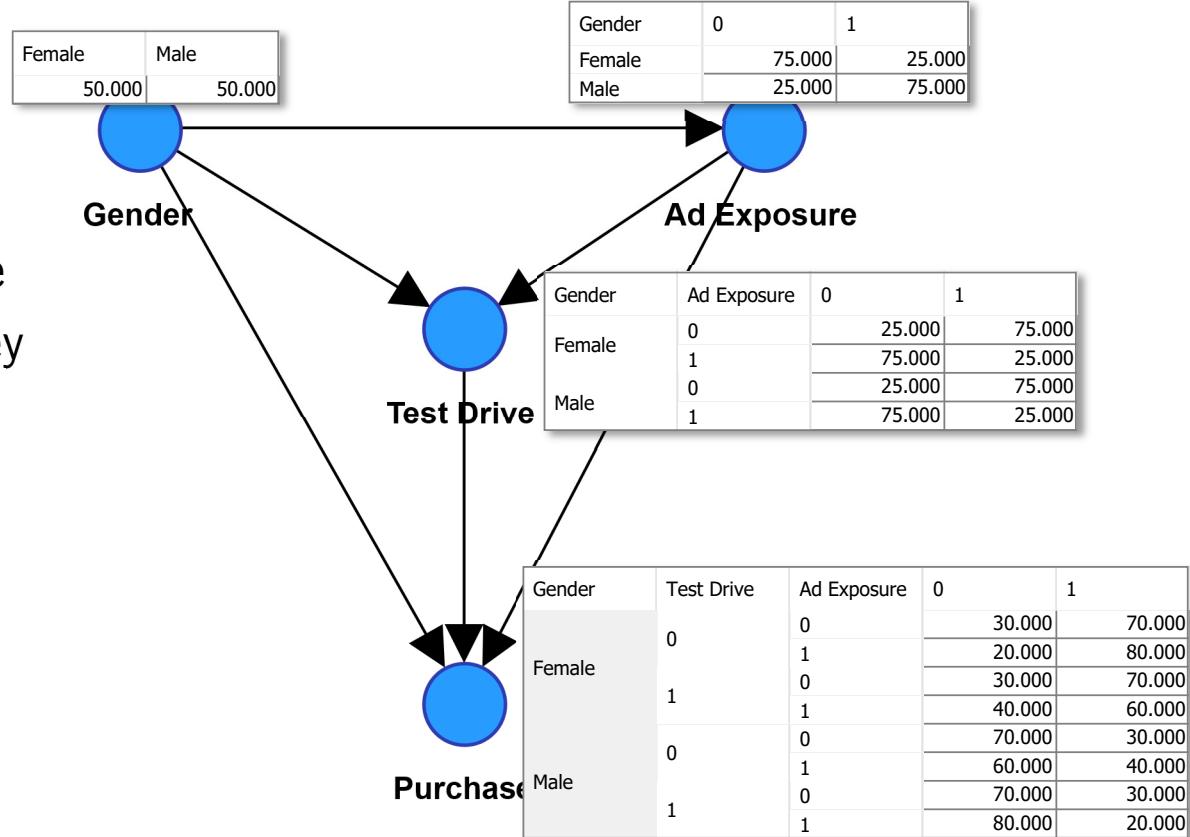
That's the story! Now we have the qualitative part of a causal Bayesian network.



Introductory Example

“Parameters”

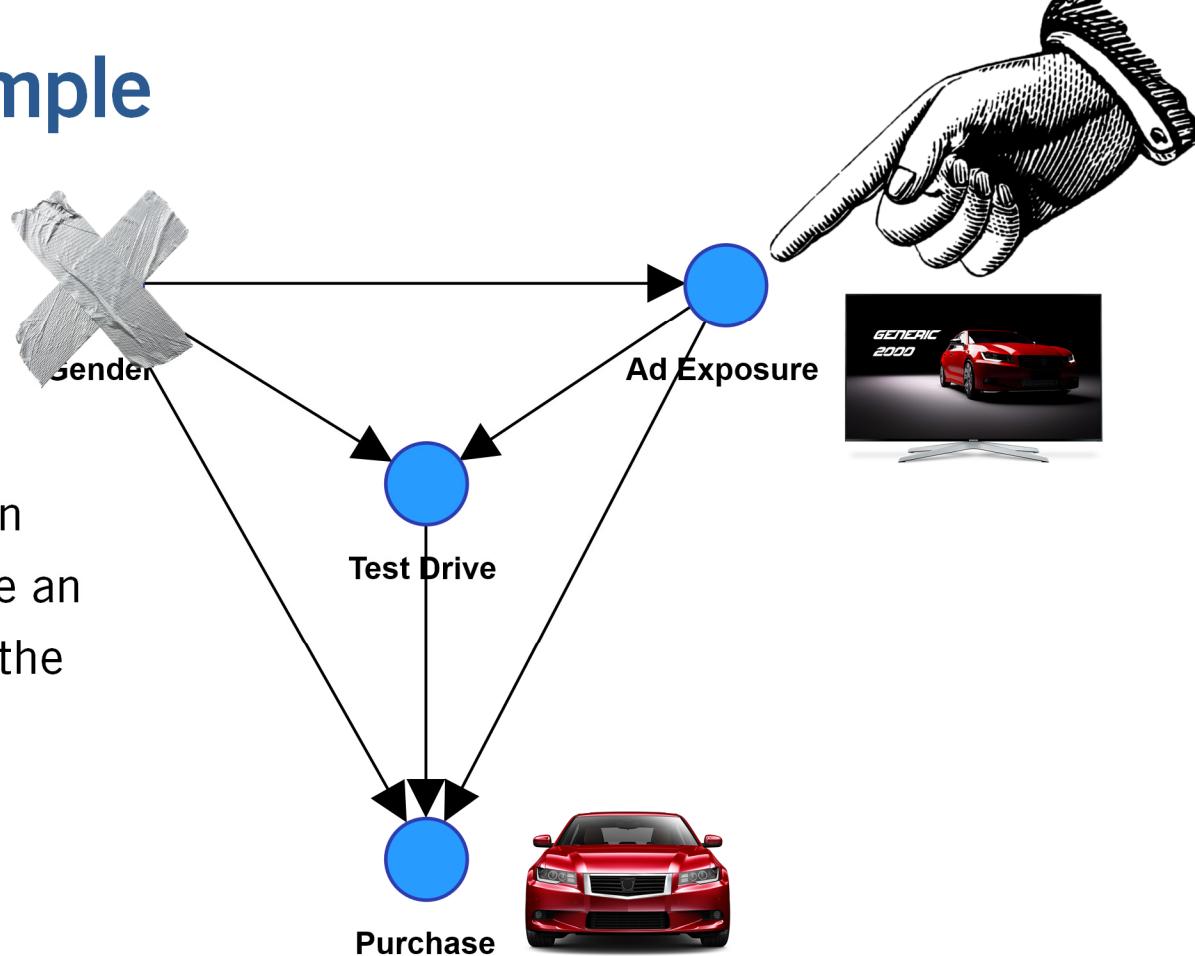
- We can estimate the quantitative part of the network from the survey data.
- As a result, we have a Bayesian network, which we can use for inference.



Introductory Example

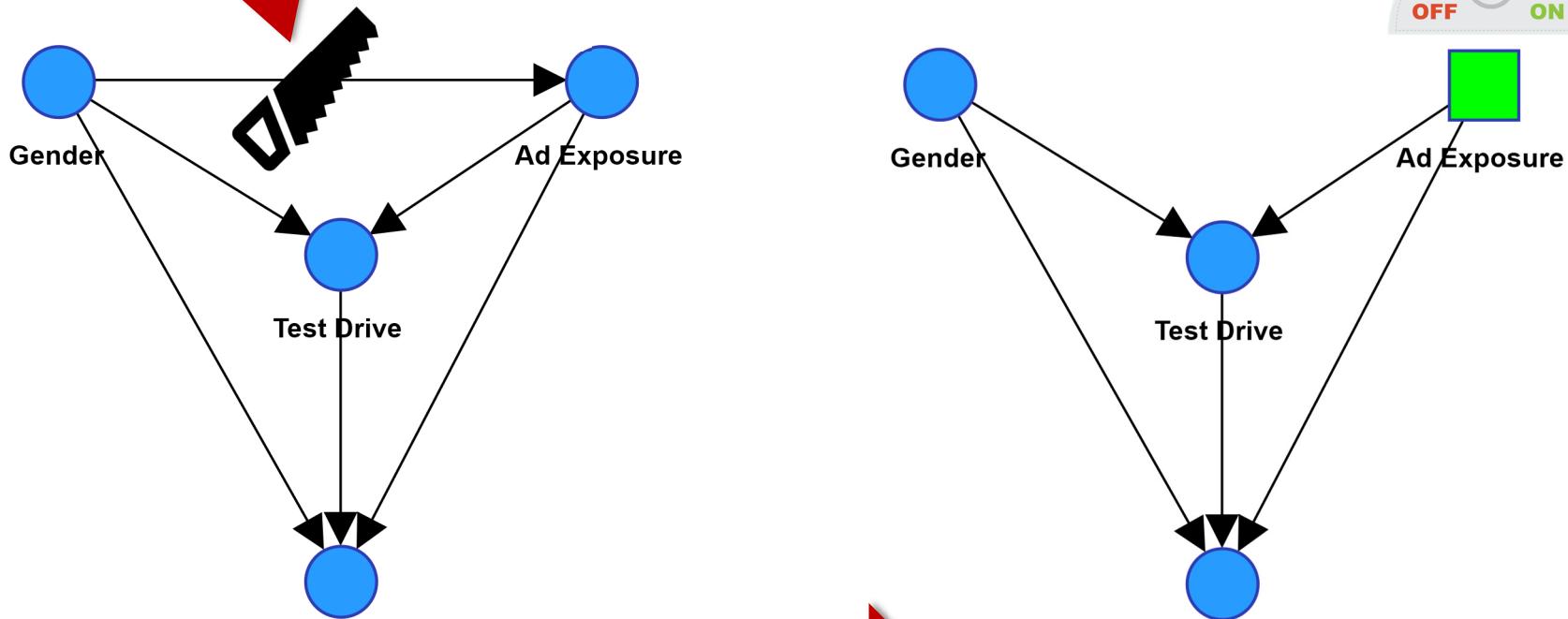
Our “Model of the World”

- How can we obtain the effect of Ad Exposure?
- With this causal Bayesian network, we can simulate an intervention to estimate the causal effect.



Introductory Example

Causal Model → “Graph Surgery” → Intervention Model



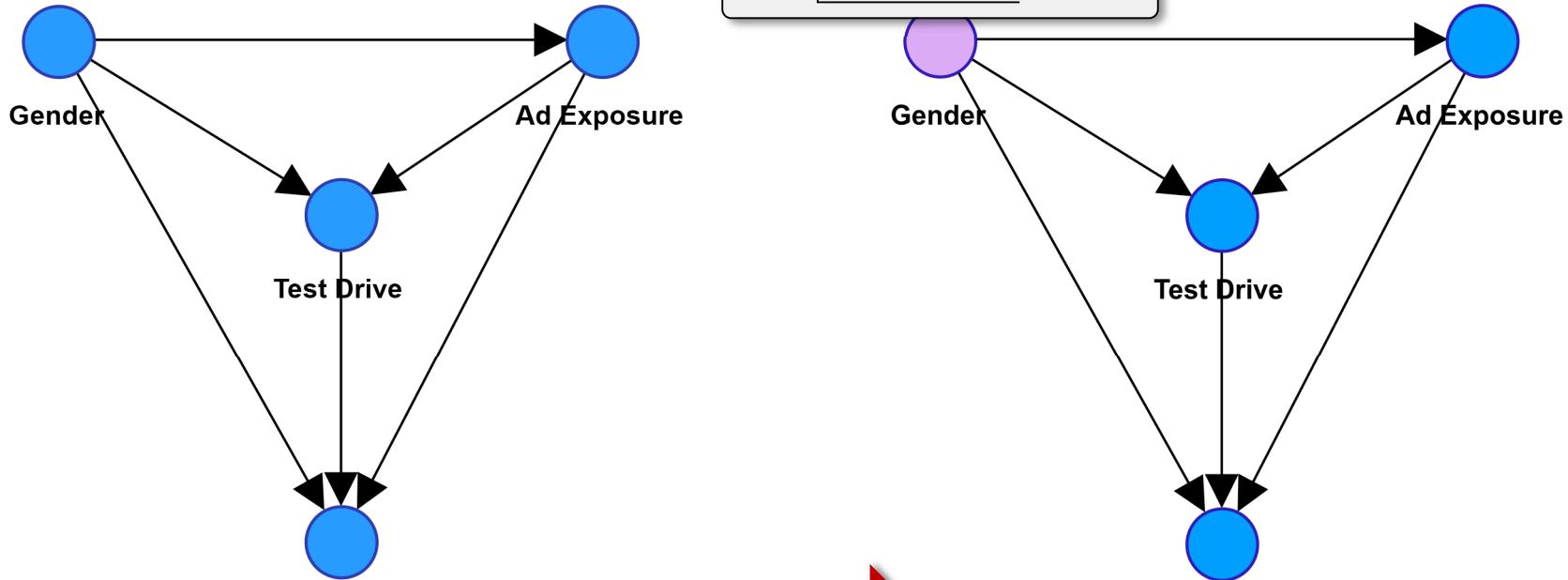
Causal Model

Intervention Model

Introductory Example

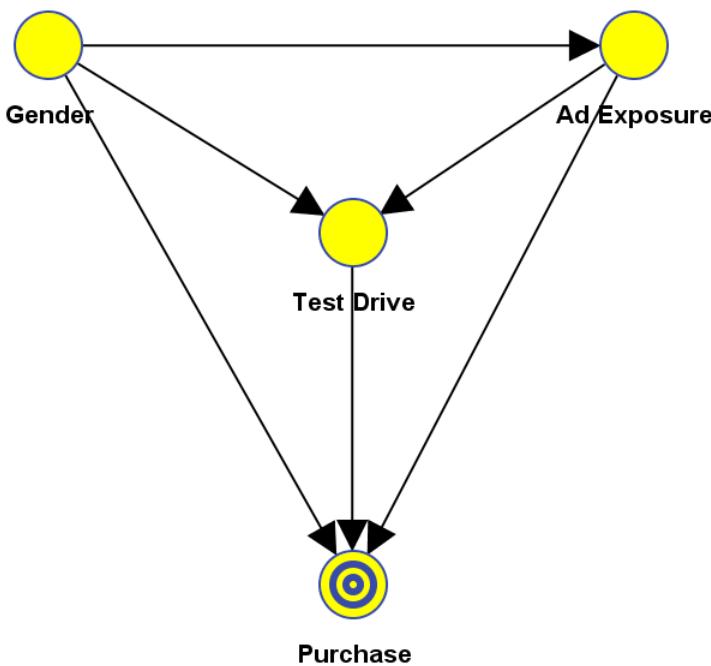
Fix Probabilities with
Likelihood Matching

Causal Inference: Simulating an



Causal Model

Intervention Model



Joint Probability: 100.00%
Log-Loss: 0
Cases: 100,000
Total Value: 1.525
Mean Value: 0.508

Gender

50.00%

50.00%

Intervention Node

Ad Exposure

Mean: 0.500 Dev: 0.500
Value: 0.500

50.00%

50.00%

0
1

Test Drive

Mean: 0.500 Dev: 0.500
Value: 0.500

50.00%

50.00%

0
1

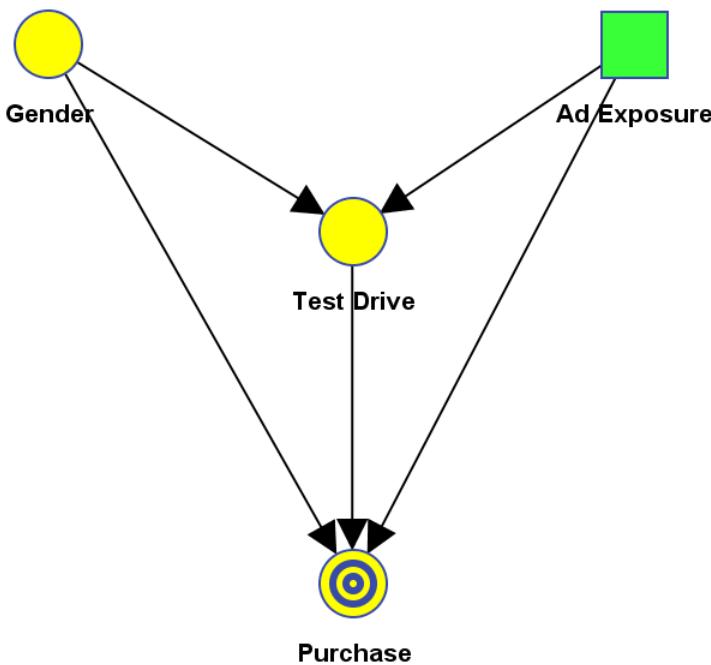
Purchase

Mean: 0.525 Dev: 0.499
Value: 0.525

47.50%

52.50%

0
1



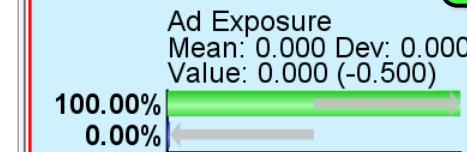
Joint Probability: 50.00%
Log-Loss: 1
Cases: 50,000
Total Value: 1.250
Mean Value: 0.417

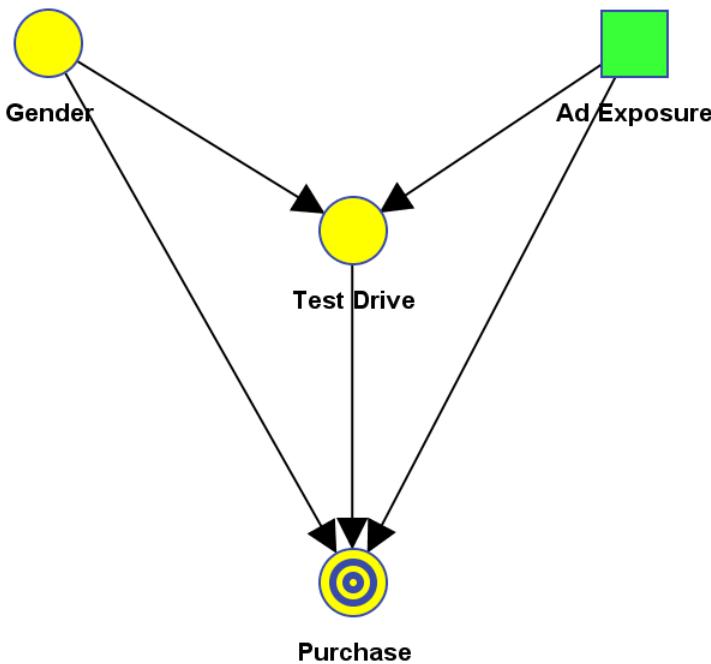
Gender



Female

Intervention





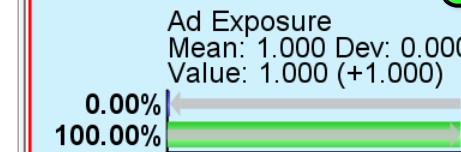
Joint Probability: 50.00%
Log-Loss: 1
Cases: 50,000
Total Value: 1.800
Mean Value: 0.600

Gender



Female

Intervention



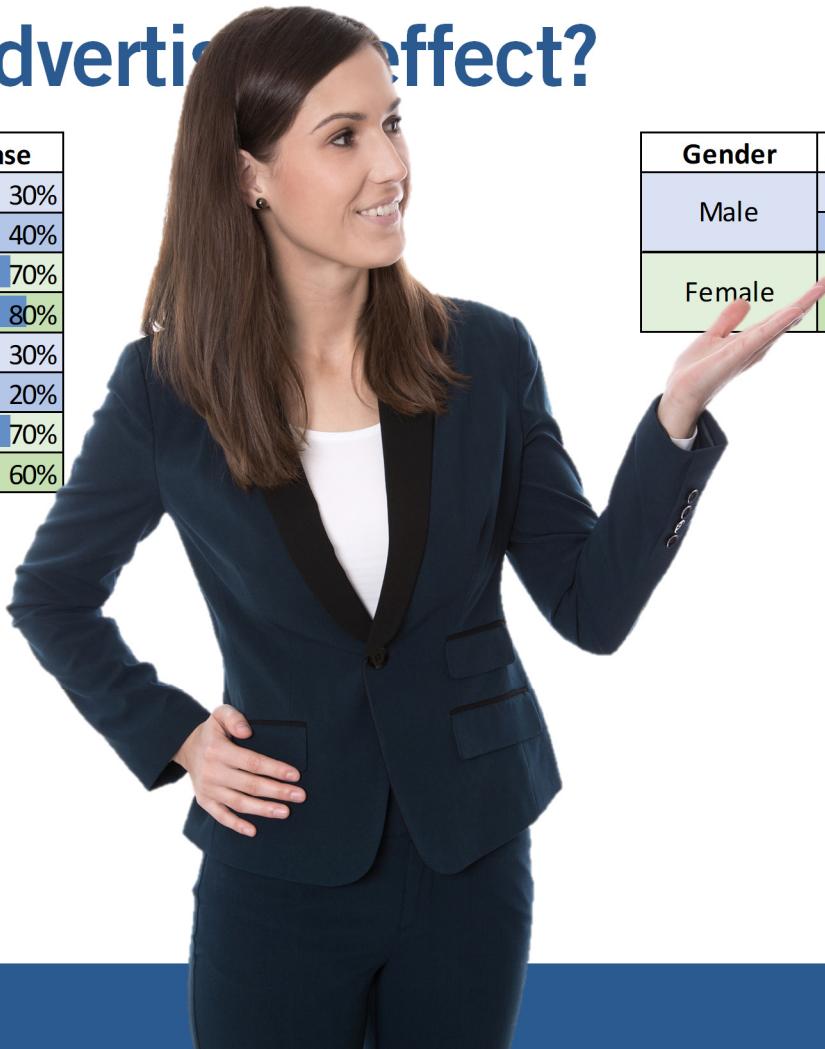
Effect



So, what's the advertising effect?

Test Drive	Gender	Ad Exposure	Purchase
No	Male	No	30%
		Yes	40%
	Female	No	70%
		Yes	80%
Yes	Male	No	30%
		Yes	20%
	Female	No	70%
		Yes	60%

≈ 0



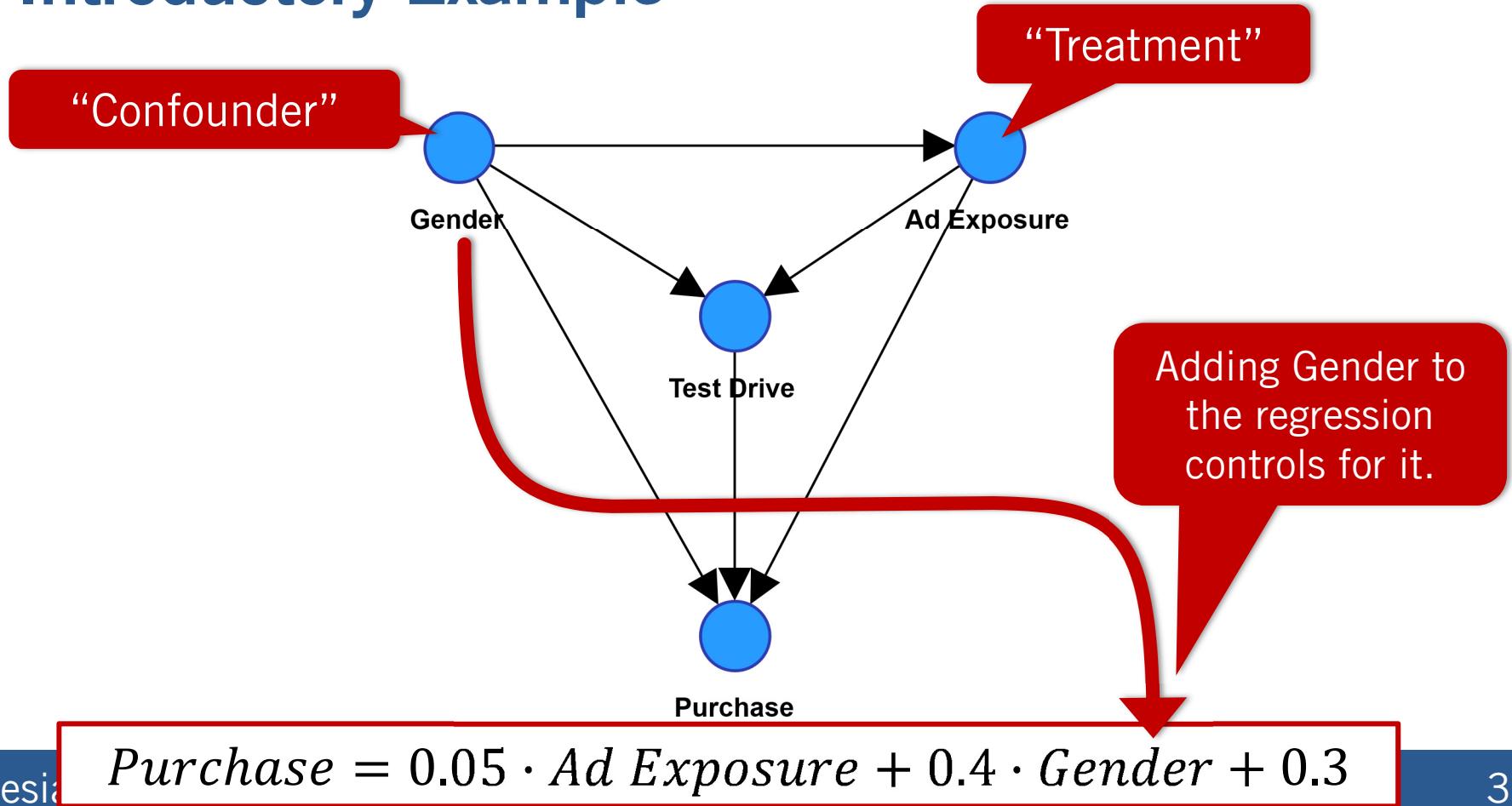
Gender	Ad Exposure	Purchase
Male	No	30%
	Yes	35%
Female	No	70%
	Yes	75%

Ad Exposure	Purchase
No	-0.15
Yes	45%

Test Drive	Ad Exposure	Purchase
No	No	60%
	Yes	50%
Yes	No	60%
	Yes	30%

-0.2

Introductory Example



A photograph showing a row of modern SUVs parked in a lot. The cars are arranged in a staggered pattern, with their front ends facing towards the left. They come in various colors, including black, white, and grey. In the background, there is a long, low-profile building with a red facade. On the side of the building, the words "ACME GENERIC AUTO CENTER" are written in large, white, sans-serif letters.

ACME GENERIC
AUTO CENTER





J. Wanamaker



H. Ford



J.C. Penney

I know I waste half of my advertising dollars; I just wish I knew which half.

Marketing Mix Optimization

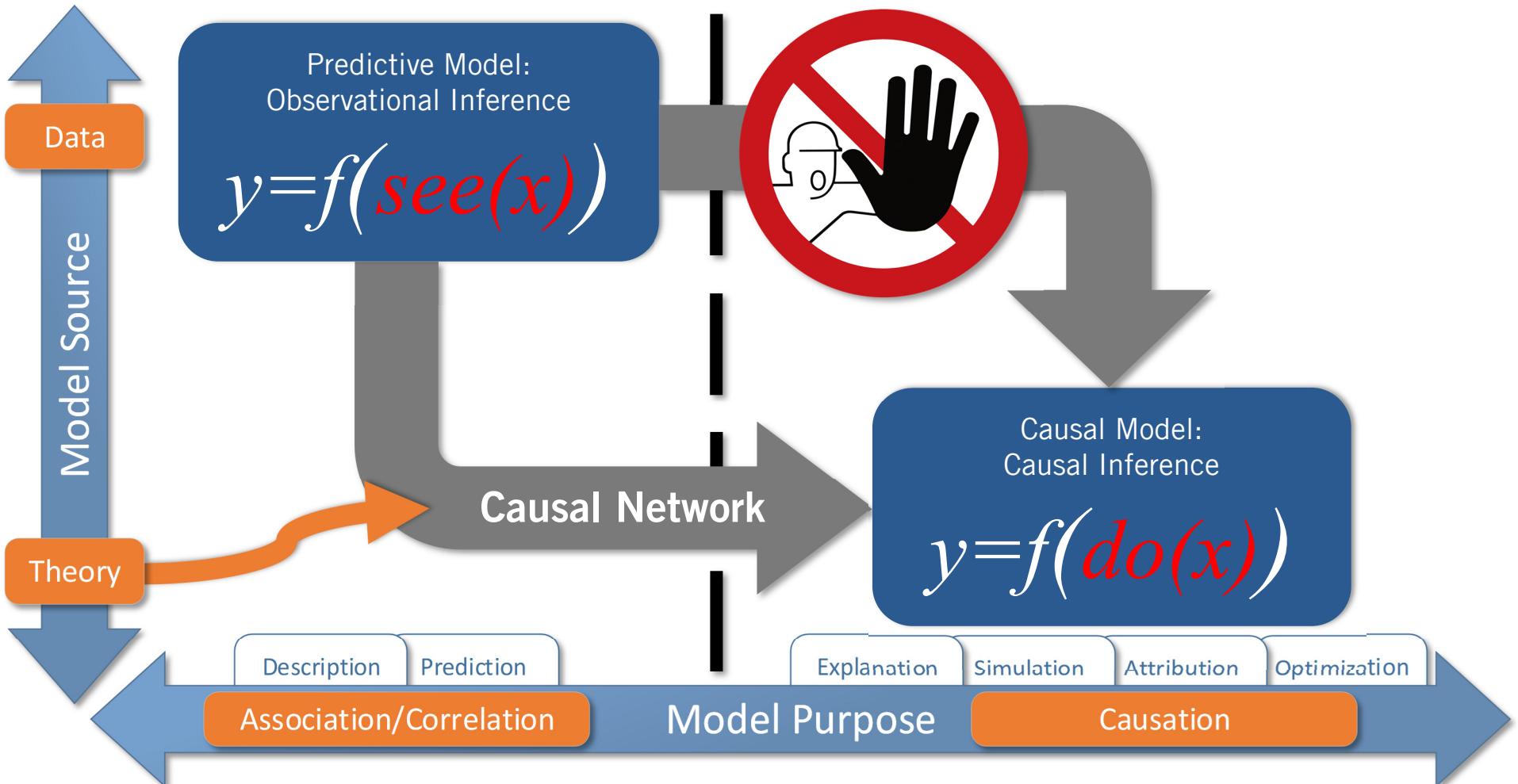
ACME GENERIC
AUTO CENTER

Objective

- Maximize sales within a given marketing budget.

Historical Sales & Media Data

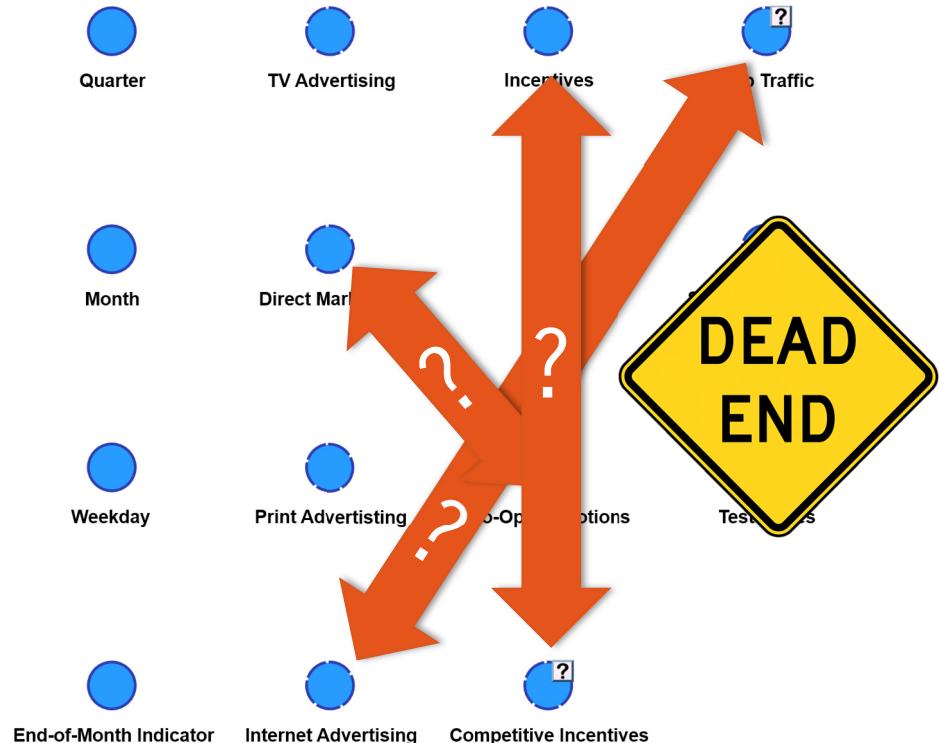
- | | | |
|--------------------------|------------------------|--------------------------|
| • Quarter | • Direct Marketing | • Co-Op Promotions |
| • Month | • Print Advertising | • Competitive Incentives |
| • Weekday | • Internet Advertising | • Web Traffic |
| • End-of-Month Indicator | • Incentives | • Showroom Traffic |
| • TV Advertising | • Sales | • Test Drives |

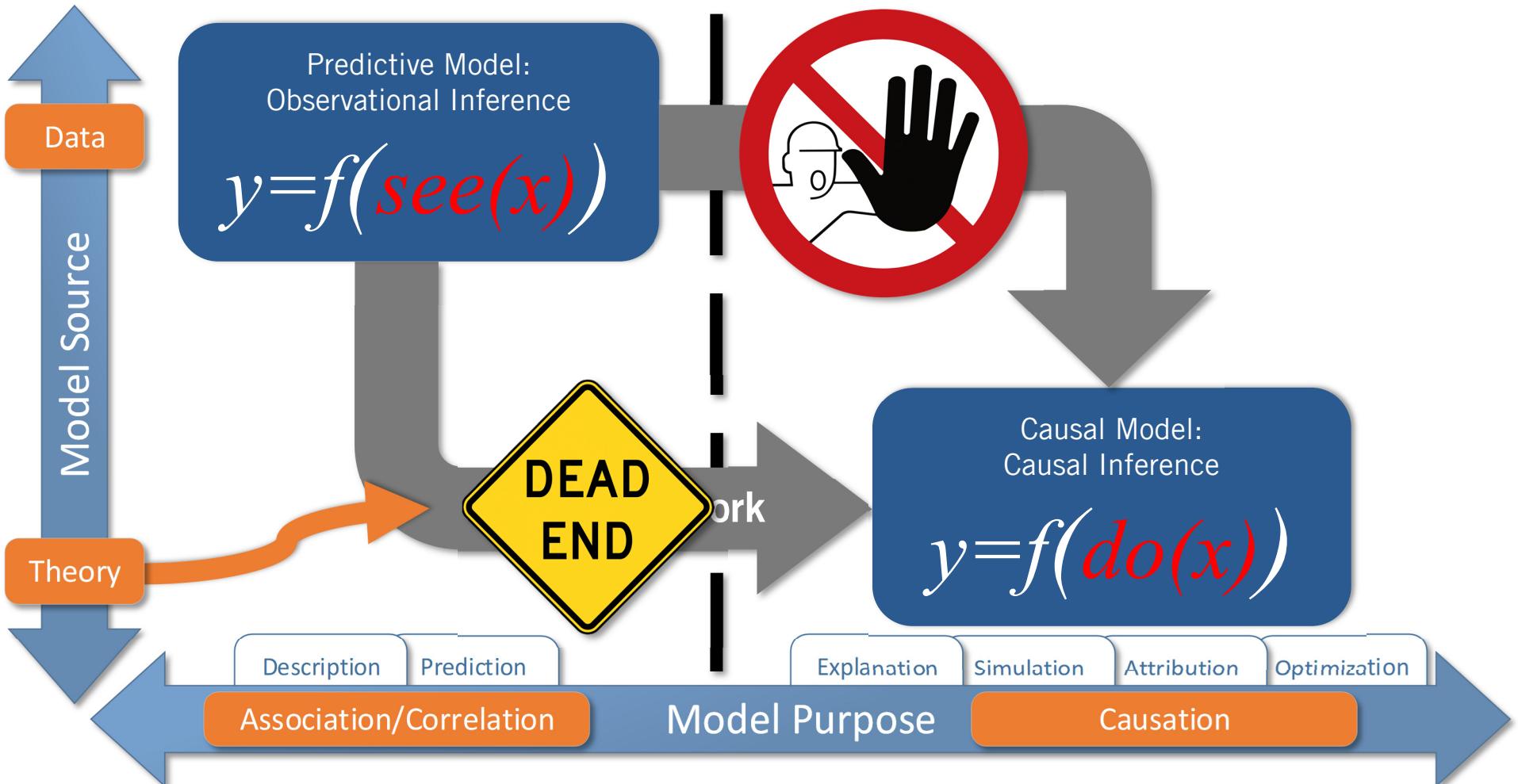


Marketing Mix Optimization

Causal Assumptions?

- Recall: Causal inference requires causal assumptions, e.g., a causal networks!
- But, given the number of variables, there are 2.38×10^{41} possible causal network graphs!
- Causal directions are not always obvious.





Now What?

We need a different
kind of theory



Disjunctive Cause Criterion



NIH Public Access Author Manuscript

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Biometrics. 2011 December ; 67(4): 1406–1413. doi:10.1111/j.1541-0420.2011.01619.x.

A new criterion for confounder selection

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Abstract

We propose a new criterion for confounder selection when the underlying causal structure is unknown and only limited knowledge is available. We assume all covariates being considered are pretreatment variables and that for each covariate it is known (i) whether the covariate is a cause of treatment, and (ii) whether the covariate is a cause of the outcome. The causal relationships the covariates have with one another is assumed unknown. We propose that control be made for any covariate that is either a cause of treatment or of the outcome or both. We show that irrespective of the actual underlying causal structure, if any subset of the observed covariates suffices to control

Disjunctive Cause Criterion

VanderWeele and Shpitser (2011)

- “We propose that control be made for any [pre-treatment] **covariate** that is either a cause of **treatment** or of the **outcome** or both.”

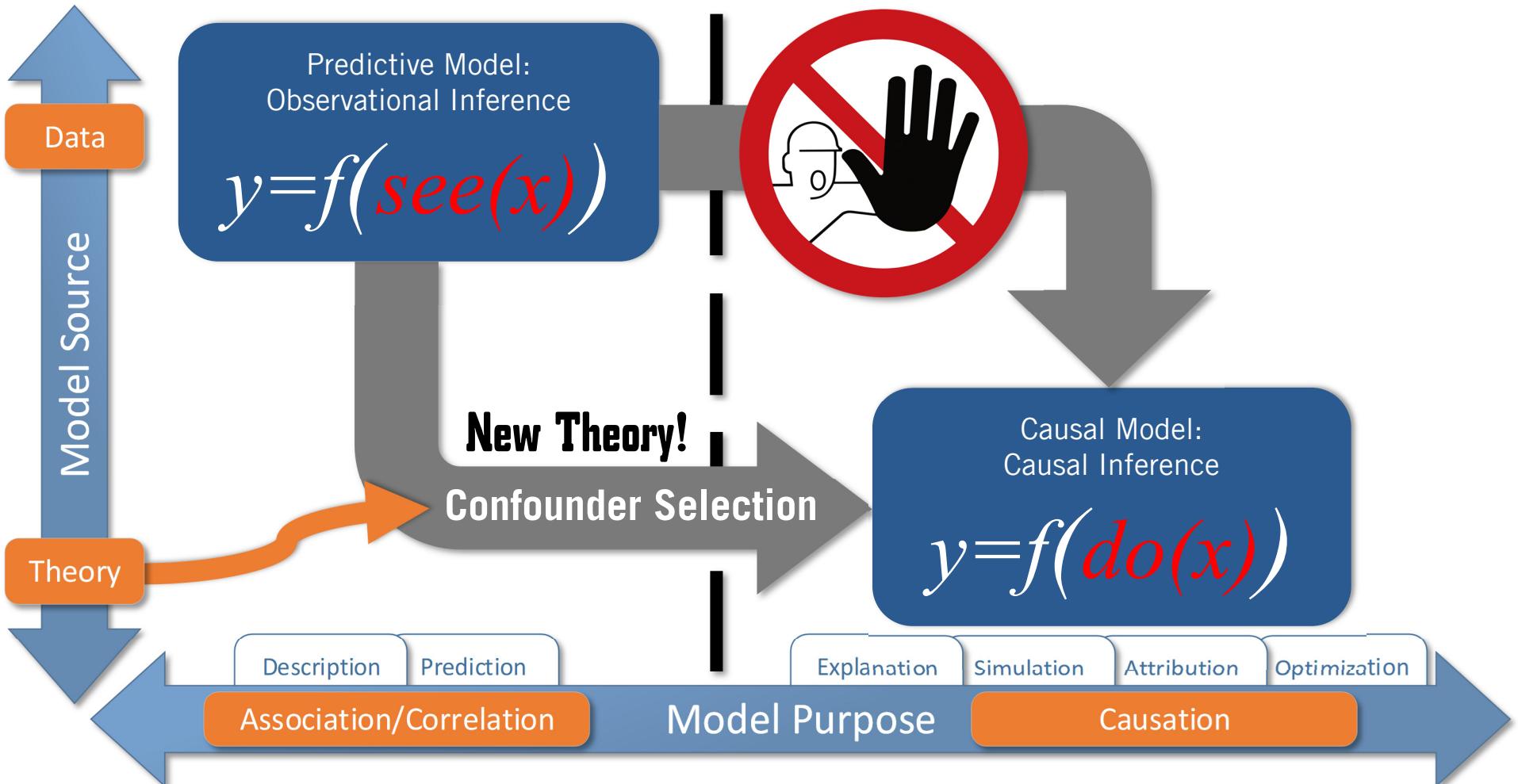
Confounder

Advertisement

Sales

Implementation in BayesiaLab:
Likelihood Matching on Confounders in
Direct Effects Analysis
→ Causal Effect, i.e., the Advertising Effect

IMPORTANT ASSUMPTION:
NO UNOBSERVED CONFOUNDERS



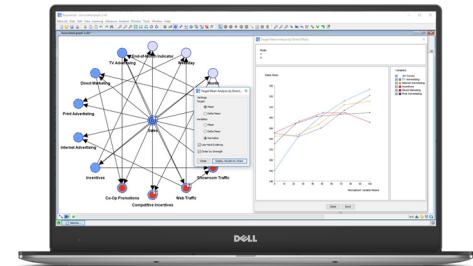
Marketing Mix Optimization



All Data is Synthetic

Proposed Workflow

- Import historical sales and marketing data.
- Machine-learn a predictive model with BayesiaLab.
- Determine **Confounders** vs. **Non-Confounders**, using the **Disjunctive Cause Criterion**.
- Estimate and evaluate **Direct Effects** response curves.
- Introduce **Function Node** and assign media costs.
- Perform **Genetic Target Optimization**.
- Apply **Network Temporalization**.
- Add **Constraint Nodes** between t and $t-1$ marketing variables.
- Perform **Genetic Target Optimization** on dynamic network.





Data Import

Define Data Structure

Separators

Tab Semicolon Comma
 Space Other

Encoding

UTF-8

Missing Values

N/R
NR
NC

Filtered Values

VF
FV
N/A

Sampling

Define Sample

Learning/Test

Define Learning/Test Sets

Options

Title Line
 End of Line Character
 Consider Identical Consecutive separators as a Unique One
 Consider Different Consecutive Separators as a Unique One
 Double Quote as String Delimiters
 Single Quote as String Delimiters
 Transpose

Data

Quarter	Month	Weekday	End-of-Mo...	TV Adverti...	Direct Mar...	Print Adve...	Internet A...	Incentives	Sales
1	1	2	0	33.3727461...	46.2795596...	18.8143290...	14.1863730...	25.4659327...	325.518332
1	1	3	0	39.2201805...	50.6651354...	22.1766038...	17.1100902...	32.7752257...	325.518332
1	1	4	0	0.58483979...	21.6886298...	9.96128288...	7.79241989...	10.3516514...	99.6351953
1	1	5	0	21.2813211...	37.2109908...	31.8617596...	47.2109908...	7.80920491...	235.482011
1	1	6	0	19.2473639...	6.69831269...	28.4687063...	16.6983126...	12.5090584...	212.640317
1	1	7	0	23.0072467...	35.6855229...	20.6922342...	27.1236819...	18.5672537...	279.775215
1	1	1	0	13.7276643...	38.5054350...	12.8541668...	9.00362336...	44.5352183...	217.120784
1	1	2	0	3.16579608...	31.5457482...	7.51840698...	4.36383216...	34.4188431...	103.703461
1	1	3	0	8.58478816...	23.6243470...	4.15482878...	1.79239408...	27.9639347...	109.988720
1	1	4	0	49.0430109...	27.6885911...	34.7903646...	32.0215054...	31.6578220...	318.555398
1	1	5	0	48.0059201...	58.0322582...	47.3061859...	49.6942371...	25.7330030...	355.061154
1	1	6	0	29.3288059...	57.2544401...	55.5216020...	29.3500379...	42.5981801...	339.772321

< >

Cancel Previous Next Save Finish

Data Import Wizard



Data Import

Define Variable Type

Type	Action	Information
<input type="radio"/> Not Distributed	Columns with Missing Values	Number of Rows 16801 100.00%
<input checked="" type="radio"/> Discrete	All not Distributed	Not Distributed 0 0.00%
<input type="radio"/> Continuous	All Discrete	Discrete 4 26.67%
<input type="radio"/> Weight	All Continuous	Continuous 11 73.33%
<input type="radio"/> Learning/Test		Others 0 0.00%
<input type="radio"/> Row Identifier		Missing Values 6 0.00%
		Filtered Values 0 0.00%

Data

Quarter	Month	Weekday	End-of-Mo...	TV Adverti...	Direct Mar...	Print Adve...	Internet A...	Incentives	Sales
1	1	2	0	33.3727461...	46.2795596...	18.8143290...	14.1863730...	25.4659327...	325.518332
1	1	3	0	39.2201805...	50.6651354...	22.1766038...	17.1100902...	32.7752257...	325.518332
1	1	4	0	0.58483979...	21.6886298...	9.79241989...	10.3516514...	99.6351953	
1	1	5	0	21.2813211...	37.2109908...	31.8617596...	47.2109908...	7.80920491...	235.482011
1	1	6	0	19.2473639...	6.69831269...	28.4687063...	16.6983126...	12.5090584...	212.640317
1	1	7	0	23.0072467...	35.66515229...	20.6922342...	27.1236819...	18.5672537...	279.775215
1	1	1	0	13.7276643...	38.5054350...	12.8541668...	9.00362336...	44.5352183...	217.120764
1	1	2	0	3.16579608...	31.5457482...	7.51840698...	4.36383216...	34.4188431...	103.703461
1	1	3	0	8.58478816...	23.6243470...	4.15482878...	1.79239408...	27.9639347...	109.988720
1	1	4	0	49.0430109...	27.6885911...	34.7903646...	32.0215054...	31.6578220...	318.555398
1	1	5	0	48.0059201...	58.0322582...	47.3061859...	49.6942371...	25.7330030...	355.061154
1	1	6	0	29.3288059...	57.2544401...	55.5216020...	29.3500379...	42.5981801...	339.772321
1	1	7	0	44.4346604...	43.2466044...	10.5580191...	32.0630377...	48.8700524...	304.693249
1	1	1	0	29.1636534...	54.5759953...	17.5206372...	12.6097153...	36.6784392...	287.837859

Buttons: Cancel Previous Next Save Finish

Variable Type Definition



Data Import

Data Selection and Filtering

Missing Value Processing

Filter
 OR
 AND
 Replace by :
 Value
 Mean/Modal
 Infer
 Static Imputation
 Dynamic Imputation
 Structural EM
 Entropy-Based Static Imputation
 Entropy-Based Dynamic Imputation

Information

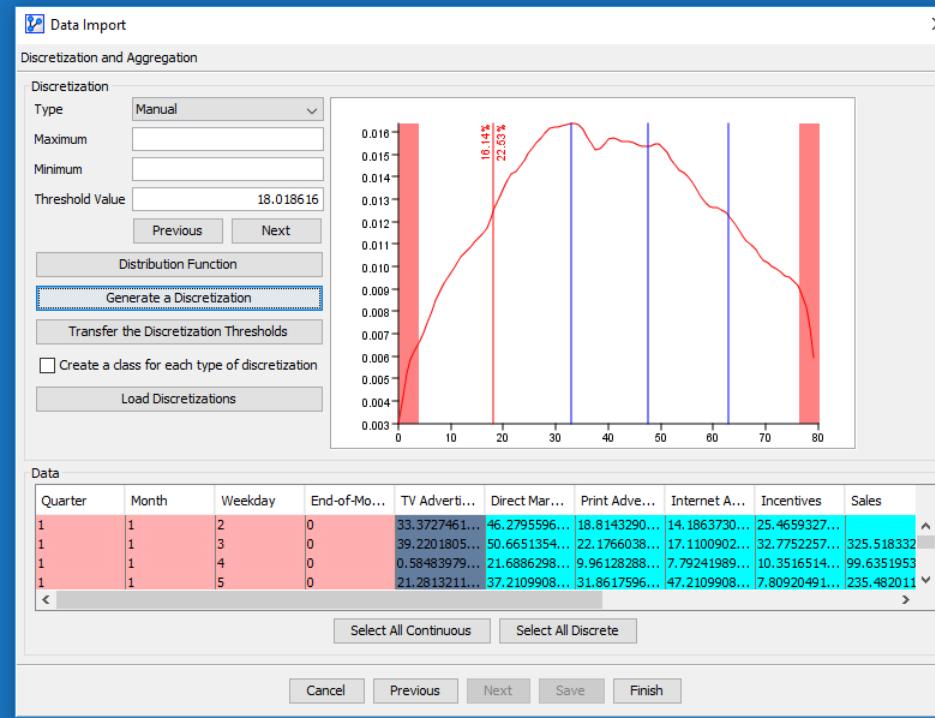
Number of Rows	16801	100.00%
Not Distributed	0	0.00%
Discrete	4	26.67%
Continuous	11	73.33%
Others	0	0.00%
Missing Values	6	0.00%
Filtered Values	0	0.00%

Select Values
 OR
 AND

Data

Quarter	Month	Weekday	End-of...	TV Adv...	Direct M...	Print Ad...	Interne...	Incentives	Sales
1	1	2	0	33.3727461...	46.2795596...	18.8143290...	14.1863730...	25.4659327...	12.100902...
1	1	3	0	39.2201805...	50.6651354...	22.1766038...	17.1100902...	32.7752257...	325.518332
1	1	4	0	0.58483979...	21.6886298...	9.96128288...	7.79241989...	10.3516514...	99.6351953
1	1	5	0	21.2813211...	37.2109908...	31.8617596...	47.2109908...	7.80920491...	235.482011
1	1	6	0	19.2473639...	6.69831269...	28.4687063...	16.6983126...	12.5090584...	212.640317

Missing Values Processing



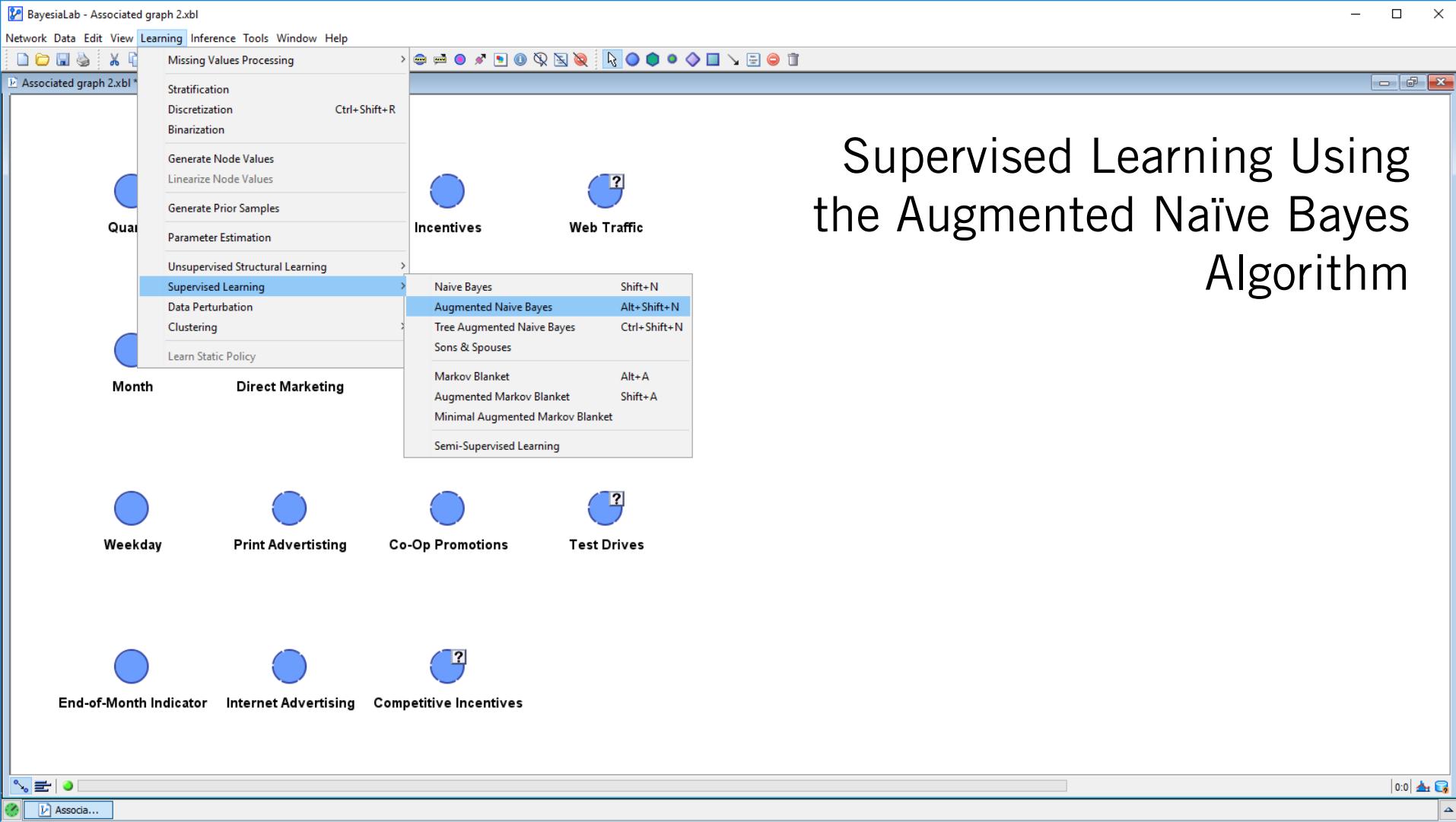
Discretization



Associated graph 2.xaml *

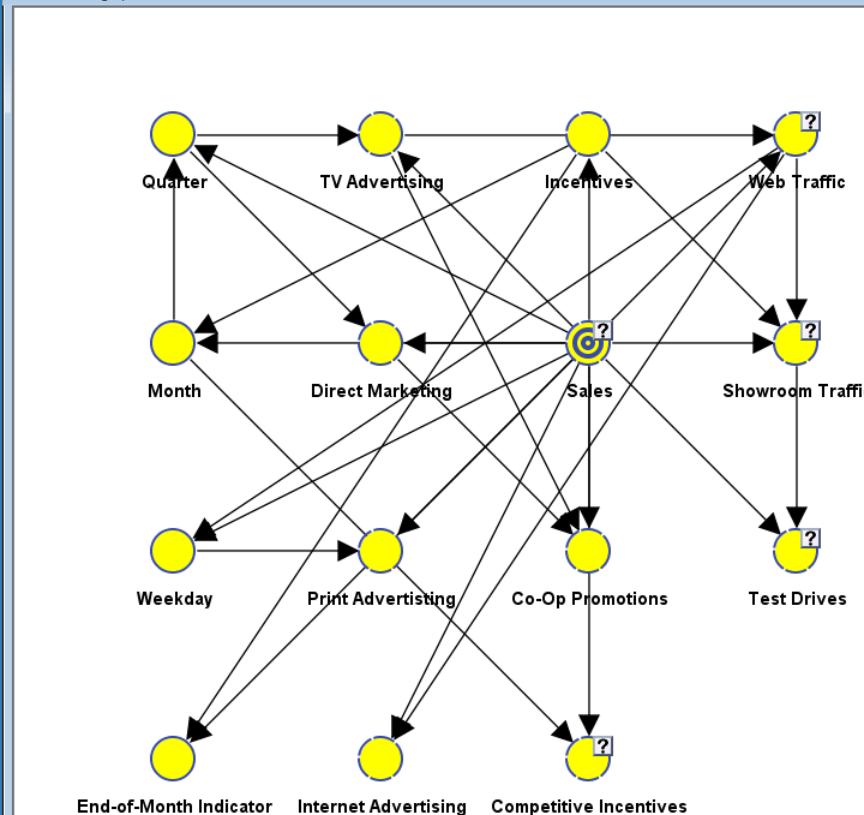
Unconnected Network







Associated graph 2.xbl *



Joint Probability: 100.00%

Log-Loss: 0

Cases: 16,801

Total Value: 570.093

Mean Value: 38.006

Sales
Mean: 295.998 Dev: 73.702

Value: 295.998

10.62% @<=205.642

24.95% <=268.244

30.22% <=325.755

24.52% <=390.789

9.70% >390.789

Internet Advertising
Mean: 23.646 Dev: 13.844

Value: 23.646

19.35% <=9.91

23.40% <=18.986

20.53% <=28.786

18.37% <=39.171

18.34% >39.171

TV Advertising
Mean: 40.528 Dev: 20.519

Value: 40.528

16.19% <=18.019

22.50% <=32.981

22.57% <=47.454

21.36% <=62.786

17.38% >62.786

Co-Op Promotions
Mean: 0.051 Dev: 0.048

Value: 0.051

44.24% <=0.007

1.98% <=0.017

2.57% <=0.049

3.18% <=0.085

48.03% >0.085

Month
Mean: 6.523 Dev: 3.449

Value: 6.523

8.49% 1

7.74% 2

8.49% 3

8.22% 4

8.49% 5

8.22% 6

8.49% 7

8.49% 8

8.22% 9

8.49% 10

8.22% 11

8.49% 12

Test Drives
Mean: 2.179 Dev: 0.079

Value: 2.179

5.44% <=2.035

15.79% <=2.122

25.09% <=2.185

30.88% <=2.241

22.80% >2.241

Competitive Incentives
Mean: 66.279 Dev: 23.593

Value: 66.279

15.97% <=41.418

24.93% <=59.661

26.97% <=77.632

21.17% <=96.918

10.96% >96.918

Print Advertising
Mean: 25.170 Dev: 13.251

Value: 25.170

19.04% <=12.673

25.94% <=21.367

23.31% <=30.668

16.29% <=41.47

15.42% >41.47

Web Traffic
Mean: 16.490 Dev: 2.459

Value: 16.490

12.01% <=13.51

23.77% <=15.342

22.85% <=17.157

22.17% <=19.013

19.20% >19.013

Direct Marketing
Mean: 35.048 Dev: 18.454

Value: 35.048

18.05% <=15.424

22.19% <=29.193

21.27% <=41.816

20.49% <=54.778

17.99% >54.778

Quarter
Mean: 2.508 Dev: 1.117

Value: 2.508

24.71% 1

24.92% 2

25.19% 3

25.19% 4

Weekday
Mean: 4.000 Dev: 2.000

Value: 4.000

14.28% 1

14.29% 2

14.28% 3

14.28% 4

14.28% 5

14.28% 6

14.28% 7

End-of-Month Indicator
Mean: 0.183 Dev: 0.387

Value: 0.183

81.67% 0

18.33% 1

Incentives
Mean: 47.058 Dev: 22.2119

Value: 47.058

17.81% <=24.343

23.96% <=40.389

23.15% <=56.721

21.37% <=73.699

13.70% >73.699

<=3.746

<=4.164

<=4.47

<=4.747

>4.747

Showroom Traffic
Mean: 4.432 Dev: 0.387

Value: 4.432

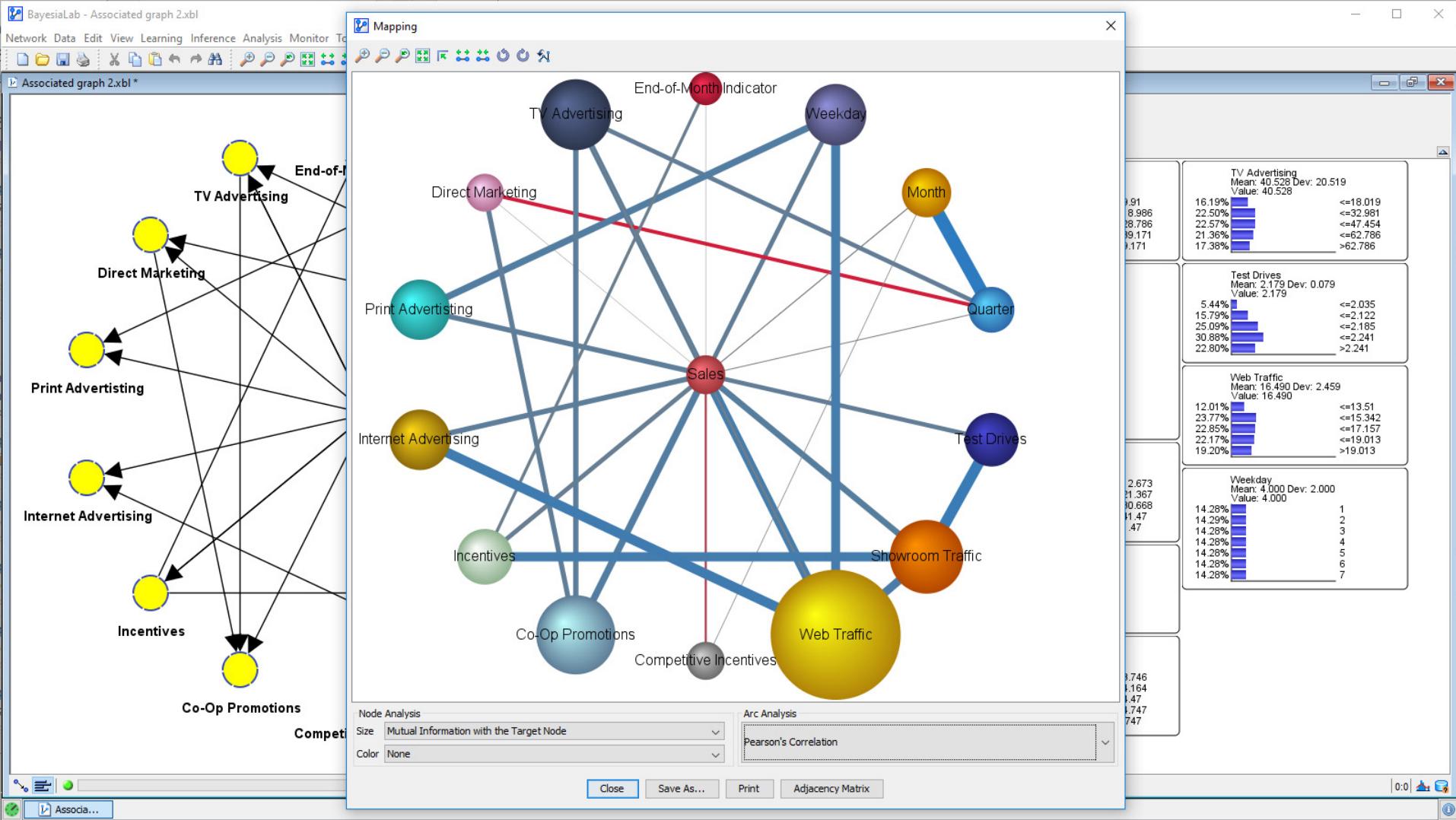
5.55% 1

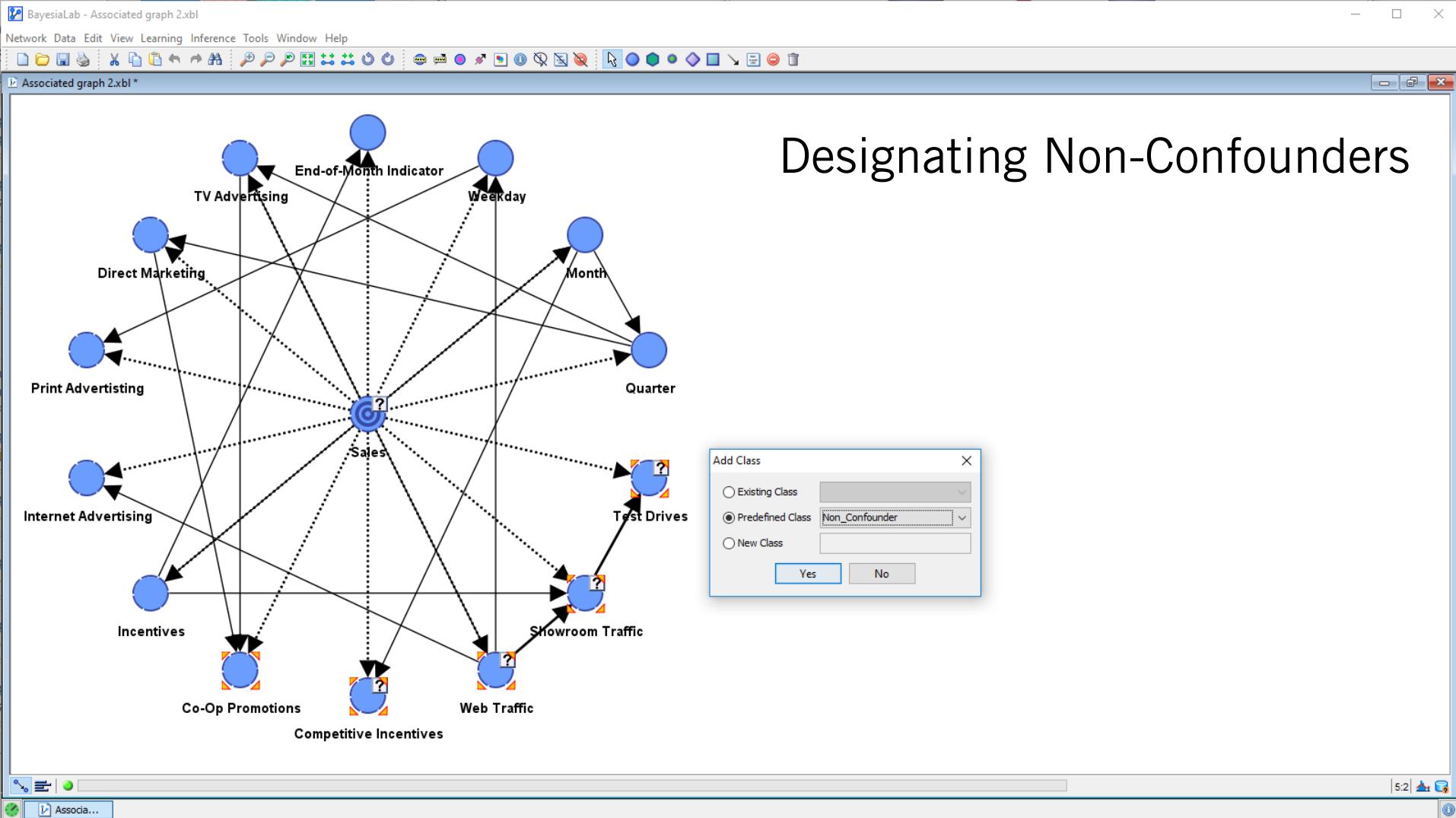
17.01% 2

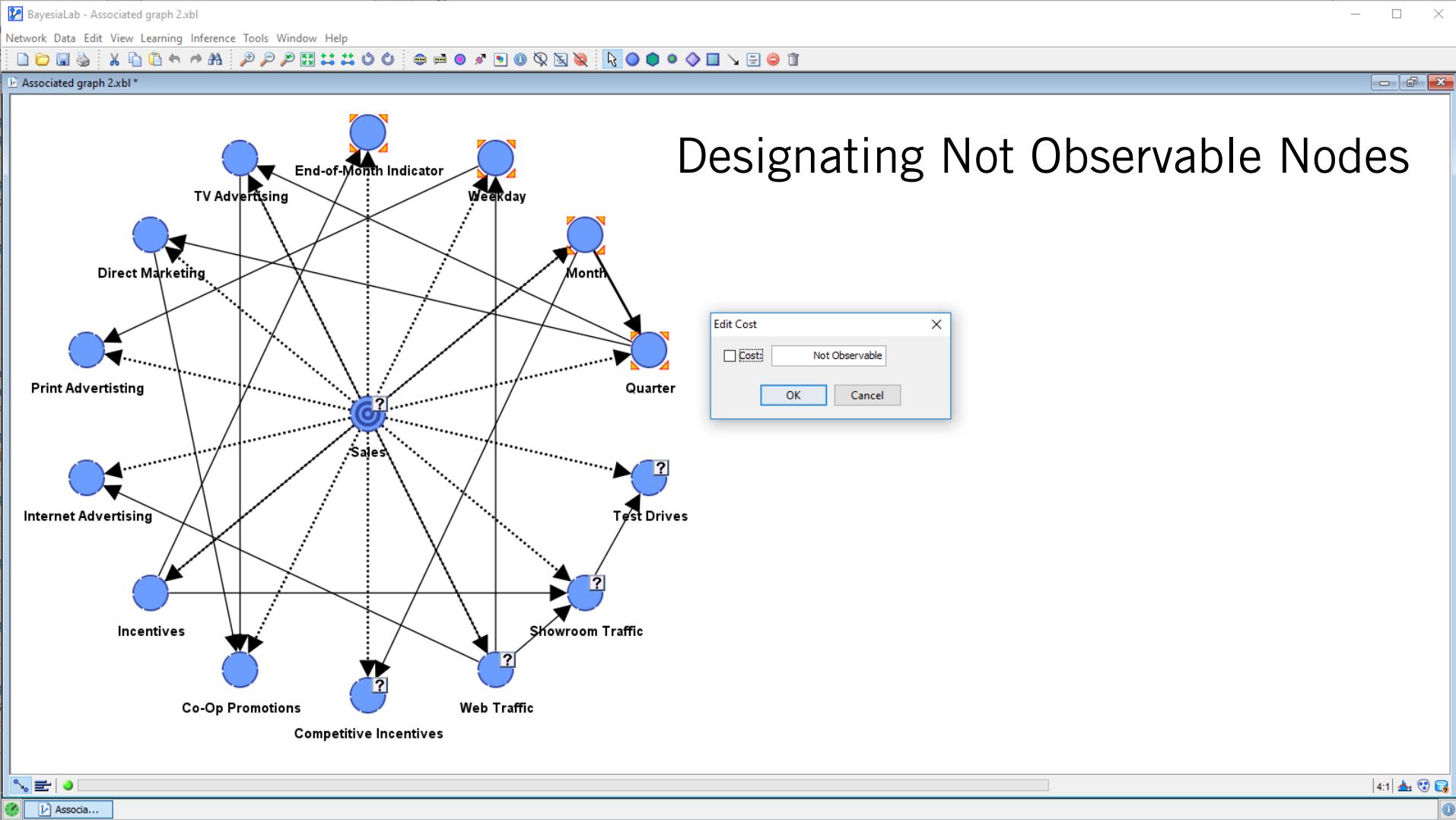
26.50% 3

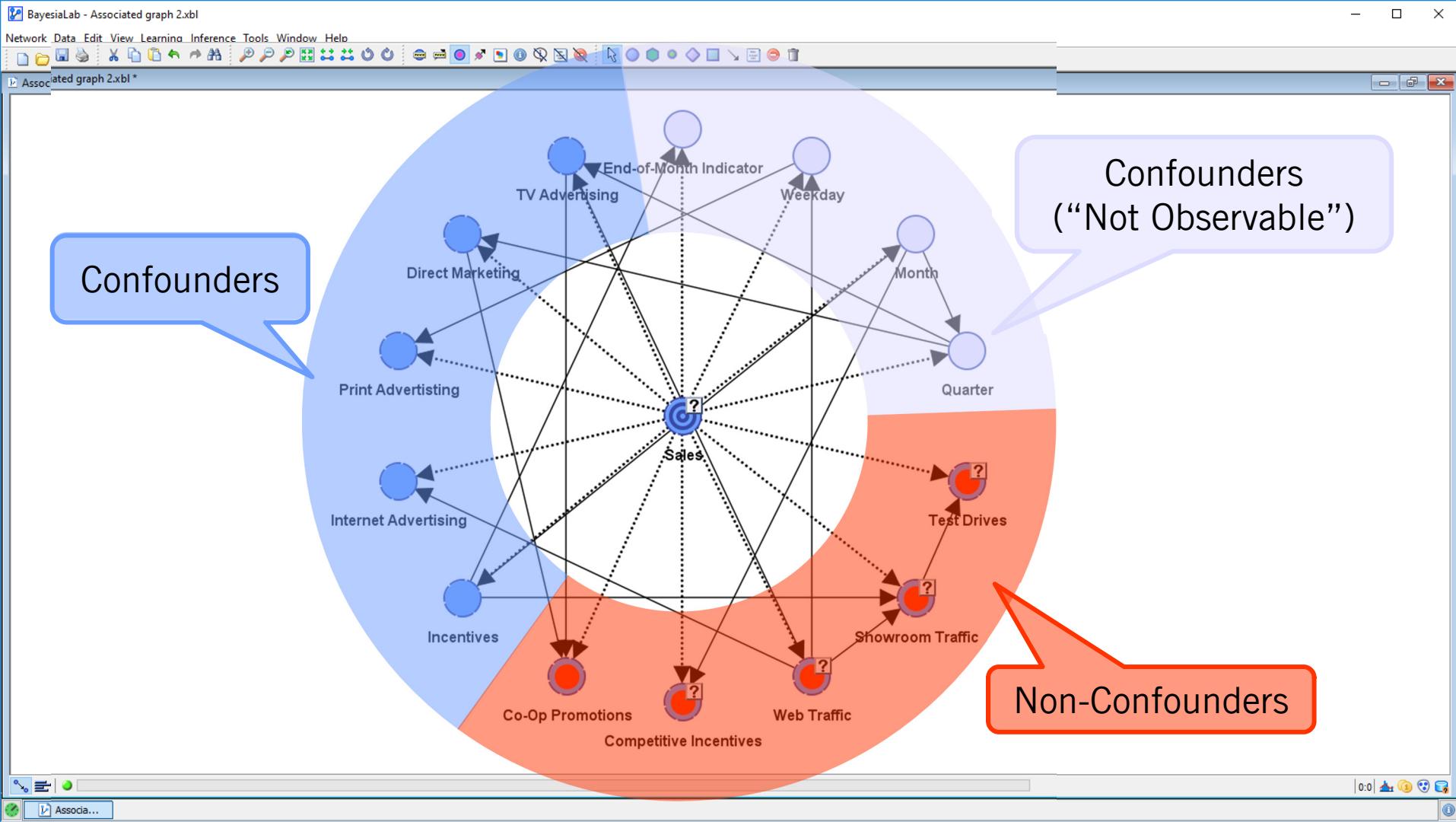
28.45% 4

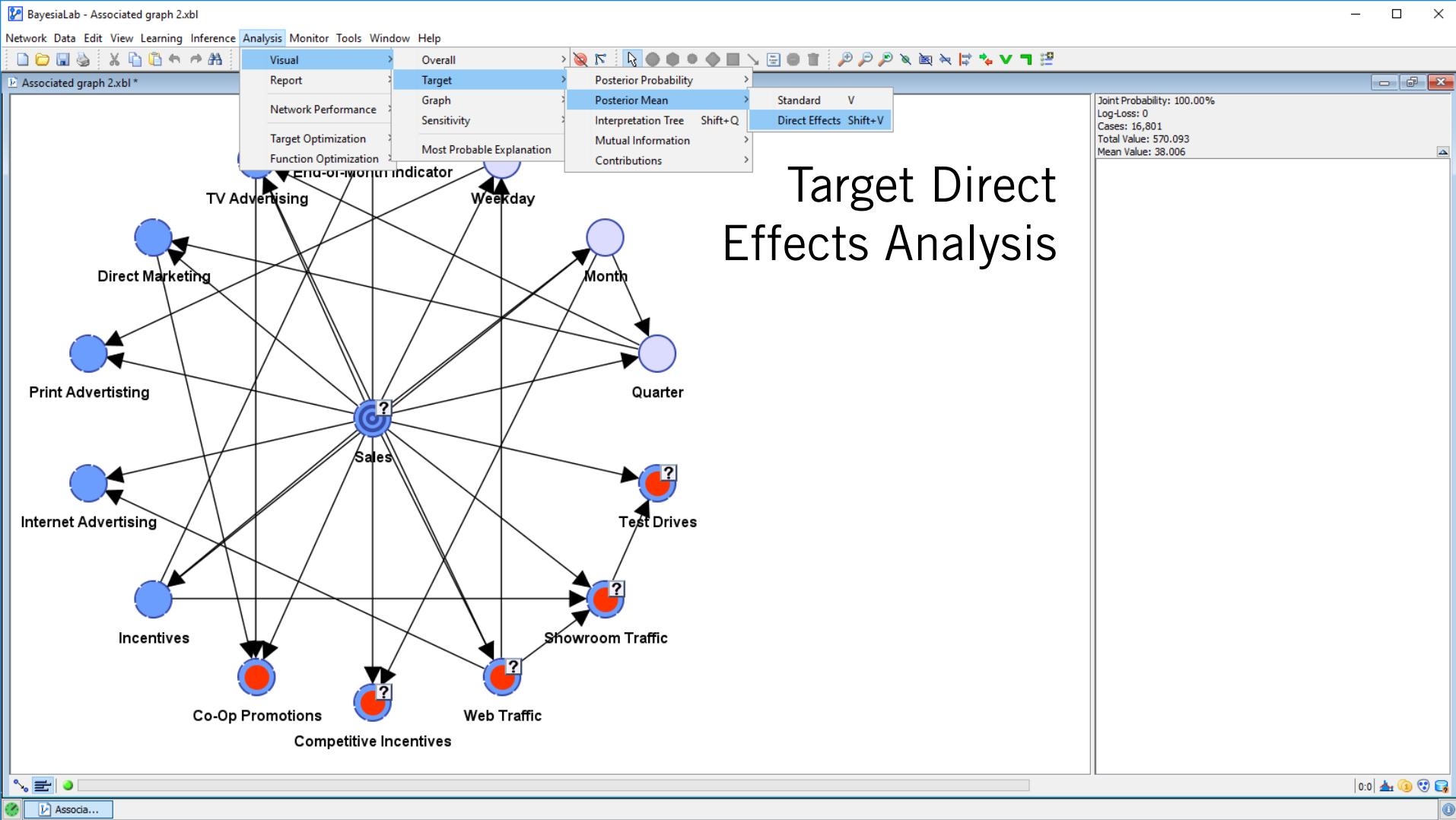
22.49% >4.747











BayesiaLab - Associated graph 2.xbl

Network Data Edit View Learning Inference Analysis Monitor Tools Window Help

Associated graph 2.xbl *

The network diagram illustrates causal relationships between variables. Sales is influenced by TV Advertising, Internet Advertising, Print Advertising, Direct Marketing, Incentives, Co-Op Promotions, Competitive Incentives, Weekday, Month, End-of-Month Indicator, Showroom Traffic, and Web Traffic.

Target Mean Analysis by Direct Effects

Target Direct Effects Analysis

Sales Mean

Variables

- All Curves
- TV Advertising
- Internet Advertising
- Incentives
- Direct Marketing
- Print Advertising

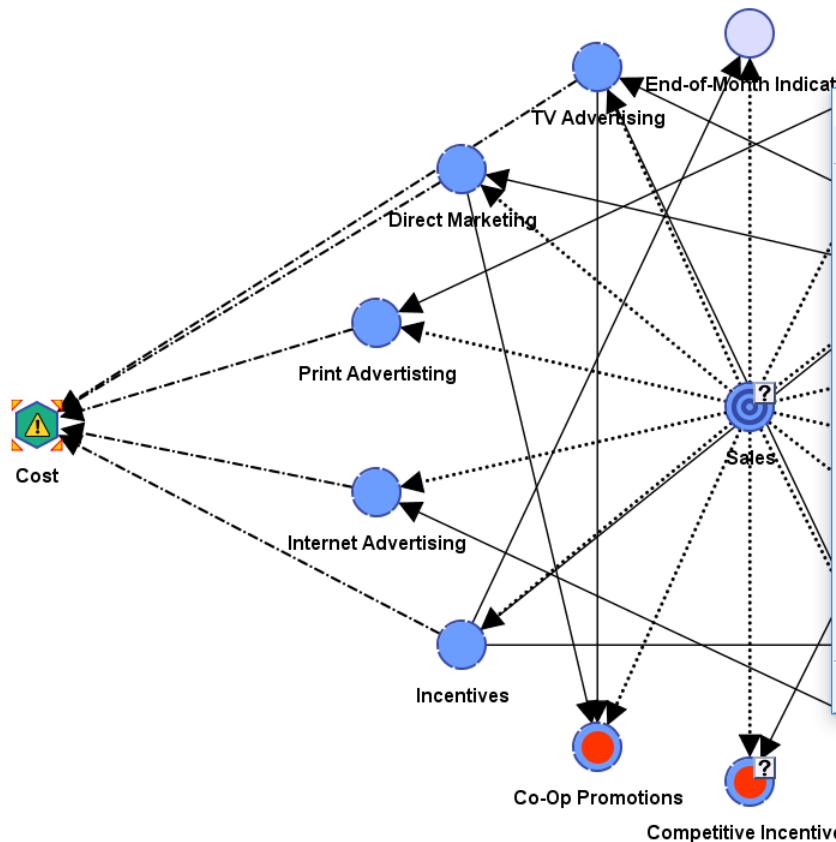
Response Curves

Normalized Variable Means	TV Advertising	Internet Advertising	Incentives	Direct Marketing	Print Advertising
0	250	285	285	285	275
20	285	285	295	295	295
40	305	295	305	305	305
50	310	305	310	310	310
70	315	310	315	315	315
100	330	315	315	295	315

0.0



Defining Media Costs



Node Editor

Node Selection: Cost Rename

Equation Properties Classes Comment

?Cost? =
MeanValue(?TV Advertising?) + MeanValue(?Direct Marketing?) + MeanValue(?Print Advertising?) + MeanValue(?Internet Advertising?) + MeanValue(?Incentives?)

Please validate

Samples: 1 Fixed Seed: 31 Validate

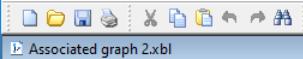
Discrete Proba Distributions
Continuous Proba Distributions
Special Functions
Inference Functions
Arithmetic Functions
Transformation Functions
Conversion Functions
Trigonometric Functions
Relational Operators

TV Advertising
Direct Marketing
Print Advertising
Internet Advertising
Incentives

Domain: [0.2759110152971571, 104.231996355]

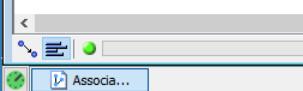
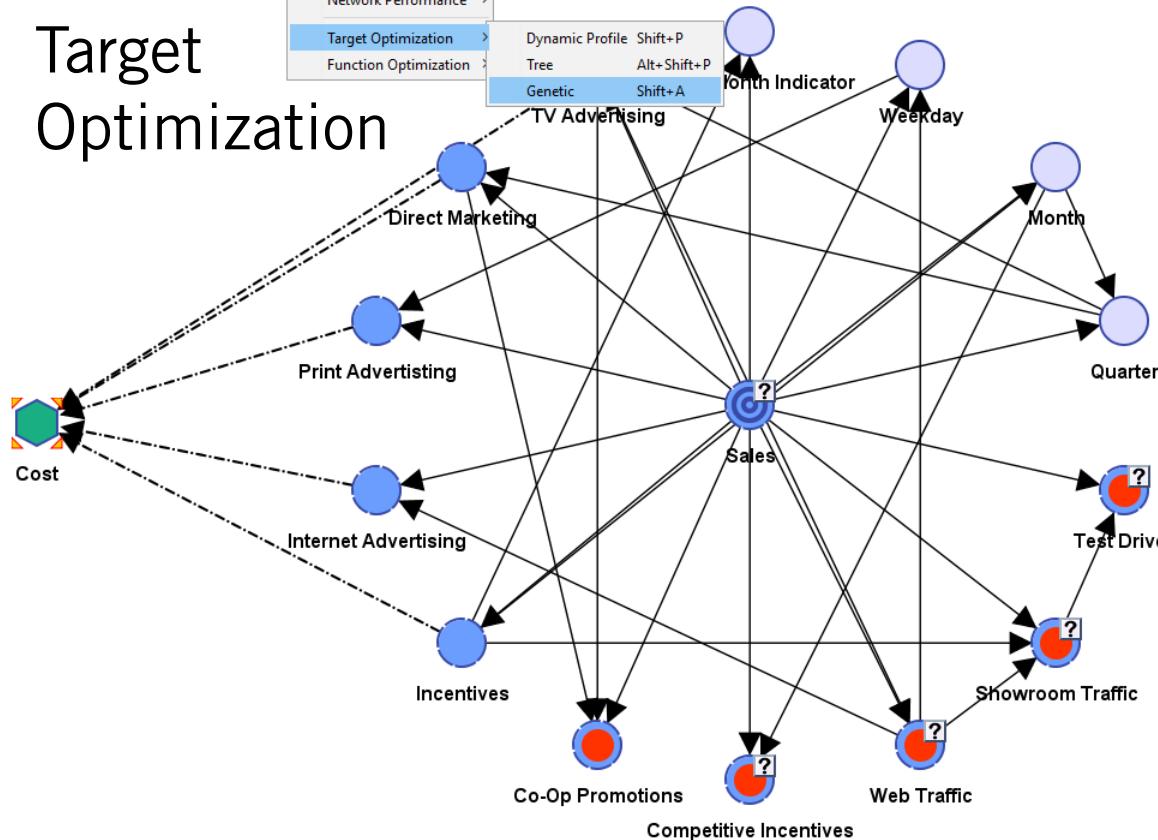
OK Cancel

Excel-style formula



Joint Probability: 100.00%
Log-Loss: 0
Cases: 16,801
Total Value: 570.216
Mean Value: 38.014

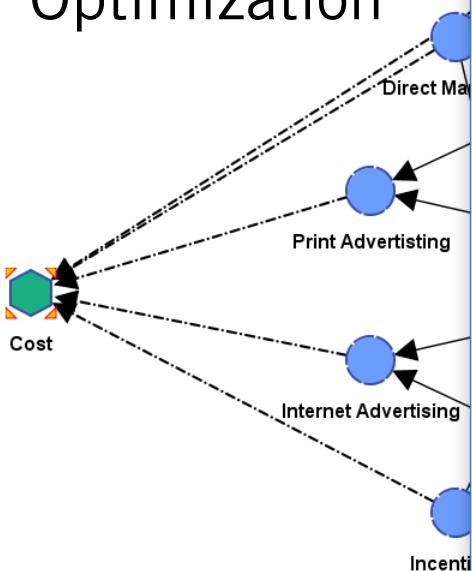
Target Optimization





Associated graph 2.xbl *

Target Optimization



Target Optimization

Profile Search Criterion
 Probability State ≤ 205.642
 Mean

Search Method
 Hard Evidence

Value/Mean Variations in % of
 Mean Domain Progression Margins

Criterion Optimization
 Maximization
 Minimization
 Target Value

Mean: 296.023

Direct Effects

Take Into Account the Resources
Minimum: 154.3606
Maximum: 188.6629
 Target Resources: 171.5117
 Take Into Account the Joint Probability

Genetic Settings
Number of Kingdoms: 5
Population Size: 10
Crossover Rate (%): 10
Gene Mutation Rate (%): 25
Selection Rate (%): 50
 Fixed Seed: 31

Weighting
Target Value: 1
Resources: 2
Joint Probability: 1

Genetic Stop Criterion
 Consecutive Number of Generations Without Improvement: 25
 For Each Kingdom
 Across all Kingdoms

Output
 Store the n Best Solutions in Evidence Scenarios: 10
 Store All the Solutions in Evidence Scenarios
Save All Generated Solutions

Joint Probability: 100.00%
Log-Loss: 0
Cases: 16,801
Total Value: 570.216
Mean Value: 38.014



Associated graph 2.xbl *

Optimization Results

Optimization Report of Sales (Associated graph 2)

Initial State	
Value/Mean	Resources
296.0229	171.5117

Search Method: Value/Mean Variations in % of Mean - Fix Probabilities (Binary) - Direct Effects

Not Fixed Nodes			
Node	Non Confounder	Factor	Not Observable
Co-Op Promotions	X		
Test Drives	X		
Competitive Incentives	X		
Showroom Traffic	X		
Web Traffic	X		

Synthesis					
Nodes	Incentives	Direct Marketing	TV Advertising	Internet Advertising	Print Advertising
Initial State	47.0845	35.0508	40.5250	23.6563	25.1951
Best Solution	25.3532 (-21.7313)	39.0952 (0.0443)	48.3183 (7.7933)	34.5745 (10.9183)	24.2261 (-0.9690)
Min	25.3532 (-21.7313)	26.9622 (-8.0887)	42.0837 (1.5587)	31.8450 (8.1887)	24.2261 (-0.9690)
Max	36.2189 (-10.8657)	39.0952 (0.0443)	48.3183 (7.7933)	35.4844 (11.8281)	30.0403 (4.8452)

Best Solutions							
Incentives	Direct Marketing	TV Advertising	Internet Advertising	Print Advertising	Score	Value/Mean	Resources
25.3532	39.0952	48.3183	34.5745	24.2261	1.6340	327.5442 (31.5213)	171.5671 (0.0554)
27.1641	36.3989	48.3183	34.5745	25.1951	1.6463	326.8260 (30.8031)	171.6510 (0.1393)
25.3532	39.0952	48.3183	34.5745	25.1951	1.6827	328.2943 (32.2714)	172.5361 (1.0244)
27.1641	36.3989	42.0837	35.4844	30.0403	1.7003	322.8792 (26.8563)	171.1714 (-0.3404)
30.7860	28.3103	48.3183	33.6647	30.0403	1.7175	321.5962 (25.5733)	171.1198 (-0.3920)
36.2189	26.9622	48.3183	31.8450	28.1022	1.7504	317.0880 (21.0651)	171.4467 (-0.0650)
36.2189	26.9622	48.3183	33.6647	28.1022	1.8097	320.4690 (24.4461)	173.2665 (1.7548)

Joint Probability: 3.76927E-4%

Log-Loss: 18.02

Cases: 0.06

Total Value: 599,986

Mean Value: 39,999

Resources: 171.567 (0.055)

Sales Mean: 327.544 Dev: 60.594 Value: 327.544 (+31.521) 1.97% 12.06% 32.21% 41.40% 12.36%	TV Advertising Mean: 48.318 Dev: 8.439 Value: 48.318 (-7.793) 0.00% 0.00% 44.07% 55.93% 0.00%	Co-Op Promotions Mean: 0.075 Dev: 0.041 Value: 0.075 (+0.024) 18.59% 2.72% 3.96% 4.12% 70.61%
<=205.642 <=268.244 <=325.755 <=390.789 >390.789	<=18.019 <=32.981 <=47.454 <=62.786 >62.786	<=0.007 <=0.017 <=0.049 <=0.085 >0.085

Quarter Mean: 2.508 Dev: 1.117 Value: 2.508 (+0.000) 24.72% 24.92% 25.18% 25.18%	Direct Marketing Mean: 39.095 Dev: 6.730 Value: 39.095 (-4.044) 0.00% 0.00% 71.76% 28.24% 0.00%	Competitive Incentives Mean: 63.631 Dev: 23.443 Value: 63.631 (-2.666) 19.05% 26.86% 26.27% 18.78% 9.04%
1 2 3 4	<=15.424 <=29.193 <=41.816 <=54.778 >54.778	<=41.418 <=59.661 <=77.632 <=96.918 >96.918

Month Mean: 6.523 Dev: 3.449 Value: 6.523 (+0.000) 8.48% 7.75% 8.48% 8.22% 8.48% 8.22% 8.48% 8.48% 8.48% 8.22% 8.48% 8.48% 8.48% 8.48% 8.48% 8.48%	Print Advertising Mean: 24.226 Dev: 4.260 Value: 24.226 (-0.969) 0.00% 0.00% 17.73% 82.27% 0.00% 0.00%	Web Traffic Mean: 17.515 Dev: 1.837 Value: 17.515 (+1.029) 1.54% 7.74% 32.79% 35.87% 22.05%
1 2 3 4 5 6 7 8 9 10 11 12	<=12.673 <=21.367 <=30.668 <=41.47 >41.47	<=13.51 <=15.342 <=17.157 <=19.013 >19.013

Internet Advertising Mean: 34.574 Dev: 3.948 Value: 34.574 (+10.918) 0.00% 0.00% 0.00% 93.93% 6.07%	Showroom Traffic Mean: 4.282 Dev: 0.328 Value: 4.282 (-0.148) 5.79% 26.33% 39.42% 25.52% 2.94%
<=9.91 <=18.986 <=28.786 <=39.171 >39.171	<=3.746 <=4.164 <=4.47 <=4.747 >4.747

Weekday Mean: 4.000 Dev: 2.000 Value: 4.000 (-0.000) 14.29% 14.29% 14.29% 14.29% 14.29% 14.29% 14.29% 14.29% 14.29% 14.29% 14.29% 14.29% 14.29% 14.29% 14.29% 14.29%	Incentives Mean: 25.353 Dev: 9.613 Value: 25.353 (-21.731) 43.66% 56.34% 0.00% 0.00% 0.00%
1 2 3 4 5 6 7	<=24.343 <=40.369 <=56.721 <=73.699 >73.699

End-of-Month Indicator Mean: 0.188 Dev: 0.391 Value: 0.188 (-0.000) 81.21% 18.79%	Test Drives Mean: 2.153 Dev: 0.075 Value: 2.153 (-0.026) 7.00% 23.69% 33.37% 27.94% 8.01%
0 1	<=2.035 <=2.122 <=2.185 <=2.241 >2.241

Cost
171.5671321886
 (171.5117434445)

Close

Save As...

Print

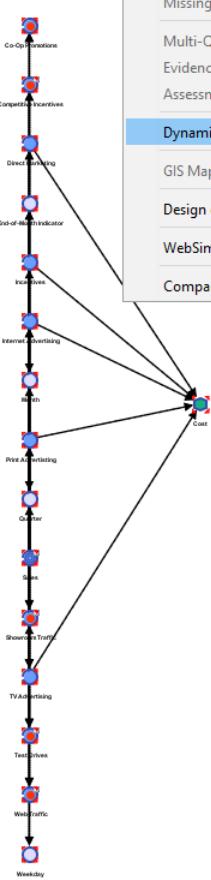
GA Score: 1.6339506

16:34 |

Network Data Edit View Learning Inference Tools Window Help

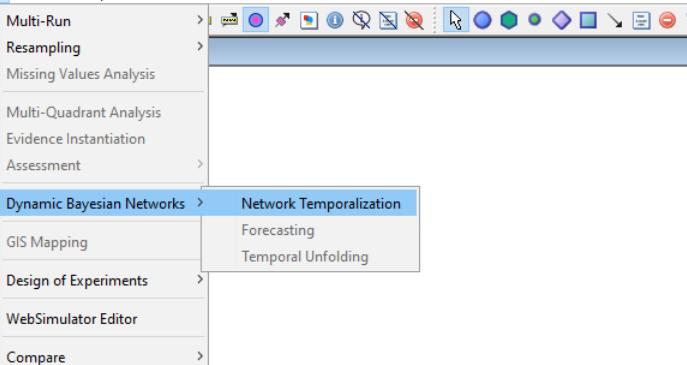
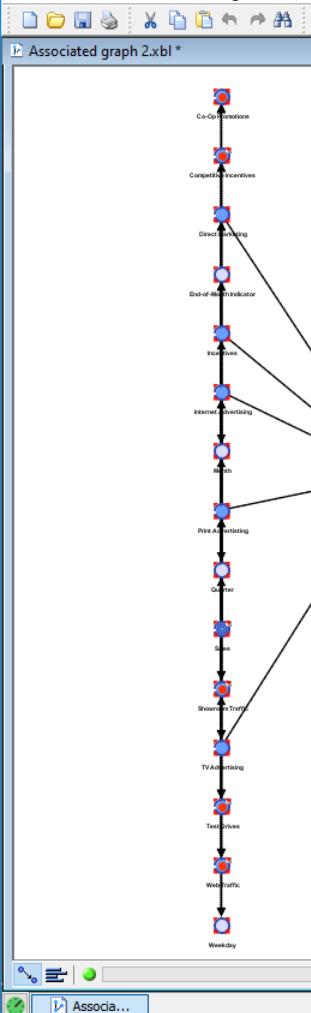


- Multi-Run >
- Resampling >
- Missing Values Analysis
- Multi-Quadrant Analysis
- Evidence Instantiation
- Assessment >
- Dynamic Bayesian Networks > Network Temporalization**
- GIS Mapping
- Design of Experiments >
- WebSimulator Editor
- Compare >

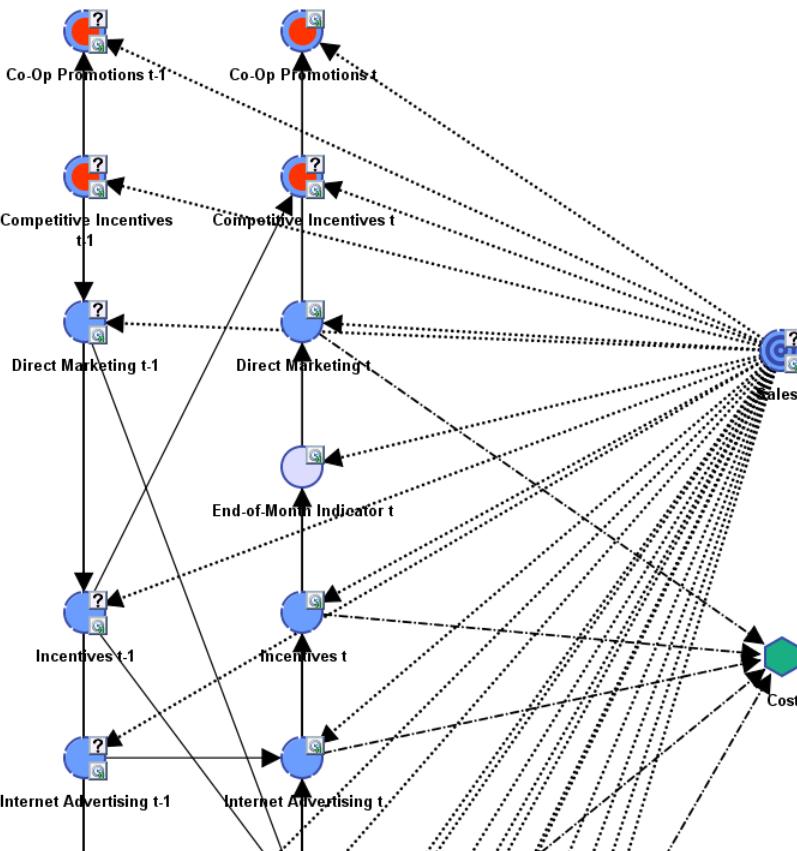


Network Temporalization

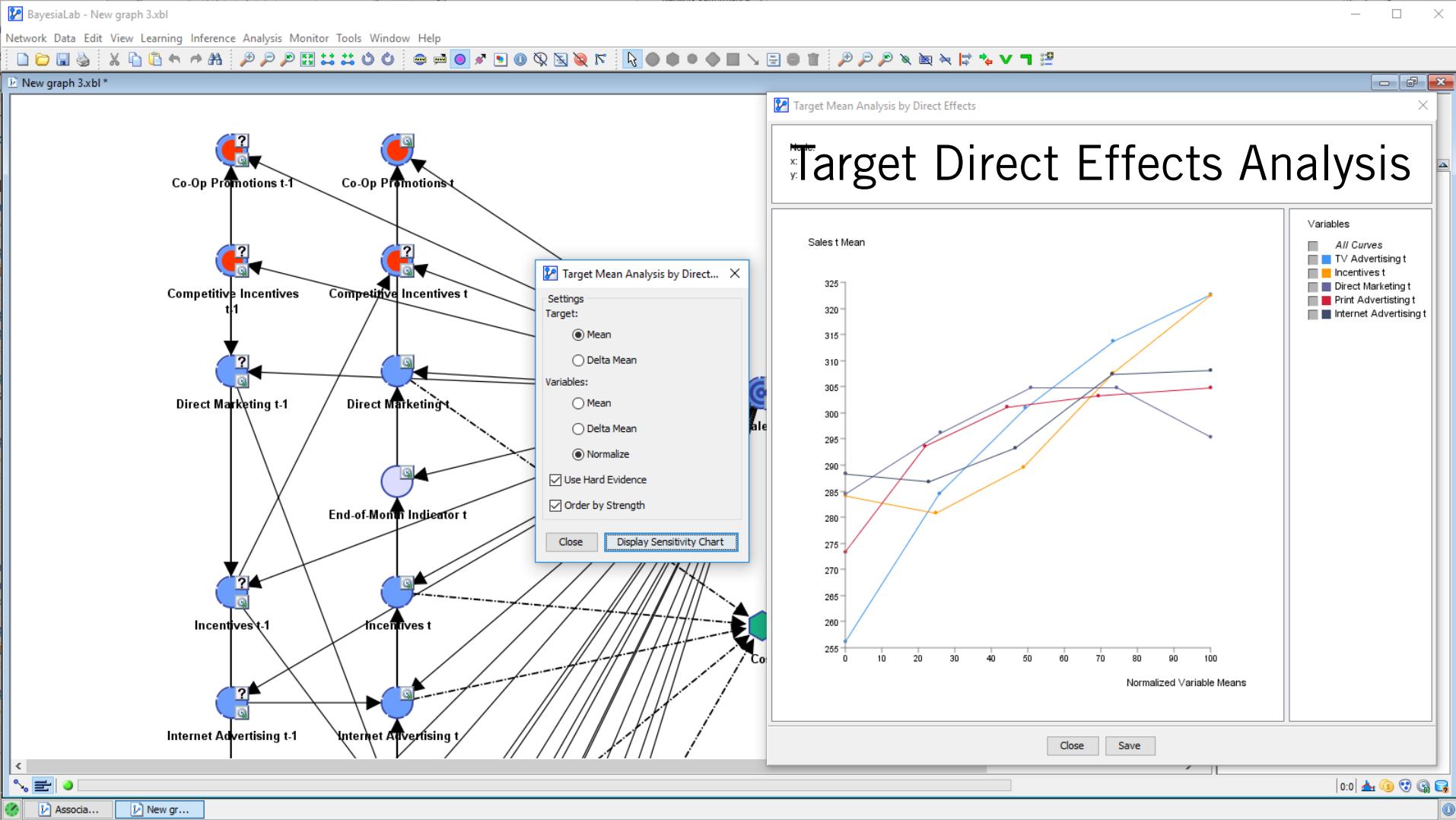
Network Data Edit View Learning Inference Tools Window Help

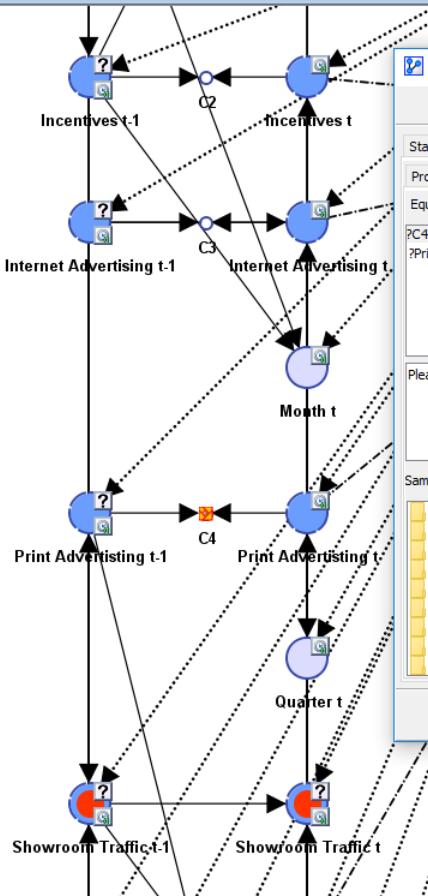


Network Temporalization



Network Temporalization





Node Editor

Node Selection: C4 Rename

States Probability Distribution Classes Comment

Probabilistic Deterministic Tree Equation

Equation Type: Deterministic Probabilistic

?C4? =
?Print Advertising t?=?Print Advertising t-1?

Please validate formula!

Samples: 1000 Smoothing: 0 Fixed Seed: 31 Validate

Discrete Proba Distributions
Continuous Proba Distributions
Special Functions
Arithmetic Functions
Transformation Functions
Conversion Functions
Trigonometric Functions
Relational Operators
Boolean Operators

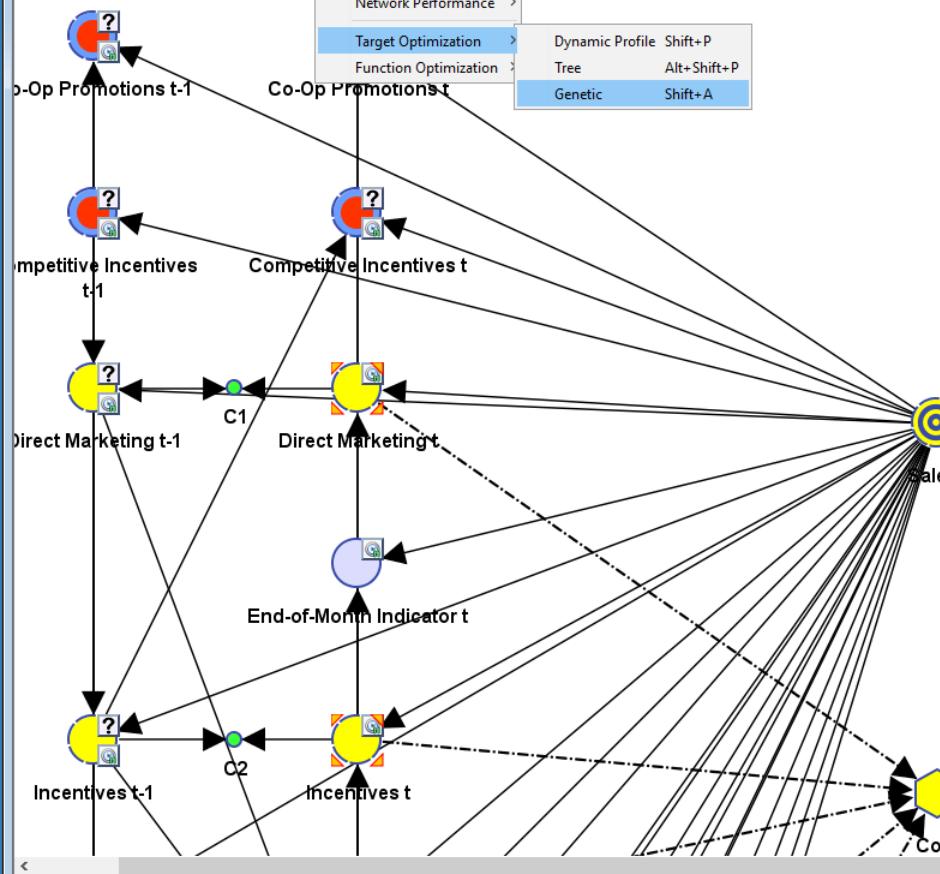
C4
Print Advertising t-1
Print Advertising t Domain: [0.3303802912319805, 56.794545097]

OK Cancel

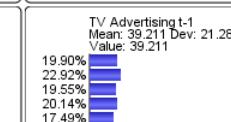
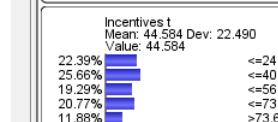
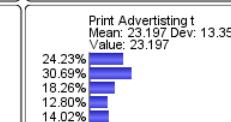
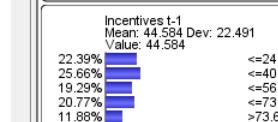
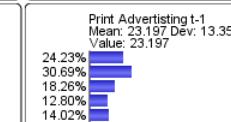
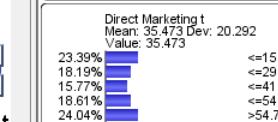
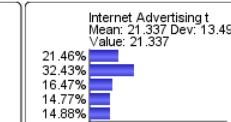
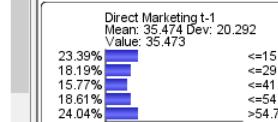
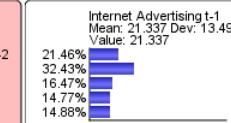
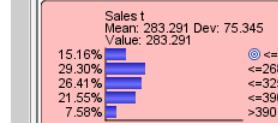
Adding Constraints



Visual > Report > Network Performance > Target Optimization > Dynamic Profile Shift+P
 Function Optimization > Tree Alt+Shift+P
 Genetic Shift+A



Joint Probability: 0.10%
 Log-Loss: 9.93
 Cases: 17.22
 Total Value: 800.602
 Mean Value: 32.024
 Resources: 163.803 (0.000)



Target Optimization



New graph 3.xbl

Target Optimization

Profile Search Criterion: Mean

Search Method: Hard Evidence

Criterion Optimization: Maximization

Intermediate Points: 10

Direct Effects: Checked

Genetic Settings:

- Number of Kingdoms: 5
- Population Size: 10
- Crossover Rate (%): 10
- Gene Mutation Rate (%): 25
- Selection Rate (%): 50
- Fixed Seed: 31

Genetic Stop Criterion:

- Consecutive Number of Generations Without Improvement: 10
- For Each Kingdom (Selected)
- Across all Kingdoms

Output:

- Store the n Best Solutions in Evidence Scenarios: 10
- Replace Evidence Scenarios (Selected)
- Append to Evidence Scenarios

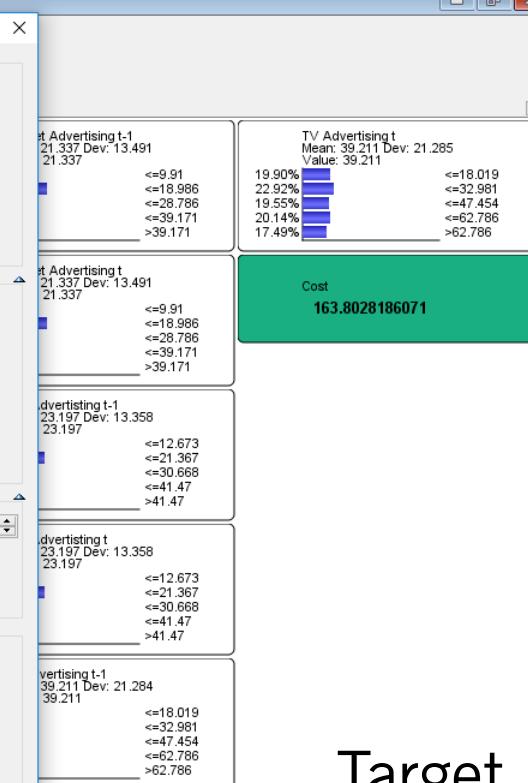
Save All Generated Solutions: Browse

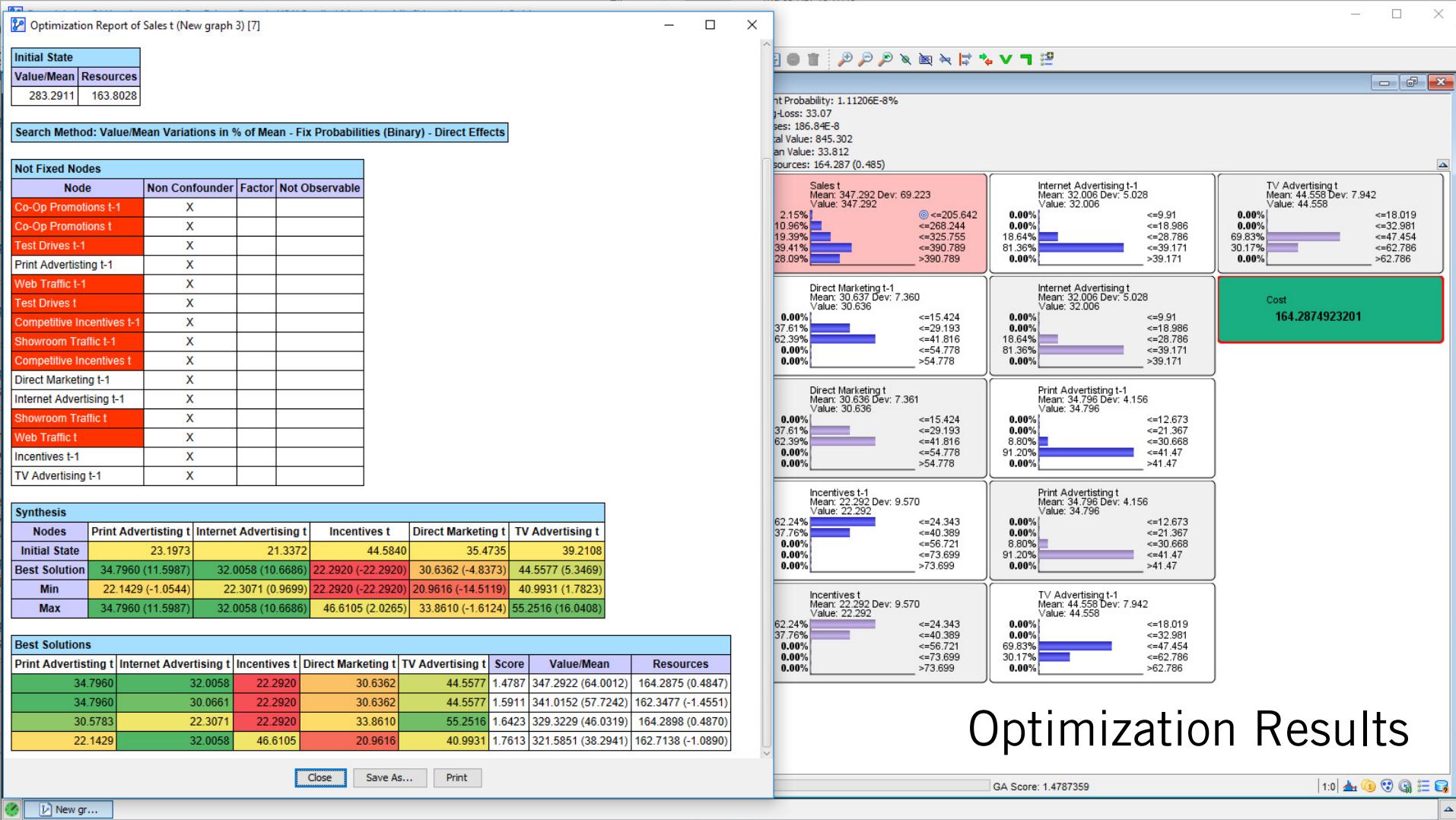
OK | **Cancel**

Diagram Nodes and Edges:

- b-Op Promotions t-1** → **Co-Op Promotions t**
- Co-Op Promotions t** → **Competitive Incentives t-1**
- Co-Op Promotions t** → **Competitive Incentives t**
- Competitive Incentives t-1** → **Competitive Incentives t**
- Competitive Incentives t-1** → **Direct Marketing t-1**
- Competitive Incentives t** → **Direct Marketing t-1**
- Competitive Incentives t** → **End-of-Month Indicator t**
- Direct Marketing t-1** → **End-of-Month Indicator t**
- Incentives t-1** → **Incentives t**
- Incentives t** → **End-of-Month Indicator t**
- End-of-Month Indicator t** → **C1**
- C1** → **Incentives t-1**
- C1** → **Incentives t**
- C1** → **Direct Marketing t-1**
- C1** → **End-of-Month Indicator t**
- C2** → **Incentives t-1**
- C2** → **Incentives t**
- C2** → **End-of-Month Indicator t**

Target Optimization







BAYESIALAB

In Conclusion...

Webinar Series: Friday at 1 p.m. (Central)

Upcoming Webinars:

- April 13 Analyzing Capital Flows of Exchange-Traded Funds
- April 20 GIS Mapping with BayesiaLab

Register here: bayesia.com/events

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April 11–13, 2018: Sydney
Introductory BayesiaLab Course

May 16–18, 2018: Seattle
Introductory BayesiaLab Course

May 21–23, 2018: Seattle
Advanced BayesiaLab Course

June 5–7, 2018: Paris, France
Introductory BayesiaLab Course

June 26–28, 2018: Boston
Introductory BayesiaLab Course

July 23–25, 2018: San Francisco
Introductory BayesiaLab Course

September 26–28, 2018: New Delhi
Introductory BayesiaLab Course

October 29–31, 2018: Chicago
Introductory BayesiaLab Course

November 5–7, 2018: Chicago
Advanced BayesiaLab Course



BayesiaLab 7

Artificial Intelligence for Research, Analytics, and Reasoning

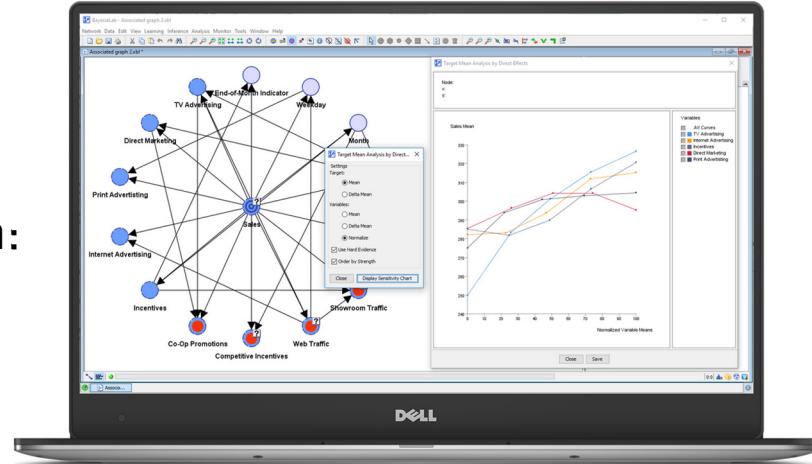
User Forum: bayesia.com/community

The screenshot shows the BayesiaLab User Forum website. At the top, there is a navigation bar with links to "BayesiaLab Software", "Bayesian Networks", "User Guide & Library", "User Forum" (which is underlined to indicate it is the current page), "BayesiaLab Store", "Courses & Events", "Learning Resources", "News Feed", and "About". Below the navigation bar is a search bar with a dropdown menu set to "This Category" and a "Search" button. To the right of the search bar are "Log In" and "Register" buttons. A sidebar on the left has a "≡" icon. The main content area features a breadcrumb trail "← BayesiaLab Seminars" and a "START NEW TOPIC" button. Below this, there are three filter buttons: "Latest", "New", and "Top". A post by "stefanconrady" titled "Webinar on Diagnostic Decision Support with Bayesian Networks" is displayed, along with a timestamp "a minute ago" and a note that "The answers to all webinar questions will be posted here." To the right of the post are icons for comments (0), likes (0), and views (0). Below the post, it says "Started by stefanconrady a minute ago". At the bottom of the page, there is a language selection bar with a globe icon and the text "English ▾".

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- July 23–25
San Francisco, CA
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- September 26–28
New Delhi, India
- October 29–31
Chicago, IL
- December 4–6
New York, NY



Learn More & Register: bayesia.com/events

6th Annual BayesiaLab Conference in Chicago

November 1–2, 2018



Thank You!



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[BayesianNetwork](#)



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