Contents

1 Basic

1.1 .vimrc

```
syntax on
se ru nu ai
se ts=4 sts=4 sw=4 st=4 smarttab laststatus=2 expandtab
inoremap {<ENTER> {}<LEFT><ENTER>;<LEFT><DEL><ENTER><UP><TAB>
"se mouse=a expandtab
```

1.2 Check

```
| for i in $(seq 1 10000);
| do
| ./gen > input
| ./ac < input > out_ac
| ./wa < input > out_wa
| diff out_ac out_wa || break
```

1.3 Factor Count List

```
factor number of i) 80 72, 50400
10080
                                   108,
             72,
168,
                                          110880
                                   192,
                                                        200,
221760
                     332640
                                          498960
             216,
256,
554400
                     665280
                                   224,
                                          720720
                                                        240,
1081080
                     2162160
                                   320,
                                          3603600
                                                        360,
4324320
             384,
                     6486480
                                   400,
                                          7207200
                                                        432,
8648640
             448,
                     10810800
                                   480,
                                          21621600
                                                        576
32432400
                                   672,
             600.
                     43243200
                                          61261200
                                                        720
73513440
                    110270160
                                   800,
                                          245044800
                                                        1008.
             768
             1152, 551350800 1200, 698377680 1280
1344, 1102701600 1440, 1396755360 1536
367567200
                                                        1280
735134400
*/
```

1.4 Default

1.5 Pragma

1.6 Random Int

```
|#include <random>
|mt19937 rng(chrono::steady_clock::now().time_since_epoch().
| count());
|int rand_int(int lb, int ub)
|{ return uniform_int_distribution<int>(lb, ub)(rng); }
|double rand_double(double lb, double ub)
|{ return uniform_real_distribution<double>(lb, ub)(rng); }
```

1.7 Increase Stack Size

```
const int size = 256 << 20;
register long rsp asm("rsp");
char *p = (char*)malloc(size) + size, *bak = (char*)rsp;
__asm__("movq %0, %%rsp\n"::"r"(p));
// main
__asm__("movq %0, %%rsp\n"::"r"(bak));</pre>
```

1.8 FasterIO

```
static inline char getRawChar() {
    static char buf[1 << 16], *p = buf, *end = buf;
    if (p == end) {
        if ((end = buf + fread_unlocked(buf, 1, 1 << 16, stdin)) ==
            buf) return '\0';
        p = buf;
    }
    return *p++;
}
while (c = getRawChar() && (unsigned)(c - '0') > 10U) n = n *
        10 + (c - '0');
```

2 Bitwise Trick

2.1 Builtin Function

```
// count left 0s
int __builtin_clz (unsigned int x) // 31 - __builtin_clz is lg
int __builtin_clzll (unsigned long long x) // 63 - clz
// count number of 1's
int __builtin_popcount (unsigned int x)
int __builtin_popcountll (unsigned long long x)
```

2.2 Subset Enumeration

```
int subset_enumeration(int s) {
  for (int now = s; now > 0; now = (now - 1) & s) {
    cout << now << ' ';
  }
  cout << "0\n";
}</pre>
```

2.3 Next Permutation on Binary

```
|ll next_perm(ll v) {
| ll t = v | (v - 1);
| return (t + 1) | (((~t & -~t) - 1) >> (__builtin_ctz(v) + 1))
| ;
|}
```

2.4 SOS DP

```
|// 0 is 0, 1 can be 1 or 0
| for (int i = 0; i < n; ++i)
| for (int j = 0; j < (1 << n); ++j)
| if ( j & (1 << i) )
| a[j] += a[ j ^ (1 << i) ];
```

3 Theorem and Formula

- Pick's theorem $A = i + \frac{b}{2} 1$
- Laplacian matrix L = D A
- Derangement $D_n = (n-1)(D_{n-1} + D_{n-2})$
- Möbius function $\sum\limits_{i\,|\,n}\mu(i)=[n=1]$
- Euler's totient function $\sum_{i|n} \phi(i) = n$
- Inversion formula

$$f(n) = \sum_{i=0}^{n} {n \choose i} g(i), g(n) = \sum_{i=0}^{n} (-1)^{n-i} {n \choose i} f(i)$$

$$f(n) = \sum_{d \mid n} g(d), g(n) = \sum_{d \mid n} \mu(\frac{n}{d}) f(d)$$

• Sum of powers

$$\sum_{k=1}^{m} k^m = \frac{1}{m+1} \sum_{k=0}^{m} {m+1 \choose k} B_k^+ n^{m+1-k}$$

$$\sum_{j=0}^{m} {m+1 \choose j} B_j^- = 0$$

$$\text{note} : B_1^+ = -B_1^- B_i^+ = B_i^-$$

• Cipolla's algorithm

$$\left(\frac{u}{p}\right) = u^{\frac{p-1}{2}}$$

1.
$$\left(\frac{a^2 - n}{p}\right) = -1$$

2. $x = \left(a + \sqrt{a^2 - n}\right)^{\frac{p+1}{2}}$

 $\bullet \quad \text{High order residue} \\$

$$[d^{\frac{p-1}{(n,p-1)}} \equiv 1]$$
 (p is odd prime and p $\not|d$)

```
- Packing and Covering |\mbox{Maximum Independent Set}| + |\mbox{Minimum Vertex Cover}| = |\mbox{V}|
```

• Dilworth's theorem

 $\label{eq:width} width = |smallest\ chain\ decomposition|\ (vertex\ split\ and\ matching) = |largest\ antichain| = |maximim\ clique\ in\ Complement|\ (easy)$

· Mirsky's theorem

 $\begin{array}{l} \mbox{height} = |\mbox{longest chain}|(\mbox{easy DP}) = |\mbox{smallest antichain decomposition}| \\ = |\mbox{minimum anticlique partition}| \ (\mbox{subset DP}) \end{array}$

• Triangle center

```
-G: (1, 1, 1)
-O: (a^{2}(b^{2} + c^{2} - a^{2}), \cdots) = (\sin 2A, \sin 2B, \sin 2C)
-I: (a, b, c) = (\sin A, \sin B, \sin C)
-E: (-a, b, c) = (-\sin A, \sin B, \sin C)
-H: (\frac{1}{b^{2} + c^{2} - a^{2}}, \cdots) = (\tan A, \tan B, \tan C)
```

• $\lfloor \frac{n}{i} \rfloor$ enumeration $T_0 = 1, T_i = \lfloor \frac{n}{\lfloor \frac{n}{T_{i-1}+1} \rfloor} \rfloor$

4 Data Structure

$4.1 < ext/pb_ds >$

```
#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/priority_queue.hpp>
#include <ext/rope>
using namespace __gnu_pbds;
using namespace __gnu_cxx;
using namespace std;
__gnu_pbds::priority_queue<<mark>int</mark>> pq, pq2;
__gnu_pbds::priority_queue<<mark>int</mark>>::point_iterator idx[10];
__gnu_pbds::priority_queue<<mark>int</mark>, less<int>, pairing_heap_tag>
     heap;
pairing_heap_tag, thin_heap_tag, binomial_heap_tag
rc_binomial_heap_tag, binary_heap_tag
*/
idx[0] = pq.push(1);
pq.modify(idx[0], 2); // change the iterator's value to 2
pq.join(pq2);
typedef tree<int,null_type,less<int>,rb_tree_tag,
     tree_order_statistics_node_update> TREE;
TREE name:
*name.find_by_order(0);
name.order_of_key(1);
name.insert(2);
name.delete(3):
name.split(v, b); /// value < v of a split to b
name.join(another TREE);
```

4.2 Unordered Map Hash

```
| struct KeyHasher {
| size_t operator()(const Key& k) const {
| return k.first + k.second * 100000;
| }
| };
| typedef unordered_map<Key, int, KeyHasher> map_t;
```

4.3 Rope

```
#include <ext/rope>
using namespace __gnu_cxx;
int main() {
  rope<int> v; // can be cout directly if it's char
  rope<int> v1(v);
  rope<int> v2(arr, arr + 10); //int arr[100];
  v.find(3); // return the first position of 3
  v.push_back(4); v.pop_back();
  //append not for iterator
  v.insert(pos, s); // pos can be iterator, integer. s can be
      rope, int, array
  v.replace(pos, len, s); // (pos, len) can be (it1, it2). s is
      same as insert.
  v.erase(pos, len); // or v.erase(it1, it2)
  v2 = v.substr(pos, len); // same as erase
```

```
v.copy(pos, len, arr); // int arr[100]; (pos, len) can be
   omitted
v[0], v[1]
auto it1 = v.mutable_begin(), it2 = v.mutable_end();
}
```

4.4 Disjoint Set

```
struct DJS{
   int p[N], rk[N];
  vectorvector<int*,int>> memo;
  vector<size_t> stk;
  void save(){
     stk.push_back(memo.size());
  void undo(){
    while(memo.size() > stk.back()){
       *memo.back().first = memo.back().second;
       memo.pop_back();
    stk.pop_back();
  }
  void assign(int *x, int v){
     memo.push_back({x, *x});
   //assign(&a, b); //a = b
} djs;
```

4.5 Persistent Treap

```
#include <bits/stdc++.h>
using namespace std;
struct Treap {
  static Treap mem[P];
Treap *lc, *rc;
  char c; int sz;
  Treap(){}
  Treap(char _c) : lc(NULL), rc(NULL), sz(1), c(_c){}
} Treap::mem[P], *ptr=Treap::mem ;
int Sz(Treap* t)
 return t?t->sz:0;
void pull(Treap* t) {
  if (!t) return
  t->sz = Sz(t->lc) + Sz(t->rc) + 1;
Treap* merge(Treap* a, Treap* b) {
  if (!a || !b) return a?a:b;
Treap* ret;
  if (myRnd() % (Sz(a) + Sz(b)) < Sz(a)) {
    ret = new (ptr++) Treap(*a);
    ret->rc = merge(a->rc, b);
  else {
    ret = new(ptr++) Treap(*b);
    ret->lc=merge(a, b->lc);
  pull(ret);
  return ret;
void split(Treap* t, int k, Treap* &a, Treap* &b) {
  if (!t) a=b=NULL;
  else if (Sz(t->lc) + 1 <= k) {
    a = new(ptr++) Treap(*t);
    split(t->rc, k-Sz(t->lc)-1, a->rc, b);
    pull(a);
  else {
    b=new(ptr++) Treap(*t);
    split(t->lc, k, a, b->lc);
    pull(b);
int d;
char buf[M];
Treap* ver[N];
ptr = Treap::mem:
v_cnt++;
ver[v_cnt] = ver[v_cnt-1];
split(ver[v_cnt], p, tl, tr);
tl = merge(tl, new(ptr++)Treap(buf[j]));
4.6 Link Cut Tree
```

```
struct SplayNode {
                                                                             return x:
  static SplayNode HOLE;
  SplayNode *ch[2], *par;
                                                                           SplayNode *query(SplayNode *x, SplayNode *y) {
  bool rev:
                                                                             makeRoot(x);
  SplayNode(): par(\&HOLE), rev(false) { ch[0] = ch[1] = \&HOLE; }
                                                                             return access(y);
                                                                           SplayNode *queryLca(SplayNode *x, SplayNode *y) {
  bool isRoot() {
    return (par->ch[0] != this && par->ch[1] != this);
                                                                             access(x);
                                                                             auto lca = access(y);
  void push() {
                                                                             x->splay();
    if (rev) {
                                                                             return lca \rightarrow data + lca \rightarrow ch[1] \rightarrow sum + (x == lca ? 0 : x \rightarrow sum
      if (ch[0]) ch[0]->rev ^= 1;
      if (ch[1]) ch[1]->rev ^= 1;
      swap(ch[0], ch[1]);
rev ^= 1;
                                                                           void modify(SplayNode *x, int data) {
                                                                             x->splay();
    }
                                                                             x->data = data;
                                                                             x->pull();
  void pushFromRoot() {
    if (!isRoot()) par->pushFromRoot();
                                                                        }
    push();
                                                                         4.7
                                                                               Li Chao Tree
  void pull() {
    if (ch[0]) ch[0]->d = d + ch[0]->parLen;
                                                                         struct line {
    if (ch[1]) ch[1]->d = d + ch[1]->parLen;
                                                                           ll a, b;
                                                                           line(): a(0), b(0) {}
 void rotate() {
   SplayNode *p = par, *gp = p->par;
                                                                           line(ll a, ll b): a(a), b(b) {}
                                                                           11 operator()(11 x) const { return a * x + b; }
    bool dir = (p->ch[1] == this);
    par = gp;
    if (!p->isRoot()) gp->ch[gp->ch[1] == p] = this;
                                                                         struct lichao {
    p->ch[dir] = ch[dir \land 1];
                                                                           line st[NN];
    p->ch[dir]->par = p;
                                                                           int sz, lc[NN], rc[NN];
    p->par = this:
                                                                           int gnode() {
    ch[dir ^ 1] = p
                                                                             st[sz] = line(0, -1e18); //min: st[sz] = line(0, 1e18);
    p->pull(), pull();
                                                                             lc[sz] = -1, rc[sz] = -1;
                                                                             return sz++;
  void splay() {
    pushFromRoot();
                                                                           void init() {
    while (!isRoot()) {
                                                                             sz = 0; gnode();
      if (!par->isRoot()) {
   SplayNode *gp = par->par;
                                                                           void add(int l, int r, line tl, int o) {
         if ((gp->ch[0] == par) == (par->ch[0] == this)) rotate
                                                                             //[l, r)
bool lcp = st[o](l) < tl(l); //min: change < to >
              ():
        else par->rotate();
                                                                             bool mcp = st[o]((l + r) / 2) < tl((l + r) / 2); //min:
                                                                                   change < to
      rotate();
                                                                             if (mcp) swap(st[o], tl);
    }
                                                                             if (r - l == 1) return;
                                                                             if (lcp != mcp) {
                                                                               if (lc[o] == -1) lc[o] = gnode();
add(l, (l + r) / 2, tl, lc[o]);
} SplayNode::HOLE;
namespace LCT {
 SplayNode *access(SplayNode *x) {
   SplayNode *last = &SplayNode::HOLE;
                                                                             } else {
                                                                                if (rc[o] == -1) rc[o] = gnode();
    while (x != &SplayNode::HOLE) {
                                                                               add((l + r) / 2, r, tl, rc[o]);
      x->splay();
                                                                             }
      x \rightarrow ch[1] = last;
      x->pull();
                                                                           11 query(int l, int r, int x, int o) {
      last = x;
                                                                             if (r - l == 1) return st[o](x);
      x = x->par;
                                                                             if (x < (1 + r) / 2) {
                                                                               if (lc[o] == -1) return st[o](x);
    return last;
                                                                                return max(st[o](x), query(l, (l + r) / 2, x, lc[o]));
 }
                                                                             } else {
  void makeRoot(SplayNode *x) {
                                                                                if (rc[o] == -1) return st[o](x);
    access(x);
                                                                                return max(st[o](x), query((l + r) / 2, r, x, rc[o]));
    x->splay();
x->rev ^= 1;
                                                                             }
                                                                           }
                                                                        } solver;
  void link(SplayNode *x, SplayNode *y) {
    makeRoot(x);
                                                                         4.8 Dancing Link
    x->par = y;
                                                                         #define MAX 1050
  void cut(SplayNode *x, SplayNode *y) {
                                                                         #define INF 0x3f3f3f3f
    makeRoot(x);
    access(y);
                                                                         struct DLX{
                                                                           int n, sz, s[MAX];
int row[MAX * 100], col[MAX * 100];
    y->splay();
    y->ch[0] = &SplayNode::HOLE;
x->par = &SplayNode::HOLE;
                                                                           int l[MAX * 100], r[MAX * 100], u[MAX * 100], d[MAX * 100];
                                                                           int ans:
 }
  void cutParent(SplayNode *x) {
                                                                           void init(int n) {
                                                                             this -> n = n;
ans = INF;
    access(x);
    x->splay();
                                                                             for (int i = 0; i <= n; ++ i) {
    x->ch[0]->par = &SplayNode::HOLE;
    x->ch[0] = &SplayNode::HOLE;
                                                                               u[i] = d[i] = i;
                                                                               l[i] = i - 1;
                                                                               r[i] = i + 1;
  SplayNode *findRoot(SplayNode *x) {
    x = access(x);
                                                                             r[n] = 0, l[0] = n;

sz = n + 1;
    while (x->ch[0] != \&SplayNode::HOLE) x = x->ch[0];
    x->splay();
                                                                             memset(s, 0, sizeof s);
```

```
void AddRow(int rr, vector<int> sol) {
    int tmp = sz;
    for(auto to : sol) {
      l[sz] = sz - 1;
      r[sz] = sz + 1;
      d[sz] = to;
      u[sz] = u[to];
      d[u[to]] = sz, u[to] = sz;
      row[sz] = rr, col[sz] = to;
      s[to] ++, sz ++;
    r[sz - 1] = tmp, l[tmp] = sz - 1;
#define FOR(i, way, to) for(int i = way[to] ; i != to ; i = way
     Γi<sub>1</sub>)
  void remove(int c) {
    l[r[c]] = l[c];
r[l[c]] = r[c];
    FOR(i, d, c) FOR(j, r, i) {
      u[d[j]] = u[j];
d[u[j]] = d[j];
      --s[col[j]];
  int restore(int c) {
    FOR(i, u, c) FOR(j, l, i) {
      ++s[col[j]];
      u[d[j]] = j;
      d[u[j]] = j;
    l[r[c]] = c;
    r[l[c]] = c;
  void DFS(int floor) {
    if(r[0] == 0) {
      ans = min(ans, floor);
      return;
    if(floor >= ans) return;
    int c = r[0];
    FOR(i, r, 0) if(s[i] < s[c]) c = i;
    remove(c);
    FOR(i, d, c) {
      FOR(j, r, i) remove(col[j]);
      DFS(floor + 1);
      FOR(j, l, i) restore(col[j]);
    restore(c);
 }
} solver;
int n, m;
int32_t main() {
  IOS;
  while(cin >> n >> m) {
    solver.init(m);
    for (int i = 0; i < n; ++ i) {
      int nn, in;
      cin >> nn;
      vector<int> sol;
      for (int j = 0; j < nn; ++ j)
        cin >> in, sol.emplace_back(in);
      solver.AddRow(i, sol);
    solver.DFS(0);
    if(solver.ans == INF) cout << "No" << endl;</pre>
    else cout << solver.ans << endl;</pre>
  return 0;
```

4.9 Range Modify and Query BIT

```
int bit[4][MAX][MAX];
void update(int c[MAX][MAX], int a, int b, int val) {
  for(int i = a + 10; i < MAX; i += i & -i)</pre>
      for(int j = b + 10; j < MAX; j += j \& -j)
        c[i][j] += val;
int update(int x, int y, int val) {
   update(bit[0], x, y, val);
   update(bit[1], x, y, -val * x);
  update(bit[2], x, y, -val * y);
update(bit[3], x, y, val * x * y);
void update(int a, int b, int x, int y, int val){
```

```
update(a, b, val);
  update(a, y + 1, -val);
update(x + 1, b, -val);
  update(x + 1, y + 1, val);
int query(int c[MAX][MAX], int a, int b){
  int cnt = 0;
  for(int i = a + 10; i > 0; i -= i \& -i)
     for(int j = b + 10; j > 0; j -= j \& -j)
       cnt += c[i][j];
  return cnt;
}
int query(int x, int y){
  int cnt = 0;
  cnt += query(bit[0], x, y) * (x + 1) * (y + 1);
  cnt += query(bit[1], x, y) * (y + 1);
cnt += query(bit[2], x, y) * (x + 1);
  cnt += query(bit[3], x, y);
  return cnt;
}
int query(int a, int b, int x, int y){
  int cnt = 0;
  cnt += query(a - 1, b - 1);
  cnt -= query(a - 1, y);
  cnt -= query(x, b - 1);
  cnt += query(x, y);
  return cnt;
}
/* usage:
void update(x1, y1, x2, y2, val);
int query(x1, y1, x2, y2);
```

5 Flow

ISAP with bound 5.1

```
Maximum density subgraph ( \sum W_e + \sum W_v  ) / IVI
Binary search on answer:
For a fixed D, construct a Max flow model as follow:
Let S be Sum of all weight( or inf)
1. from source to each node with cap = S
2. For each (u,v,w) in E, (u->v,cap=w), (v->u,cap=w)
3. For each node v, from v to sink with cap = S + 2 * D - deg[v]
     ] - 2 * (W of v)
where deg[v] = \sum_{s=0}^{\infty} weight of edge associated with v If maxflow < S * IVI, D is an answer.
Requiring subgraph: all vertex can be reached from source with
edge whose cap > 0.
//Be careful that it's zero base !!!!!!!!
#include <bits/stdc++.h>
using namespace std;
typedef long long 11;
#define SZ(x) ((int)(x).size())
#define eb emplace_back
const 11 \text{ INF} = 0x3f3f3f3f3f3f3f3f3f;
const 11 N = 5e2 + 5;
struct isap{
  struct edge{
    int t, r;
    edge(int _t, int _r, ll _c) : t(_t), r(_r), c(_c) {}
  int n, S, T;
  vector<edge> adj[N];
  int dis[N], gap[N], ok;
  isap(int _n, int _s, int _t) : n(_n), S(_s), T(_t) {
    for(int i = 0; i < n + 2; ++ i) adj[i].clear();</pre>
  void add(int u, int v, ll c){
   adj[u].eb( v, adj[v].size(), c );
   adj[v].eb( u, adj[u].size() - 1, 0 );
  ll dfs(int now, ll f){
    if(now == T) return f;
     int mi = n;
    for(edge &e : adj[now]){
       if(e.c){
         Ìl x;
         if( dis[now] == dis[e.t] + 1 && (x = dfs(e.t, min(f, e.
              c))) ){
           e.c -= x
           adj[e.t][e.r].c += x;
```

```
return x:
         mi = min(mi, dis[e.t]);
     if( --gap[dis[now]] == 0) ok = 0;
     dis[now] = mi + 1;
     gap[ dis[now] ]++;
     return 0;
   11 flow(){
     memset(dis, 0, n * 4);
memset(gap, 0, n * 4);
     gap[0] = n;
     ok = 1;
ll r = 0;
     while(dis[S] < n && ok) r += dfs(S, INF);
     return r:
  }
   // below for bounded only
   ll D[N];
   void bounded_init() {
     memset(D, 0, n * 8);
   void add2(int u, int v, ll b, ll c) {
     add(u, v, c - b);
     D[u] -= b;
     D[v] += b;
   ll bounded_flow() {
     int SS = n, TT = n + 1;
ll base = 0;
     for(int i = 0; i < n; ++ i) {</pre>
       if (D[i] > 0) base += D[i];
       if (D[i] > 0) add(SS, i, D[i]);
       if (D[i] < 0) add(i ,TT, -D[i]);
     add(T, S, INF);
     int tmps = S, tmpt = T;
n += 2; S = SS, T = TT;
     11 f = flow();
     n \rightarrow 2; S = tmps; T = tmpt;
     return f == base ? flow() : -1LL;
|};
        Min Cost Max Flow
```

```
struct Cost_Flow {
 struct Edge {
   int to, cap, rev, cost;
   Edge(int _to, int _cap, int _rev, int _cost): to(_to), cap(
        _cap), rev(_rev), cost(_cost) {}
 vector<Edge> G[N];
 void add_edge(int from, int to, int cap, int cost) {
   G[from].push_back(Edge(to, cap, (int)G[to].size(), cost));
    G[to].push_back(Edge(from, 0, (int)G[from].size() - 1, -
         cost));
 int n, s, t;
 void init(int _n, int _s, int _t) {
    n = _n, s = _s, t = _t;
   for (int i = 0; i \le n; ++i) {
      G[i].clear();
   }
 bool in_que[N];
  int dis[N], par[N], par_id[N];
 pair<int, int> flow() {
   int flow = 0, cost = 0;
   while (true) {
      for (int i = 0; i <= n; ++i) {
        dis[i] = INF, in_que[i] = false;
      queue<int> que; que.push(s);
      dis[s] = 0;
      while (!que.empty()) {
        int t = que.front(); que.pop();
        int ptr = 0;
        in_que[t] = false;
        for (Edge e: G[t]) {
          if (e.cap > 0) {
            if (dis[e.to] > dis[t] + e.cost) {
              dis[e.to] = dis[t] + e.cost;
              par[e.to] = t, par_id[e.to] = ptr;
```

if (!in_que[e.to]) {

```
que.push(e.to);
                   in_que[e.to] = true;
                 }
              }
            }
            ++ptr;
          }
        }
        if (dis[t] == INF) break;
        int mn_flow = INF;
        for (int i = t; i != s; i = par[i]) {
         mn_flow = min(mn_flow, G[ par[i] ][ par_id[i] ].cap);
        flow += mn_flow;
cost += mn_flow * dis[t];
        for (int i = t; i != s; i = par[i]) {
   G[ par[i] ][ par_id[i] ].cap -= mn_flow;
          G[ i ][ G[ par[i] ][ par_id[i] ].rev ].cap += mn_flow;
     return make_pair(flow, cost);
} flow;
```

5.3 S-W Global Min Cut

```
| struct SW {
   //find global min cut in O(V^3)
   //points are ZERO-BASE!!!
   static const int N = 506;
   int adj[N][N], wei[N], n;
   bool vis[N], del[N];
   void init(int _n) {
     n = n:
     memset(adj, 0, sizeof(adj));
memset(del, 0, sizeof(del));
   void add_edge(int x, int y, int w) {
     adj[x][y] += w;
     adj[y][x] += w;
   void search(int & s, int & t) {
     memset(wei, 0, sizeof(wei));
memset(vis, 0, sizeof(vis));
     s = t = -1;
     while (true) {
        int mx = -1, mx_id = 0;
        for (int i = 0; i < n; ++i) {
          if (!del[i] && !vis[i] && mx < wei[i]) {</pre>
            mx_id = i
            mx = wei[i];
          }
        if (mx == -1) break;
        vis[mx_id] = true;
        t = mx id:
        for (int i = 0; i < n; ++i)
          if (!vis[i] && !del[i])
            wei[i] += adj[mx_id][i];
     }
   int solve() {
     int ret = INF;
     for (int i = 0; i < n - 1; ++i) {
       int x, y;
       search(x, y);
        ret = min(ret, wei[y]);
        del[y] = true;
        for (int j = 0; j < n; ++j) {
  adj[x][j] += adj[y][j];</pre>
          adj[j][x] += adj[y][j];
       }
     return ret;
} SW;
```

5.4 Gomory Hu Tree

```
| def cut(G,s,t) :
    return minimum s-t cut in G
| def gomory_hu(G):
    T = {}
    p = [1] * |V(G)|
    for s in [2,n] :
```

```
t = p[s]
w(C) = cut(G, s, t)
add(s, t, w(C)) to T
for i in [s + 1, n] :
   if p[i] == t and s-i path exists in G\C :
    p[i] = s
return T;
```

6 Tree

6.1 Minimum Steiner Tree

```
Minimum Steiner Tree
 // 0(V 3^T + V^2 2^T)
struct SteinerTree{
 #define V 33
 #define T 8
 #define INF 1023456789
   int n , dst[V][V] , dp[1 << T][V] , tdst[V];</pre>
   void init( int _n ){
      for( int i = 0 ; i < n ; i ++ ){</pre>
        for( int j = 0 ; j < n ; j ++ )
  dst[ i ][ j ] = INF;</pre>
        dst[ i ][ i ] = 0;
     }
   void add_edge( int ui , int vi , int wi ){
     dst[ ui ][ vi ] = min( dst[ ui ][ vi ] , wi );
     dst[ vi ][ ui ] = min( dst[ vi ][ ui ] , wi );
   void shortest_path(){
     for( int k = 0 ; k < n ; k ++ )
        for( int i = 0 ; i < n ; i ++ )</pre>
           for( int j = 0 ; j < n ; j ++ )
  dst[ i ][ j ] = min( dst[ i ][ j ],</pre>
                  dst[ i ][ k ] + dst[ k ][ j ] );
   int solve( const vector<int>& ter ){
     int t = (int)ter.size();
      for( int i = 0 ; i < ( 1 << t ) ; i ++ )
      for( int j = 0 ; j < n ; j ++ )
    dp[ i ][ j ] = INF;
for( int i = 0 ; i < n ; i ++ )</pre>
        dp[0][i] = 0;
      for( int msk = 1 ; msk < ( 1 << t ) ; msk ++ ){</pre>
        if( msk == (msk \& (-msk))){
          int who = __lg( msk );

for( int i = 0 ; i < n ; i ++ )

    dp[ msk ][ i ] = dst[ ter[ who ] ][ i ];
           continue:
        for( int i = 0 ; i < n ; i ++ )
  for( int submsk = ( msk - 1 ) & msk ; submsk ;</pre>
             submsk = ( submsk - 1 ) & msk )

dp[ msk ][ i ] = min( dp[ msk ][ i ],
                  dp[ submsk ][ i ] +
                  dp[ msk ^ submsk ][ i ] );
        for( int i = 0 ; i < n ; i ++ ){
          tdst[ i ] = INF;
for( int j = 0 ; j < n ; j ++ )
tdst[ i ] = min( tdst[ i ],
                  dp[ msk ][ j ] + dst[ j ][ i ] );
        for( int i = 0 ; i < n ; i ++ )
           dp[ msk ][ i ] = tdst[ i ];
      int ans = INF:
      for( int i = 0 ; i < n ; i ++ )
        ans = min(ans, dp[(1 << t) - 1][i]);
     return ans:
|} solver;
```

6.2 Zhu Liu Algo

```
struct ZL{
    //1 base edge and vertex
static const int N=556,M=2660, MM = M * 10,inf=1e9;
    //MM = M * log N
    struct bian{
        int u,v,w,use,id;
        }b[M],a[MM];
        int n,m=0,ans,pre[N],id[N],vis[N],root,In[N],h[N],len,way[M];
        void init(int _n,int _root){
        for (int i = 0; i < MM; ++i) {</pre>
```

```
a[i] = \{0, 0, 0, 0, 0\};
    n=_n; m=0; b[0].w=1e9; root=_root;
  void add(int u,int v,int w){
    b[++m]=(bian)\{u,v,w,0,m\};
    a[m]=b[m];
  int work(){
    len=m;
     for (;;){
       for (int i=1;i<=n;i++){pre[i]=0; In[i]=inf; id[i]=0; vis[</pre>
       i]=0; h[i]=0;}
for (int i=1;i<=m;i++)
         if (b[i].u!=b[i].v&&b[i].w<In[b[i].v]){</pre>
           pre[b[i].v]=b[i].u; In[b[i].v]=b[i].w; h[b[i].v]=b[i
                7.id;
       for (int i=1;i<=n;i++) if (pre[i]==0&&i!=root) return 0;</pre>
       int cnt=0; In[root]=0;
       for (int i=1;i<=n;i++){</pre>
         if (i!=root) a[h[i]].use++;
         int now=i; ans+=In[i];
while (vis[now]==0&&now!=root){
           vis[now]=i; now=pre[now];
         if (now!=root&&vis[now]==i){
           cnt++; int kk=now;
while (1){
             id[now]=cnt; now=pre[now];
              if (now==kk) break;
         }
       if (cnt==0) return 1;
       for (int i=1;i<=n;i++) if (id[i]==0) id[i]=++cnt;</pre>
       for (int i=1;i<=m;i++){</pre>
         int k1=In[b[i].v]; int k2=b[i].v;
b[i].u=id[b[i].u]; b[i].v=id[b[i].v];
         if (b[i].u!=b[i].v){
           b[i].w-=k1; a[++len].u=b[i].id; a[len].v=h[k2];
           b[i].id=len;
         }
       n=cnt;
       root=id[root];
     return 1;
  int getway(){
     for (int i=1;i<=m;i++) way[i]=0;</pre>
     for (int i=len;i>m;i--){
       a[a[i].u].use+=a[i].use; a[a[i].v].use-=a[i].use;
     for (int i=1;i<=m;i++) way[i]=a[i].use;</pre>
    int ret = 0;
     for (int i = 1; i <= m; ++i){
      if (way[i] == 1) {
         ret += a[i].w;
      }
     return ret;
  }
} zl;
//if zl.work() == 0, then it is not connected
//otherwise, use zl.getway() to check bian is selected or not
```

6.3 Centroid Decomposition

```
const int Mlg = __lg(MAX) + 2;
struct edge {
  int to,weight;
  edge(int _to,int _w):to(_to),weight(_w){}
};

vector<edge> edg[MAX];

struct Cen {
  ll val;
  int p, sz, dep;
  Cen(){}
  Cen(int _p,int _d):val(0),p(_p),sz(0),dep(_d){}
} cen[MAX];
ll dis[Mlg][MAX];

bool visit[MAX];
```

```
vector<int> v;
int sz[MAX], mx[MAX];
void dfs_sz(int id) {
  visit[id]=1;
  v.push_back(id);
  sz[id]=1;
  mx[id]=0;
  for (edge i:edg[id]) {
    if (!visit[i.to]) {
      dfs_sz(i.to);
      mx[id] = max(mx[id],sz[i.to]);
      sz[id] += sz[i.to];
    }
void dfs_dis(int id,int cen_dep,ll weight) {
  dis[cen_dep][id] = weight;
  visit[id]=1;
  for (edge i:edg[id])
    if (!visit[i.to])
      dfs_dis(i.to,cen_dep,weight+i.weight);
void build(int id,int cen_dep,int p) {
  dfs_sz(id);
  int nn=v.size();
  int ccen=-1;
  for (int i:v) {
    if (max(nn-sz[i],mx[i])*2 <= nn)</pre>
      ccen=i;
    visit[i]=0;
  dfs_dis(ccen,cen_dep,0);
  for (int i:v)
                  visit[i]=0;
  v.clear();
  visit[ccen]=1;
  cen[ccen] = Cen(p,cen_dep);
  for (edge i:edg[ccen])
    if (!visit[i.to])
      build(i.to,cen_dep+1,ccen);
}
void add(int id, int d) {
  for(int p=id;p!=-1;p=cen[p].p){
    cen[p].val += dis[cen[p].dep][id]*d;
    cen[p].val -= dis[cen[p].dep-1][id]*d;
    cen[p].sz += d;
}
11 query(int id) {
  ll ret=0:
  int pre_sz=0;
  for(int p=id;p!=-1;p=cen[p].p){
    ret += cen[p].val;
    ret += (cen[p].sz - pre_sz)*dis[cen[p].dep][id];
    pre_sz = cen[p].sz;
  return ret;
// edg[u].push_back(edge(v,w));
// edg[v].push_back(edge(u,w));
// memset(visit,0,sizeof(visit));
// build(1,1,-1);
// add(u, d)
// query(u)
```

6.4 Dynamic MST

```
|/* Dynamic MST O( Q lg^2 Q )
| (qx[i], qy[i])->chg weight of edge No.qx[i] to qy[i]
| delete an edge: (i, \infty)
| add an edge: change from \infty to specific value
| */
| const int SZ=M+3*MXQ;
| int a[N],*tz;
| int find(int xx){
| int root=xx; while(a[root]) root=a[root];
| int next; while((next=a[xx])){a[xx]=root; xx=next; }
| return root;
| }
| bool cmp(int aa,int bb){ return tz[aa]<tz[bb]; }
| int kx[N],ky[N],kt, vd[N],id[M], app[M];
| bool extra[M];
| void solve(int *qx,int *qy,int Q,int n,int *x,int *y,int *z,int
| m1,long long ans){
| if(Q==1){
| for(int i=1;i<=n;i++) a[i]=0;</pre>
```

```
z[ qx[0] ]=qy[0]; tz = z;
for(int i=0;i<m1;i++) id[i]=i;</pre>
    sort(id,id+m1,cmp); int ri,rj;
    for(int i=0;i<m1;i++){</pre>
       ri=find(x[id[i]]); rj=find(y[id[i]]);
       if(ri!=rj){ ans+=z[id[i]]; a[ri]=rj; }
    printf("%lld\n",ans);
    return;
  int ri,rj;
  //contract
  kt=0;
  for(int i=1;i<=n;i++) a[i]=0;</pre>
  for(int i=0;i<Q;i++){</pre>
    ri=find(x[qx[i]]); rj=find(y[qx[i]]); if(ri!=rj) a[ri]=rj;
  int tm=0;
  for(int i=0;i<m1;i++) extra[i]=true;</pre>
  for(int i=0;i<0;i++) extra[ qx[i] ]=false;</pre>
  for(int i=0;i<m1;i++) if(extra[i]) id[tm++]=i;</pre>
  tz=z; sort(id,id+tm,cmp);
  for(int i=0;i<tm;i++){</pre>
    ri=find(x[id[i]]); rj=find(y[id[i]]);
    if(ri!=rj){
      a[ri]=rj; ans += z[id[i]];
       kx[kt]=x[id[i]]; ky[kt]=y[id[i]]; kt++;
    }
  }
  for(int i=1;i<=n;i++) a[i]=0;</pre>
  for(int i=0;i<kt;i++) a[ find(kx[i]) ]=find(ky[i]);</pre>
  int n2=0;
  for(int i=1;i<=n;i++) if(a[i]==0)</pre>
  vd[i]=++n2;
  for(int i=1;i<=n;i++) if(a[i])</pre>
  vd[i]=vd[find(i)];
  int m2=0, *Nx=x+m1, *Ny=y+m1, *Nz=z+m1;
  for(int i=0;i<m1;i++) app[i]=-1;</pre>
  for(int i=0;i<Q;i++) if(app[qx[i]]==-1){</pre>
     Nx[m2] = vd[ x[ qx[i] ] ]; Ny[m2] = vd[ y[ qx[i] ] ]; Nz[m2] = z[ \\
           qx[i] ];
    app[qx[i]]=m2; m2++;
  for(int i=0;i<0;i++){ z[ qx[i] ]=qy[i]; qx[i]=app[qx[i]]; }</pre>
  for(int i=1;i<=n2;i++) a[i]=0;</pre>
  for(int i=0;i<tm;i++){</pre>
    ri=find(vd[ x[id[i]] ]); rj=find(vd[ y[id[i]] ]);
    if(ri!=rj){
       a[ri]=rj; Nx[m2]=vd[ x[id[i]] ];
       Ny[m2]=vd[ y[id[i]] ]; Nz[m2]=z[id[i]]; m2++;
    }
  int mid=Q/2;
  solve(qx,qy,mid,n2,Nx,Ny,Nz,m2,ans);
  solve(qx+mid,qy+mid,Q-mid,n2,Nx,Ny,Nz,m2,ans);
int x[SZ],y[SZ],z[SZ],qx[MXQ],qy[MXQ],n,m,Q;
void init(){
  scanf("%d%d",&n,&m);
  for(int i=0;i<m;i++) scanf("%d%d%d",x+i,y+i,z+i);</pre>
  scanf("%d",&Q);
  for(int i=0;i<Q;i++){ scanf("%d%d",qx+i,qy+i); qx[i]--; }</pre>
void work(){ if(Q) solve(qx,qy,Q,n,x,y,z,m,0); }
int main(){init(); work(); }
```

6.5 Heavy-Light Decomposition

 $if(to != fa){$

```
int siz[MAX] , son[MAX] , dep[MAX] , ffa[MAX];
int top[MAX] , idx[MAX] , idpo = 0;
int n , m;
int e[MAX][3];
vector<int> v[MAX];
struct node{ int big , sml; } st[MAX * 4];
void init(){
   REP(i , 0 , MAX) v[i].clear();
   MEM(siz , 0) , MEM(son , 0) , MEM(dep , 0) , MEM(ffa , 0);
   MEM(top , 0) , MEM(idx , 0) , idpo = 0;
}
void DFS1(int now , int fa , int deep){
   siz[now] = 1;
   dep[now] = deep;
   ffa[now] = fa;
   int big = 0;
   REP(i , 0 , v[now].size()){
    int to = v[now][i];
```

```
DFS1(to , now , deep + 1);
siz[now] += siz[to];
       if(siz[to] > big) big = siz[to] , son[now] = to;
  }
}
void DFS2(int now , int fa , int root){
  top[now] = root;
idx[now] = ++idpo;
  if(son[now] != 0) DFS2(son[now] , now , root);
  REP(i , 0 , v[now].size()){
    int to = v[now][i];
    if(to != fa && to != son[now]) DFS2(to , now , to);
void solveinit(){
  DFS1(1 , 0 , 0);
  DFS2(1 , 0 , 1);
REP(i , 2 , n + 1){
    int a = e[i][0], b = e[i][1], c = e[i][2];
    if(dep[a] < dep[b]) swap(a , b);</pre>
    update(1 , 1 , n , idx[a] , c);
  }
void query(int a , int b){
  ans.big = -INF, ans.sml = INF;
  int t1 = top[a] , t2 = top[b];
while(t1 != t2){
    if(dep[t1] < dep[t2]) swap(t1 , t2) , swap(a , b);
ans = pull(ans , query(1 , 1 , n , idx[t1] , idx[a]));
a = ffa[t1] , t1 = top[a];</pre>
  if(dep[a] > dep[b]) swap(a, b);
  if(a != b) ans = pull(ans , query(1 , 1 , n , idx[son[a]] ,
        idx[b]));
  return cout << ans.sml << " " << ans.big << endl , void();</pre>
init();
REP(i, 2, n + 1){
  int a , b , c; cin >> a >> b >> c;
e[i][0] = a , e[i][1] = b , e[i][2] = c;
  v[a].pb(b); v[b].pb(a);
solveinit();
query(a, b);
6.6 Block tree
#include <bits/stdc++.h>
using namespace std;
const int N = 30006;
const int K = 177; // 2 2 2 2 2 2 2 2 K 2 2
int w[N], sum[N], mx[N];
int root[N], sz[N], fa[N], dep[N]; vector<int> G[N], T[N]; // T @ @ @ @ @ @ @ // root[i] @ @ @ i @ @ @ @ @ @ @ @
// sum[i], mx[i] @@@@i @@@@@@@@
void dfs1(int now, int par, int depth) {
  fa[now] = par; dep[now] = depth;
  if (!root[now]) { // @ @ @ @ @ @ @ @ @ @ @ @
    root[now] = now;
    sz[now] = 1;
  for (int i = 0; i < (int)G[now].size(); ++i) {</pre>
    int to = G[now][i];
     if (to == par) continue;
    if (sz[root[now]] + 1 < K) {
// a a a now a a a a a a a a a a a a a a a
```

T[now].push_back(to);

root[to] = root[now];

dfs1(to, now, depth + 1);

void dfs2(int now, int pre_sum, int pre_mx) {
 // ② ② ② ② ② ② ② mx, sum

for (int i = 0; i < (int)T[now].size(); ++i) {</pre>

dfs2(to, pre_sum + w[to], max(pre_mx, w[to]));

sum[now] = pre_sum, mx[now] = pre_mx;

++sz[root[now]];

int to = T[now][i];

}

}

```
void change(int pos, int val) {
  w[pos] = val;
  dfs2(root[pos], w[ root[pos] ], w[ root[pos] ]);
// @ @ @ @ @ @ @ @ @ @ @ @ @ @ @ @ pos @ @ @ @
void qmax(int u, int v) {
   // @ @ @ @ @ @ qsum @ @ @ @ @ @ @ @ @ @
void qsum(int u, int v) {
  int ans = 0;
  while (u != v) {
    if (root[u] == root[v]) {
// @ @ @ @ @ @ @ @ @ @ @ @ @
      if (dep[u] < dep[v]) swap(u, v);</pre>
      ans += w[u];
      u = fa[u];
    }
    if (dep[ root[u] ] < dep[ root[v] ]) swap(u, v);
      ans += sum[u]
      u = fa[root[u]];
  }
  ans += w[u]; // 2 2 2 2 2 LCA 2 2 2
  printf("%d\n", ans);
```

7 Graph

7.1 Biconnected Component

```
int low[N], dfn[N];
bool vis[N];
int cnt[N], e[N], x[N], y[N]; // e[i] = x[i] ^ y[i]
 int stamp, bcc_no = 0;
vector<int> G[N], bcc[N];
stack<int> sta;
void dfs(int now,int par) {
  vis[now] = true;
   dfn[now] = low[now] = (++stamp);
   for (int i : G[now]) {
     int to = ( e[i] ^ now );
     if (to == par) continue;
     if (!vis[to]) {
  sta.push(i); dfs(to,now);
       low[now] = min(low[now], low[to]);
       if (low[to] >= dfn[now]) {
         ++bcc_no; int p; // p is edge index
         do {
           p = sta.top(); sta.pop();
           bcc[bcc_no].push_back(p);
         } while (p != i);
      }
     else if (dfn[to] < dfn[now]) {</pre>
       sta.push(i);
       low[now] = min(low[now], dfn[to]);
  }
1 }
```

7.2 General Graph Macthing

```
const int N = 100006, E = (2e5) * 2;
struct Graph{
    //1-index
    int to[E],bro[E],head[N],e;
    int lnk[N],vis[N],stp,n;
    int per[N];
    void init( int _n ){
        //remember to set every array to 0
        stp = 0; e = 1; n = _n;
        for( int i = 1 ; i <= n ; i ++ )
            head[i] = lnk[i] = vis[i] = 0, per[i] = i;
        //random_shuffle(per+1, per+n+1);
    }
    void add_edge(int u,int v){
        u=per[u], v=per[v];
        to[e]=v,bro[e]=head[u],head[u]=e++;
        to[e]=u,bro[e]=head[v],head[v]=e++;</pre>
```

Graph)

| struct WeightGraph {

```
static const int INF = INT MAX:
                                                                        static const int N = 514;
  bool dfs(int x){
    vis[x]=stp;
                                                                        struct edge{
     for(int i=head[x];i;i=bro[i]){
                                                                          int u,v,w; edge(){}
       int v=to[i];
                                                                          edge(int ui,int vi,int wi)
       if(!lnk[v]){
                                                                            :u(ui),v(vi),w(wi){}
        lnk[x]=v,lnk[v]=x;
return true;
                                                                        int n,n_x;
       }else if(vis[lnk[v]]<stp){</pre>
                                                                        edge g[N*2][N*2];
         int w=lnk[v];
                                                                        int lab[N*2];
         lnk[x]=v, lnk[v]=x, lnk[w]=0;
                                                                        int match[N*2],slack[N*2],st[N*2],pa[N*2];
                                                                        int flo_from[N*2][N+1],S[N*2],vis[N*2];
         if(dfs(w)){
           return true;
                                                                        vector<int> flo[N*2];
                                                                        queue<int> q;
         lnk[w]=v, lnk[v]=w, lnk[x]=0;
                                                                        int e_delta(const edge &e){
      }
                                                                          return lab[e.u]+lab[e.v]-g[e.u][e.v].w*2;
    return false;
                                                                        void update_slack(int u,int x){
                                                                          if(!slack[x]||e_delta(g[u][x])<e_delta(g[slack[x]][x]))</pre>
  int solve(){
                                                                               slack[x]=u;
    int ans = 0;
     for(int i=1;i<=n;i++)</pre>
                                                                        void set_slack(int x){
       if(!lnk[i]){
                                                                          slack[x]=0;
        stp++; ans += dfs(i);
                                                                          for(int u=1;u<=n;++u)</pre>
                                                                            if(g[u][x].w>0&&st[u]!=x&&S[st[u]]==0)
    return ans;
                                                                              update_slack(u,x);
  }
|} graph;
                                                                        void q_push(int x){
                                                                          if(x<=n)q.push(x);</pre>
7.3
       KM
                                                                          else for(size_t i=0;i<flo[x].size();i++)</pre>
                                                                            q_push(flo[x][i]);
const int INF = 0x3f3f3f3f;
const int maxn = 610:
                                                                        void set_st(int x,int b){
                                                                          st[x]=b;
int n, w[maxn][maxn], lx[maxn], ly[maxn], slk[maxn];
                                                                          if(x>n)for(size_t i=0;i<flo[x].size();++i)</pre>
int s[maxn], t[maxn], good[maxn];
                                                                            set_st(flo[x][i],b);
int match(int now) {
                                                                        int get_pr(int b,int xr){
  s[now] = 1;
                                                                          int pr=find(flo[b].begin(),flo[b].end(),xr)-flo[b].begin();
  for (int to = 1; to <= n; to ++) {
                                                                          if(pr%2==1){
     if(t[to]) continue;
                                                                            reverse(flo[b].begin()+1,flo[b].end());
    if(lx[now] + ly[to] == w[now][to]) {
                                                                            return (int)flo[b].size()-pr;
       t[to] = 1;
                                                                          }else return pr;
       if(good[to] == 0 || match(good[to]))
         return good[to] = now, 1;
                                                                        void set_match(int u,int v){
                                                                          match[u]=g[u][v].v;
    else slk[to] = min(slk[to], lx[now] + ly[to] - w[now][to]);
                                                                          if(u<=n) return;</pre>
                                                                          edge e=g[u][v];
  return 0;
                                                                          int xr=flo_from[u][e.u],pr=get_pr(u,xr);
                                                                          for(int i=0;i<pr;++i)set_match(flo[u][i],flo[u][i^1]);</pre>
void update() {
                                                                          set_match(xr,v);
  int val = INF;
  for (int i = 1; i \le n; i ++)
                                                                          rotate(flo[u].begin(),flo[u].begin()+pr,flo[u].end());
    if(t[i] == 0) val = min(val, slk[i]);
                                                                        void augment(int u,int v){
  for (int i = 1; i <= n; i ++) {
                                                                          for(;;){
    if(s[i]) lx[i] -= val;
                                                                            int xnv=st[match[u]];
    if(t[i]) ly[i] += val;
  }
                                                                            set_match(u,v);
                                                                            if(!xnv)return;
}
                                                                            set_match(xnv,st[pa[xnv]]);
void run_km() {
                                                                            u=st[pa[xnv]],v=xnv;
  for (int i = 1; i <= n; i ++) {
                                                                          }
    lx[i] = w[i][1];
    for (int j = 1; j \le n; j ++)
                                                                        int get_lca(int u,int v){
      lx[i] = max(lx[i], w[i][j]);
                                                                          static int t=0;
                                                                          for(++t;ullv;swap(u,v)){
  for (int i = 1; i <= n; i ++)
                                                                            if(u==0)continue;
    ly[i] = 0, good[i] = 0;
  for (int i = 1; i <= n; i ++) {
                                                                            if(vis[u]==t)return u;
                                                                            vis[u]=t;
    for (int j = 1; j \ll n; j \leftrightarrow slk[j] = INF;
                                                                            u=st[match[u]];
    while(1) {
       for (int j = 1; j <= n; j ++)
s[j] = t[j] = 0;
                                                                            if(u)u=st[pa[u]];
                                                                          return 0;
       if(match(i)) break;
                                                                        }
       else update();
                                                                        void add_blossom(int u,int lca,int v){
  }
                                                                          while(b<=n_x&&st[b])++b;</pre>
                                                                          if(b>n_x)++n_x
/* how_to_use:
                                                                          lab[b]=0, S[b]=0;
1. put edge in w[i][j]
2. run_km
                                                                          match[b]=match[lca];
                                                                          flo[b].clear();
3. match: (good[i], i)
*/
                                                                          flo[b].push_back(lca);
                                                                          for(int x=u,y;x!=lca;x=st[pa[y]])
       Maximum Weighted Matching(General
                                                                            flo[b].push_back(x),flo[b].push_back(y=st[match[x]]),
                                                                                 q_push(y);
```

reverse(flo[b].begin()+1,flo[b].end());
for(int x=v,y;x!=lca;x=st[pa[y]])

```
flo[b].push_back(x),flo[b].push_back(y=st[match[x]]),
         q_push(y);
  set_st(b,b);
  for(int x=1;x<=n_x;++x)g[b][x].w=g[x][b].w=0;</pre>
  for(int x=1;x<=n;++x)flo_from[b][x]=0;</pre>
  for(size_t i=0;i<flo[b].size();++i){</pre>
    int xs=flo[b][i];
    for(int x=1;x<=n_x;++x)</pre>
      if(g[b][x].w==0|le_delta(g[xs][x]) < e_delta(g[b][x]))
        g[b][x]=g[xs][x],g[x][b]=g[x][xs];
    for(int x=1;x<=n;++x)</pre>
      if(flo_from[xs][x])flo_from[b][x]=xs;
  set_slack(b);
void expand_blossom(int b){
  for(size_t i=0;i<flo[b].size();++i)</pre>
    set_st(flo[b][i],flo[b][i]);
  int xr=flo_from[b][g[b][pa[b]].u],pr=get_pr(b,xr);
  for(int i=0;i<pr;i+=2){</pre>
    int xs=flo[b][i],xns=flo[b][i+1];
    pa[xs]=g[xns][xs].u;
    S[xs]=1,S[xns]=0;
    slack[xs]=0,set_slack(xns);
    q_push(xns);
  S[xr]=1,pa[xr]=pa[b];
  for(size_t i=pr+1;i<flo[b].size();++i){</pre>
    int xs=flo[b][i];
    S[xs]=-1,set_slack(xs);
  }
  st[b]=0;
bool on_found_edge(const edge &e){
  int u=st[e.u],v=st[e.v];
  if(S[v]==-1){
    pa[v]=e.u,S[v]=1;
    int nu=st[match[v]];
    slack[v]=slack[nu]=0;
  S[nu]=0,q_push(nu);
}else if(S[v]==0){
    int lca=get_lca(u,v);
    if(!lca)return augment(u,v),augment(v,u),true;
    else add_blossom(u,lca,v);
  }
  return false;
bool matching(){
  memset(S+1,-1,sizeof(int)*n_x);
  memset(slack+1,0,sizeof(int)*n_x);
  q=queue<int>();
  for(int x=1;x<=n_x;++x)</pre>
    if(st[x]==x&&!match[x])pa[x]=0,S[x]=0,q_push(x);
  if(q.empty())return false;
  for(;;){
    while(q.size()){
      int u=q.front();q.pop();
      if(S[st[u]]==1)continue;
      for(int v=1;v<=n;++v)</pre>
        if(g[u][v].w>0&&st[u]!=st[v]){
          if(e_delta(g[u][v])==0){
             if(on_found_edge(g[u][v]))return true;
          }else update_slack(u,st[v]);
    int d=INF;
    for(int b=n+1;b<=n_x;++b)</pre>
      if(st[b]==b&&S[b]==1)d=min(d,lab[b]/2);
    for(int x=1;x<=n_x;++x)</pre>
      if(st[x]==x\&&slack[x]){
         if(S[x]==-1)d=min(d,e_delta(g[slack[x]][x]));
         else if(S[x]==0)d=min(d,e_delta(g[slack[x]][x])/2);
    for(int u=1;u<=n;++u){</pre>
      if(S[st[u]]==0){
         if(lab[u]<=d)return 0;</pre>
        lab[u]-=d;
      }else if(S[st[u]]==1)lab[u]+=d;
    for(int b=n+1;b<=n_x;++b)</pre>
      if(st[b]==b){
        if(S[st[b]]==0)lab[b]+=d*2;
        else if(S[st[b]]==1)lab[b]-=d*2;
    a=aueue<int>():
    for(int x=1;x<=n_x;++x)</pre>
```

```
if(st[x]==x&&slack[x]&&st[slack[x]]!=x&&e_delta(g[slack
               [x]][x])==0)
            if(on_found_edge(g[slack[x]][x]))return true;
        for(int b=n+1;b<=n_x;++b)</pre>
          if(st[b]==b&&S[b]==1&&lab[b]==0)expand_blossom(b);
     }
     return false:
   pair<long long,int> solve(){
     memset(match+1,0,sizeof(int)*n);
     int n_matches=0;
     long long tot_weight=0;
for(int u=0;u<=n;++u)st[u]=u,flo[u].clear();</pre>
      int w_max=0;
     for(int u=1;u<=n;++u)</pre>
        for(int v=1; v<=n; ++v){</pre>
          flo_from[u][v]=(u==v?u:0);
          w_max=max(w_max,g[u][v].w);
     for(int u=1;u<=n;++u)lab[u]=w_max;</pre>
     while(matching())++n_matches;
     for(int u=1;u<=n;++u)</pre>
        if(match[u]&&match[u]<u)</pre>
          tot_weight+=g[u][match[u]].w;
     return make_pair(tot_weight,n_matches);
   void add_edge( int ui , int vi , int wi ){
     g[ui][vi].w = g[vi][ui].w = wi;
   void init( int _n ){
     n = _n;
     for(int u=1;u<=n;++u)</pre>
        for(int v=1;v<=n;++v)</pre>
          g[u][v]=edge(u,v,0);
} graph;
 7.5 Minimum Mean Cycle
 /* minimum mean cycle O(VE) */
 struct MMC{
   struct Edge { int v,u; double c; };
   int n, m, prv[V][V], prve[V][V], vst[V];
   Edge e[E];
   vector<int> edgeID, cycle, rho;
   double d[V][V];
   void init( int _n )
   { n = _n; m = 0; }
// WARNING: TYPE matters
   void addEdge( int vi , int ui , double ci )
{ e[ m ++ ] = { vi , ui , ci }; }
   void bellman_ford() {
     for(int i=0; i<n; i++) d[0][i]=0;
for(int i=0; i<n; i++) {</pre>
       fill(d[i+1], d[i+1]+n, inf);
for(int j=0; j<m; j++) {
          int v = e[j].v, u = e[j].u;
          if(d[i][v]<inf && d[i+1][u]>d[i][v]+e[j].c) {
            d[i+1][u] = d[i][v]+e[j].c;
            prv[i+1][u] = v;
            prve[i+1][u] = j;
         }
       }
     }
   double solve(){
     // returns inf if no cycle, mmc otherwise
     double mmc=inf;
     int st = -1
     bellman_ford();
     for(int i=0; i<n; i++) {</pre>
        double avg=-inf;
        for(int k=0; k<n; k++) {</pre>
          if(d[n][i] < inf-eps) avg=max(avg,(d[n][i]-d[k][i])/(n-k)
          else avg=max(avg,inf);
        if (avg < mmc) tie(mmc, st) = tie(avg, i);</pre>
     FZ(vst); edgeID.clear(); cycle.clear(); rho.clear();
     for (int i=n; !vst[st]; st=prv[i--][st]) {
        vst[st]++;
```

edgeID.PB(prve[i][st]);

while (vst[st] != 2) {

rho.PB(st);

int s;

int vl, v[LEN];

// vector<int> v;

```
int v = rho.back(); rho.pop_back();
                                                                         Bigint() : s(1) \{ vl = 0; \}
       cycle.PB(v);
                                                                         Bigint(long long a) {
   s = 1; vl = 0;
       vst[v]++;
                                                                           if (a' < 0) \{ s = -1; a = -a; \}
    reverse(ALL(edgeID));
                                                                           while (a) {
                                                                             push_back(a % BIGMOD);
    edgeID.resize(SZ(cycle));
                                                                             a /= BIGMOD;
    return mmc;
  }
|} mmc;
                                                                         Bigint(string str) {
   s = 1; vl = 0;
7.6 Maximum Clique
                                                                           int stPos = 0, num = 0;
                                                                           if (!str.empty() && str[0] == '-') {
struct BKB{
                                                                             stPos = 1;
   static const int MAX_N = 50;
                                                                             s = -1;
   typedef bitset<MAX_N> bst;
  bst N[MAX_N];
                                                                           for (int i=SZ(str)-1, q=1; i>=stPos; i--) {
   int n;
                                                                             num += (str[i] - '0') * q;
  11 wei[MAX_N], ans, cc;
                                                                             if ((q *= 10) >= BIGMOD) {
  BKB(int _n = 0): n(_n), ans(0), cc(0){
                                                                               push back(num):
    for(int i = 0; i < _n; ++ i)
                                                                               num = 0; q = 1;
      N[i].reset();
  void add_edge(int a, int b) {
                                                                           if (num) push_back(num);
    N[a][b] = N[b][a] = 1;
                                                                           n();
                                                                         }
  void set_wei(int a, ll w) {
                                                                         int len() const {
    wei[a] = w;
                                                                           return vl;//return SZ(v);
  11 CNT(bst P) {
                                                                         bool empty() const { return len() == 0; }
    //if vertices have no weight: return P.count();
                                                                         void push_back(int x) {
     11 \text{ rt} = 0;
                                                                           v[vl++] = x; //v.PB(x);
    for(int i = P._Find_first(); i < n; i = P._Find_next(i) )</pre>
       rt += wei[i];
                                                                         void pop_back() {
    return rt;
                                                                           vl--; //v.pop_back();
  void pro(bst P, ll cnt = 0) {
                                                                         int back() const {
    if (!P.any()){
                                                                           return v[vl-1]; //return v.back();
       if(cnt == ans)
         ++ cc;
                                                                         void n() {
       else if(cnt > ans) {
                                                                           while (!empty() && !back()) pop_back();
        ans = cnt;
         cc = 1;
                                                                         void resize(int nl) {
       return;
                                                                           vl = nl; //v.resize(nl);
                                                                           fill(v, v+vl, 0); //fill(ALL(v), 0);
    // "<" can be change to "<=" if we don't need to count</pre>
    if ( CNT(P) + cnt < ans)</pre>
                                                                         void print() const {
       return;
                                                                           if (empty()) { putchar('0'); return; }
     int u = P._Find_first();
                                                                           if (s == -1) putchar('
    bst now = P \& \sim N[u];
                                                                           printf("%d", back());
    for (int i = now._Find_first(); i < n; i = now._Find_next(i</pre>
                                                                           for (int i=len()-2; i>=0; i--) printf("%.4d",v[i]);
         )){
       pro(P & N[i], cnt + wei[i]);
                                                                         friend std::ostream& operator << (std::ostream& out, const</pre>
       P[i] = 0;
                                                                              Bigint &a) {
                                                                           if (a.empty()) { out << "0"; return out; }
if (a.s == -1) out << "-";</pre>
     return;
                                                                           out << a.back();
  pll solve() {
                                                                           for (int i=a.len()-2; i>=0; i--) {
    bst tmp;
                                                                             char str[10];
    tmp.reset();
                                                                             snprintf(str, 5, "%.4d", a.v[i]);
    for(int i = 0; i < n; ++ i)
                                                                             out << str;
      tmp[i] = 1;
    pro(tmp);
                                                                           return out;
    return pll(ans, cc);
                                                                         int cp3(const Bigint &b)const {
|} ss(0);
                                                                           if (s != b.s) return s - b.s;
if (s == -1) return -(-*this).cp3(-b);
                                                                           if (len() != b.len()) return len()-b.len();//int
      Math
                                                                           for (int i=len()-1; i>=0; i--)
                                                                             if (v[i]!=b.v[i]) return v[i]-b.v[i];
8.1 Extended Euclidean
                                                                           return 0;
// ax + by = gcd(a, b)
                                                                         bool operator<(const Bigint &b)const
ll exgcd(ll a, ll b, ll &x, ll &y){
                                                                         { return cp3(b)<0; }
   if(a == 0) return x = 0, y = 1, b;
                                                                         bool operator <= (const Bigint &b) const
  ll g = exgcd(b % a, a, y, x);
x -= b / a * y;
                                                                         { return cp3(b)<=0; }
                                                                         bool operator==(const Bigint &b)const
  return g;
                                                                         { return cp3(b)==0; }
į }
                                                                         bool operator!=(const Bigint &b)const
                                                                         { return cp3(b)!=0; }
8.2 Big Integer
                                                                         bool operator>(const Bigint &b)const
                                                                         { return cp3(b)>0; }
struct Bigint{
                                                                         bool operator>=(const Bigint &b)const
  static const int LEN = 60;
                                                                         { return cp3(b)>=0; }
   static const int BIGMOD = 10000;
                                                                         Bigint operator - () const {
```

Bigint r = (*this);

r.s = -r.s;

```
return r:
   Bigint operator + (const Bigint &b) const {
     if (s == -1) return -(-(*this)+(-b));
     if (b.s == -1) return (*this)-(-b);
     Bigint r;
     int nl = max(len(), b.len());
     r.resize(nl + 1);
for (int i=0; i<nl; i++) {
        if (i < len()) r.v[i] += v[i];</pre>
        if (i < b.len()) r.v[i] += b.v[i];</pre>
        if(r.v[i] >= BIGMOD) {
          r.v[i+1] += r.v[i] / BIGMOD;
          r.v[i] %= BIGMOD;
     }
     r.n();
     return r:
   Bigint operator - (const Bigint &b) const {
     if (s == -1) return -(-(*this)-(-b));
     if (b.s == -1) return (*this)+(-b);
     if ((*this) < b) return -(b-(*this));</pre>
     Biaint r:
     r.resize(len());
     for (int i=0; i<len(); i++) {</pre>
       r.v[i] += v[i];
        if (i < b.len()) r.v[i] -= b.v[i];</pre>
        if (r.v[i] < 0) {</pre>
          r.v[i] += BIGMOD;
          r.v[i+1]--;
     }
     r.n();
return r;
   Bigint operator * (const Bigint &b) {
     r.resize(len() + b.len() + 1);
r.s = s * b.s;
for (int i=0; i<len(); i++) {</pre>
       for (int j=0; j<b.len(); j++) {
  r.v[i+j] += v[i] * b.v[j];</pre>
          if(r.v[i+j] >= BIGMOD) {
            r.v[i+j+1] += r.v[i+j] / BIGMOD;
            r.v[i+j] %= BIGMOD;
          }
       }
     }
     r.n();
     return r;
   Bigint operator / (const Bigint &b) {
     Bigint r;
     r.resize(max(1, len()-b.len()+1));
     int oriS = s;
     Bigint b2 = b; // b2 = abs(b)
s = b2.s = r.s = 1;
     for (int i=r.len()-1; i>=0; i--) {
       int d=0, u=BIGMOD-1;
        while(d<u) {
          int m = (d+u+1)>>1;
          r.v[i] = m;
          if((r*b2) > (*this)) u = m-1;
          else d = m;
       }
       r.v[i] = d;
     }
     s = oriS;
r.s = s * b.s;
     r.n();
  Bigint operator % (const Bigint &b) {
     return (*this)-(*this)/b*b;
| };
```

8.3 Gaussian Elimination

```
const int GAUSS_MOD = 100000007LL;
struct GAUSS{
  int n;
  vector<vector<int>> v;
  int ppow(int a , int k){
   if(k == 0) return 1;
  if(k % 2 == 0) return ppow(a * a % GAUSS_MOD , k >> 1);
```

```
if(k % 2 == 1) return ppow(a * a % GAUSS_MOD , k >> 1) * a
        % GAUSS_MOD;
  }
  vector<int> solve(){
    vector<int> ans(n);
    REP(now , 0 , n){
     REP(i , now , n) if(v[now][now] == 0 && v[i][now] != 0)
       swap(v[i], v[now]); // det = -det;
     if(v[now][now] == 0) return ans;
     int inv = ppow(v[now][now] , GAUSS_MOD - 2);
     REP(i , 0 , n) if(i != now){
       int tmp = v[i][now] * inv % GAUSS_MOD;
       }
    return ans;
  }
  // gs.v.clear() , gs.v.resize(n , vector<int>(n + 1 , 0));
|} gs;
```

8.4 Linear Basis

```
const int MAX_M = 500; //maximum number of variable
typedef bitset<MAX_M+1> bst;
struct linear_basis{
  int m:
  bst mat[MAX_M];
  linear_basis(int _m):m(_m){
    for(int i = 0; i < _m; ++ i) mat[i].reset();</pre>
  // True means "No solution"
  int add_constraint(bst now) {
    for(int j = 0; j < m; ++ j) {
      if(now[j]){
         if(mat[j][j]) now ^= mat[j];
        else{
          mat[j] = now;
           for(int k = j + 1; k < m; ++ k)
             if(mat[j][k])
           mat[j] ^= mat[k];
for(int k = 0; k < j; ++ k)
             if(mat[k][j])
               mat[k] ^= mat[j];
          return 0:
        }
      }
    }
    return now[m];
  // get one possible solution
  bst get_ans() {
    bst rt; rt.reset();
    for(int i = 0; i < m; ++ i)</pre>
      if(mat[i][i] && mat[i][m])
        rt[i] = 1;
    return rt;
  }
};
/* usage :
1. Init it with # of variables
2. Adding constraint with format x1, x2..., xm, C
   get_ans return one possible solution
```

8.5 Build Prime

```
// MAX, eb
void build_prime(int min_fc[], vector<int> &P){
   for(int i = 2; i < MAX; ++ i){
      if(min_fc[i] == 0) min_fc[i] = i , P.eb(i);
      for(auto j : P){
       if(i * j >= MAX) break;
      min_fc[i * j] = j;
      if(i % j == 0) break;
   }
}
```

8.6 Miller Rabin

```
ll mul(ll a,ll b,ll mod) {
  //calculate a*b % mod
  ll r=0; a%=mod; b%=mod;
  while (b) {
```

```
if (b&1) r=(a+r)=mod?a+r-mod:a+r;
    a=(a+a>=mod?a+a-mod:a+a):
    b>>=1;
  return r:
ll power(ll a,ll n,ll mod) {
  if (n==0) return 1ll;
  else if (n==1) return a%mod;
  return mul( power(mul(a,a,mod),n/2,mod),n%2?a:1,mod );
const bool PRIME = 1, COMPOSITE = 0;
bool miller_robin(ll n,ll a) {
  if (__gcd(a,n) == n) return PRIME;
  if (__gcd(a,n) != 1) return COMPOSITE;
 ll d=n-1,r=0,ret;
  while (d%2==0) {
   r++; d/=2;
 }
 ret = power(a,d,n);
  if (ret==1 ||ret==n-1) return PRIME;
  while (r--)
    ret = mul(ret,ret,n);
    if (ret==n-1) return PRIME;
  return COMPOSITE;
bool isPrime(ll n) {
  //for int: 2,7,61
  11 as[7] = \{2,325,9375,28178,450775,9780504,1795265022\};
  for (int i=0;7>i;i++) {
   if (miller_robin(n,as[i]) == COMPOSITE) return COMPOSITE;
  return PRIME:
```

8.7 Pollard Rho

```
// isPrime (miller rabin)
map<ll, int> cnt;
 void PollardRho(ll n) {
   if (n == 1) return;
   if (isPrime(n)) return ++cnt[n], void();
   if (n % 2 == 0) return PollardRho(n / 2), ++cnt[2], void();
  11 x = 2, y = 2, d = 1, p = 1;
   auto f = [\&](auto x, auto n, int p) { return (mul(x, x, n) + auto n, int p) } 
       p) % n; }
   while (true) {
     if (d != n && d != 1) {
       PollardRho(n / d);
       PollardRho(d);
    if (d == n) ++p;
    x = f(x, n, p); y = f(f(y, n, p), n, p);
     d = \_gcd(abs(x - y), n);
| }
```

8.8 Build Phi and Mu

```
void build_phi(int ax[], int n){
  for(int i = 1; i <= n; ++i)
    ax[i] = i;
  for(int i = 1; i <= n; ++i)
    for(int j = i + i; j <= n; j += i)
    ax[j] -= ax[i];
}
void build_mu(int ax[], int n){
  for(int i = 1; i <= n; ++i)
    ax[i] = 0;
  ax[1] = 1;
  for(int i = 1; i <= n; ++i)
    for(int j = i + i; j <= n; j += i)
    ax[j] -= ax[i];
}</pre>
```

8.9 Primitive Root

```
// build_phi, power, eb
// M has primitive root when M = 2, 4, p^n, 2p^n
|ll Primitive_root(ll n) {
   if(n == 2)    return 1;
   vector<ll> sol;
   ll val = phi[n];
   for(ll i = 2; i * i <= val ; ++ i){
      if(val % i == 0){</pre>
```

8.10 Cipolla's Algorithm

```
struct Cipolla {
   ll p, n, a, w;
   Cipolla(ll'_p, ll _n) : p(_p), n(_n){
     n %= p;
a = -1;
   il power(ll a, ll x) {
     if(x == 0) return 1;
     return power(a * a % p, x >> 1) * (x & 1 ? a : 1) % p;
   inline int lgd(ll x) {
     return power(x, (p - 1) / 2);
   ll rnd() {
     return ( ((11)rand() << 28) + rand() );</pre>
  pll mul(pll a, pll b) {
     pll power(pll ii, ll x)
     if(x == 0) return pll(1, 0);
     return mul(power(mul(ii, ii), x >> 1), (x & 1 ? ii : pll(1,
   ll solve() {
     if(p == 2)
  return n & 1;
if(lgd(n) == p - 1) return -1;
     if(n == 0) return 0;
     while(a = rnd() % p, lgd((a * a - n + p)% p) == 1);
w = (a * a - n + p) % p;
     pll ii = power(pll(a, 1), (p + 1) / 2);
     assert(ii.S == 0);
     return ii.F;
};
```

8.11 Discrete Log

```
// power
int DiscreteLog_with_s(int s, int x, int y, int m) {
   int kStep = max((int)sqrt(m), 10);
   unordered_map<int, int> p;
   int b = 1:
   for (int i = 0; i < kStep; ++i) {
     p[y] = i;
y = 1LL * y * x % m;
b = 1LL * b * x % m;
  for (int i = 0; i < m + 10; i += kStep) {
    s = 1LL * s * b % m;</pre>
     if (p.find(s) != p.end()) return i + kStep - p[s];
   return -1:
int DiscreteLog(int x, int y, int m) {
   // x ^? === y % m
  if (m == 1) return 0;
// y %= m;
   for (int i = 0; i < 70; ++i) {
     if (s == y) return i;
s = 1LL * s * x % m;
  if (s == y) return 70;
```

return p;

if (power(x, p, m) != y) return -1;

int p = 70 + DiscreteLog_with_s(s, x, y, m);

```
8.12 Integer Partition
 void build_partition(int _dp[], int n, int mod){
    _dp[0] = 1;
   for(int i = 1; i \le n; ++ i){
     for(int j = 1; j <= n; ++ j){
int tmp = j * (j * 3 - 1) / 2;
        if(tmp > i) break;
        else if(j % 2 == 1) _{dp[i]} = (_{dp[i]} + _{dp[i - tmp]}) %
             mod:
        else if(j % 2 == 0) _{dp[i]} = (_{dp[i]} - _{dp[i - tmp]} + mod
             ) % mod;
     for(int j = 1; j <= n; ++ j){
  int tmp = j * (j * 3 + 1) / 2;</pre>
        if(tmp > i) break;
        else if(j % 2 == 1) _{dp[i]} = (_{dp[i]} + _{dp[i - tmp]}) %
             mod:
        else if(j % 2 == 0) _{dp[i]} = (_{dp[i]} - _{dp[i} - _{tmp]} + mod
     }
   return:
| }
```

Meissel-Lehmer Algorithm 8.13

```
// count number of prime that is <= n
int64_t PrimeCount(int64_t n) {
 if (n <= 1) return 0;
  const int v = sqrt(n);
 vector<int> smalls(v + 1);
 for (int i = 2; i \leftarrow v; ++i) smalls[i] = (i + 1) / 2;
 int s = (v + 1) / 2
 vector<int> roughs(s);
 for (int i = 0; i < s; ++i) roughs[i] = 2 * i + 1;
 vector<int64_t> larges(s);
 for (int i = 0; i < s; ++i) larges[i] = (n / (2 * i + 1) + 1)
        / 2;
 vector<bool> skip(v + 1);
 int pc = 0;
  for (int p = 3; p \ll v; ++p) {
    if (smalls[p] > smalls[p - 1]) {
      int q = p * p; pc++;
if (1LL * q * q > n) break;
      skip[p] = true;
      for (int i = q; i <= v; i += 2 * p) skip[i] = true;
      int ns = 0;
      for (int k = 0; k < s; ++k) {
        int i = roughs[k];
        if (skip[i]) continue;
        int64_t d = 1LL * i * p;
        larges[ns] = larges[k] - (d \ll v ? larges[smalls[d] -
             pc] : smalls[n / d]) + pc;
        roughs[ns++] = i;
      s = ns:
      for (int j = v / p; j >= p; --j) {
        int c = smalls[j] - pc;
        for (int i = j * p, e = min(i + p, v + 1); i < e; ++i)
             smalls[i] -= c;
   }
 for (int k = 1; k < s; ++k) {
  const int64_t m = n / roughs[k];</pre>
    int64_t s = larges[k] - (pc + k - 1);
    for (int l = 1; l < k; ++l) {
      int p = roughs[l];
      if (1LL * p * p > m) break;
      s = smalls[m / p] - (pc + l - 1);
    larges[0] -= s;
  return larges[0];
```

8.14 De Bruijn

```
// sz_lim, MAX, MAX_len
int res[MAX], aux[MAX_len];
void db(int t, int p, int len, int k, int &sz) {
```

```
if (sz >= sz_lim) return;
  if (t > len) {
    if (len % p == 0) {
      for (int i = 1; i <= p && sz < sz_lim; ++i) res[sz++] =</pre>
  } else {
    aux[t] = aux[t - p];
    db(t + 1, p, len, k, sz);
    for (int i = aux[t - p] + 1; i < k; ++i) {
      aux[t] = i;
      db(t + 1, t, len, k, sz);
    }
 }
// return cyclic string such that every string of length len
     using k character appears as a substring.
int de_bruijn(int k, int len) {
  if (k == 1) {
    res[0] = 0;
    return 1;
  for (int i = 0; i < k * len; i++) aux[i] = 0;
  int sz = 0:
  db(1, 1, len, k, sz);
return sz; // k^n
```

Simplex Algorithm 8.15

```
maximize Cx under
Ax <=b
x >= 0
b >= 0
n variables
m constraints
A is m by n
const int MAX = 45:
int n, m;
double arr[MAX][MAX];
bool pro(){
  double mi = 0:
  int x = 1;
  for(int i = 1; i <= n + m; i ++) if(arr[0][i] < mi){</pre>
    mi = arr[0][i];
    x = i;
  if(abs(mi) < eps)</pre>
                        return 0; // sigma <= 0</pre>
  mi = INF;
               // theta
  for(int i = 1; i <= m; i ++){</pre>
    if(arr[i][x] > eps && arr[i][n + m + 1] / arr[i][x] < mi) {
    mi = arr[i][n + m + 1] / arr[i][x];</pre>
  assert(y);
  double weed = arr[y][x];
  for(int i = 1; i \le n + m + 1; ++ i)
    arr[y][i] /= weed;
  // now arr[y][n + m + 1] == theta
  for(int i = 0; i \le m; i ++){
    if(i == y) continue;
    double f = arr[i][x];
    for(int j = 1; j <= m + n + 1; j ++)
  arr[i][j] -= f * arr[y][j];</pre>
  return 1;
}
int main(){
  cin >> n;
  cin >> m;
  memset(arr, 0, sizeof arr);
  // input C
  for(int i = 1; i \le n; i ++){
    cin >> arr[0][i];
    arr[0][i] = - arr[0][i];
  for(int i = 1; i <= m; i++){
    // input A
    for(int j = 1; j \le n; j++)
      cin >> arr[i][j];
    arr[i][n + i] = 1;
    // input b
    cin >> arr[i][n + m + 1];
```

```
| }
| while(pro());
| cout << arr[0][n + m + 1] << "\n";
| return 0;
|}</pre>
```

8.16 Middle Speed Linear Recursion

```
#define MAX 100000
 #define INF 0x3f3f3f3f
 #define mod 10000
int n , k , x[MAX] , c[MAX];
 vector<int> mul(vector<int> a , vector<int> b){
   vector < int > ans(n + n + 1);
   REP(i, 1, n + 1) REP(j, 1, n + 1)
     ans[i + j] = (ans[i + j] + (a[i] * b[j])) % mod;
   RREP(i , n + n , n + 1){
     REP(j , 1 , n + 1) ans[i - j] = (ans[i - j] + ans[i] * c[j]
          ]) % mod;
     ans[i] = 0;
   return ans;
 vector<int> ppow(vector<int> a , int k){
   if(k == 1) return a;
   if(k % 2 == 0) return
                            ppow(mul(a, a), k >> 1);
   if(k % 2 == 1) return mul(ppow(mul(a , a) , k >> 1) , a);
int main(){
   IOS;
   while(cin >> n && n){
     REP(i , 1 , n + 1) cin >> x[i];
REP(i , 1 , n + 1) cin >> c[i];
     vector < int > v(n + n + 1);
     v[1] = 1;
     cin >> k , k ++;
     v = ppow(v, k);
     int ans = 0;
     REP(i , 1 , n + 1) ans = (ans + x[i] * v[i]) % mod;
cout << ans << endl;
   return 0;
i}
```

8.17 Chinese Remainder Theorem

```
const int INF = 0x3f3f3f3f
void extgcd(ll a , ll b , ll &d , ll &x , ll &y){
    if(b == 0) d = a , x = 1 , y = 0;
    else extgcd(b , a % b , d , y , x) , y -= (a / b) * x;
}
ll n;
vector<ll> v , m;
int main(){
    while(cin >> n){
        v.clear() , m.clear();
        ll ans , mod , d , x , y;
        REP(i , 0 , n) cin >> mod >> ans , m.pb(mod) , v.pb(ans);
        mod = m[0] , ans = v[0];
        REP(i , 1 , n){
        ll res = ((v[i] - ans) % m[i] + m[i]) % m[i];
        extgcd(mod , m[i] , d , x , y);
        if(res % d != 0){ ans = -1; break; }

        res = (res / d * x % m[i] + m[i]) % m[i];
        ans = ans + res * mod;
        mod = mod * m[i] / d;
    }
    if(ans == -1) cout << ans << endl;
    else cout << ans % mod << endl;
}
return 0;
}</pre>
```

9 Convolution

9.1 FFT

9.2 NTT

```
// Remember coefficient are mod P
/*
| (mod, root)
| (65537, 3)
| (23068673, 3)
| (998244353, 3)
| (1107296257, 10)
| (2013265921, 31)
```

```
(2885681153, 3)
 typedef long long ll;
 const int maxn = 65536;
 struct NTT{
    ll mod = 2013265921, root = 31;
   ll\ omega[maxn + 1];
   void prentt() {
     ll x=fpow(root, (mod - 1) / maxn);
     omega[0] = 1;
     for (int i=1;i<=maxn;++i) {
  omega[i] = omega[i - 1] * x % mod;</pre>
   }
   void real_init(ll _mod, ll _root) {
     mod = _mod;
root = _root;
     prentt();
   ll fpow(ll a, ll n) {
      (n += mod-1) \%= mod - 1;
     ll r = 1;
     for (; n; n>>=1) {
        if (n\&1) (r*=a)\%=mod;
       (a*=a)\%=mod;
     return r;
   }
   void bitrev(vector<ll> &v, int n) {
     int z = __builtin_ctz(n)-1;
     for (int i=0;i<n;++i) {</pre>
       int x=0;
        for (int j=0; j<=z;++j) x ^= ((i>>j&1) << (z-j));
       if (x>i) swap(v[x], v[i]);
   void ntt(vector<ll> &v, int n) {
     bitrev(v, n);
     for (int s = 2; s <= n; s <<= 1) {
        int z = s \gg 1;
        for (int i = 0; i < n; i += s) {
          for (int k = 0; k < z; ++k) {
    ll x = v[i + k + z] * omega[maxn / s * k] % mod;</pre>
            v[i + k + z] = (v[i + k] + mod - x) mod;
            (v[i+k] += x) \%= mod;
         }
       }
     }
   void intt(vector<ll> &v, int n) {
     ntt(v, n);
     reverse(v.begin() + 1, v.end());
     11 inv = fpow(n, mod - 2);
     for (int i = 0; i < n; ++i) {
       (v[i] *= inv) %= mod;
   }
   vector<ll> conv(vector<ll> a, vector<ll> b) {
     int sz=1;
     while (sz < a.size() + b.size() - 1) sz <<= 1;
     vector<ll> c(sz);
     while (a.size() < sz) a.push_back(0);
while (b.size() < sz) b.push_back(0);</pre>
     ntt(a, sz), ntt(b, sz);
      for (int i=0;i<sz;++i) c[i] = (a[i] * b[i]) % mod;
     intt(c, sz);
     while (c.size() && c.back() == 0) c.pop_back();
     return c;
 ll chinese(ll b1, ll m1, ll b2, ll m2) {
   ll a1 = bigpow(m2, m1 - 2, m1) * b1 % m1;
   11 a2 = bigpow(m1, m2 - 2, m2) * b2 % m2;
   ll ret= (a1 * m2 + a2 * m1) % (m1 * m2);
   assert(ret % m1 == b1 && ret % m2 == b2);
   return ret;
1}
```

9.3 FWT

```
a[j] = x + y; //FWT AND
a[j + d] = y + x; //FWT OR
a[j] = (x + y) / 2; a[j + d] = (x - y) / 2; //IFWT
XOR
a[j] = x - y; //IFWT AND
a[j + d] = y - x; //IFWT OR
}
```

9.4 Subset Convolution

9.5 Ternary Xor

```
pii operator*(const pii &p1, const pii &p2) {
  return {subb(mull(p1.F, p2.F) - mull(p1.S, p2.S))
       subb(addd(mull(p1.F, p2.S) + mull(p1.S, p2.F)) - mull(p1.
            S, p2.S))};
pii cal1(pii p) {
  return {subb(-p.S), subb(p.F - p.S)};
pii cal2(pii p) {
  return {subb(p.S - p.F), subb(-p.F)};
//C is the size of a
void DFT(vector<pii> &a) {
  for (int mid = 1; mid < C; mid *= 3) {
  for (int j = 0; j < C; j += mid * 3) {</pre>
       for (int k = 0; k < mid; ++k) {
         pii x = a[j + k], y = a[j + k + mid], z = a[j + k + (j + k)]
              mid << 1)];
         a[j + k] = x + y + z;

a[j + k + mid] = x + cal1(y) + cal2(z);
         a[j + k + (mid << 1)] = x + cal2(y) + cal1(z);
    }
  }
const int invn = ppow(C, mod - 2);
void IDFT(vector<pii> &a) {
  for (int mid = 1; mid < C; mid *= 3) {</pre>
    for (int j = 0; j < C; j += mid * 3) {
  for (int k = 0; k < mid; ++k) {</pre>
         pii x = a[j + k], y = a[j + k + mid],
           z = a[j + k + (mid << 1)];
         a[j + k] = x + y + z;

a[j + k + mid] = x + cal2(y) + cal1(z);
         a[j + k + (mid << 1)] = x + cal1(y) + cal2(z);
    }
  for (int i = 0; i < C; ++i) {
    a[i].F = mull(a[i].F, invn);
  }
}
void ff(vector<pii> &a, vector<pii> b) {
  DFT(a); DFT(b);
for (int i = 0; i < C; ++i) {
   a[i] = a[i] * b[i];</pre>
  IDFT(a);
```

10 String10.1 KMP

```
const KMP_SIZE = ;
struct KMP{
  string s;
  int f[KMP_SIZE] , pos;
  void solve(){
   f[0] = pos = -1;
  for (int i = 1; i < s.size(); ++ i) {</pre>
```

```
while(pos != -1 && s[pos + 1] != s[i]) pos = f[pos];
if(s[pos + 1] == s[i]) pos ++;
f[i] = pos;
}
}
};
```

10.2 **Z** value

```
const int ZVALUE_SIZE = ;
struct Z_VALUE{
  string s;
  int l = 0 , r = 0 , z[ZVALUE_SIZE];
  void solve() {
    for (int i = 0; i < s.size(); ++ i) {
        z[i] = max(min(z[i - l] , r - i) , 0LL);
        while(i + z[i] < s.size() && s[z[i]] == s[i + z[i]]) {
        l = i , r = i + z[i];
        z[i] ++;
    }
    }
}</pre>
```

10.3 Longest Palindrome

```
const int PALINDROME MAX = 2 * :
struct Palindrome{
   string s , ss; // ss = input
   int z[PALINDROME_MAX];
   void solve(){
      s.resize(ss.size() + ss.size() + 1 , '.');
for (int i = 0; i < ss.size(); ++ i)</pre>
         s[i + i + 1] = ss[i];
      int l = 0, r = 0;
for (int i = 0; i < s.size(); ++ i) {
        z[i] = max(min(z[l + l - i], r - i), 1);

while(i - z[i] >= 0 && i + z[i] < s.size() && s[i - z[i]]
                == s[i + z[i]]){
           l = i , r = i + z[i];
           z[i] ++;
        }
     }
   }
};
```

10.4 Aho-Corasick Algorithm

10.5 Suffix Array

int tmp = 0, n = s.size();

```
const int SA_SIZE = ;
const int logn = 1 + ;
string s;
int sa[SA_SIZE], rk[SA_SIZE], lcp[SA_SIZE];
int tma[2][SA_SIZE], c[SA_SIZE], sp[SA_SIZE][logn];
int getsa() {
   -> update m = ? // how many char
  int *x = tma[0], *y = tma[1], n = s.size(), m = 200;
for (int i = 0; i < m; ++ i) c[i] = 0;
for (int i = 0; i < n; ++ i) c[x[i] = s[i]] ++;
   for (int i = 1; i < m; ++ i) c[i] += c[i - 1];
for (int i = n - 1; i >= 0; -- i) sa[--c[x[i]]] = i;
   for(int k = 1; k <= n; k <<= 1) {
     for (int i = 0; i < m; ++ i) c[i] = 0; for (int i = 0; i < n; ++ i) c[x[i]] ++;
     for (int i = 1; i < m; ++ i) c[i] += c[i - 1];
     int p = 0;
     for (int i = n - k; i < n; ++ i) y[p ++] = i;
     for (int i = 0; i < n; ++ i) if(sa[i] >= k) y[p ++] = sa[i]
     for (int i = n - 1; i >= 0; -- i) sa[--c[x[y[i]]]] = y[i];
     y[sa[0]] = p = 0;
     for (int i = 1; i < n; ++ i) {
       if(x[sa[i]] == x[sa[i - 1]] \&\& sa[i] + k < n \&\& sa[i -
             1] + k < n &&
          x[sa[i] + k] == x[sa[i - 1] + k]);
       else p ++;
       y[sa[i]] = p;
     swap(x, y);
     if(p + 1 == n) break;
     m = p + 1;
  }
}
void getlcp() {
```

```
for (int i = 0; i < n; ++ i) rk[sa[i]] = i;
for (int i = 0; i < n; ++ i) {</pre>
    if(rk[i] == 0) lcp[0] = 0;
      if(tmp) tmp --
      int po = sa[rk[i] - 1];
      while(tmp + po < n && tmp + i < n && s[tmp + i] == s[tmp
            + po]) tmp ++;
      lcp[rk[i]] = tmp;
 }
}
void getsp() {
  int n = s.size();
  for (int i = 0; i < n; ++ i) sp[rk[i]][0] = s.size() - i;</pre>
  for (int i = 1; i < n; ++ i) sp[i - 1][1] = lcp[i];
  for (int i = 2; i < logn; ++ i) {</pre>
    for (int j = 0; j < n; ++ j) {
  if(j + (1 << (i - 2)) >= s.size()) continue;
      sp[j][i] = min(sp[j][i - 1], sp[j + (1 << (i - 2))][i -
 }
int Query(int L, int R) {
  int tmp = (L == R) ? 0 : 32 - __builtin_clz(R - L);
  if(tmp == 0) return sp[L][0];
  else return min(sp[L][tmp], sp[R - (1 << (tmp - 1))][tmp]);</pre>
int Find(string ss) {
  int L = 0, R = s.size(), now;
while(R - L > 1) {
    now = (L + R) / 2;
    if(s[sa[now]] == ss[0]) break;
    else if(s[sa[now]] > ss[0]) R = now;
    else if(s[sa[now]] < ss[0]) L = now;
  if(s[sa[now]] != ss[0]) return 0;
  for (int i = 1; i < ss.size(); ++ i) {</pre>
    int pre = now, ty = 0;
    if(sa[now] + i >= s.size()) L = now, ty = 0;
    else if(s[sa[now] + i] == ss[i]) continue;
    else if(s[sa[now] + i] > ss[i]) R = now, ty = 1;
    else if(s[sa[now] + i] < ss[i]) L = now, ty = 0;
    while(R - L > 1) {
      now = (L + R) / 2;
      if(sa[now] + i >= s.size()) {
         if(ty == 0) R = now;
         if(ty == 1) L = now;
      else if(ty == 0 && Query(pre, now) < i) R = now;</pre>
      else if(ty == 1 && Query(now, pre) < i) L = now;
else if(s[sa[now] + i] == ss[i]) break;
      else if(s[sa[now] + i] > ss[i]) R = now;
      else if(s[sa[now] + i] < ss[i]) L = now;
    if(sa[now] + i >= s.size()) return 0;
    if(s[sa[now] + i] != ss[i]) return 0;
  L = now, R = now;
  for (int i = 19; i >= 0; -- i) {
    if(R + (1 << i) >= s.size()) continue;
    else if(Query(L, R + (1 << i)) >= ss.size()) R += (1 << i);</pre>
  for (int i = 19; i >= 0; -- i) {
    if(L - (1 << i) < 0) continue;
    else if(Query(L - (1 << i), R) >= ss.size()) L -= (1 << i);
  return R - L + 1;
how to use :
1. cin >> s;
2. getsa(), getlcp(), getsp();
string ss;
4. cin >> ss
5. cout << Find(ss) << endl;
*/</pre>
```

10.6 Palindromic Tree

```
|//MAXN
| const int N = 26;
| struct Palindromic_Tree {
| int next[MAXN][N]; //trie tree edge
| int len[MAXN]; //tree edge depth*2 (-1)
```

```
int fail[MAXN]; //fail link
   int num[MAXN]; //fail link depth
   int cnt[MAXN]; //# of this Palindrom
   int S[MAXN]; //string
   int p; //# of different Palindrom + 2
   int n; //string len
   int last;
   int newnode(int 1) {
     memset(next[p], 0, N * 4);
     cnt[p] = num[p] = 0;
     len[p] = 1;
     return p ++;
   }
   void init() {
  p = n = 0;
  last = 1;
     newnode (0):
     newnode (-1);
     S[n] = -1;
     fail[0] = 1;
   int get_fail(int x) {
     while (S[n - len[x] - 1] != S[n]) x = fail[x];
     return x;
   void add(int c) {
     S[++ n] = c;
     int cur = get_fail (last);
     if (!next[cur][c]) {
       int now = newnode (len[cur] + 2);
       fail[now] = next[get_fail (fail[cur])][c];
       next[cur][c] = now;
       num[now] = num[fail[now]] + 1;
     last = next[cur][c];
     cnt[last] ++;
   void count () {
     for (int i = p - 1; i >= 0; -- i) cnt[fail[i]] += cnt[i];
};
```

10.7 Lexicographically Smallest Rotation

```
string s;
 const int N = 4000006;
 int f[N];
 void solve() {
   S = S + S
    int n = (int)s.size();
    for (int i = 0; i < n; ++i) f[i] = -1;
   int k = 0;
   for (int j = 1; j < n; ++j) {
  char sj = s[j];
  int i = f[j - k - 1];
  while (i != -1 && sj != s[k + i + 1]) {</pre>
        if (sj < s[k + i + 1])
           k = j - i - 1;
        i = f[\tilde{i}];
      if (sj != s[k + i + 1]) {
         if (sj < s[k]) k = j;
        f[j-k] = -1;
      else f[j-k] = i+1;
   n >>= 1;
   if (k >= n) k -= n;
   for (int i = k; i < k + n; ++i)
      cout << s[i];</pre>
    cout << endī;
}
```

11 Geometry

11.1 Circle

```
//Note that this code will crash if circle A and B are the same
typedef pair<double, double> pdd;
|pdd rtcw(pdd p){return pdd(p.Y, -p.X); }
|vector<pdd> circlesintersect(pdd A, pdd B, double r1, double r2
      ){
      vector<ppdd> ret;
      double d = dis(A, B);
      if(d > r1 + r2 || d + min(r1, r2) < max(r1, r2))
      return ret;</pre>
```

```
double x = (d * d + r1 * r1 - r2 * r2) / (2 * d);
double y = sqrt(r1 * r1 - x * x);
pdd v = (B - A) / d;
ret.eb(A + v * x + rtcw(v) * y);
if(y > 0)
    ret.eb(A + v * x - rtcw(v) * y);
return ret;
}
```

11.2 Half Plane Intersection

```
Pt interPnt( Line 11, Line 12, bool &res ){
   Pt p1, p2, q1, q2;
tie(p1, p2) = l1; tie(q1, q2) = l2;
   double f1 = (p2 - p1) \land (q1 - p1);
double f2 = (p2 - p1) \land (p1 - q2);
   double f = (f1 + f2);
   if( fabs(f) < eps){ res=0; return {0, 0}; }</pre>
   res = true
   return q1 * (f2 / f) + q2 * (f1 / f);
 bool isin( Line 10, Line 11, Line 12 ){
   // Check inter(l1, l2) in l0
   bool res; Pt p = interPnt(l1, l2, res);
   return ( (10.SE - 10.FI) ^ (p - 10.FI) ) > eps;
 /* If no solution, check: 1. ret.size() < 3</pre>
 * Or more precisely, 2. interPnt(ret[0], ret[1])
* in all the lines. (use (l.S - l.F) ^ (p - l.F) > 0
 */
 /* --^- Line.FI --^- Line.SE --^- */
 vector<Line> halfPlaneInter( vector<Line> lines ){
   int sz = lines.size();
   vector<double> ata(sz), ord(sz);
   for( int i=0; i<sz; i++) {</pre>
     ord[i] = i;
Pt d = lines[i].SE - lines[i].FI;
     ata[i] = atan2(d.Y, d.X);
   sort( ord.begin(), ord.end(), [&](int i, int j) {
   if( fabs(ata[i] - ata[j]) < eps )</pre>
        return ( (lines[i].SE - lines[i].FI) ^
             (lines[j].SE - lines[i].FI)) < 0;
        return ata[i] < ata[j];</pre>
       });
   vector<Line> fin;
   for (int i=0; i<sz; i++)</pre>
     if (!i or fabs(ata[ord[i]] - ata[ord[i-1]]) > eps)
        fin.PB(lines[ord[i]]);
   deque<Line> dq;
   for (int i=0; i<(int)(fin.size()); i++) {</pre>
     while((int)(dq.size()) >= 2 and
          not isin(fin[i], dq[(int)(dq.size())-2],
            dq[(int)(dq.size())-1]))
        dq.pop_back();
     while((int)(dq.size()) >= 2 and
  not isin(fin[i], dq[0], dq[1]))
        dq.pop_front();
     dq.push_back(fin[i]);
   while( (int)(dq.size()) >= 3 and
  not isin(dq[0], dq[(int)(dq.size())-2],
          dq[(int)(dq.size())-1]))
     dq.pop_back();
   while( (int)(dq.size()) >= 3 and
       not isin(dq[(int)(dq.size())-1], dq[0], dq[1]))
     dq.pop_front();
   vector<Line> res(dq.begin(),dq.end());
   return res;
į }
```

11.3 Convex Hull 3D

```
{ return mix(info[b] - info[a], info[c] - info[a], info[d] -
     info[a]); }
struct Face{
  int a, b, c; Face(){}
  Face(int a, int b, int c): a(a), b(b), c(c) {}
  int &operator [](int k)
  { if (k == 0) return a; if (k == 1) return b; return c; }
};
vector<Face> face;
void insert(int a, int b, int c)
{ face.push_back(Face(a, b, c)); }
void add(int v) {
  vector <Face> tmp; int a, b, c; cnt++;
  for (int i = 0; i < SIZE(face); i++) {</pre>
     a = face[i][0]; b = face[i][1]; c = face[i][2];
     if(Sign(volume(v, a, b, c)) < 0)
       mark[a][b] = mark[b][a] = mark[b][c] = mark[c][b] = mark[
             c][a] = mark[a][c] = cnt;
     else tmp.push_back(face[i]);
  } face = tmp;
  for (int i = 0; i < SIZE(tmp); i++) {
     a = face[i][0]; b = face[i][1]; c = face[i][2];
     if (mark[a][b] == cnt) insert(b, a, v);
if (mark[b][c] == cnt) insert(c, b, v);
     if (mark[c][a] == cnt) insert(a, c, v);
  }}
int Find(){
  for (int i = 2; i < n; i++) {
     Pt ndir = (info[0] - info[i]) \wedge (info[1] - info[i]);
     if (ndir == Pt()) continue; swap(info[i], info[2]);
for (int j = i + 1; j < n; j++) if (Sign(volume(0, 1, 2, j))</pre>
          ) != 0) {
       swap(info[j], info[3]); insert(0, 1, 2); insert(0, 2, 1);
              return 1;
     } } return 0; }
int main() {
  for (; scanf("%d", &n) == 1; ) {
     for (int i = 0; i < n; i++) info[i].Input();</pre>
     sort(info, info + n); n = unique(info, info + n) - info;
     face.clear(); random_shuffle(info, info + n);
     if (Find()) { memset(mark, 0, sizeof(mark)); cnt = 0;
for (int i = 3; i < n; i++) add(i); vector<Pt> Ndir;
       for (int i = 0; i < SIZE(face); ++i) {
  Pt p = (info[face[i][0]] - info[face[i][1]]) ^</pre>
            (info[face[i][2]] - info[face[i][1]]);
       p = p / norm( p ); Ndir.push_back(p);
} sort(Ndir.begin(), Ndir.end());
       int ans = unique(Ndir.begin(), Ndir.end()) - Ndir.begin()
       printf("%d\n", ans);
     } else printf("1\n");
double calcDist(const Pt &p, int a, int b, int c)
{ return fabs(mix(info[a] - p, info[b] - p, info[c] - p) / area
      (a, b, c)); }
//compute the minimal distance of center of any faces
double findDist() { //compute center of mass
  double totalWeight = 0; Pt center(.0, .0, .0);
  Pt first = info[face[0][0]];
  for (int i = 0; i < SIZE(face); ++i) {
     Pt p = (info[face[i][0]]+info[face[i][1]]+info[face[i][2]]+
          first)*.25;
     double weight = mix(info[face[i][0]] - first, info[face[i
          ][1]]
           first, info[face[i][2]] - first);
     totalWeight += weight; center = center + p * weight;
  } center = center / totalWeight;
  double res = 1e100; //compute distance
for (int i = 0; i < SIZE(face); ++i)</pre>
     res = min(res, calcDist(center, face[i][0], face[i][1],
          face[i][2]));
  return res; }
```

11.4 Dynamic convexhull

```
|/* Given a convexhull, answer querys in O(\lg N)
| CH should not contain identical points, the area should
| be > 0, min pair(x, y) should be listed first */
|double det( const Pt& p1 , const Pt& p2 )
| { return p1.X * p2.Y - p1.Y * p2.X; }
| struct Conv{
| int n;
| vector<Pt> a;
| vector<Pt> upper, lower;
| Conv(vector<Pt> _a) : a(_a){
| n = a.size();
| int ptr = 0;
```

```
for(int i=1; i<n; ++i) if (a[ptr] < a[i]) ptr = i;
for(int i=0; i<=ptr; ++i) lower.push_back(a[i]);
for(int i=ptr; i<n; ++i) upper.push_back(a[i]);</pre>
  upper.push_back(a[0]);
int sign( LL x ){ // fixed when changed to double
  return x < 0 ? -1 : x > 0; }
pair<LL,int> get_tang(vector<Pt> &conv, Pt vec){
  int l = 0, r = (int)conv.size() - 2;
  for(; l + 1 < r; ){
     int mid = (l + r) / 2;
     if(sign(det(conv[mid+1]-conv[mid],vec))>0)r=mid;
     else l = mid;
  return max(make_pair(det(vec, conv[r]), r),
       make_pair(det(vec, conv[0]), 0));
void upd_tang(const Pt &p, int id, int &i0, int &i1){
  if(det(a[i0] - p, a[id] - p) > 0) i0 = id;
  if(det(a[i1] - p, a[id] - p) < 0) i1 = id;</pre>
void bi_search(int l, int r, Pt p, int &i0, int &i1){
  if(l == r) return;
  upd_tang(p, 1 % n, i0, i1);
  int sl=sign(det(a[l % n] - p, a[(l + 1) % n] - p));
  for( ; l + 1 < r; ) {
  int mid = (l + r) / 2;</pre>
     int smid=sign(det(a[mid%n]-p, a[(mid+1)%n]-p));
     if (smid == sl) l = mid;
     else r = mid;
  }
  upd_tang(p, r % n, i0, i1);
int bi_search(Pt u, Pt v, int l, int r) {
  int sl = sign(det(v - u, a[l % n] - u));
  for(; l + 1 < r; ) {
  int mid = (l + r) / 2;
     int smid = sign(det(v - u, a[mid % n] - u));
     if (smid == sl) l = mid;
    else r = mid;
  return 1 % n;
}
// 1. whether a given point is inside the CH
bool contain(Pt p) {
  if (p.X < lower[0].X || p.X > lower.back().X) return 0;
  int id = lower_bound(lower.begin(), lower.end(), Pt(p.X, -
        INF)) - lower.begin();
  if (lower[id].X == p.X) {
     if (lower[id].Y > p.Y) return 0;
  }else if(det(lower[id-1]-p,lower[id]-p)<0)return 0;</pre>
  id = lower_bound(upper.begin(), upper.end(), Pt(p.X, INF),
        greater<Pt>()) - upper.begin();
  if (upper[id].X == p.X) {
                                                                           } solver;
     if (upper[id].Y < p.Y) return 0;</pre>
  }else if(det(upper[id-1]-p,upper[id]-p)<0)return 0;</pre>
                                                                           double f(ld a, ld b) {
  ld ret = b - a;
// 2. Find 2 tang pts on CH of a given outside point
// return true with i0, i1 as index of tangent points
// return false if inside CH
bool get_tang(Pt p, int &i0, int &i1) {
                                                                           ld solve_small(pdd cen, ld r, pdd p1, pdd p2) { p1 = p1 - cen, p2 = p2 - cen;
  if (contain(p)) return false;
  i0 = i1 = 0;
  int id = lower_bound(lower.begin(), lower.end(), p) - lower
        .begin();
  bi_search(0, id, p, i0, i1);
  bi_search(id, (int)lower.size(), p, i0, i1);
  id = lower\_bound(upper.begin(), \; upper.end(), \; p, \; greater < Pt
        >()) - upper.begin();
  bi_search((int)lower.size() - 1, (int)lower.size() - 1 + id
        , p, i0, i1);
  bi_search((int)lower.size() - 1 + id, (int)lower.size() - 1
        + (int)upper.size(), p, i0, i1);
  return true;
}
^{\prime\prime} 3. Find tangent points of a given vector
// ret the idx of vertex has max cross value with vec
int get_tang(Pt vec){
  pair<Ll, int> ret = get_tang(upper, vec);
ret.second = (ret.second+(int)lower.size()-1)%n;
  ret = max(ret, get_tang(lower, vec));
  return ret.second;
// 4. Find intersection point of a given line
// return 1 and intersection is on edge (i, next(i))
```

```
// return 0 if no strictly intersection
   bool get_intersection(Pt u, Pt v, int &i0, int &i1){
      int p0 = get_tang(u - v), p1 = get_tang(v - u);
      if(sign(det(v-u,a[p0]-u))*sign(det(v-u,a[p1]-u))<0){
        if (p0 > p1) swap(p0, p1);
        i0 = bi_search(u, v, p0, p1);
        i1 = bi\_search(u, v, p1, p0 + n);
        return 1;
      return 0:
   }
|};
 11.5
          Polar Angle Sort
 #define is_neg(_k) (_k.Y < 0 || (_k.Y == 0 && _k.X < 0) )
 bool cmp(pll a,pll b){
   int A = is_neg(a), B = is_neg(b);
   return (A == B ? (a \land b) > 0 : A < B);
 11.6 Circle and Polygon intersection
struct Circle_and_Segment_Intersection {
  const ld eps = 1e-9;
   vector<pdd> solve(pdd p1, pdd p2, pdd cen, ld r) {
      //please notice that p1 != p2
      //condiser p = p2 + (p1 - p2) * t, 0 <= t <= 1
      //condiser p = p2 + (p1 - p2)

vector<pdd> ret;

p1 = p1 - cen; p2 = p2 - cen;

ld a = (p1 - p2) * (p1 - p2);

ld b = 2 * (p2 * (p1 - p2));

ld c = p2 * p2 - r * r;

ld bb4ac = b * b - 4 * a * c;
```

if (bb4ac < -eps) return ret; //no intersection
vector<ld> ts;

ts.push_back((-b + sqrt(bb4ac)) / (a * 2));

ts.push_back((-b - sqrt(bb4ac)) / (a * 2));

if ((bb4ac) <= eps) {

else {

}

}

return ret;

cen = $\{0, 0\}$;

else {

ts.push_back(-b / 2 / a);

sort(ts.begin(), ts.end());

t = max(t, 0.0); t = min(t, 1.0);

ret.push_back(pt);

if ((int)inter.size() == 0) {

if (in_cir(cen, r, p1)) {

else if ((int)inter.size() == 1) {

else if (!in_cir(cen, r, p1)) {

pdd _p1 = inter[0];

)) / 2;

ret = $(p1 ^ p2) / 2;$

if (-eps <= t && t <= 1 + eps) {</pre>

pdd pt = p2 + t * (p1 - p2); pt = pt + cen;

while (ret <= -pi - eps) ret += 2 * pi;

while (ret >= pi + eps) ret -= 2 * pi;

vector<pdd> inter = solver.solve(p1, p2, cen, r);
ld ret = 0.0;

if (!in_cir(cen, r, p1) && !in_cir(cen, r, p2)) {

ret = (r * r * f(atan2(p1.Y, p1.X), atan2(p2.Y, p2.X))) / 2;

ret = (r * r * f(atan2(p1.Y, p1.X), atan2(p2.Y, p2.X))) / 2;

ret += ((_p1 ^ p2) / 2); ret += (r * r * f(atan2(p1.Y, p1.X), atan2(_p1.Y, _p1.X)

for (ld t: ts) {

```
else if (!in_cir(cen, r, p2)) {
        pdd _p2 = inter[0];
        ret += ((p1 ^ _p2) / 2);
ret += (r * r * f(atan2(_p2.Y, _p2.X), atan2(p2.Y, p2.X)
     }
   }
   else if ( (int)inter.size() == 2) {
     pdd _p2 = inter[0], _p1 = inter[1];
ret += ((_p1 ^ _p2) / 2);
ret += (r * r * f(atan2(_p2.Y, _p2.X), atan2(p2.Y, p2.X)))
     ret += (r * r * f(atan2(p1.Y, p1.X), atan2(_p1.Y, _p1.X)))
/ 2;
   return ret;
}
ld solve(pdd cen, ld r, vector<pdd> pts) {
   ld ret = 0;
   for (int i = 0; i < (int)pts.size(); ++i) {</pre>
     ret += solve_small(cen, r, pts[i], pts[(i + 1) % int(pts.
           size())]);
   ret = max(ret, -ret);
   return ret;
| }
```

11.7 Segment Intersection

```
int intersect(PII a , PII b , PII c , PII d){
   if(max(a.F , b.F) < min(c.F , d.F)) return 0;
   if(max(c.F , d.F) < min(a.F , b.F)) return 0;
   if(max(a.S , b.S) < min(c.S , d.S)) return 0;
   if(max(c.S , d.S) < min(a.S , b.S)) return 0;
   if(cross(b - a , c - a) * cross(b - a , d - a) == 1) return 0;
   if(cross(d - c , a - c) * cross(d - c , b - c) == 1) return 0;
   return 1;
}</pre>
```

11.8 Line Intersection Point

```
pdd intersect(pdd p1, pdd p2, pdd q1, pdd q2) {
   //make sure that p1p2 is not parallel to q1q2
   return p1 + ((q1 - p1) ^ (q2 - q1)) / ((p2 - p1) ^ (q2 - q1))
   * (p2 - p1);
}
```

11.9 Rotating Calipers

```
#define NXT(x) ((x + 1) \% m)
 int main () {
  vector<pii> v; // v is the input points
  sort(v.begin(), v.end());
   vector<pii> up, down;
  for (pii p: v) {
     while (SZ(down) >= 2 \&\& sgn((p - down[SZ(down) - 2]) \land (p -
           down.back())) >= 0) {
       down.pop_back();
     down.push_back(p);
  }
  reverse(v.begin(), v.end());
   for (pii p: v) {
     while (SZ(up) >= 2 \&\& sgn((p - up[SZ(up) - 2]) \land (p - up.
         back()) >= 0) {
       up.pop_back();
     up.push_back(p);
   vector<pii> all;
  for (pii p: down) { all.push_back(p); } all.pop_back();
  for (pii p: up) { all.push_back(p); }
  all.pop_back();
  int m = all.size();
   int ptr = (int)down.size() - 1;
  for (int i = 0; i < m; ++i) {
    while (((all[NXT(ptr)] - all[ptr]) ^ (all[NXT(i)] - all[i])
          ) > 0) {
       ptr = NXT(ptr);
    }
  }
| }
```

12 Ad hoc

12.1 Joseph Problem

```
// 0(m + log N)
// n people, k-th dead. Find out the last alive person
int main() {
  long long n, k, i, x = 0, y;
  scanf( "%I64d%I64d", &n, &k );
  for( i = 2; i <= k && i <= n; ++i ) x = ( x + k ) % i;
  for( ; i <= n; ++i ) {
    y = ( i - x - 1 ) / k;
    if( i + y > n ) y = n - i;
    i += y;
    x = ( x + ( y + 1 ) % i * k ) % i;
  }
  printf( "%I64d\n", x + 1 );
  return 0;
}
```

12.2 Segment Max Segment Sum

```
int n , m , x[MAX];
class N{
public: int tag , sml , sum , none;
} b[MAX * 4];
void Pull(int now , int l , int r){
  if(1 == r){
    if(b[now].tag){
       b[now].sum = b[now].tag;
       b[now].none = 0;
       b[now].sml = b[now].tag;
     else{
       b[now].sum = 0;
       b[now].none = 1
       b[now].sml = INF;
    }
  }
  else {
    b[now].sml = min(b[ls].sml , b[rs].sml);
     if(b[now].tag) b[now].sml = min(b[now].sml , b[now].tag);
    b[now].sum = b[ls].sum + b[rs].sum;
    b[now].none = b[ls].none + b[rs].none;
     if(b[now].tag) b[now].sum += b[now].tag * b[now].none , b[
          now].none = 0;
  }
}
void take_tag(int now , int l , int r , int val){
  if(b[now].tag && b[now].tag < val) b[now].tag = 0;</pre>
  if(l != r && b[ls].sml < val) take_tag(ls , l , mid , val);</pre>
  if(l != r \&\& b[rs].sml < val) take_tag(rs , mid + 1 , r , val)
  Pull(now , l , r);
void Build(int now , int l , int r){
  b[now].none = 0;
  if(l == r) b[now].tag = b[now].sml = b[now].sum = x[l];
  else {
    Build(ls , l , mid) , Build(rs , mid + 1 , r);
     Pull(now , l , r);
  }
}
void update(int now , int l , int r , int ql , int qr , int val
  if(b[now].tag >= val) return ;
  if(ql \ll l \& r \ll qr)
     take_tag(now , l , r , val);
    b[now].tag = val;
Pull(now , l , r);
     if(qr <= mid) update(ls , l , mid , ql , qr , val);</pre>
     else if(mid + 1 \leftarrow ql) update(rs , mid + 1 , r , ql , qr ,
         val):
     else update(ls , l , mid , ql , qr , val) , update(rs , mid
     + 1 , r , ql , qr , val);
Pull(now , l , r);
PII query(int now , int l , int r , int ql , int qr){
  if(ql <= l && r <= qr) return mp(b[now].sum , b[now].none);</pre>
  else {
    PII ans = mp(0, 0);
     if(qr <= mid) ans = query(ls , l , mid , ql , qr);</pre>
```

```
int val = v[now] + v[now + 1];
 ans += val;
 v.erase(v.begin() + now);
 v.erase(v.begin() + now);
 int id = 0;
 for (int i = now - 1; i >= 0; -- i)
   if(v[i] >= val) { id = i + 1; break; }
 v.insert(v.begin() + id, val);
while(id >= 2 && v[id - 2] <= v[id]) {</pre>
    int dis = v.size() - id;
    DFS(id - 2);
    id = v.size() - dis;
 }
int32_t main() {
 IOS;
 cin >> n;
  for (int i = 0; i < n; ++ i) cin >> x[i];
 for (int i = 0; i < n; ++ i) {
    v.emplace_back(x[i]);
    while(v.size() >= 3 && v[v.size() - 3] <= v[v.size() - 1])</pre>
      DFS(v.size() - 3);
 while(v.size() > 1) DFS(v.size() - 2);
 cout << ans << endl;
  return 0;
```

12.4 Manhattan Spanning Tree

for (int i = 0; i < n; ++ i) sol[i] = i;</pre>

```
#define edge pair<int, PII>
int n, sol[maxn];
PII x[maxn];
vector<edge> v;
class djs{
public:
 int x[maxn];
  void init(){ for (int i = 0; i < maxn; ++ i) x[i] = i; }
  int Find(int now){ return x[now] == now ? now : x[now] = Find
       (x[now]); }
  void Union(int a, int b){ x[Find(a)] = Find(b); }
  int operator[](int now){ return Find(now); }
} ds:
PII bit[maxn];
void update(int from, int val, int id){
  for(int i = from; i < maxn; i += i \& -i)
    bit[i] = maxn(bit[i], mp(val, id));
int query(int from){
  PII res = bit[from];
  for(int i = from; i > 0; i -= i & -i)
  res = maxn(res, bit[i]);
  return res.B;
int cmp(int a, int b){
 return x[a] < x[b];
int DIS(int q, int w){
 return abs(x[q].A - x[w].A) + abs(x[q].B - x[w].B);
void BuildEdge(){
  vector<int> uni;
  for (int i = 0; i < maxn; ++ i)
   bit[i] = mp(-INF, -1);
```

```
for (int i = 0; i < n; ++ i) uni.pb(x[i].B - x[i].A);
  sort(ALL(uni))
  uni.resize(unique(ALL(uni)) - uni.begin());
   sort(sol, sol + n, cmp);
   for (int i = 0; i < n; ++ i){
     int now = sol[i];
     int tmp = x[sol[i]].B - x[sol[i]].A;
     int po = lower_bound(ALL(uni), tmp) - uni.begin() + 1;
     int id = query(po);
     if(id >= 0) v.pb(mp(DIS(id, now), mp(id, now)));
     update(po, x[now].A + x[now].B, now);
void Build(){
  BuildEdge();
  for (int i = 0; i < n; ++ i) swap(x[i].A, x[i].B);
  BuildEdge();
  for (int i = 0; i < n; ++ i) x[i].A *= -1;
  BuildEdge();
  for (int i = 0; i < n; ++ i) swap(x[i].A, x[i].B);
  BuildEdge();
}
int solveKruskal(){
  ds.init();
  sort(ALL(v));
  int res = 0;
  for (int i = 0; i < v.size(); ++ i) {</pre>
     int dis = v[i].A;
     PII tmp = v[i].B;
     if(ds[tmp.A] != ds[tmp.B]){
       ds.Union(tmp.A, tmp.B);
       res += dis;
    }
  return res;
int32_t main(){
  IOS;
  cin >> n;
  for (int i = 0; i < n; ++ i) cin >> x[i].A >> x[i].B;
  Build();
  int ans = solveKruskal();
  cout << ans << endl;</pre>
  return 0;
}
```

12.5 K Cover Tree

```
int n , k , dp[MAX] , ans;
vector<int> v[MAX];
void DFS(int now , int fa){
  if(v[now].size() == 1 && v[now][0] == fa)
      return dp[now] = -1 , void();
   int sml = INF , big = -INF;
   for(auto to : v[now]) if(to != fa){
     DFS(to , now);
      sml = min(sml , dp[to]);
     big = max(big , dp[to]);
   if(sml == -k) dp[now] = k , ans ++;
else if(big - 1 >= abs(sml)) dp[now] = big - 1;
   else dp[now] = sml - 1;
int32_t main(){
   IOS;
   cin >> n >> k;
   REP(i , 2 , n + 1){
int a , b; cin >> a >> b;
     v[a].pb(b); v[b].pb(a);
   if(k == 0) cout << n << endl;
   else {
     DFS(0 , 0) , ans += dp[0] < 0;
cout << ans << endl;
   return 0:
}
```

12.6 M Segments' Maximum Sum

```
|------Greedy------|
int n, m, fr[MAX], ba[MAX];
|int v[MAX], idx = 1;
|set<PII> cc;
|void erase(int id){
| if(id == 0) return;
| int f = fr[id], b = ba[id];
```

```
ba[fr[id]] = b, fr[ba[id]] = f;
                                                                              return hypot(p1.F - p2.F, p1.S - p2.S);
  cc.erase(mp(abs(v[id]), id));
                                                                            inline double sq(double x) {
  return x * x;
int32_t main(){
  cin >> n >> m;
  int sum = 0, pos = 0, ans = 0;
                                                                            pdd external(pdd p1, pdd p2, pdd p3) {
  double a1 = p1.F - p2.F, a2 = p1.F - p3.F;
  double b1 = p1.S - p2.S, b2 = p1.S - p3.S;
  REP(i, 0, n){
    int tmp; cin >> tmp;
    if(tmp == 0) continue;
                                                                              double c1 = (sq(p1.F) - sq(p2.F)
    if((tmp >= 0 \&\& sum >= 0) || (tmp <= 0 \&\& sum <= 0)){}
                                                                                           +  sq(p1.S) -  sq(p2.S)) / 2;
      sum += tmp;
                                                                              double c2 = (sq(p1.F) - sq(p3.F)
                                                                             + sq(p1.S) - sq(p3.S)) / 2;

double dd = a1 * b2 - a2 * b1;

return make_pair((c1 * b2 - c2 * b1) / dd
    else {
      if(sum > 0) ans += sum, pos ++;
       v[idx ++] = sum, sum = tmp;
                                                                                                , (a1 * c2 - a2 * c1) / dd);
                                                                            int main() {
  if(sum) v[idx ++] = sum;
                                                                              cin >> n;
  if(sum > 0) ans += sum, pos ++;
                                                                              for (int i = 0; i < n; ++ i)
  REP(i, 0, idx){
                                                                                cin >> a[i].F >> a[i].S;
    fr[i + 1] = i;
                                                                              shuffle(a, a + n, rng);
    ba[i] = i + 1;
  if(i) cc.insert(mp(abs(v[i]), i));
} ba[idx - 1] = 0;
                                                                              pdd center = a[0];
                                                                              double r = 0;
  while(pos > m){
    auto tmp = cc.begin();
                                                                              for (int i = 0; i < n; ++ i) {
    int val = (*tmp).A, id = (*tmp).B;
                                                                                 if (dis(center, a[i]) <= r) continue;</pre>
    cc.erase(tmp)
                                                                                 center = a[i], r = 0;
    if(v[id] < 0 \&\& (fr[id] == 0 || ba[id] == 0)) continue;
                                                                                for (int j = 0; j < i; ++ j) {
    if (dis(center, a[j]) <= r) continue;
    if(v[id] == 0) continue;
    ans -= val, pos --;
                                                                                   center.F = (a[i].F + a[j].F) / 2;
center.S = (a[i].S + a[j].S) / 2;
    v[id] = v[fr[id]] + v[id] + v[ba[id]];
    cc.insert(mp(abs(v[id]), id));
                                                                                   r = dis(center, a[i]);
    erase(fr[id]), erase(ba[id]);
                                                                                   for (int k = 0; k < j; ++ k) {
                                                                                     if (dis(center, a[k]) <= r) continue;</pre>
  cout << ans << endl;
                                                                                     center = external(a[i], a[j], a[k]);
  return 0;
                                                                                     r = dis(center, a[i]);
}
                                                                                  }
               -----Aliens-----
                                                                                }
int n, k, x[MAX];
                                                                              }
PII dp[MAX], rd[MAX]; // max value, times, can be buy, times
int judge(int now){
                                                                              cout << fixed << setprecision(10) << r << endl;</pre>
  dp[1] = mp(0, 0), rd[1] = mp(-x[1], 0);
                                                                                                        ' << center.S << "\n";</pre>
                                                                              cout << center.F <<</pre>
  REP(i, 2, n + 1){
                                                                              return 0;
    dp[i] = max(dp[i - 1], mp(rd[i - 1].A + x[i] - now, rd[i - 1])
         1].B + 1));
    rd[i] = max(rd[i - 1], mp(dp[i - 1].A - x[i])
                                                           , dp[i -
                                                                                      Rotating Sweep Line
                                                                            12.8
         1].B));
                                                                            12.9
                                                                                      Hilbert Curve
  }
  return dp[n].B;
                                                                            // soring Mo's with hilbert(nn, L, R) can be faster !! // needed: nn >= n, no need to change n, nn = 2^k
int32_t main(){
                                                                            // usage: sort (ql_i, qr_i) by hilbert(nn, ql_i, qr_i)
  IOS;
                                                                            11 hilbert(int nn, int x, int y) {
  cin >> n >> k;
                                                                              ll res = 0;
                                                                              for (int s = nn / 2; s; s >>= 1) {
  for (int i = 2; i \le n + 1; ++ i)
                                                                                 int rx = (x \& s) > 0;
    cin >> x[i];
                                                                                int ry = (y & s) > 0;
res += s * 1ll * s * ((3 * rx) ^ ry);
  for (int i = 1; i \le n; ++ i)
    x[i] += x[i - 1];
                                                                                 if (ry == 0) {
  if(judge(0) <= k) cout << dp[n].A << endl;</pre>
                                                                                   if (rx == 1) {
 x = s - 1 -
  else {
    int l = 0, r = 10000000000000L;
                                                                                     y = s - 1 - y;
    while(r - l > 1){
       int mid = l + ((r - l) \gg 1), res = judge(mid);
                                                                                   swap(x, y);
       if(res == k) return cout << dp[n].A + dp[n].B * mid <<</pre>
                                                                                }
            endl, 0;
       else if(res < k) r = mid;</pre>
                                                                              return res;
       else if(res > k) l = mid;
                                                                           1 }
    judge(l);
    cout << dp[n].A + k * l << endl;
  return 0;
```

12.7 Minimum Enclosing Cycle