#### Contents Circle and Polygon intersection $\ \ldots \ \ldots \ \ldots \ \ldots$ 11.6 11.7 22 Basic Rotating Calipers . . . . . . . . . . . . . . . . 11.9 1.1 $.vimrc \ \ldots \ldots \ldots \ldots \ldots \ldots \ldots$ 1.2 12 Ad hoc 1.3 12.1 1.4 12.2 Segment Max Segment Sum . . . . . . . . . . . . . Pragma 17 124 12.5 24 1.8 12.6 24 12.8 Builtin Function Hilbert Curve . . . . . . . 12.9 2.2 2.3 1 Basic 2.4 1.1.vimrc Theorem and Formula syntax on Data Structure se ru nu ai se ts=4 sts=4 sw=4 st=4 smarttab laststatus=2 expandtab inoremap {<ENTER> {}<LEFT><ENTER>;<LEFT><DEL><ENTER><UP><TAB> "se mouse=a expandtab 4.4 4.5 4.6 1.2 Check 4.7 Dancing Link . . . . . . for i in \$(seq 1 10000); ./gen > input Flow ./ac < input > out\_ac 5.1 ./wa < input > out\_wa 5.2 diff out\_ac out\_wa || break 5.3 5.4 1.3 Factor Count List 6 Tree 6.1Zhu Liu Algo Centroid Decomposition 6.2 ζi. 6.3 factor number of i) 80 72, 50400 6.4 10080 72, 168, 108, 110880 144 6.5 192, 221760 332640 498960 200 6.6 554400 216, 665280 720720 240, 256, 1081080 2162160 320, 3603600 360 Graph 4324320 384, 6486480 400, 7207200 432, 448, 10810800 576, 720. 8648640 480, 21621600 7.132432400 672, 600, 43243200 61261200 7.2Maximum Weighted Matching(General Graph) Minimum Mean Cycle Maximum Clique 768, 110270160 800, 1152, 551350800 1200, 1344, 1102701600 1440, 73513440 245044800 1008 7.3 10 367567200 1200, 698377680 1280, 7.4 735134400 1396755360 1536 1.4 Default Math Extended Euclidean Big Integer Gaussian Elimination Linear Basis Build Prime Miller Rabin Pollard Rho Build Phi and Mu Primitive Root Cipolla's Algorithm Discrete Log Integer Partition Meissel-Lehmer Algorithm De Bruijn Simplex Algorithm Middle Speed Linear Recursion 8.1 // Compile with "g++ -std=c++11 -Wall -Wextra -Wconversion -Wshadow -fsanitize=undefined -Dlawfung" 8.4 #ifdef lawfung 8.5 14 8.6 14 8.7 8.8 \_DO(\_\_VA\_ARGS\_\_);\ 8.10 }while(0) 8.11 template<typename I> void \_DO(I&&x) {cerr << x << '\n';}</pre> 8.12 template<typename I, typename ...T> void \_DO(I&&x,T&&...tail) { cerr << x << ", "; \_DO(tail...);}</pre> 8.13 8.14 #define IOS 8.15 #else #define debug(...) #define IOS ios\_base::sync\_with\_stdio(0);cin.tie(0) #endif 16 Convolution 9.1 16 9.2 1.5 Pragma 9.3 9.4 17 #pragma GCC optimize("Ofast", "unroll-loops") #pragma GCC optimize("no-stack-protector") 9.5 17 #pragma GCC target("sse,sse2,sse3,ssse3,sse4,sse4.2,popcnt,abm, 10 String mmx, avx, tune=native") 10.1Z value . Longest Palindrome . Aho-Corasick Algorithm . Suffix Array . Palindromic Tree . #pragma GCC diagnostic ignored "-W" 10.2 18 10.3 18 1.6 Random Number 10.4 10.5 10.6 #include <random> Lexicographically Smallest Rotation . . . . . . . . . . . . . . . mt19937 rng(chrono::steady\_clock::now().time\_since\_epoch(). count()); 11 Geometry int rand\_int(int lb, int ub) Circle 11.1 Half Plane Intersection Convex Hull 3D Dynamic convexhull Polar Angle Sort { return uniform\_int\_distribution<int>(lb, ub)(rng); } double rand\_double(double lb, double ub) { return uniform\_real\_distribution<double>(lb, ub)(rng); }

11.5

### 1.7 Increase Stack Size

```
const int size = 256 << 20;
register long rsp asm("rsp");
char *p = (char*)malloc(size) + size, *bak = (char*)rsp;
__asm__("movq %0, %%rsp\n"::"r"(p));
// main
__asm__("movq %0, %%rsp\n"::"r"(bak));</pre>
```

#### 1.8 FasterIO

```
| static inline char getRawChar() {
| static char buf[1 << 16], *p = buf, *end = buf;
| if (p == end) {
| if ((end = buf + fread_unlocked(buf, 1, 1 << 16, stdin)) ==
| buf) return '\0';
| p = buf;
| }
| return *p++;
| }
| while (c = getRawChar() && (unsigned)(c - '0') > 10U) n = n *
| 10 + (c - '0');
```

## 2 Bitwise Trick

## 2.1 Builtin Function

```
|// count left 0s
|int __builtin_clz (unsigned int x) // 31 - __builtin_clz is lg
|int __builtin_clzll (unsigned long long x) // 63 - clz
|// count number of 1's
|int __builtin_popcount (unsigned int x)
|int __builtin_popcountll (unsigned long long x)
```

#### 2.2 Subset Enumeration

```
int subset_enumeration(int s) {
  for (int now = s; now > 0; now = (now - 1) & s) {
    cout << now << ' ';
  }
  cout << "0\n";
}</pre>
```

## 2.3 Next Permutation on Binary

```
|ll next_perm(ll v) {
| ll t = v | (v - 1);
| return (t + 1) | (((~t & -~t) - 1) >> (__builtin_ctz(v) + 1))
| ;
|}
```

## 2.4 SOS DP

```
|// 0 is 0, 1 can be 1 or 0
| for (int i = 0; i < n; ++i)
| for (int j = 0; j < (1 << n); ++j)
| if (j & (1 << i))
| a[j] += a[j ^ (1 << i)];</pre>
```

# 3 Theorem and Formula

- Pick's theorem  $A = i + \frac{b}{2} 1$
- Laplacian matrix L = D A
- Derangement  $D_n = (n-1)(D_{n-1} + D_{n-2})$
- Möbius function  $\sum_{i|n} \mu(i) = [n=1]$
- Euler's totient function  $\sum\limits_{i\,|\,n}\phi(i)=n$
- Inversion formula

$$\begin{split} f(n) &= \sum_{i=0}^{n} \binom{n}{i} g(i), \ g(n) = \sum_{i=0}^{n} (-1)^{n-i} \binom{n}{i} f(i) \\ f(n) &= \sum_{d \mid n} g(d), \ g(n) = \sum_{d \mid n} \mu(\frac{n}{d}) f(d) \end{split}$$

• Sum of powers

$$\sum_{k=1}^{n} k^{m} = \frac{1}{m+1} \sum_{k=0}^{m} {m+1 \choose k} B_{k}^{+} n^{m+1-k}$$

$$\sum_{j=0}^{m} {m+1 \choose j} B_{j}^{-} = 0$$

$$\text{note}: B_{1}^{+} = -B_{1}^{-} B_{i}^{+} = B_{i}^{-}$$

• Cipolla's algorithm

$$\left(\frac{u}{p}\right)=u^{\frac{p-1}{2}}$$

$$1. \left(\frac{a^2 - n}{p}\right) = -1$$

2. 
$$x = (a + \sqrt{a^2 - n})^{\frac{p+1}{2}}$$

• High order residue

$$[d^{\frac{p-1}{(n,p-1)}}\equiv 1]$$
  $(p\text{ is odd prime and }p\not|d)$ 

· Packing and Covering

 $|{\rm Maximum~Independent~Set}| + |{\rm Minimum~Vertex~Cover}| = |{\rm V}|$ 

Kőnig's theorem

|Maximum matching|(easy) = |Minimum vertex cover|

• Dilworth's theorem

width = |smallest chain decomposition| (vertex split and matching) = |largest antichain| = |maximim clique in Complement| (easy)

· Mirsky's theorem

 $\begin{array}{l} \mbox{height} = |\mbox{longest chain}|(\mbox{easy DP}) = |\mbox{smallest antichain decomposition}| \\ = |\mbox{minimum anticlique partition}| \ (\mbox{subset DP}) \end{array}$ 

• Triangle center

```
-G: (1, 1, 1)
-O: (a^{2}(b^{2} + c^{2} - a^{2}), \cdots) = (\sin 2A, \sin 2B, \sin 2C)
-I: (a, b, c) = (\sin A, \sin B, \sin C)
-E: (-a, b, c) = (-\sin A, \sin B, \sin C)
-H: (\frac{1}{b^{2} + c^{2} - a^{2}}, \cdots) = (\tan A, \tan B, \tan C)
```

•  $\lfloor \frac{n}{i} \rfloor$  enumeration  $T_0 = 1, T_i = \lfloor \frac{n}{\lfloor \frac{n}{T_{i-1}+1} \rfloor} \rfloor$ 

## 4 Data Structure

## $4.1 < ext/pb_ds >$

```
#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/priority_queue.hpp>
#include <ext/rope>
using namespace __gnu_pbds;
using namespace __gnu_cxx;
using namespace std;
__gnu_pbds::priority_queue<int> pq, pq2;
__gnu_pbds::priority_queue<int>::point_iterator idx[10];
__gnu_pbds::priority_queue<int, less<int>, pairing_heap_tag>
pairing_heap_tag, thin_heap_tag, binomial_heap_tag
rc_binomial_heap_tag, binary_heap_tag
*/
idx[0] = pq.push(1);
pq.modify(idx[0], 2); // change the iterator's value to 2
pq.join(pq2);
typedef tree<int,null_type,less<int>,rb_tree_tag,
     tree_order_statistics_node_update> TREE;
TREE name;
*name.find_by_order(0);
name.order_of_key(1);
name.insert(2);
name.delete(3);
name.split(v, b); /// value < v of a split to b</pre>
name.join(another TREE);
```

# 4.2 Unordered Map Hash

```
| struct KeyHasher {
    size_t operator()(const Key& k) const {
        return k.first + k.second * 100000;
    }
    };
    typedef unordered_map<Key, int, KeyHasher> map_t;
```

## 4.3 Rope

```
#include <ext/rope>
using namespace __gnu_cxx;
int main() {
  rope<int> v;
                // can be cout directly if it's char
  rope<int> v1(v);
  rope<int> v2(arr, arr + 10); //int arr[100];
  v.find(3); // return the first positoin of 3
  v.push_back(4); v.pop_back();
  //append not for iterator
  v.insert(pos, s); // pos can be iterator, integer. s can be
  rope, int, array
v.replace(pos, len, s); // (pos, len) can be (it1, it2). s is
        same as insert.
  v.erase(pos, len); // or v.erase(it1, it2)
  v2 = v.substr(pos, len); // same as erase
v.copy(pos, len, arr); // int arr[100]; (pos, len) can be
       omitted
  v[0], v[1]
  auto it1 = v.mutable_begin(), it2 = v.mutable_end();
```

## 4.4 Disjoint Set

```
struct DJS{
  int p[N], rk[N];
  vector<pair<int*,int>> memo;
  vector<size_t> stk;
  void save() {
    stk.push_back(memo.size());
  void undo() {
    while(memo.size() > stk.back()) {
      *memo.back().first = memo.back().second;
      memo.pop_back();
    stk.pop_back();
  }
  void assign(int *x, int v) {
    memo.push_back({x, *x});
  //assign(&a, b); //a = b
} djs;
```

#### 4.5 Persistent Treap

```
#include <bits/stdc++.h>
using namespace std;
struct Treap {
  static Treap mem[P];
Treap * lc, * rc;
  char c;
  int sz;
  Treap() {}
  Treap(char _c): lc(NULL), rc(NULL), sz(1), c(_c) {}
Treap::mem[P], * ptr = Treap::mem;
int Sz(Treap * t) {
    return t ? t -> sz : 0;
void pull(Treap * t) {
  if (!t) return;
  t \rightarrow sz = Sz(t \rightarrow lc) + Sz(t \rightarrow rc) + 1;
Treap * merge(Treap * a, Treap * b) {
  if (!a | | !b) return a ? a : b;
Treap * ret;
  if (myRnd() % (Sz(a) + Sz(b)) < Sz(a)) {
    ret = new(ptr++) Treap( * a);
    ret -> rc = merge(a -> rc, b);
  } else {
    ret = new(ptr++) Treap(*b);
    ret -> lc = merge(a, b -> lc);
  pull(ret);
  return ret;
void split(Treap * t, int k, Treap * & a, Treap * & b) {
  if (!t) a = b = NULL;
  else if (Sz(t -> lc) + 1 <= k) {
    a = new(ptr++) Treap(*t);
    split(t -> rc, k - Sz(t -> lc) - 1, a -> rc, b);
    pull(a);
```

```
} else {
    b = new(ptr++) Treap(*t);
    split(t \rightarrow lc, k, a, b \rightarrow lc);
    pull(b);
}
int d:
char buf[M];
Treap * ver[N];
ptr = Treap::mem;
v_cnt++:
ver[v_cnt] = ver[v_cnt - 1];
split(ver[v_cnt], p, tl, tr);
tl = merge(tl, new(ptr++) Treap(buf[j]));
4.6 Link Cut Tree
struct SplayNode {
  static SplayNode HOLE;
  SplayNode *ch[2], *par;
  SplayNode(): par(&HOLE), rev(false) { ch[0] = ch[1] = &HOLE;}
  bool isRoot() {
    return (par->ch[0] != this && par->ch[1] != this);
  void push() {
    if (rev) {
      if (ch[0]) ch[0]->rev ^= 1;
      if (ch[1]) ch[1]->rev ^= 1;
      swap(ch[0], ch[1]);
      rev ^= 1;
    }
  void pushFromRoot() {
    if (!isRoot()) par->pushFromRoot();
    push();
  void pull() {
    if (ch[0]) ch[0] -> d = d + ch[0] -> parLen;
    if (ch[1]) ch[1]->d = d + ch[1]->parLen;
  void rotate() {
    SplayNode *p = par, *gp = p->par;
    bool dir = (p->ch[1] == this);
    par = gp;
    if (!p->isRoot()) gp->ch[gp->ch[1] == p] = this;
    p \rightarrow ch[dir] = ch[dir \land 1];
    p->ch[dir]->par = p;
    p->par = this;
    ch[dir ^ 1] = p
    p->pull(), pull();
  void splay() {
    pushFromRoot();
    while (!isRoot()) {
      if (!par->isRoot()) {
         SplayNode *gp = par->par;
         if ((gp \rightarrow ch[0] == par) == (par \rightarrow ch[0] == this)) rotate
              ();
        else par->rotate();
      rotate();
    }
} SplayNode::HOLE;
namespace LCT {
  SplayNode *access(SplayNode *x) {
   SplayNode *last = &SplayNode::HOLE;
    while (x != &SplayNode::HOLE) {
      x->splay();
      x \rightarrow ch[1] = last;
      x->pull();
      last = x
      x = x - par;
    return last:
  void makeRoot(SplayNode *x) {
    access(x);
    x->splay()
  void link(SplayNode *x, SplayNode *y) {
    makeRoot(x);
```

x->par = y;

```
void cut(SplayNode *x, SplayNode *y) {
                                                                      #define INF 0x3f3f3f3f3f
    makeRoot(x);
                                                                       struct DLX{
                                                                         int n, sz, s[MAX];
int row[MAX * 100], col[MAX * 100];
    access(y)
    y->splay();
    y->ch[0] = &SplayNode::HOLE;
                                                                         int l[MAX * 100], r[MAX * 100], u[MAX * 100], d[MAX * 100];
    x->par = &SplayNode::HOLE;
                                                                         int ans
  }
                                                                         void init(int n) {
  void cutParent(SplayNode *x) {
                                                                           this -> n = n;
ans = INF;
    access(x)
    x->splay();
                                                                           for (int i = 0; i \le n; ++ i) {
    x->ch[0]->par = &SplayNode::HOLE;
                                                                             u[i] = d[i] = i;
l[i] = i - 1;
    x->ch[0] = &SplayNode::HOLE;
                                                                             r[i] = i + 1;
  SplayNode *findRoot(SplayNode *x) {
    x = access(x);
                                                                           r[n] = 0, l[0] = n;
    while (x->ch[0] != \&SplayNode::HOLE) x = x->ch[0];
                                                                           sz = n + 1;
    x->splay();
                                                                           memset(s, 0, sizeof s);
    return x;
                                                                         void AddRow(int rr, vector<int> sol) {
                                                                           int tmp = sz;
  SplayNode *query(SplayNode *x, SplayNode *y) {
    makeRoot(x);
                                                                           for(auto to : sol) {
    return access(y);
                                                                             l[sz] = sz - 1;
                                                                             r[sz] = sz + 1;
                                                                             d[sz] = to;
  SplayNode *queryLca(SplayNode *x, SplayNode *y) {
    access(x);
                                                                             u[sz] = u[to];
    auto lca = access(y);
                                                                             d[u[to]] = sz, u[to] = sz;
    x->splay();
                                                                             row[sz] = rr, col[sz] = to;
    return lca \rightarrow data + lca \rightarrow ch[1] \rightarrow sum + (x == lca ? 0 : x \rightarrow sum)
                                                                             s[to] ++, sz ++;
                                                                           r[sz - 1] = tmp, l[tmp] = sz - 1;
  void modify(SplayNode *x, int data) {
    x->splay();
x->data = data;
                                                                      #define FOR(i, way, to) for(int i = way[to]; i != to; i = way
                                                                            [i])
    x->pull();
                                                                         void remove(int c) {
                                                                           l[r[c]] = l[c];
ĺ}
                                                                           r[l[c]] = r[c]
                                                                           FOR(i, d, c) FOR(j, r, i) {
        Li Chao Tree
                                                                             u[d[j]] = u[j];
                                                                             d[u[j]] = d[j];
struct line {
                                                                             --s[col[j]];
   ll a, b;
                                                                           }
  line(): a(0), b(0) {}
line(ll a, ll b): a(a), b(b) {}
                                                                         int restore(int c) {
                                                                           FOR(i, u, c) FOR(j, l, i) {
  11 operator()(11 x) const { return a * x + b; }
                                                                             ++s[col[j]];
                                                                             u[d[j]] =
struct lichao {
                                                                             d[u[j]] = j;
  line st[NN];
  int sz, lc[NN], rc[NN];
                                                                           ĺ[r[c]] = c;
  int gnode() {
                                                                           r[l[c]] = c;
    st[sz] = line(0, -1e18); //min: st[sz] = line(0, 1e18);
    lc[sz] = -1, rc[sz] = -1;
                                                                         void DFS(int floor) {
    return sz++;
                                                                           if(r[0] == 0) {
                                                                             ans = min(ans, floor);
  void init() {
                                                                             return;
    sz = 0; gnode();
                                                                           if(floor >= ans) return;
   void add(int l, int r, line tl, int o) {
                                                                           int c = r[0];
    //[l, r)
                                                                           FOR(i, r, 0) if(s[i] < s[c]) c = i;
    bool lcp = st[o](l) < tl(l); //min: change < to >
                                                                           remove(c);
    FOR(i, d, c) {
                                                                             FOR(j, r, i) remove(col[j]);
    if (mcp) swap(st[o], tl);
                                                                             DFS(floor + 1);
     if (r - l == 1) return;
                                                                             FOR(j, l, i) restore(col[j]);
     if (lcp != mcp) {
       if (lc[o] == -1) lc[o] = gnode();
add(l, (l + r) / 2, tl, lc[o]);
                                                                           restore(c);
                                                                         }
    } else {
                                                                      } solver;
       if (rc[o] == -1) rc[o] = gnode();
                                                                      int n, m;
       add((l + r) / 2, r, tl, rc[o]);
                                                                      int32_t main() {
                                                                         while(cin >> n >> m) {
  11 query(int 1, int r, int x, int o) {
                                                                           solver.init(m);
     if (r - l == 1) return st[o](x);
                                                                           for (int i = 0; i < n; ++ i) {
     if (x < (l + r) / 2) {
                                                                             int nn, in;
       if (lc[o] == -1) return st[o](x);
                                                                             cin >> nn;
       return max(st[o](x), query(l, (l + r) / 2, x, lc[o]));
                                                                             vector<int> sol;
    } else {
                                                                             for (int j = 0; j < nn; ++ j)
       if (rc[o] == -1) return st[o](x);
                                                                               cin >> in, sol.emplace_back(in);
       return max(st[o](x), query((l + r) / 2, r, x, rc[o]));
                                                                             solver.AddRow(i, sol);
    }
  }
                                                                           solver.DFS(0);
|} solver;
                                                                           if(solver.ans == INF) cout << "No" << endl;</pre>
                                                                           else cout << solver.ans << endl;</pre>
```

return 0:

}

## 4.8 Dancing Link

## 4.9 Range Modify and Query BIT

```
int n, m, k;
int bit[4][MAX][MAX];
void update(int c[MAX][MAX], int a, int b, int val) {
  for (int i = a + 10 ; i < MAX ; i += i & -i)
    for (int j = b + 10 ; j < MAX ; j += j & -j)</pre>
       c[i][j] += val;
int update(int x, int y, int val) {
  update(bit[0], x, y, val);
update(bit[1], x, y, -val * x);
update(bit[2], x, y, -val * y);
update(bit[3], x, y, val * x * y);
void update(int a, int b, int x, int y, int val) {
  update(a, b, val);
  update(a, y + 1, -val);
update(x + 1, b, -val);
  update(x + 1, y + 1, val);
int query(int c[MAX][MAX], int a, int b) {
  int cnt = 0;
  for (int i = a + 10; i > 0; i -= i \& -i)
     for (int j = b + 10; j > 0; j -= j \& -j)
       cnt += c[i][j];
  return cnt;
}
int query(int x, int y) {
  int cnt = 0;
  cnt += query(bit[2], x, y) * (x + 1);
  cnt += query(bit[3], x, y);
  return cnt;
int query(int a, int b, int x, int y) {
  int cnt = 0;
  cnt += query(a - 1, b - 1);
  cnt -= query(a - 1, y);
cnt -= query(x, b - 1);
  cnt += query(x, y);
  return cnt;
}
/* usage:
void update(x1, y1, x2, y2, val);
int query(x1, y1, x2, y2); */
```

## 5 Flow

#### 5.1 ISAP with bound

```
Maximum density subgraph (\sum W_e + \sum W_v) / IVI
 Binary search on answer:
 For a fixed D, construct a Max flow model as follow:
 Let S be Sum of all weight(or inf)
 1. from source to each node with cap = S
2. For each (u,v,w) in E, (u->v,cap=w), (v->u,cap=w)
3. For each node v, from v to sink with cap = S + 2 * D - deg[v] - 2 * (W of v)
 where deg[v] = \sum deg = c deg
 If maxflow < S * IVI, D is an answer.
 Requiring subgraph: all vertex can be reached from source with
edge whose cap > 0.
 //Be careful that it's zero base !!!!!!!!
 #include <bits/stdc++.h>
 using namespace std;
 typedef long long ll;
 #define SZ(x) ((int)(x).size())
 #define eb emplace_back
 const 11 N = 5e2 + 5;
 struct isap{
      struct edge{
             int t, r;
             11 c:
             edge(int _t, int _r, ll _c) : t(_t), r(_r), c(_c) {}
       int n, S, T;
       vector<edge> adj[N];
       int dis[N], gap[N], ok;
       isap(int _n, int _s, int _t) : n(_n), S(_s), T(_t) {
```

```
for(int i = 0; i < n + 2; ++ i) adj[i].clear();</pre>
  void add(int u, int v, ll c){
    adj[u].eb(v, adj[v].size(), c);
    adj[v].eb(u, adj[u].size() - 1, 0);
  11 dfs(int now, ll f){
    if(now == T) return f;
int mi = n;
    for(edge &e : adj[now]){
      if(e.c){
         if(dis[now] == dis[e.t] + 1 && (x = dfs(e.t, min(f, e.c))
           )))){
e.c -= x
           adj[e.t][e.r].c += x;
           return x;
         mi = min(mi, dis[e.t]);
      }
    if(--gap[dis[now]] == 0) ok = 0;
    dis[now] = mi + 1;
    gap[ dis[now] ]++;
     return 0;
  il flow(){
    memset(dis, 0, n * 4);
    memset(gap, 0, n * 4);
    gap[0] = n;
    0k = 1;

11 r = 0;
    while(dis[S] < n && ok) r += dfs(S, INF);
    return r;
  // below for bounded only
  ll D[N];
  void bounded_init() {
    memset(D, 0, n * 8);
  void add2(int u, int v, ll b, ll c) {
    add(u, v, c - b);
    D[u] -= b;
D[v] += b;
  11 bounded_flow() {
    int SS = n, TT = n + 1;
ll base = 0;
    for(int i = 0; i < n; ++ i) {
      if (D[i] > 0) base += D[i];
if (D[i] > 0) add(SS, i, D[i]);
      if (D[i] < 0) add(i, TT, -D[i]);</pre>
    add(T, S, INF);
    int tmps = S, tmpt = T;
n += 2; S = SS, T = TT;
ll f = flow();
n -= 2; S = tmps; T = tmpt;
    return f == base ? flow() : -1LL;
5.2
      Min Cost Max Flow
```

```
struct Cost_Flow {
  struct Edge {
     int to, cap, rev, cost;
     Edge(int _to, int _cap, int _rev, int _cost): to(_to), cap(
           _cap), rev(_rev), cost(_cost) {}
  };
  vector<Edge> G[N];
  void add_edge(int from, int to, int cap, int cost) {
     G[from].push_back(Edge(to, cap, (int)G[to].size(), cost));
G[to].push_back(Edge(from, 0, (int)G[from].size() - 1, -
           cost));
  int n, s, t;
  void init(int _n, int _s, int _t) {
  n = _n, s = _s, t = _t;
  for (int i = 0; i <= n; ++i) {</pre>
       G[i].clear();
  bool in_que[N];
  int dis[N], par[N], par_id[N];
  pair<int, int> flow() {
     int flow = 0, cost = 0;
```

```
while (true) {
       for (int i = 0; i \le n; ++i) {
         dis[i] = INF, in_que[i] = false;
       queue<int> que; que.push(s);
       dis[s] = 0;
       while (!que.empty()) {
         int t = que.front(); que.pop();
         int ptr = 0;
         in_que[t] = false;
         for (Edge e: G[t]) {
           if (e.cap > 0) {
             if (dis[e.to] > dis[t] + e.cost) {
               dis[e.to] = dis[t] + e.cost;
par[e.to] = t, par_id[e.to] = ptr;
                if (!in_que[e.to]) {
                  que.push(e.to);
                  in_que[e.to] = true;
             }
           }
           ++ptr;
         }
       if (dis[t] == INF) break;
       int mn_flow = INF;
       for (int i = t; i != s; i = par[i]) {
         mn_flow = min(mn_flow, G[par[i]][par_id[i]].cap);
       flow += mn_flow;
cost += mn_flow * dis[t];
       for (int i = t; i != s; i = par[i]) {
         G[par[i]][par_id[i]].cap -= mn_flow;
         G[i][G[par[i]][par_id[i]].rev].cap += mn_flow;
     return make_pair(flow, cost);
} flow;
```

## 5.3 S-W Global Min Cut

```
struct SW {
  //find global min cut in O(V^3)
  //points are ZERO-BASE!!!
  static const int N = 506;
 int adj[N][N], wei[N], n;
 bool vis[N], del[N];
  void init(int _n) {
   memset(adj, 0, sizeof(adj));
   memset(del, 0, sizeof(del));
 void add_edge(int x, int y, int w) {
   adj[x][y] += w;
   adj[y][x] += w;
  void search(int & s, int & t) {
   memset(wei, 0, sizeof(wei));
   memset(vis, 0, sizeof(vis));
    s = t = -1;
   while (true) {
      int mx = -1, mx_id = 0;
      for (int i = 0; i < n; ++i) {
       if (!del[i] && !vis[i] && mx < wei[i]) {</pre>
          mx_id = i
          mx = wei[i];
       }
     }
     if (mx == -1) break;
     vis[mx_id] = true;
      t = mx_id;
      for (int i = 0; i < n; ++i)
        if (!vis[i] && !del[i])
          wei[i] += adj[mx_id][i];
  int solve() {
   int ret = INF;
    for (int i = 0; i < n - 1; ++i) {
     int x, y;
      search(x, y);
      ret = min(ret, wei[y]);
      del[y] = true;
      for (int j = 0; j < n; ++j) {
        adj[x][j] += adj[y][j];
```

```
adj[j][x] += adj[y][j];
}
     }
    return ret;
}
SW;
```

## 5.4 Gomory Hu Tree

```
def cut(G,s,t) :
    return minimum s-t cut in G

def gomory_hu(G):
    T = {}
    p = [1] * |V(G)|
    for s in [2,n] :
        t = p[s]
    w(C) = cut(G, s, t)
    add(s, t, w(C)) to T
    for i in [s + 1, n] :
        if p[i] == t and s-i path exists in G\C :
        p[i] = s
    return T;
```

## 6 Tree

#### 6.1 Minimum Steiner Tree

```
// Minimum Steiner Tree
// 0(V 3^T + V^2 2^T)
struct SteinerTree {
     const int V = 33;
const int T = 8;
     const int INF = 0x3f3f3f3f;
   int n, dst[V][V], dp[1 << T][V], tdst[V];</pre>
   void init(int _n) {
     for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++)
  dst[i][j] = INF;</pre>
        dst[i][i] = 0;
   void add_edge(int ui, int vi, int wi) {
     dst[ui][vi] = min(dst[ui][vi], wi);
     dst[vi][ui] = min(dst[vi][ui], wi);
   void shortest_path() {
     for (int k = 0; k < n; k++)
for (int i = 0; i < n; i++)
          for (int j = 0; j < n; j++)
  dst[i][j] = min(dst[i][j],</pre>
               dst[i][k] + dst[k][j]);
   int solve(const vector < int > & ter) {
     int t = (int) ter.size();
     for (int i = 0; i < (1 << t); i++)
  for (int j = 0; j < n; j++)
    dp[i][j] = INF;</pre>
     for (int i = 0; i < n; i++)
        dp[0][i] = 0;
     for (int msk = 1; msk < (1 << t); msk++) {</pre>
        if (msk == (msk & (-msk))) {
          int who = __lg(msk);
for (int i = 0; i < n; i++)
             dp[msk][i] = dst[ter[who]][i];
          continue;
        for (int i = 0; i < n; i++)
for (int submsk = (msk - 1) & msk; submsk; submsk = (
             submsk - 1) & msk)
dp[msk][i] = min(dp[msk][i],
               dp[submsk][i] +
                dp[msk ^ submsk][i]);
        for (int i = 0; i < n; i++) {
           tdst[i] = INF;
          for (int j = 0; j < n; j++)
  tdst[i] = min(tdst[i],</pre>
               dp[msk][j] + dst[j][i]);
        for (int i = 0; i < n; i++)
          dp[msk][i] = tdst[i];
     int ans = INF:
     for (int i = 0; i < n; i++)
```

```
ans = min(ans, dp[(1 << t) - 1][i]);
return ans;
|  }
|}
|solver;</pre>
```

## 6.2 Zhu Liu Algo

```
struct ZL {
  //1 base edge and vertex
  static
  const int N = 556, M = 2660, MM = M * 10, inf = 1e9; /\!/MM = M * log N
  struct bian {
   int u. v. w. use. id:
  b[M], a[MM];
  int n, m = 0, ans, pre[N], id[N], vis[N], root, In[N], h[N],
       len, way[M];
  void init(int _n, int _root) {
    for (int i = 0; i < MM; ++i) {
      a[i] = \{0, 0, 0, 0, 0\};
    n = _n, m = 0;
    b[0].w = 1e9;
    root = _root;
  void add(int u, int v, int w) {
    b[++m] = (bian) \{u, v, w, 0, m\};
    a[m] = b[m];
  int work() {
    len = m;
    for (;;) {
      for (int i = 1; i <= n; i++) {
        pre[i] = 0;
        In[i] = inf;
id[i] = 0;
        vis[i] = 0;
        h[i] = 0;
      for (int i = 1; i <= m; i++)
         if (b[i].u != b[i].v && b[i].w < In[b[i].v]) {</pre>
          pre[b[i].v] = b[i].u;
          In[b[i].v] = b[i].w;
h[b[i].v] = b[i].id;
      for (int i = 1; i <= n; i++)
        if (pre[i] == 0 && i != root) return 0;
      int cnt = 0;
In[root] = 0;
      for (int i = 1; i <= n; i++) {
         if (i != root) a[h[i]].use++;
         int now = i;
        ans += In[i];
        while (vis[now] == 0 && now != root) {
           vis[now] = i;
           now = pre[now];
         if (now != root && vis[now] == i) {
          cnt++;
           int kk = now;
          while (1) {
             id[now] = cnt;
             now = pre[now];
             if (now == kk) break;
          }
        }
      if (cnt == 0) return 1;
      for (int i = 1; i <= n; i++)
      if (id[i] == 0) id[i] = ++cnt;
for (int i = 1; i <= m; i++) {</pre>
         int k1 = In[b[i].v], k2 = b[i].v;
        b[i].u = id[b[i].u];
        b[i].v = id[b[i].v];
        if (b[i].u != b[i].v) {
          b[i].w -= k1;
           a[++len].u = b[i].id;
           a[len].v = h[k2];
          b[i].id = len;
        }
      n = cnt;
      root = id[root];
    return 1;
```

```
int getway() {
    for (int i = 1; i <= m; i++) way[i] = 0;
    for (int i = len; i > m; i--) {
        a[a[i].u].use += a[i].use;
        a[a[i].v].use -= a[i].use;
    }
    for (int i = 1; i <= m; i++) way[i] = a[i].use;
    int ret = 0;
    for (int i = 1; i <= m; ++i) {
        if (way[i] == 1) {
            ret += a[i].w;
        }
    }
    return ret;
}

//if zl.work() == 0, then it is not connected
//otherwise, use zl.getway() to check bian is selected or not
</pre>
```

# 6.3 Centroid Decomposition

```
const int Mlg = __lg(MAX) + 2;
struct edge {
  int to, weight;
  edge(int _to, int _w): to(_to), weight(_w) {}
vector<edge> edg[MAX];
struct Cen {
  ll val;
  int p, sz, dep;
  Cen() {}
  Cen(int _p, int _d): val(0), p(_p), sz(0), dep(_d) {}
cen[MAX];
ll dis[Mlg][MAX];
bool visit[MAX];
vector < int > v
int sz[MAX], mx[MAX];
void dfs_sz(int id) {
  visit[id] = 1;
  v.push_back(id);
  sz[id] = 1;
  mx[id] = 0;
  for (edge i: edg[id]) {
    if (!visit[i.to]) {
      dfs_sz(i.to);
      mx[id] = max(mx[id], sz[i.to]);
      sz[id] += sz[i.to];
 }
void dfs_dis(int id, int cen_dep, ll weight) {
  dis[cen_dep][id] = weight;
  visit[id] = 1;
  for (edge i: edg[id])
    if (!visit[i.to])
      dfs_dis(i.to, cen_dep, weight + i.weight);
}
void build(int id, int cen_dep, int p) {
  dfs_sz(id);
  int nn = v.size();
  int ccen = -1;
  for (int i: v) {
    if (max(nn - sz[i], mx[i]) * 2 <= nn)</pre>
      ccen = i;
    visit[i] = 0;
  dfs_dis(ccen, cen_dep, 0);
  for (int i: v) visit[i] = 0;
  v.clear();
  visit[ccen] = 1;
  cen[ccen] = Cen(p, cen_dep);
  for (edge i: edg[ccen])
    if (!visit[i.to])
      build(i.to, cen_dep + 1, ccen);
void add(int id, int d) {
  for (int p = id; p != -1; p = cen[p].p) {
    cen[p].val += dis[cen[p].dep][id] * d;
    cen[p].val -= dis[cen[p].dep - 1][id] * d;
```

ans += z[id[i]];

```
cen[p].sz += d;
                                                                                kx[kt] = x[id[i]];
                                                                                ky[kt] = y[id[i]];
}
                                                                                kt++;
                                                                              }
ll_query(int id) {
                                                                            }
  ll ret = 0:
                                                                            for (int i = 1; i \le n; i++) a[i] = 0;
  int pre_sz = 0;
                                                                            for (int i = 0; i < kt; i++) a[find(kx[i])] = find(ky[i]);</pre>
  for (int p = id; p != -1; p = cen[p].p) {
                                                                            int n2 = 0;
    ret += cen[p].val;
                                                                            for (int i = 1; i <= n; i++)
    ret += (cen[p].sz - pre_sz) * dis[cen[p].dep][id];
                                                                              if (a[i] == 0)
    pre_sz = cen[p].sz;
                                                                                vd[i] = ++n2;
                                                                            for (int i = 1; i <= n; i++)
  return ret;
                                                                              if (a[i])
}
                                                                                vd[i] = vd[find(i)];
// edg[u].push_back(edge(v,w));
                                                                            int m2 = 0, * Nx = x + m1, * Ny = y + m1, * Nz = z + m1;
// edg[v].push_back(edge(u,w));
                                                                            for (int i = 0; i < m1; i++) app[i] = -1;
for (int i = 0; i < 0; i++)
if (app[ax[i]] == -1) {
// memset(visit,0,sizeof(visit));
// build(1,1,-1);
// add(u, d)
                                                                                Nx[m2] = vd[x[qx[i]]];
// query(u)
                                                                                Ny[m2] = vd[y[qx[i]]];
                                                                                Nz[m2] = z[qx[i]];
                                                                                app[qx[i]] = m2;
6.4 Dynamic MST
                                                                                m2++;
/* Dynamic MST 0( Q lg^2 Q )
                                                                            for (int i = 0; i < 0; i++) {
 (qx[i], qy[i])->chg weight of edge No.qx[i] to qy[i]
                                                                              z[qx[i]] = qy[i];
 delete an edge: (i, \infty)
                                                                              qx[i] = app[qx[i]];
 add an edge: change from \infty to specific value
                                                                            for (int i = 1; i <= n2; i++) a[i] = 0;
for (int i = 0; i < tm; i++) {
const int SZ = M + 3 * MXQ;
int a[N], * tz;
                                                                              ri = find(vd[x[id[i]]]);
int find(int xx) {
                                                                              rj = find(vd[y[id[i]]);
  int root = xx;
                                                                              if (ri != rj) {
  while (a[root]) root = a[root];
                                                                                a[ri] = rj;
  int next:
                                                                                Nx[m2] = vd[x[id[i]]];
  while ((next = a[xx])) {
                                                                                Ny[m2] = vd[y[id[i]]];
    a[xx] = root;
                                                                                Nz[m2] = z[id[i]];
    xx = next;
                                                                                m2++;
  return root;
                                                                            }
                                                                            int mid = Q / 2;
bool cmp(int aa, int bb) {
                                                                            solve(qx, qy, mid, n2, Nx, Ny, Nz, m2, ans);
  return tz[aa] < tz[bb];</pre>
                                                                            solve(qx + mid, qy + mid, Q - mid, n2, Nx, Ny, Nz, m2, ans);
int kx[N], ky[N], kt, vd[N], id[M], app[M];
                                                                          int x[SZ], y[SZ], z[SZ], qx[MXQ], qy[MXQ], n, m, Q;
bool extra[M];
                                                                         void init() {
void solve(int *qx, int *qy, int Q, int n, int *x, int *y, int
                                                                            scanf("%d%d", & n, & m);
     *z, int m1, long long ans) {
                                                                            for (int i = 0; i < m; i++) scanf("%d%d%d", x + i, y + i, z + i
  if (Q == 1) {
                                                                                  i);
    for (int i = 1; i \le n; i++) a[i] = 0;
                                                                            scanf("%d", & Q);
for (int i = 0; i < Q; i++) {</pre>
    z[qx[0]] = qy[0];
                                                                              scanf("%d%d", qx + i, qy + i);
    for (int i = 0; i < m1; i++) id[i] = i;</pre>
    sort(id, id + m1, cmp);
                                                                              qx[i]--;
                                                                           }
    int ri, rj;
     for (int i = 0; i < m1; i++) {
                                                                         }
                                                                         void work() {
      ri = find(x[id[i]]);
       rj = find(y[id[i]]);
                                                                           if (Q) solve(qx, qy, Q, n, x, y, z, m, 0);
       if (ri != rj)
        ans += z[id[i]];
                                                                         int main() {
                                                                            init();
         a[ri] = rj;
      }
                                                                            work();
    printf("%lld\n", ans);
                                                                          6.5 Heavy-Light Decomposition
    return;
  }
                                                                         |int siz[MAX], son[MAX], dep[MAX], ffa[MAX];
|int top[MAX], idx[MAX], idpo = 0;
  int ri, rj;
  //contract
                                                                         int n, m;
  for (int i = 1; i <= n; i++) a[i] = 0;
for (int i = 0; i < 0; i++) {
                                                                          int e[MAX][3];
                                                                         vector < int > v[MAX];
                                                                         struct node {
    ri = find(x[qx[i]]);
    rj = find(y[qx[i]]);
                                                                           int big, sml;
    if (ri != rj) a[ri] = rj;
                                                                         st[MAX * 4];
                                                                         void init() {
  int tm = 0;
                                                                           REP(i, 0, MAX) v[i].clear();
MEM(siz, 0), MEM(son, 0), MEM(dep, 0), MEM(ffa, 0);
  for (int i = 0; i < m1; i++) extra[i] = true;</pre>
  for (int i = 0; i < Q; i++) extra[qx[i]] = false;
for (int i = 0; i < m1; i++)</pre>
                                                                            MEM(top, 0), MEM(idx, 0), idpo = 0;
    if (extra[i]) id[tm++] = i;
                                                                         void DFS1(int now, int fa, int deep) {
  sort(id, id + tm, cmp);
for (int i = 0; i < tm; i++) {</pre>
                                                                            siz[now] = 1;
                                                                            dep[now] = deep;
    ri = find(x[id[i]]);
                                                                            ffa[now] = fa;
    rj = find(y[id[i]]);
                                                                            int big = 0;
     if (ri != rj) {
                                                                            REP(i, 0, v[now].size()) {
                                                                              int to = v[now][i];
       a[ri] = rj
```

**if** (to != fa) {

```
DFS1(to, now, deep + 1);
siz[now] += siz[to];
       if (siz[to] > big) big = siz[to], son[now] = to;
  }
}
void DFS2(int now, int fa, int root) {
  top[now] = root;
  idx[now] = ++idpo;
   if (son[now] != 0) DFS2(son[now], now, root);
  REP(i, 0, v[now].size()) {
    int to = v[now][i];
    if (to != fa && to != son[now]) DFS2(to, now, to);
void solveinit() {
  DFS1(1, 0, 0);
  DFS2(1, 0, 1);
  REP(i, 2, n + 1) {
    int a = e[i][0], b = e[i][1], c = e[i][2];
    if (dep[a] < dep[b]) swap(a, b);</pre>
    update(1, 1, n, idx[a], c);
  }
void query(int a, int b) {
  ans.big = -INF, ans.sml = INF;
  int t1 = top[a], t2 = top[b];
while (t1 != t2) {
    if (dep[t1] < dep[t2]) swap(t1, t2), swap(a, b);</pre>
    ans = pull(ans, query(1, 1, n, idx[t1], idx[a]);
    a = ffa[t1], t1 = top[a];
  if (dep[a] > dep[b]) swap(a, b);
  if (a != b) ans = pull(ans, query(1, 1, n, idx[son[a]], idx[b
       ]));
  return cout << ans.sml << " " << ans.big << endl, void();</pre>
init();
REP(i, 2, n + 1) {
  int a, b, c;
  cin >> a >> b >> c;
  e[i][0] = a, e[i][1] = b, e[i][2] = c;
  v[a].pb(b);
  v[b].pb(a);
solveinit();
query(a, b);
```

## 6.6 Block tree

```
#include <bits/stdc++.h>
using namespace std;
const int N = 30006;
const int K = 177;
int w[N], sum[N], mx[N];
int root[N], sz[N], fa[N], dep[N];
vector < int > G[N], T[N];
void dfs1(int now, int par, int depth) {
 fa[now] = par;
dep[now] = depth;
  if (!root[now]) {
    root[now] = now;
    sz[now] = 1;
 for (int i = 0; i < (int) G[now].size(); ++i) {</pre>
    int to = G[now][i];
    if (to == par) continue;
    if (sz[root[now]] + 1 < K) {</pre>
      T[now].push_back(to);
      root[to] = root[now];
      ++sz[root[now]];
    dfs1(to, now, depth + 1);
 }
void dfs2(int now, int pre_sum, int pre_mx) {
  sum[now] = pre_sum, mx[now] = pre_mx;
  for (int i = 0; i < (int) T[now].size(); ++i) {</pre>
    int to = T[now][i];
    dfs2(to, pre_sum + w[to], max(pre_mx, w[to]));
```

```
void change(int pos, int val) {
  w[pos] = val;
  dfs2(root[pos], w[root[pos]], w[root[pos]]);
void qmax(int u, int v) {
 // TODO
}
void qsum(int u, int v) {
  int ans = 0;
  while (u != v) {
    if (root[u] == root[v]) {
      if (dep[u] < dep[v]) swap(u, v);</pre>
      ans += w[u];
      u = fa[u];
    } else {
      if (dep[root[u]] < dep[root[v]]) swap(u, v);</pre>
      ans += sum[u];
      u = fa[root[u]];
  }
  ans += w[u];
  printf("%d\n", ans);
```

# Graph

## Biconnected Component

```
int low[N], dfn[N];
bool vis[N];
int cnt[N], e[N], x[N], y[N]; // e[i] = x[i] ^ y[i]
 int stamp, bcc_no = 0;
 vector<int> G[N], bcc[N];
stack<int> sta:
 void dfs(int now,int par) {
   vis[now] = true;
   dfn[now] = low[now] = (++stamp);
   for (int i : G[now]) {
     int to = ( e[i] ^ now );
if (to == par) continue;
     if (!vis[to]) {
       sta.push(i); dfs(to,now);
       low[now] = min(low[now], low[to]);
       if (low[to] >= dfn[now]) {
    ++bcc_no; int p; // p is edge index
            p = sta.top(); sta.pop();
            bcc[bcc_no].push_back(p);
          } while (p != i);
       }
     else if (dfn[to] < dfn[now]) {</pre>
       sta.push(i);
       low[now] = min(low[now], dfn[to]);
  }
13
```

## General Graph Macthing

```
const int N = 100006,
  E = (2e5) * 2;
struct Graph {
  //1-index
  int to[E], bro[E], head[N], e;
  int lnk[N], vis[N], stp, n;
  int per[N];
  void init(int _n) {
    //remember to set every array to 0
    stp = 0;
    n = _n;
    for (int i = 1; i <= n; i++)
      head[i] = lnk[i] = vis[i] = 0, per[i] = i;
    //random_shuffle(per+1, per+n+1);
  void add_edge(int u, int v) {
    u = per[u], v = per[v];
to[e] = v, bro[e] = head[u], head[u] = e++;
    to[e] = u, bro[e] = head[v], head[v] = e++;
```

```
bool dfs(int x) {
                                                                            struct WeightGraph {
    vis[x] = stp;
for (int i = head[x]; i; i = bro[i]) {
                                                                               static
                                                                               const int INF = INT_MAX;
       int v = to[i];
                                                                               static
       if (!lnk[v]) {
                                                                               const int N = 514;
         lnk[x] = v, lnk[v] = x;
return true;
                                                                               struct edge {
                                                                                 int u, v, w;
       } else if (vis[lnk[v]] < stp) {
  int w = lnk[v];</pre>
                                                                                 edge() {}
                                                                                 edge(int ui, int vi, int wi): u(ui), v(vi), w(wi) {}
         lnk[x] = v, lnk[v] = x, lnk[w] = 0;
                                                                              };
         if (dfs(w)) {
                                                                               int n, n_x;
                                                                               edge g[N * 2][N * 2];
                                                                              int lab[N * 2];
int match[N * 2], slack[N * 2], st[N * 2], pa[N * 2];
int flo_from[N * 2][N + 1], S[N * 2], vis[N * 2];
         lnk[w] = v, lnk[v] = w, lnk[x] = 0;
      }
    }
                                                                               vector < int > flo[N * 2];
    return false;
                                                                               queue < int > q;
                                                                               int e_delta(const edge & e) {
  int solve() {
                                                                                 return lab[e.u] + lab[e.v] - g[e.u][e.v].w * 2;
    int ans = 0;
    for (int i = 1; i <= n; i++)
                                                                               void update_slack(int u, int x) {
       if (!lnk[i]) {
                                                                                  \begin{tabular}{ll} \textbf{if} & (!slack[x] & || & e_delta(g[u][x]) & e_delta(g[slack[x]][x]) \\ \end{tabular} 
         stp++;
                                                                                       ) slack[x] = u;
         ans += dfs(i);
                                                                               void set_slack(int x) {
    return ans;
                                                                                 slack[x] = 0;
  }
                                                                                 for (int u = 1; u \le n; ++u)
                                                                                   if (g[u][x].w > 0 \&\& st[u] != x \&\& S[st[u]] == 0)
graph;
                                                                                      update_slack(u, x);
7.3 KM
                                                                               void q_push(int x) {
                                                                                 if (x \le n) q.push(x);
const int INF = 0x3f3f3f3f3f;
                                                                                 else
const int maxn = 610;
                                                                                   for (size_t i = 0; i < flo[x].size(); i++)
                                                                                      q_push(flo[x][i]);
int n, w[maxn][maxn], lx[maxn], ly[maxn], slk[maxn];
int s[maxn], t[maxn], good[maxn];
                                                                               void set_st(int x, int b) {
                                                                                 st[x] = b;
int match(int now) {
                                                                                 if (x > n)
  s[now] = 1;
                                                                                   for (size_t i = 0; i < flo[x].size(); ++i)
  for (int to = 1; to <= n; to ++) {
                                                                                      set_st(flo[x][i], b);
     if(t[to]) continue;
    if(lx[now] + ly[to] == w[now][to]) {
                                                                               int get_pr(int b, int xr) {
       t\Gamma to = 1
                                                                                 int pr = find(flo[b].begin(), flo[b].end(), xr) - flo[b].
       if(good[to] == 0 || match(good[to]))
                                                                                      begin();
         return good[to] = now, 1;
                                                                                 if (pr % 2 == 1) {
                                                                                   reverse(flo[b].begin() + 1, flo[b].end());
    else slk[to] = min(slk[to], lx[now] + ly[to] - w[now][to]);
                                                                                   return (int) flo[b].size() - pr;
                                                                                 } else return pr;
  return 0;
}
                                                                               void set_match(int u, int v) {
void update() {
                                                                                 match[u] = g[u][v].v;
  int val = INF;
                                                                                 if (u <= n) return;</pre>
  for (int i = 1; i <= n; i ++)
                                                                                 edge e = g[u][v];
    if(t[i] == 0) val = min(val, slk[i]);
                                                                                 int xr = flo_from[u][e.u], pr = get_pr(u, xr);
  for (int i = 1; i <= n; i ++) {
  if(s[i]) lx[i] -= val;</pre>
                                                                                 for (int i = 0; i < pr; ++i) set_match(flo[u][i], flo[u][i</pre>
                                                                                      ^ 17);
    if(t[i]) ly[i] += val;
                                                                                 set_match(xr, v);
                                                                                 rotate(flo[u].begin(), flo[u].begin() + pr, flo[u].end());
}
void run_km() {
  for (int i = 1; i <= n; i ++) {</pre>
                                                                               void augment(int u, int v) {
                                                                                 for (;;) {
    lx[i] = w[i][1];
                                                                                   int xnv = st[match[u]];
    for (int j = 1; j <= n; j ++)
                                                                                   set_match(u, v);
      lx[i] = max(lx[i], w[i][j]);
                                                                                   if (!xnv) return;
                                                                                   set_match(xnv, st[pa[xnv]]);
u = st[pa[xnv]], v = xnv;
  for (int i = 1; i <= n; i ++)
  ly[i] = 0, good[i] = 0;
for (int i = 1; i <= n; i ++) {
   for (int j = 1; j <= n; j ++) slk[j] = INF;</pre>
                                                                                 }
                                                                               int get_lca(int u, int v) {
    while(1) {
                                                                                 static int t = 0;
       for (int j = 1; j <= n; j ++)
s[j] = t[j] = 0;</pre>
                                                                                 for (++t; u || v; swap(u, v)) {
                                                                                   if (u == 0) continue;
if (vis[u] == t) return u;
       if(match(i)) break;
       else update();
                                                                                   vis[u] = \dot{t};
    }
                                                                                   u = st[match[u]];
  }
                                                                                   if (u) u = st[pa[u]];
}
/* how_to_use:
                                                                                 return 0;
1. put edge in w[i][j]
                                                                              }
2. run_km
                                                                               void add_blossom(int u, int lca, int v) {
3. match: (good[i], i)
*/
                                                                                 int b = n + 1;
```

while (b <= n\_x && st[b]) ++b;</pre>

if (b > n\_x) ++n\_x;

lab[b] = 0, S[b] = 0;

match[b] = match[lca];

# 7.4 Maximum Weighted Matching(General Graph)

```
flo[b].clear();
  flo[b].push_back(lca);
  for (int x = u, y; x != lca; x = st[pa[y]])
    flo[b].push_back(x), flo[b].push_back(y = st[match[x]]),
         q_push(y);
  reverse(flo[b].begin() + 1, flo[b].end());
for (int x = v, y; x != lca; x = st[pa[y]])
    flo[b].push_back(x), flo[b].push_back(y = st[match[x]]),
         q_push(y);
  set_st(b, b);
  for (int x = 1; x <= n_x; ++x) g[b][x].w = g[x][b].w = 0;
for (int x = 1; x <= n; ++x) flo_from[b][x] = 0;
  for (size_t i = 0; i < flo[b].size(); ++i) {</pre>
    int xs = flo[b][i];
    for (int x = 1; x <= n_x; ++x)
      if (g[b][x].w == 0 \mid \mid e_delta(g[xs][x]) < e_delta(g[b][
           x1))
        g[b][x] = g[xs][x], g[x][b] = g[x][xs];
    for (int x = 1; x <= n; ++x)
      if (flo_from[xs][x]) flo_from[b][x] = xs;
  set_slack(b);
}
void expand_blossom(int b) {
  for (size_t i = 0; i < flo[b].size(); ++i)</pre>
    set_st(flo[b][i], flo[b][i]);
  int xr = flo_from[b][g[b][pa[b]].u], pr = get_pr(b, xr);
  for (int i = 0; i < pr; i += 2) {
    int xs = flo[b][i], xns = flo[b][i + 1];
    pa[xs] = g[xns][xs].u;
    S[xs] = 1, S[xns] = 0;
slack[xs] = 0, set_slack(xns);
    q_push(xns);
  S[xr] = 1, pa[xr] = pa[b];
  for (size_t i = pr + 1; i < flo[b].size(); ++i) {</pre>
    int xs = flo[b][i];
    S[xs] = -1, set_slack(xs);
  st[b] = 0;
bool on_found_edge(const edge & e) {
  int u = st[e.u], v = st[e.v];
  if (S[v] == -1) {
    pa[v] = e.u, S[v] = 1;
    int nu = st[match[v]];
    slack[v] = slack[nu] = 0;
    S[nu] = 0, q_push(nu);
  } else if (S[v] == 0) {
    int lca = get_lca(u, v);
    if (!lca) return augment(u, v), augment(v, u), true;
    else add_blossom(u, lca, v);
  return false;
bool matching() {
  memset(S + 1, -1, sizeof(int) * n_x);
  memset(slack + 1, 0, sizeof(int) * n_x);
  q = queue < int > ();
  for (int x = 1; x <= n_x; ++x)
    if (st[x] == x \&\& !match[x]) pa[x] = 0, S[x] = 0, q_push(
  if (q.empty()) return false;
  for (;;) {
    while (q.size()) {
      int u = q.front();
      q.pop();
       if (S[st[u]] == 1) continue;
      for (int v = 1; v <= n; ++v)
        if (g[u][v].w > 0 && st[u] != st[v]) {
          if (e_delta(g[u][v]) == 0) {
             if (on_found_edge(g[u][v])) return true;
          } else update_slack(u, st[v]);
    int d = INF;
    for (int b = n + 1; b \le n_x; ++b)
      if (st[b] == b \&\& S[b] == 1) d = min(d, lab[b] / 2);
    for (int x = 1; x <= n_x; ++x)
      if (st[x] == x \&\& slack[x]) {
        if (S[x] == -1) d = min(d, e_delta(g[slack[x]][x]));
         else if (S[x] == 0) d = min(d, e_delta(g[slack[x]][x])
             ]) /\bar{2};
    for (int u = 1; u <= n; ++u) {
      if (S[st[u]] == 0) {
```

```
if (lab[u] <= d) return 0;</pre>
        lab[u] -= d;
} else if (S[st[u]] == 1) lab[u] += d;
      for (int b = n + 1; b \ll n_x; ++b)
        if (st[b] == b) {
  if (S[st[b]] == 0) lab[b] += d * 2;
           else if (S[st[b]] == 1) lab[b] -= d * 2;
      q = queue < int > ();
      for (int x = 1; x <= n_x; ++x)
  if (st[x] == x && slack[x] && st[slack[x]] != x &&</pre>
              e_delta(g[slack[x]][x]) == 0)
           if (on_found_edge(g[slack[x]][x])) return true;
      for (int b = n + 1; b \le n_x; ++b)
        if (st[b] == b \&\& S[b] == 1 \&\& lab[b] == 0)
              expand_blossom(b);
    return false;
  pair < long long, int > solve() {
    memset(match + 1, 0, sizeof(int) * n);
    n x = n:
    int n_matches = 0;
    long long tot_weight = 0;
    for (int u = 0; u <= n; ++u) st[u] = u, flo[u].clear();</pre>
    int w_max = 0;
    for (int u = 1; u \ll n; ++u)
      for (int v = 1; v \le n; ++v) {
        flo_from[u][v] = (u == v ? u : 0);
        w_max = max(w_max, g[u][v].w);
    for (int u = 1; u <= n; ++u) lab[u] = w_max;</pre>
    while (matching()) ++n_matches;
    for (int u = 1; u \le n; ++u)
      if (match[u] && match[u] < u)</pre>
         tot_weight += g[u][match[u]].w;
    return make_pair(tot_weight, n_matches);
  void add_edge(int ui, int vi, int wi) {
    g[ui][vi].w = g[vi][ui].w = wi;
  void init(int _n) {
    for (int u = 1; u <= n; ++u)
      for (int v = 1; v <= n; ++v)
        g[u][v] = edge(u, v, 0);
 }
graph;
```

#### 7.5 Minimum Mean Cycle

```
/* minimum mean cycle O(VE) */
struct MMC {
  struct Edge {
    int v, u;
double c;
  };
  int n, m, prv[V][V], prve[V][V], vst[V];
  Edge e[E];
  vector < int > edgeID, cycle, rho;
  double d[V][V];
  void init(int _n) {
    n = _n;
m = 0;
  // WARNING: TYPE matters
  void addEdge(int vi, int ui, double ci) {
    e[m++] = {
      vi,
      ui,
      ci
    };
  void bellman_ford() {
    for (int i = 0; i < n; i++) d[0][i] = 0;
    for (int i = 0; i < n; i++) {
      fill(d[i + 1], d[i + 1] + n, inf);
      for (int j = 0; j < m; j++) {
        int v = e[j].v, u = e[j].u;
        if (d[i][v] < inf && d[i + 1][u] > d[i][v] + e[j].c) {
          d[i + 1][u] = d[i][v] + e[j].c;
          prv[i + 1][u] = v;
          prve[i + 1][u] = j;
        }
      }
```

```
}
  double solve() {
   // returns inf if no cycle, mmc otherwise
    double mmc = inf;
    int st = -1;
   bellman_ford();
    for (int i = 0; i < n; i++) {
     double avg = -inf;
      for (int k = 0; k < n; k++) {
       else avg = max(avg, inf);
     if (avg < mmc) tie(mmc, st) = tie(avg, i);</pre>
   FZ(vst);
   edgeID.clear();
    cycle.clear();
    rho.clear();
    for (int i = n; !vst[st]; st = prv[i--][st]) {
     vst[st]++;
     edgeID.PB(prve[i][st]);
     rho.PB(st);
   while (vst[st] != 2) {
     int v = rho.back();
     rho.pop_back();
     cycle.PB(v);
     vst[v]++;
   }
   reverse(ALL(edgeID));
   edgeID.resize(SZ(cycle));
    return mmc;
 }
mmc;
```

## 7.6 Maximum Clique

```
struct BKB {
  static
  const int MAX_N = 50;
  typedef bitset < MAX_N > bst;
  bst N[MAX_N];
  int n;
  ll wei[MAX_N], ans, cc;
  BKB(int _n = 0): n(_n), ans(0), cc(0) {
    for (int i = 0; i < _n; ++i)
      N[i].reset();
  void add_edge(int a, int b) {
   N[a][b] = N[b][a] = 1;
  void set_wei(int a, ll w) {
    wei[a] = w;
  11 CNT(bst P) {
    //if vertices have no weight: return P.count();
    for (int i = P._Find_first(); i < n; i = P._Find_next(i))</pre>
      rt += wei[i];
    return rt;
  void pro(bst P, ll cnt = 0) {
    if (!P.any()) {
      if (cnt == ans)
        ++cc;
      else if (cnt > ans) {
        ans = cnt;
cc = 1;
      return;
    ^{\prime}/^{\prime} "<" can be change to "<=" if we don't need to count
    if (CNT(P) + cnt < ans)</pre>
    int u = P._Find_first();
    bst now = P \& \sim N[u];
    for (int i = now._Find_first(); i < n; i = now._Find_next(i</pre>
         )) {
      pro(P & N[i], cnt + wei[i]);
      P[i] = 0;
    return;
  }
  pll solve() {
```

```
bst tmp;
  tmp.reset();
  for (int i = 0; i < n; ++i)
     tmp[i] = 1;
  pro(tmp);
  return pll(ans, cc);
}
ss(0);</pre>
```

## 8 Math

## 8.1 Extended Euclidean

```
|// ax + by = gcd(a, b)
|ll exgcd(ll a, ll b, ll & x, ll & y) {
    if (a == 0) return x = 0, y = 1, b;
    ll g = exgcd(b % a, a, y, x);
    x -= b / a * y;
    return g;
|}
```

# 8.2 Big Integer

```
| struct Bigint {
   static
   const int LEN = 60;
   static
   const int BIGMOD = 10000;
   int s:
   int vl, v[LEN];
   // vector<int> v;
   Bigint(): s(1) {
     vl = 0;
   Bigint(long long a) {
     vl = 0;
     if (a < 0) {
       s = -1;
     while (a) {
       push_back(a % BIGMOD);
       a /= BIGMOD;
     }
   Bigint(string str) {
     vl = 0;
     int stPos = 0, num = 0;
     if (!str.empty() && str[0] == '-') {
       stPos = 1;
       s = -1;
     for (int i = SZ(str) - 1, q = 1; i >= stPos; i--) {
  num += (str[i] - '0') * q;
  if ((q *= 10) >= BIGMOD) {
         push_back(num);
         num = 0;
         q = 1;
       }
     if (num) push_back(num);
     n();
   int len() const {
     return vl; //return SZ(v);
   bool empty() const {
     return len() == 0;
   void push_back(int x) {
     v[v]++] = x; //v.PB(x);
   void pop_back() {
     vl--; //v.pop_back();
   int back() const {
     return v[vl - 1]; //return v.back();
   void n() {
     while (!empty() && !back()) pop_back();
   void resize(int nl) {
     vl = nl; //v.resize(nl);
     fill(v, v + vl, 0); //fill(ALL(v), 0);
```

```
void print() const {
  if (empty()) {
     putchar('0');
     return;
  if (s == -1) putchar('-');
  printf("%d", back());
for (int i = len() - 2; i >= 0; i--) printf("%.4d", v[i]);
friend std::ostream & operator << (std::ostream & out,</pre>
  const Bigint & a) {
  if (a.empty()) {
  out << "0";</pre>
     return out;
  if (a.s == -1) out << "-";
  out << a.back();
  for (int i = a.len() - 2; i >= 0; i--) {
     char str[10];
     snprintf(str, 5, "%.4d", a.v[i]);
     out << str;
  return out;
}
int cp3(const Bigint & b) const {
  if (s != b.s) return s - b.s;
if (s == -1) return -(- * this).cp3(-b);
   if (len() != b.len()) return len() - b.len(); //int
  for (int i = len() - 1; i >= 0; i--)
     if (v[i] != b.v[i]) return v[i] - b.v[i];
  return 0;
bool operator < (const Bigint & b) const {</pre>
  return cp3(b) < 0;</pre>
bool operator <= (const Bigint & b) const {</pre>
  return cp3(b) \ll 0;
bool operator == (const Bigint & b) const {
  return cp3(b) == 0;
bool operator != (const Bigint & b) const {
  return cp3(b) != 0;
bool operator > (const Bigint & b) const {
  return cp3(b) > 0;
bool operator >= (const Bigint & b) const {
  return cp3(b) >= 0;
Bigint operator - () const {
  Bigint r = (*this);
  r.s = -r.s;
  return r:
Bigint operator + (const Bigint & b) const {
  if (s == -1) return -(-(* this) + (-b));
if (b.s == -1) return (* this) - (-b);
  Bigint r;
  int nl = max(len(), b.len());
  r.resize(nl + 1);
   for (int i = 0; i < nl; i++) {
    if (i < len()) r.v[i] += v[i];
if (i < b.len()) r.v[i] += b.v[i];</pre>
     if (r.v[i] >= BIGMOD) {
       r.v[i + 1] += r.v[i] / BIGMOD;
       r.v[i] %= BIGMOD;
  }
  r.n();
  return r:
Bigint operator - (const Bigint & b) const {
  if (s == -1) return -(-( * this) - (-b));
if (b.s == -1) return ( * this) + (-b);
if (( * this) < b) return -(b - ( * this));</pre>
  Bigint r
  r.resize(len());
  for (int i = 0; i < len(); i++) {
    r.v[i] += v[i];
    if (i < b.len()) r.v[i] -= b.v[i];
     if (r.v[i] < 0) {
       r.v[i] += BIGMOD;
       r.v[i + 1]--;
  }
```

```
r.n();
     return r:
   Bigint operator * (const Bigint & b) {
     Bigint r;
     r.resize(len() + b.len() + 1);
r.s = s * b.s;
     for (int i = 0; i < len(); i++) {</pre>
       for (int j = 0; j < b.len(); j++) {
         r.v[i + j] += v[i] * b.v[j];
         if (r.v[i + j] >= BIGMOD) {
  r.v[i + j + 1] += r.v[i + j] / BIGMOD;
           r.v[i + j] %= BIGMOD;
         }
       }
     }
     r.n();
     return r;
   Bigint operator / (const Bigint & b) {
     Bigint r:
     r.resize(max(1, len() - b.len() + 1));
     int oriS = s;
     Bigint b2 = b; // b2 = abs(b)
     s = b2.s = r.s = 1;
     for (int i = r.len() - 1; i >= 0; i--) {
       int d = 0, u = BIGMOD - 1;
       while (d < u) {</pre>
         int m = (d + u + 1) >> 1;
         r.v[i] = m;
         if ((r * b2) > ( * this)) u = m - 1;
         else d = m;
       r.v[i] = d;
     }
     s = oriS;
r.s = s * b.s;
     r.n();
     return r;
   Bigint operator % (const Bigint & b) {
     return ( * this) - ( * this) / b * b;
|};
```

### 8.3 Gaussian Elimination

```
const int GAUSS_MOD = 100000007LL;
struct GAUSS {
     int n:
     vector<vector<int>> v:
     int ppow(int a, int k) {
         if (k == 0) return 1;
         if (k \% 2 == 0) return ppow(a * a % GAUSS_MOD, k >> 1);
         if (k % 2 == 1) return ppow(a * a % GAUSS_MOD, k >> 1)

* a % CAUSS_MOD, k >> 1)
                a % GAUŚS_MOD;
     vector<int> solve() -
         vector<int> ans(n);
         REP(now, 0, n) {
             REP(i, now, n) if (v[now][now] == 0 && v[i][now] != 0)
                  swap(v[i], v[now]); // det = -det;
              if (v[now][now] == 0) return ans;
              int inv = ppow(v[now][now], GAUSS_MOD - 2);
             REP(i, 0, n) if (i != now) {
   int tmp = v[i][now] * inv % GAUSS_MOD;
                  REP(j, now, n + 1)(v[i][j] += GAUSS_MOD - tmp *
                         v[now][j] % GAUSS_MOD) %= GAUSS_MOD;
         REP(i, 0, n) ans[i] = v[i][n + 1] * ppow(v[i][i],
              GAUSS_MOD - 2) % GAUSS_MOD;
         return ans;
     // gs.v.clear() , gs.v.resize(n , vector<int>(n + 1 , 0));
}
gs;
```

#### 8.4 Linear Basis

```
const int MAX_M = 500; //maximum number of variable
typedef bitset<MAX_M + 1> bst;
struct linear_basis {
  int m;
  bst mat[MAX_M];
  linear_basis(int _m): m(_m) {
```

```
for (int i = 0; i < _m; ++i) mat[i].reset();</pre>
  // True means "No solution"
  int add_constraint(bst now) {
    for (int j = 0; j < m; ++j) {
      if (now[j]) {
         if (mat[j][j]) now ^= mat[j];
         else {
          mat[j] = now;
           for (int k = j + 1; k < m; ++k)
             if (mat[j][k])
           mat[j] ^= mat[k];
for (int k = 0; k < j; ++k)</pre>
             if (mat[k][j])
               mat[k] ^= mat[j];
          return 0;
      }
    }
    return now[m];
  // get one possible solution
  bst get_ans() {
    bst rt:
    rt.reset();
    for (int i = 0; i < m; ++i)
      if (mat[i][i] && mat[i][m])
    rt[i] = 1;
return rt;
  }
};
/* usage :
1. Init it with # of variables
2. Adding constraint with format x1,x2...,xm,C
  get_ans return one possible solution
```

#### 8.5 Build Prime

```
// MAX, eb
void build_prime(int min_fc[], vector < int > & P) {
   for (int i = 2; i < MAX; ++i) {
      if (min_fc[i] == 0) min_fc[i] = i, P.eb(i);
      for (auto j: P) {
        if (i * j >= MAX) break;
        min_fc[i * j] = j;
        if (i % j == 0) break;
      }
   }
}
```

#### 8.6 Miller Rabin

```
ll mul(ll a, ll b, ll mod) {
  //calculate a*b % mod
  ll r = 0;
a %= mod;
   b %= mod;
   while (b) {
     if (b & 1) r = (a + r) = mod ? a + r - mod : a + r;
     a = (a + a > = mod ? a + a - mod : a + a);
     b >>= 1;
   return r;
 ll power(ll a, ll n, ll mod) {
   if (n == 0) return 1 ll;
   else if (n == 1) return a % mod;
   return mul(power(mul(a, a, mod), n / 2, mod), n % 2 ? a : 1,
        mod);
 const bool PRIME = 1, COMPOSITE = 0;
 bool miller_robin(ll n, ll a) {
  if (__gcd(a, n) == n) return PRIME;
if (__gcd(a, n) != 1) return COMPOSITE;
ll d = n - 1, r = 0, ret;
   while (d % 2 == 0) {
     r++;
d /= 2;
  }
   ret = power(a, d, n);
   if (ret == 1 || ret == n - 1) return PRIME;
   while (r--) {
     ret = mul(ret, ret, n);
     if (ret == n - 1) return PRIME;
   return COMPOSITE;
| }
```

## 8.7 Pollard Rho

```
// isPrime (miller rabin)
 map < ll, int > cnt;
 void PollardRho(ll n) {
   if (n == 1) return;
   if (isPrime(n)) return ++cnt[n], void();
   if (n % 2 == 0) return PollardRho(n / 2), ++cnt[2], void(); ll x = 2, y = 2, d = 1, p = 1; auto f = [ \& ](auto \ x, \ auto \ n, \ int \ p)  {
     return (mul(x, x, n) + p) % n;
   while (true) {
      if (d != n && d != 1) {
        PollardRho(n / d);
        PollardRho(d);
        return;
      if (d == n) ++p;
     x = f(x, n, p);
     y = f(f(y, n, p), n, p);
      d = \_gcd(abs(x - y), n);
}
```

#### 8.8 Build Phi and Mu

```
void build_phi(int ax[], int n) {
   for (int i = 1; i <= n; ++i)
      ax[i] = i;
   for (int i = 1; i <= n; ++i)
      for (int j = i + i; j <= n; j += i)
      ax[j] -= ax[i];
}
void build_mu(int ax[], int n) {
   for (int i = 1; i <= n; ++i)
      ax[i] = 0;
   ax[1] = 1;
   for (int i = 1; i <= n; ++i)
      for (int j = i + i; j <= n; j += i)
      ax[j] -= ax[i];
}</pre>
```

## 8.9 Primitive Root

```
|// build_phi, power, eb
// M has primitive root when M = 2, 4, p^n, 2p^n
ll Primitive_root(ll n) {
   if (n == 2) return 1;
vector < ll > sol;
   ll val = phi[n];
   for (ll i = 2; i * i <= val; ++i) {
     if (val % i == 0) {
       sol.eb(i);
       while (val % i == 0) val /= i;
   if (val != 1) sol.eb(val);
   for (ll i = 2; i < n; ++i) {
     if (__gcd(i, n) != 1) continue;
ll ok = 1;
     for (auto to: sol) {
       if (power(i, phi[n] / to, n) == 1) {
         ok = 0;
         break;
     if (ok)
       return i:
   return -1;
}
```

## 8.10 Cipolla's Algorithm

```
struct Cipolla {
   ll p, n, a, w;
```

```
Cipolla(ll _p, ll _n): p(_p), n(_n) {
   ll power(ll a, ll x) {
     if (x == 0) return 1;
     return power(a * a % p, x >> 1) * (x & 1 ? a : 1) % p;
   inline int lgd(ll x) {
     return power(x, (p - 1) / 2);
  ll rnd() {
     return (((11) rand() << 28) + rand());</pre>
   pll mul(pll a, pll b) {
     return pll((a.F * b.F + a.S * b.S % p * w) % p,
(a.F * b.S + a.S * b.F) % p);
   pll power(pll ii, ll x) {
     if (x == 0) return pll(1, 0);
return mul(power(mul(ii, ii), x >> 1), (x & 1 ? ii : pll(1,
           0)));
   ll solve() {
     if (p == 2)
return n & 1;
     if (lgd(n) == p - 1) return -1;
     if (n == 0) return 0;
     while (a = rnd() \% p, lgd((a * a - n + p) \% p) == 1);
     w = (a * a - n + p) \% p;
     pll ii = power(pll(a, 1), (p + 1) / 2);
     assert(ii.S == 0);
     return ii.F;
|};
```

## 8.11 Discrete Log

```
int DiscreteLog_with_s(int s, int x, int y, int m) {
     int kStep = max((int) sqrt(m), 10);
     unordered_map<int, int> p;
      int b = 1:
     for (int i = 0; i < kStep; ++i) {</pre>
          p[y] = i;
y = 1 LL * y * x % m;
b = 1 LL * b * x % m;
     for (int i = 0; i < m + 10; i += kStep) {
    s = 1 LL * s * b % m;</pre>
          if (p.find(s) != p.end()) return i + kStep - p[s];
     return -1;
 int DiscreteLog(int x, int y, int m) {
     // x ^ ? === y % m
     if (m == 1) return 0;
     // y %= m;
      int s = 1;
     for (int i = 0; i < 70; ++i) {
          if (s == y) return i;
s = 1 LL * s * x % m;
     if (s == y) return 70;
     int p = 70 + DiscreteLog_with_s(s, x, y, m);
      if (power(x, p, m) != y) return -1;
| }
```

## 8.12 Integer Partition

## 8.13 Meissel-Lehmer Algorithm

```
// count number of prime that is <= n</pre>
 int64_t PrimeCount(int64_t n) {
   if (n <= 1) return 0;</pre>
   const int v = sqrt(n);
   vector<int> smalls(v + 1);
   for (int i = 2; i \le v; ++i) smalls[i] = (i + 1) / 2;
   int s = (v + 1) / 2;
   vector<int> roughs(s);
   for (int i = 0; i < s; ++i) roughs[i] = 2 * i + 1;
vector<int64_t > larges(s);
   for (int i = 0; i < s; ++i) larges[i] = (n / (2 * i + 1) + 1)
         / 2;
   vector<bool> skip(v + 1);
   int pc = 0;
   for (int p = 3; p <= v; ++p) {
     if (smalls[p] > smalls[p - 1]) {
  int q = p * p;
        pc++
        if (1 LL * q * q > n) break;
        skip[p] = true;
        for (int i = q; i <= v; i += 2 * p) skip[i] = true;</pre>
        int ns = 0;
        for (int k = 0; k < s; ++k) {
          int i = roughs[k];
          if (skip[i]) continue;
          int64_t d = 1 LL * i * p;
          larges[ns] = larges[k] - (d <= v ? larges[smalls[d] -</pre>
               pc] : smalls[n / d]) + pc;
          roughs[ns++] = i;
        s = ns:
        for (int j = v / p; j >= p; --j) {
          int c = smalls[j] - pc;
for (int i = j * p, e = min(i + p, v + 1); i < e; ++i)
    smalls[i] -= c;
     }
   for (int k = 1; k < s; ++k) {
     const int64_t m = n / roughs[k];
     int64_t = larges[k] - (pc + k - 1);
     for (int l = 1; l < k; ++l) {
        int p = roughs[l];
       if (1 LL * p * p > m) break;
s -= smalls[m / p] - (pc + l - 1);
     larges[0] -= s;
   return larges[0];
}
```

#### 8.14 De Bruijn

```
// sz_lim, MAX, MAX_len
int res[MAX], aux[MAX_len];
void db(int t, int p, int len, int k, int & sz) {
  if (sz >= sz_lim) return;
  if (t > len) {
    if (len % p == 0) {
      for (int i = 1; i <= p && sz < sz_lim; ++i) res[sz++] =
            aux[i];
  } else {
    aux[t] = aux[t - p];
    db(t + 1, p, len, k, sz);
for (int i = aux[t - p] + 1; i < k; ++i) {
      aux[t] = i;
      db(t + 1, t, len, k, sz);
    }
  }
}
\ensuremath{/\!/} return cyclic string such that every string of length len
     using k character appears as a substring.
int de_bruijn(int k, int len) {
  if (k == 1) {
res[0] = 0;
    return 1;
  }
```

```
for (int i = 0; i < k * len; i++) aux[i] = 0;
int sz = 0;
db(1, 1, len, k, sz);
return sz; // k^n
}</pre>
```

# 8.15 Simplex Algorithm

```
maximize Cx under
Ax <=b
b >= 0
n variables
m constraints
A is m by n
const int MAX = 45;
int n, m;
double arr[MAX][MAX];
bool pro() {
  double mi = 0;
  int x = 1:
  for (int i = 1; i <= n + m; i++)
  if (arr[0][i] < mi) {</pre>
      mi = arr[0][i];
  if (abs(mi) < eps) return 0; // sigma <= 0</pre>
  mi = INF; // theta
  int y = 0;
  for (int i = 1; i <= m; i++) {
    if (arr[i][x] > eps && arr[i][n + m + 1] / arr[i][x] < mi)</pre>
      mi = arr[i][n + m + 1] / arr[i][x];
    }
  }
  assert(y);
  double weed = arr[y][x];
  for (int i = 1; i \le n + m + 1; ++i)
    arr[y][i] /= weed;
  // now arr[y][n + m + 1] == theta
  for (int i = 0; i \leftarrow m; i++) {
    if (i == y) continue;
    double f = arr[i][x];
    for (int j = 1; j <= m + n + 1; j++)
arr[i][j] -= f * arr[y][j];
  return 1;
int main() {
  cin >> n;
  cin >> m;
  memset(arr, 0, sizeof arr);
  // input C
  for (int i = 1; i <= n; i++) {
    cin >> arr[0][i];
    arr[0][i] = -arr[0][i];
  for (int i = 1; i <= m; i++) {
    // input A
    for (int j = 1; j <= n; j++)
      cin >> arr[i][j];
    arr[i][n + i] = 1;
    // input b
    cin >> arr[i][n + m + 1];
  while (pro());
  \texttt{cout} << \texttt{arr[0][n + m + 1]} << "\n";
  return 0;
```

#### 8.16 Middle Speed Linear Recursion

```
return ans;
 }
 vector < int > ppow(vector < int > a, int k) {
   if (k == 1) return a;
   if (k \% 2 == 0) return ppow(mul(a, a), k >> 1);
   if (k \% 2 == 1) return mul(ppow(mul(a, a), k >> 1), a);
 int main() {
   IOS;
while (cin >> n && n) {
     REP(i, 1, n + 1) cin >> x[i];
REP(i, 1, n + 1) cin >> c[i];
vector < int > v(n + n + 1);
     v[1] = 1;
     cin >> k, k++
      v = ppow(v, k);
     int ans = 0;
     REP(i, 1, n + 1) ans = (ans + x[i] * v[i]) % mod;
     cout << ans << endl;
   return 0:
}
```

#### 8.17 Chinese Remainder Theorem

```
const int INF = 0x3f3f3f3f
 void extgcd(ll a, ll b, ll & d, ll & x, ll & y) {
   if (b == 0) d = a, x = 1, y = 0;
   else extgcd(b, a % b, d, y, x), y = (a / b) * x;
 ĺl n;
 vector < ll > v, m;
 int main() {
   while (cin >> n) {
      v.clear(), m.clear();
      ll ans, mod, d, x, y;
REP(i, 0, n) cin >> mod >> ans, m.pb(mod), v.pb(ans);
      mod = m[0], ans = v[0];
      REP(i, 1, n) {
        ll res = ((v[i] - ans) % m[i] + m[i]) % m[i];
extgcd(mod, m[i], d, x, y);
        if (res % d != 0) {
    ans = -1;
           break;
        res = (res / d * x % m[i] + m[i]) % m[i];
ans = ans + res * mod;
mod = mod * m[i] / d;
      if (ans == -1) cout << ans << endl;</pre>
      else cout << ans % mod << endl;</pre>
   return 0;
}
```

## 9 Convolution

## 9.1 FFT

```
#include <bits/stdc++.h>
using namespace std;
const int MAXN = 2 * 262144;
typedef long double ld;
typedef complex<ld> cplx;
const ld PI = acos(-1);
const cplx I(0, 1);
cplx omega[MAXN + 1];
void pre_fft() {
 for (int i = 0; i <= MAXN; i++) {
    omega[i] = exp(i * 2 * PI / MAXN * I);
}
void fft(int n, cplx a[], bool inv = false) {
  int basic = MAXN/n:
  int theta = basic;
  for (int m = n; m >= 2; m >>= 1) {
    int mh = m >> 1;
    for (int i=0; i<mh; i++) {</pre>
      cplx w = omega[inv ? MAXN - (i * theta % MAXN) : i *
           theta % MAXN];
      for (int j = i; j < n; j += m) {
        int k = j + mh;
        cplx x = a[j] - a[k];
        a[j] += a[k];
```

}

}

```
void intt(vector < ll > & v, int n) {
        a[k] = w * x;
                                                                            ntt(v, n);
                                                                             reverse(v.begin() + 1, v.end());
                                                                             ll inv = fpow(n, mod - 2);
    theta = (theta * 2) % MAXN;
                                                                             for (int i = 0; i < n; ++i) {
  int i = 0;
                                                                               (v[i] *= inv) %= mod;
  for (int j = 1; j < n - 1; j++) {
    for (int k = n >> 1; k > (i ^= k); k >>= 1);
                                                                          }
    if (j<i) swap(a[i],a[j]);</pre>
                                                                          vector < ll > conv(vector < ll > a, vector < ll > b) {
                                                                            int sz = 1;
  if (inv) {
                                                                            while (sz < a.size() + b.size() - 1) sz <<= 1;</pre>
                                                                            vector < ll > c(sz);
    for (int i=0; i<n; i++) a[i] /= n;
                                                                             while (a.size() < sz) a.push_back(0);</pre>
                                                                             while (b.size() < sz) b.push_back(0);</pre>
cplx a[MAXN], b[MAXN], c[MAXN];
                                                                            ntt(a, sz), ntt(b, sz);
//how to use :
/*
                                                                             for (int i = 0; i < sz; ++i) c[i] = (a[i] * b[i]) % mod;
                                                                            intt(c, sz);
pre_fft();
                                                                             while (c.size() && c.back() == 0) c.pop_back();
fft(n,a);
                                                                             return c:
fft(n,b);
                                                                          }
for (int i = 0; i < n; i++) {
 c[i] = a[i] * b[i];
                                                                        ll chinese(ll b1, ll m1, ll b2, ll m2) {
                                                                          ll a1 = bigpow(m2, m1 - 2, m1) * b1 % m1;
ll a2 = bigpow(m1, m2 - 2, m2) * b2 % m2;
fft(n,c,1);
*/
                                                                          11 \text{ ret} = (a1 * m2 + a2 * m1) \% (m1 * m2);
                                                                          assert(ret % m1 == b1 && ret % m2 == b2);
                                                                          return ret;
9.2 NTT
// Remember coefficient are mod P
/*
                                                                        9.3 FWT
(mod, root)
(65537, 3)
                                                                       void FWT(ll a[],int n){
                                                                          for(int d = 1; d < n; d <<= 1) // d = half of block size
(23068673, 3)
                                                                             (998244353, 3)
(1107296257, 10)
                                                                                ll x = a[j], y = a[j + d];

a[j] = x + y; //FWT XOR
(2013265921, 31)
(2885681153, 3)
                                                                                 a[j] = x + y;
                                                                                 a[j + d] = x - y;
                                                                                                           //FWT XOR
                                                                                 a[j] = x + y;
                                                                                                           //FWT AND
typedef long long 11;
const int maxn = 65536;
                                                                                 a[j + d] = y + x;
                                                                                                           //FWT OR
struct NTT {
    ll mod = 2013265921, root = 31;
                                                                                 a[i] = (x + y) / 2;
                                                                                                           //TFWT XOR
                                                                                 a[j+d] = (x - y) / 2; //IFWT XOR
  ll\ omega[maxn + 1];
                                                                                 a[j] = x - y;
                                                                                                           //TFWT AND
                                                                                 a[j + d] = y - x;
  void prentt() {
                                                                                                           //IFWT OR
    ll x = fpow(root, (mod - 1) / maxn);
    omega[0] = 1;
                                                                       1}
    for (int i = 1; i <= maxn; ++i) {
      omega[i] = omega[i - 1] * \times % mod;
                                                                        9.4 Subset Convolution
    }
                                                                       | for (int i = 0; i <= n; ++ i) {
  void real_init(ll _mod, ll _root) {
                                                                          // f[__builtin_popcount(s)][s] = s, otherwise = 0. So is g[i]
    mod = _mod;
root = _root;
                                                                          FWT(f[i], n) // OR
                                                                          FWT(g[i], n) // OR
    prentt();
                                                                          for (int s = 0; s < (1 << n); ++ s)
                                                                             for (int j = 0; j \le i; ++ j)
  il fpow(ll a, ll n) {
  (n += mod - 1) %= mod - 1;
                                                                              h[i][s] += f[j][s] * g[i - j][s]
                                                                          IFWT(h[i], n) // OR
    ll r = 1;
                                                                          for (int s = 0; i < (1 << n); ++ s)
h[_builtin_popcount(s)][s] // is the real answer</pre>
    for (; n; n >>= 1) {
      if (n & 1)(r *= a) %= mod;
                                                                       }
      (a *= a) \%= mod;
                                                                        9.5 Ternary Xor
    return r;
                                                                       | pii operator*(const pii &p1, const pii &p2) {
| return {subb(mull(p1.F, p2.F) - mull(p1.S, p2.S)),
  void bitrev(vector < ll > & v, int n) {
    int z = __builtin_ctz(n) - 1;
                                                                               subb(addd(mull(p1.F, p2.S) + mull(p1.S, p2.F)) - mull(p1.
    for (int i = 0; i < n; ++i) {
       int x = 0;
                                                                                    S, p2.S));
       for (int j = 0; j \ll z; ++j) x \sim ((i >> j \& 1) \ll (z - j)
                                                                        pii cal1(pii p) {
           ));
       if (x > i) swap(v[x], v[i]);
                                                                          return {subb(-p.S), subb(p.F - p.S)};
    }
                                                                        pii cal2(pii p) {
  void ntt(vector < ll > & v, int n) {
                                                                          return {subb(p.S - p.F), subb(-p.F)};
    bitrev(v, n);
    for (int s = 2; s <= n; s <<= 1) {
                                                                        //C is the size of \alpha
                                                                        void DFT(vector<pii> &a) {
      int z = s \gg 1;
       for (int i = 0; i < n; i += s) {
                                                                          for (int mid = 1; mid < C; mid *= 3) {</pre>
         for (int k = 0; k < z; ++k) {
    ll x = v[i + k + z] * omega[maxn / s * k] % mod;</pre>
                                                                             for (int j = 0; j < C; j += mid * 3) {
                                                                               for (int k = 0; k < mid; ++k) {
           v[i + k + z] = (v[i + k] + mod - x) \% mod;
                                                                                 pii x = a[j + k], y = a[j + k + mid], z = a[j + k + (
           (v[i + k] += x) \%= mod;
                                                                                      mid << 1)];
                                                                                a[j + k] = x + y + z;

a[j + k + mid] = x + cal1(y) + cal2(z);
      }
```

a[j + k + (mid << 1)] = x + cal2(y) + cal1(z);

```
}
}
const int invn = ppow(C, mod - 2);
void IDFT(vector<pii> &a) {
 for (int mid = 1; mid < C; mid *= 3) {
  for (int j = 0; j < C; j += mid * 3) {</pre>
       for (int k = 0; k < mid; ++k) {
         pii x = a[j + k], y = a[j + k + mid],
           z = a[j + k + (mid << 1)];
         a[j + k] = x + y + z;

a[j + k + mid] = x + cal2(y) + cal1(z);
         a[j + k + (mid << 1)] = x + cal1(y) + cal2(z);
    }
  }
  for (int i = 0; i < C; ++i) {
    a[i].F = mull(a[i].F, invn);
void ff(vector<pii> &a, vector<pii> b) {
  DFT(a); DFT(b);
  for (int i = 0; i < C; ++i) {
    a[i] = a[i] * b[i];
  IDFT(a);
```

# 10 String

## 10.1 KMP

```
const KMP_SIZE = ;
struct KMP {
    string s;
    int f[KMP_SIZE], pos;
    void solve() {
        f[0] = pos = -1;
        for (int i = 1; i < s.size(); ++i) {
            while (pos != -1 && s[pos + 1] != s[i]) pos = f[pos];
        if (s[pos + 1] == s[i]) pos++;
        f[i] = pos;
        }
    }
}</pre>
```

#### 10.2 **Z** value

```
const int ZVALUE_SIZE = ;
struct Z_VALUE {
   string s;
   int l = 0, r = 0, z[ZVALUE_SIZE];
   void solve() {
      for (int i = 0; i < s.size(); ++i) {
        z[i] = max(min(z[i - l], r - i), 0 LL);
      while (i + z[i] < s.size() && s[z[i]] == s[i + z[i]]) {
        l = i, r = i + z[i];
        z[i]++;
      }
   }
};</pre>
```

### 10.3 Longest Palindrome

```
const int PALINDROME_MAX = 2 *;
       struct Palindrome {
                  string s, ss; // ss = input
                    int z[PALINDROME_MAX];
                   void solve() {
                                   s.resize(ss.size() + ss.size() + 1, '.');
                                   for (int i = 0; i < ss.size(); ++i)</pre>
                                 s[i + i + 1] = ss[i];
int l = 0, r = 0;
for (int i = 0; i < s.size(); ++i) {
                                              z[i] = max(min(z[l + l - i], r - i), 1);
while (i - z[i] >= 0 && i + z[i] < s.size() && s[i - z[i] < s.size() && s[i -
                                                                           ]] == s[i + z[i]]) {
                                                             l = i, r = i + z[i];
                                                            z[i]++;
                                           }
                              }
                  }
|};
```

# 10.4 Aho-Corasick Algorithm

```
struct AC_Automata {
  static
  const int N = 2e4 + 6;
  static
  const int SIGMA = 26;
  int ch[N][SIGMA], val[N], sz;
  int last[N], fail[N];
  int que[N], qs, qe, cnt[N];
  void init() {
    sz = 1;
    memset(ch[0], 0, sizeof(ch[0]));
    qs = qe = 0;
    memset(cnt, 0, sizeof(cnt));
memset(val, 0, sizeof(val));
    memset(last, 0, sizeof(last));
  int idx(char c) {
  return c - 'a';
  int insert(string s, int v) {
    int now = 0;
    int n = s.size();
    for (int i = 0; i < n; ++i) {
      int c = idx(s[i]);
      if (!ch[now][c]) {
        memset(ch[sz], 0, sizeof(ch[sz]));
        val[sz] = 0, ch[now][c] = sz++;
      now = ch[now][c];
    val[now] = v;
    return now;
  }
  void print(int j) {
    if (j) {
      //now we match string v[j]
      print(last[j]); //may match multiple strings
  }
  void getFail() -
    qs = 0, qe = 0;
    fail[0] = 0;
    for (int c = 0; c < SIGMA; c++) {</pre>
      int now = ch[0][c];
      if (now) {
        fail[now] = 0;
         que[qe++] = now;
         last[now] = 0;
      }
    while (qs != qe) {
      int t = que[qs++];
for (int c = 0; c < SIGMA; c++) {
  int now = ch[t][c];</pre>
        if (!now) continue;
         que[qe++] = now;
         int v = fail[t];
        while (v && [c][v][c]) v = fail[v];
        fail[now] = ch[v][c]
        last[now] = val[fail[now]] ? fail[now] : last[fail[now
    }
  }
  void AC_evolution() {
    for (qs = 0; qs != qe;) {
      int now = que[qs++];
      for (int i = 0; i < SIGMA; i++) {
        if (ch[now][i] == 0) ch[now][i] = ch[fail[now]][i];
    }
  }
  void build() {
    getFail();
    AC_evolution();
  void Find(string s) {
    int n = s.size(), now = 0;
    for (int i = 0; i < n; i++) {
      int c = idx(s[i]);
      while (now && !ch[now][c]) now = fail[now];
      now = ch[now][c];
      cnt[now]++;
    for (int i = qe - 1; i >= 0; i--) {
```

```
now = (L + R) / 2;
      cnt[fail[que[i]]] += cnt[que[i]];
                                                                            if (s[sa[now]] == ss[0]) break;
 }
                                                                            else if (s[sa[now]] > ss[0]) R = now;
}
                                                                            else if (s[sa[now]] < ss[0]) L = now;
ac;
                                                                          if (s[sa[now]] != ss[0]) return 0;
const int N = 156;
                                                                          for (int i = 1; i < ss.size(); ++i) {</pre>
string s[N];
                                                                            int pre = now, ty = 0;
int ed[N];
                                                                            if (sa[now] + i >= s.size()) L = now, ty = 0;
                                                                            else if (s[sa[now] + i] == ss[i]) continue;
ac.init();
                                                                            else if (s[sa[now] + i] > ss[i]) R = now, ty = 1;
ac.insert(s[i], i); // insert small strings
                                                                            else if (s[sa[now] + i] < ss[i]) L = now, ty = 0;
ac.build();
ac.Find(large_string);
                                                                            while (R - L > 1) {
ac.cnt[ac.insert(s[i], i)]; // number of small string
                                                                               now = (L + R) / 2;
                                                                               if (sa[now] + i >= s.size()) {
                                                                                 if (ty == 0) R = now;
10.5 Suffix Array
                                                                                 if (ty == 1) L = now;
const int SA_SIZE = ;
                                                                               } else if (ty == 0 && Query(pre, now) < i) R = now;
const int logn = 1 + ;
                                                                               else if (ty == 1 && Query(now, pre) < i) L = now;</pre>
string s;
                                                                               else if (s[sa[now] + i] == ss[i]) break;
int sa[SA_SIZE], rk[SA_SIZE], lcp[SA_SIZE];
                                                                               else if (s[sa[now] + i] > ss[i]) R = now;
int tma[2][SA_SIZE], c[SA_SIZE], sp[SA_SIZE][logn];
                                                                              else if (s[sa[now] + i] < ss[i]) L = now;
int getsa() {
                                                                            if (sa[now] + i >= s.size()) return 0;
  -> update m = ? // how many char
                                                                            if (s[sa[now] + i] != ss[i]) return 0;
  int * x = tma[0], * y = tma[1], n = s.size(), m = 200;
for (int i = 0; i < m; ++i) c[i] = 0;</pre>
                                                                          L = now, R = now;
  for (int i = 0; i < n; ++i) c[x[i] = s[i]]++;
                                                                          for (int i = 19; i >= 0; --i) {
  for (int i = 1; i < m; ++i) c[i] += c[i - 1];
                                                                            if (R + (1 << i) >= s.size()) continue;
  for (int i = n - 1; i >= 0; --i) sa[--c[x[i]]] = i;
                                                                            else if (Query(L, R + (1 << i)) >= ss.size()) R += <math>(1 << i)
  for (int k = 1; k \le n; k \le 1) {
    for (int i = 0; i < m; ++i) c[i] = 0;
    for (int i = 0; i < n; ++i) c[x[i]]++
                                                                          for (int i = 19; i >= 0; --i) {
    for (int i = 1; i < m; ++i) c[i] += c[i - 1];
                                                                            if (L - (1 << i) < 0) continue;
                                                                            else if (Query(L - (1 \ll i), R) >= ss.size()) L -= (1 \ll i)
    int p = 0;
    for (int i = n - k; i < n; ++i) y[p++] = i;
    for (int i = 0; i < n; ++i)
                                                                          return R - L + 1;
      if (sa[i] >= k) y[p++] = sa[i] - k;
                                                                        }
/*
    for (int i = n - 1; i >= 0; --i) sa[--c[x[y[i]]]] = y[i];
    y[sa[0]] = p = 0;
                                                                        how to use :
    for (int i = 1; i < n; ++i) {
                                                                        1. cin >> s;
      if(x[sa[i]] == x[sa[i - 1]] &\& sa[i] + k < n &\& sa[i - 1]
                                                                        2. getsa(), getlcp(), getsp();
           1] + k < n &&
                                                                        string ss;
         x[sa[i] + k] == x[sa[i - 1] + k]);
                                                                        4. cin >> ss;
      else p++;
                                                                        5. cout << Find(ss) << endl;
*/</pre>
      y[sa[i]] = p;
    swap(x, y);
                                                                        10.6 Palindromic Tree
    if (p + 1 == n) break;
m = p + 1;
                                                                        //MAXN
                                                                        const int N = 26;
                                                                        struct Palindromic_Tree {
void getlcp() {
                                                                          int next[MAXN][N]; //trie tree edge
  int tmp = 0, n = s.size();
                                                                          int len[MAXN]; //tree edge depth*2 (-1)
  for (int i = 0; i < n; ++i) rk[sa[i]] = i;
for (int i = 0; i < n; ++i) {
                                                                          int fail[MAXN]; //fail link
int num[MAXN]; //fail link depth
    if (rk[i] == 0) lcp[0] = 0;
                                                                          int cnt[MAXN]; //# of this Palindrom
int S[MAXN]; //string
    else {
      if (tmp) tmp--;
                                                                          int p; //# of different Palindrom + 2
      int po = sa[rk[i] - 1];
                                                                          int n; //string len
      while (tmp + po < n \&\& tmp + i < n \&\& s[tmp + i] == s[tmp]
                                                                          int last;
             + po]) tmp++;
                                                                          int newnode(int 1) {
      lcp[rk[i]] = tmp;
                                                                            memset(next[p], 0, N * 4);
                                                                            cnt[p] = num[p] = 0;
  }
                                                                            len[p] = 1;
                                                                            return p++;
void getsp() {
                                                                          }
  int n = s.size();
                                                                          void init() {
  for (int i = 0; i < n; ++i) sp[rk[i]][0] = s.size() - i;
                                                                            p = n = 0;
last = 1;
  for (int i = 1; i < n; ++i) sp[i - 1][1] = lcp[i]; for (int i = 2; i < logn; ++i) {
                                                                            newnode(0)
    for (int j = 0; j < n; ++j) {
  if (j + (1 << (i - 2)) >= s.size()) continue;
                                                                            newnode(-1);
                                                                            S[n] = -1;
      sp[j][i] = min(sp[j][i - 1], sp[j + (1 << (i - 2))][i -
                                                                            fail[0] = 1;
           1]);
                                                                          int get_fail(int x) {
 }
                                                                            while (S[n - len[x] - 1] != S[n]) x = fail[x];
                                                                            return x;
int Query(int L, int R) {
  int tmp = (L == R) ? 0 : 32 - __builtin_clz(R - L);
if (tmp == 0) return sp[L][0];
                                                                          void add(int c) {
  else return min(sp[L][tmp], sp[R - (1 << (tmp - 1))][tmp]);</pre>
                                                                            S[++n] = c;
                                                                             int cur = get_fail(last);
int Find(string ss) {
                                                                            if (!next[cur][c]) {
  int L = 0, R = s.size(), now;
                                                                               int now = newnode(len[cur] + 2);
  while (R - L > 1) {
                                                                               fail[now] = next[get_fail(fail[cur])][c];
```

```
next[cur][c] = now;
num[now] = num[fail[now]] + 1;
}
last = next[cur][c];
cnt[last]++;
}
void count() {
for (int i = p - 1; i >= 0; --i) cnt[fail[i]] += cnt[i];
};
```

## 10.7 Lexicographically Smallest Rotation

```
string s;
const int N = 4000006;
int f[N];
void solve() {
  S = S + S
  int n = (int) s.size();
  for (int i = 0; i < n; ++i) f[i] = -1;
  int k = 0;
  for (int j = 1; j < n; ++j) {
     char sj = s[j];
    int i = f[j - k - 1];
while (i != -1 && sj != s[k + i + 1]) {
       if (sj < s[k + i + 1])
  k = j - i - 1;</pre>
       i = f[\tilde{i}];
    if (sj != s[k + i + 1]) {
       if (sj < s[k]) k = j;
f[j - k] = -1;
    else f[j - k] = i + 1;
  n >>= 1;
  if (k \ge n) k -= n;
  for (int i = k; i < k + n; ++i)
    cout << s[i];
  cout << endl;</pre>
```

# 11 Geometry

## 11.1 Circle

```
//Note that this code will crash if circle A and B are the same
typedef pair<double, double> pdd;
pdd rtcw(pdd p) { return pdd(p.Y, -p.X); }
vector<pdd> circlesintersect(pdd A, pdd B, double r1, double r2
    ) {
    vector<pdd> ret;
    double d = dis(A, B);
    if(d > r1 + r2 || d + min(r1, r2) < max(r1, r2))
        return ret;
    double x = (d * d + r1 * r1 - r2 * r2) / (2 * d);
    double y = sqrt(r1 * r1 - x * x);
    pdd v = (B - A) / d;
    ret.eb(A + v * x + rtcw(v) * y);
    if(y > 0)
        ret.eb(A + v * x - rtcw(v) * y);
    return ret;
}
```

## 11.2 Half Plane Intersection

```
Pt interPnt(Line 11, Line 12, bool & res) {
    Pt p1, p2, q1, q2;
    tie(p1, p2) = 11;
    tie(q1, q2) = 12;
    double f1 = (p2 - p1) \wedge (q1 - p1);
double f2 = (p2 - p1) \wedge (p1 - q2);
    double f = (f1 + f2);
    if (fabs(f) < eps) {</pre>
         res = 0;
         return {0, 0};
    return q1 * (f2 / f) + q2 * (f1 / f);
bool isin(Line 10, Line 11, Line 12) {
    // Check inter(l1, l2) in l0
    bool res;
    Pt p = interPnt(l1, l2, res);
    return ((l0.SE - l0.FI) ^ (p - l0.FI)) > eps;
/* If no solution, check: 1. ret.size() < 3</pre>
* Or more precisely, 2. interPnt(ret[0], ret[1])
```

```
in all the lines. (use (l.S - l.F) \land (p - l.F) \gt 0
 /* --^- Line.FI --^- Line.SE --^- */
vector<Line> halfPlaneInter(vector < Line > lines) {
     int sz = lines.size();
     vector < double > ata(sz), ord(sz);
     for (int i = 0; i < sz; i++) {
         ord[i] = i;
         Pt d = lines[i].SE - lines[i].FI;
         ata[i] = atan2(d.Y, d.X);
     sort(ord.begin(), ord.end(), [ & ](int i, int j) {
         if (fabs(ata[i] - ata[j]) < eps)
    return ((lines[i].SE - lines[i].FI) ^</pre>
                   (lines[j].SE - lines[i].FI)) < 0;
         return ata[i] < ata[j];</pre>
     });
     vector < Line > fin;
for (int i = 0; i < sz; i++)</pre>
         if (!i or fabs(ata[ord[i]] - ata[ord[i - 1]]) > eps)
              fin.PB(lines[ord[i]]);
     deque < Line > dq;
     for (int i = 0; i < (int)(fin.size()); i++) {
   while ((int)(dq.size()) >= 2 and not isin(fin[i], dq[(
               int)(dq.size()) - 2],
                  dq[(int)(dq.size()) - 1]))
              dq.pop_back();
         while ((int)(dq.size()) >= 2 and not isin(fin[i], dq
               [0], dq[1]))
              dq.pop_front()
          dq.push_back(fin[i]);
     while ((int)(dq.size()) >= 3 and not isin(dq[0], dq[(int)(
           dq.size()) - 2],
              dq[(int)(dq.size()) - 1]))
          dq.pop_back();
     while ((int)(dq.size()) >= 3 and not isin(dq[(int)(dq.size())) >= 3
          ()) - 1], dq[0], dq[1]))
         dq.pop_front();
     vector < Line > res(dq.begin(), dq.end());
     return res;
}
```

### 11.3 Convex Hull 3D

```
#define SIZE(X) (int(X.size()))
#define PI 3.14159265358979323846264338327950288
struct Pt{
  Pt cross(const Pt &p) const
  { return Pt(y * p.z - z * p.y, z * p.x - x * p.z, x * p.y - y
        * p.x); }
} info[N];
int mark[N][N],n, cnt;;
double mix(const Pt &a, const Pt &b, const Pt &c)
{ return a * (b ^ c); }
double area(int a, int b, int c)
{ return norm((info[b] - info[a]) ^ (info[c] - info[a])); }
double volume(int a, int b, int c, int d)
{ return mix(info[b] - info[a], info[c] - info[a], info[d] -
     info[a]); }
struct Face{
  int a, b, c; Face(){}
  Face(int a, int b, int c): a(a), b(b), c(c) {}
  int &operator [](int k)
  { if (k == 0) return a; if (k == 1) return b; return c; }
}:
vector<Face> face;
void insert(int a, int b, int c)
{ face.push_back(Face(a, b, c)); }
void add(int v)
  vector <Face> tmp; int a, b, c; cnt++;
for (int i = 0; i < SIZE(face); i++) {</pre>
    a = face[i][0]; b = face[i][1]; c = face[i][2];
    if(Sign(volume(v, a, b, c)) < 0)
      mark[a][b] = mark[b][a] = mark[b][c] = mark[c][b] = mark[
            c][a] = mark[a][c] = cnt;
    else tmp.push_back(face[i]);
  } face = tmp;
  for (int i = 0; i < SIZE(tmp); i++) {</pre>
    a = face[i][0]; b = face[i][1]; c = face[i][2];
    if (mark[a][b] == cnt) insert(b, a, v);
    if (mark[b][c] == cnt) insert(c, b, v);
    if (mark[c][a] == cnt) insert(a, c, v);
  }}
int Find(){
 for (int i = 2; i < n; i++) {
```

```
Pt ndir = (info[0] - info[i]) \wedge (info[1] - info[i]);
           if (ndir == Pt()) continue; swap(info[i], info[2]);
           for (int j = i + 1; j < n; j++) if (Sign(volume(0, 1, 2, j)
                       ) != 0) {
                swap(info[j], info[3]); insert(0, 1, 2); insert(0, 2, 1);
                               return 1;
          } } return 0; }
int main() {
     for (; scanf("%d", &n) == 1; ) {
           for (int i = 0; i < n; i++) info[i].Input();</pre>
           sort(info, info + n); n = unique(info, info + n) - info;
          face.clear(); random_shuffle(info, info + n);
if (Find()) { memset(mark, 0, sizeof(mark)); cnt = 0;
    for (int i = 3; i < n; i++) add(i); vector<Pt> Ndir;
    for (int i = 0; i < SIZE(face); ++i) {</pre>
                     Pt p = (info[face[i][0]] - info[face[i][1]]) ^
               (info[face[i][2]] - info[face[i][1]]);
p = p / norm( p ); Ndir.push_back(p);
} sort(Ndir.begin(), Ndir.end());
                int ans = unique(Ndir.begin(), Ndir.end()) - Ndir.begin()
                printf("%d\n", ans);
          } else printf("1\n");
    } }
double calcDist(const Pt &p, int a, int b, int c)
{ return fabs(mix(info[a] - p, info[b] - p, info[c] - p) / area
            (a, b, c)); }
//compute the minimal distance of center of any faces
double findDist() { //compute center of mass
     double totalWeight = 0; Pt center(.0, .0, .0);
     Pt first = info[face[0][0]];
     for (int i = 0; i < SIZE(face); ++i) {
          Pt p = (info[face[i][0]]+info[face[i][1]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][2]]+info[face[i][
                       first)*.25;
          double weight = mix(info[face[i][0]] - first, info[face[i
                       ][1]]
                      - first, info[face[i][2]] - first);
           totalWeight += weight; center = center + p * weight;
     } center = center / totalWeight;
     double res = 1e100; //compute distance
for (int i = 0; i < SIZE(face); ++i)</pre>
          res = min(res, calcDist(center, face[i][0], face[i][1],
                        face[i][2]));
     return res; }
```

## 11.4 Dynamic convexhull

```
* Given a convexhull, answer querys in O(\lg N)
   CH should not contain identical points, the area should
   be > 0, min pair(x, y) should be listed first */
double det( const Pt% p1 , const Pt% p2 )
{ return p1.X * p2.Y - p1.Y * p2.X; }
struct Conv{
  int n;
vector<Pt> a;
  vector<Pt> upper, lower;
  Conv(vector < Pt > \_a) : a(\_a){}
    n = a.size();
     int ptr = 0;
    for(int i=1; i<n; ++i) if (a[ptr] < a[i]) ptr = i;</pre>
    for(int i=0; i<=ptr; ++i) lower.push_back(a[i]);
for(int i=ptr; i<n; ++i) upper.push_back(a[i]);</pre>
    upper.push_back(a[0]);
  int sign( LL \times ){ // fixed when changed to double
  return x < 0 ? -1 : x > 0; }
pair<LL,int> get_tang(vector<Pt> &conv, Pt vec){
     int l = 0, r = (int)conv.size() - 2;
     for(; l + 1 < r; ){
       int mid = (l + r) / 2;
       if(sign(det(conv[mid+1]-conv[mid],vec))>0)r=mid;
       else l = mid;
    return max(make_pair(det(vec, conv[r]), r),
         make_pair(det(vec, conv[0]), 0));
  void upd_tang(const Pt &p, int id, int &i0, int &i1){
    if(det(a[i0] - p, a[id] - p) > 0) i0 = id;
if(det(a[i1] - p, a[id] - p) < 0) i1 = id;</pre>
  void bi_search(int l, int r, Pt p, int &i0, int &i1){
    if(l == r) return;
    upd_tang(p, 1 % n, i0, i1);
     int sl=sign(det(a[l % n] - p, a[(l + 1) % n] - p));
     for(; l + 1 < r; ) {
       int mid = (l + r) / 2;
       int smid=sign(det(a[mid%n]-p, a[(mid+1)%n]-p));
```

```
if (smid == sl) l = mid:
       else r = mid;
     upd_tang(p, r % n, i0, i1);
  int bi_search(Pt u, Pt v, int l, int r) {
  int sl = sign(det(v - u, a[l % n] - u));
     for(; l + 1 < r; ) {
       int mid = (1 + r) / 2;
       int smid = sign(det(v - u, a[mid % n] - u));
       if (smid == sl) l = mid;
       else r = mid;
     return 1 % n;
  }
   // 1. whether a given point is inside the CH
   bool contain(Pt p) {
     if (p.X < lower[0].X || p.X > lower.back().X) return 0;
int id = lower_bound(lower.begin(), lower.end(), Pt(p.X, -
          INF)) - lower.begin();
     if (lower[id].X == p.X) {
       if (lower[id].Y > p.Y) return 0;
     }else if(det(lower[id-1]-p,lower[id]-p)<0)return 0;</pre>
     id = lower_bound(upper.begin(), upper.end(), Pt(p.X, INF),
          greater<Pt>()) - upper.begin();
     if (upper[id].X == p.X) {
       if (upper[id].Y < p.Y) return 0;</pre>
     }else if(det(upper[id-1]-p,upper[id]-p)<0)return 0;</pre>
     return 1:
   ^{\prime\prime} 2. Find 2 tang pts on CH of a given outside point
   // return true with i0, i1 as index of tangent points
   // return false if inside CH
   bool get_tang(Pt p, int &i0, int &i1) {
     if (contain(p)) return false;
     i0 = i1 = 0;
     int id = lower_bound(lower.begin(), lower.end(), p) - lower
          .begin();
     bi_search(0, id, p, i0, i1);
bi_search(id, (int)lower.size(), p, i0, i1);
     id = lower_bound(upper.begin(), upper.end(), p, greater<Pt</pre>
          >()) - upper.begin();
     bi_search((int)lower.size() - 1, (int)lower.size() - 1 + id
          , p, i0, i1);
     return true;
   \ensuremath{//} 3. Find tangent points of a given vector
   // ret the idx of vertex has max cross value with vec
   int get_tang(Pt vec){
     pair<LL, int> ret = get_tang(upper, vec);
     ret.second = (ret.second+(int)lower.size()-1)%n;
     ret = max(ret, get_tang(lower, vec));
     return ret.second;
   // 4. Find intersection point of a given line
   // return 1 and intersection is on edge (i, next(i))
   // return 0 if no strictly intersection
   bool get_intersection(Pt u, Pt v, int &i0, int &i1){
     int p0 = get_tang(u - v), p1 = get_tang(v - u);
     if(sign(det(v-u,a[p0]-u))*sign(det(v-u,a[p1]-u))<0){
       if (p0 > p1) swap(p0, p1);
       i0 = bi_search(u, v, p0, p1);
       i1 = bi_search(u, v, p1, p0 + n);
       return 1;
     return 0;
};
11.5 Polar Angle Sort
#define is_neg(_k) (_k.Y < 0 || (_k.Y == 0 && _k.X < 0) )
bool cmp(pll a,pll b){
   int A = is_neg(a), B = is_neg(b);
   return (A == B ? (a \land b) > 0 : A < B);
}
 11.6 Circle and Polygon intersection
struct Circle_and_Segment_Intersection {
  const ld eps = 1e-9;
   vector<pdd> solve(pdd p1, pdd p2, pdd cen, ld r) {
```

//please notice that p1 != p2

vector<pdd> ret;

//condiser p = p2 + (p1 - p2) \* t, 0 <= t <= 1

```
p1 = p1 - cen; p2 = p2 - cen;
    ld a = (p1 - p2) * (p1 - p2);
ld b = 2 * (p2 * (p1 - p2));
ld c = p2 * p2 - r * r;
ld bb4ac = b * b - 4 * a * c;
    if (bb4ac < -eps) return ret; //no intersection</pre>
    vector<ld> ts;
    if ((bb4ac) <= eps) {</pre>
       ts.push_back(-b / 2 / a);
    else {
       ts.push_back( (-b + sqrt(bb4ac)) / (a * 2) );
ts.push_back( (-b - sqrt(bb4ac)) / (a * 2) );
    sort(ts.begin(), ts.end());
    for (ld t: ts) {
       if (-eps <= t && t <= 1 + eps) {</pre>
         t = max(t, 0.0);
         t = min(t, 1.0);
         pdd pt = p2 + t * (p1 - p2);
         pt = pt + cen;
         ret.push_back(pt);
    return ret;
  }
} solver;
double f(ld a, ld b) {
  ld ret = b - a;
  while (ret <= -pi - eps) ret += 2 * pi;
  while (ret >= pi + eps) ret -= 2 * pi;
  return ret;
ld solve_small(pdd cen, ld r, pdd p1, pdd p2) {
  p1 = p1 - cen, p2 = p2 - cen;
  cen = \{0, 0\};
  vector<pdd> inter = solver.solve(p1, p2, cen, r);
ld ret = 0.0;
  if ((int)inter.size() == 0) {
    if (in_cir(cen, r, p1)) {
       ret = (p1 ^ p2) / 2;
    else {
       ret = (r * r * f(atan2(p1.Y, p1.X), atan2(p2.Y, p2.X))) / 2;
    }
  }
  else if ( (int)inter.size() == 1) {
    if (!in_cir(cen, r, p1) && !in_cir(cen, r, p2)) {
       //outside cut
       ret = (r * r * f(atan2(p1.Y, p1.X), atan2(p2.Y, p2.X))) /
     else if (!in_cir(cen, r, p1)) {
       pdd _p1 = inter[0];
       ret += ((_p1 ^ p2) / 2);
ret += (r * r * f(atan2(p1.Y, p1.X), atan2(_p1.Y, _p1.X)
            )) / 2;
    else if (!in_cir(cen, r, p2)) {
       pdd _p2 = inter[0];
       ret += ((p1 ^ _p2) / 2);
ret += (r * r * f(atan2(_p2.Y, _p2.X), atan2(p2.Y, p2.X)
            )) / 2;
    }
  else if ( (int)inter.size() == 2) {
    pdd _p2 = inter[0], _p1 = inter[1];
    ret += ((_p1 ^ _p2) / 2);
ret += (r * r * f(atan2(_p2.Y, _p2.X), atan2(p2.Y, p2.X)))
/ 2;
    ret += (r * r * f(atan2(p1.Y, p1.X), atan2(_p1.Y, _p1.X)))
/ 2;
  return ret;
}
ld solve(pdd cen, ld r, vector<pdd> pts) {
  for (int i = 0; i < (int)pts.size(); ++i) {</pre>
    ret += solve_small(cen, r, pts[i], pts[(i + 1) % int(pts.
          size())]);
  ret = max(ret, -ret);
  return ret;
```

## 11.7 Segment Intersection

```
int intersect(PII a , PII b , PII c , PII d){
  if(max(a.F , b.F) < min(c.F , d.F)) return 0;
  if(max(c.F , d.F) < min(a.F , b.F)) return 0;
  if(max(a.S , b.S) < min(c.S , d.S)) return 0;
  if(max(c.S , d.S) < min(a.S , b.S)) return 0;
  if(cross(b - a , c - a) * cross(b - a , d - a) == 1) return 0;
  if(cross(d - c , a - c) * cross(d - c , b - c) == 1) return 0;
  return 1;
}</pre>
```

## 11.8 Line Intersection Point

```
| pdd intersect(pdd p1, pdd p2, pdd q1, pdd q2) {
| //make sure that p1p2 is not parallel to q1q2
| return p1 + ((q1 - p1) ^ (q2 - q1)) / ((p2 - p1) ^ (q2 - q1))
| * (p2 - p1);
| }
```

## 11.9 Rotating Calipers

```
#define NXT(x)((x + 1) % m)
int main() {
  vector < pii > v; // v is the input points
  sort(v.begin(), v.end());
  vector < pii > up, down;
  for (pii p: v) {
    while (SZ(down) >= 2 \&\& sgn((p - down[SZ(down) - 2]) \land (p -
          down.back())) >= 0) {
      down.pop_back();
    down.push_back(p);
  reverse(v.begin(), v.end());
  for (pii p: v) {
    while (SZ(up) \ge 2 \& sgn((p - up[SZ(up) - 2]) \land (p - up.
         back())) >= 0) {
      up.pop_back();
    up.push_back(p);
  vector < pii > all;
  for (pii p: down) all.push_back(p);
  all.pop back():
  for (pii p: up) all.push_back(p);
  all.pop_back();
  int m = all.size();
  int ptr = (int) down.size() - 1;
  for (int i = 0; i < m; ++i) {
    while (((all[NXT(ptr)] - all[ptr]) ^ (all[NXT(i)] - all[i])
         ) > 0) {
      ptr = NXT(ptr);
```

## 12 Ad hoc

## 12.1 Joseph Problem

```
// O(m + log N)
// n people, k-th dead. Find out the last alive person
int main() {
  long long n, k, i, x = 0, y;
  scanf("%I64d%I64d", &n, &k);
  for(i = 2; i <= k && i <= n; ++i) x = (x + k) % i;
  for(; i <= n; ++i) {
     y = (i - x - 1) / k;
     if(i + y > n) y = n - i;
     i += y;
     x = (x + (y + 1) % i * k) % i;
  }
  printf("%I64d\n", x + 1);
  return 0;
}
```

## 12.2 Segment Max Segment Sum

```
|int n, m, x[MAX];
|class N{
|public: int tag, sml, sum, none;
|} b[MAX * 4];
|void Pull(int now, int l, int r) {
```

DFS(id - 2);

```
id = v.size() - dis;
  if(l == r) {
    if(b[now].tag) {
                                                                          }
      b[now].sum = b[now].tag;
                                                                        }
      b[now].none = 0;
                                                                        int32_t main() {
      b[now].sml = b[now].tag;
                                                                          IOS;
                                                                           cin >> n;
                                                                           for (int i = 0; i < n; ++ i) cin >> x[i];
    else{
                                                                           for (int i = 0; i < n; ++ i) {
      b[now].sum = 0;
                                                                             v.emplace_back(x[i]);
      b[now].none = 1
      b[now].sml = INF;
                                                                             while(v.size() >= 3 && v[v.size() - 3] <= v[v.size() - 1])</pre>
                                                                               DFS(v.size() - 3);
    }
  }
                                                                          while(v.size() > 1) DFS(v.size() - 2);
cout << ans << endl;</pre>
  else {
    b[now].sml = min(b[ls].sml, b[rs].sml);
                                                                           return 0;
    if(b[now].tag) b[now].sml = min(b[now].sml, b[now].tag);
                                                                       13
    b[now].sum = b[ls].sum + b[rs].sum;
                                                                        12.4 Manhattan Spanning Tree
    b[now].none = b[ls].none + b[rs].none;
    if(b[now].tag) b[now].sum += b[now].tag * b[now].none, b[
                                                                        #define edge pair<int, PII>
         now].none = 0;
                                                                        int n, sol[maxn];
 }
                                                                        PII x[maxn];
}
                                                                        vector<edge> v;
void take_tag(int now, int l, int r, int val) {
  if(b[now].tag && b[now].tag < val) b[now].tag = 0;</pre>
                                                                        class djs{
                                                                        public:
  if(l != r && b[ls].sml < val) take_tag(ls, l, mid, val);</pre>
                                                                           int x[maxn];
  if(l != r && b[rs].sml < val) take_tag(rs, mid + 1, r, val);</pre>
                                                                           void init(){ for (int i = 0; i < maxn; ++ i) x[i] = i; }
  Pull(now, 1, r);
                                                                           int Find(int now){ return x[now] == now ? now : x[now] = Find
                                                                                (x[now]); }
void Build(int now, int l, int r) {
                                                                           void Union(int a, int b){ x[Find(a)] = Find(b); }
  b[now].none = 0;
                                                                           int operator[](int now){ return Find(now); }
  if(l == r) b[now].tag = b[now].sml = b[now].sum = x[l];
                                                                        } ds;
                                                                        PII bit[maxn];
    Build(ls, l, mid), Build(rs, mid + 1, r);
                                                                        void update(int from, int val, int id){
  for(int i = from; i < maxn; i += i & -i)</pre>
    Pull(now, 1, r);
                                                                             bit[i] = maxn(bit[i], mp(val, id));
void update(int now, int l, int r, int ql, int qr, int val) {
                                                                        int query(int from){
  if(b[now].tag >= val) return ;
                                                                          PII res = bit[from];
  if(ql \ll l \& r \ll qr) {
                                                                           for(int i = from; i > 0; i -= i \& -i)
    take_tag(now, l, r, val);
                                                                             res = maxn(res, bit[i]);
    b[now].tag = val;
                                                                           return res.B;
    Pull(now, l, r);
                                                                        int cmp(int a, int b){
  else{
                                                                          return x[a] < x[b];
    if(qr <= mid) update(ls, l, mid, ql, qr, val);</pre>
    else if(mid + 1 <= ql) update(rs, mid + 1, r, ql, qr, val);</pre>
                                                                        int DIS(int q, int w){
    else update(ls, l, mid, ql, qr, val), update(rs, mid + 1, r
                                                                          return abs(x[q].A - x[w].A) + abs(x[q].B - x[w].B);
           ql, qr, val);
    Pull(now, l, r);
                                                                        void BuildEdge(){
  }
                                                                           vector<int> uni;
                                                                           for (int i = 0; i < maxn; ++ i)</pre>
PII query(int now, int l, int r, int ql, int qr) {
                                                                             bit[i] = mp(-INF, -1);
  if(ql <= l && r <= qr) return mp(b[now].sum, b[now].none);</pre>
                                                                           for (int i = 0; i < n; ++ i) sol[i] = i;
for (int i = 0; i < n; ++ i) uni.pb(x[i].B - x[i].A);</pre>
    PII ans = mp(0, 0);
                                                                           sort(ALL(uni)):
    if(qr <= mid) ans = query(ls, l, mid, ql, qr);</pre>
                                                                           uni.resize(unique(ALL(uni)) - uni.begin());
    else if(mid + 1 \leftarrow ql) ans = query(rs, mid + 1, r, ql, qr);
                                                                           sort(sol, sol + n, cmp);
    else {
                                                                           for (int i = 0; i < n; ++ i){
      PII a = query(ls, l, mid, ql, qr);
                                                                             int now = sol[i];
      PII b = query(rs, mid + 1, r, ql, qr);
                                                                             int tmp = x[sol[i]].B - x[sol[i]].A;
      ans = mp(a.A + b.A, a.B + b.B);
                                                                             int po = lower_bound(ALL(uni), tmp) - uni.begin() + 1;
                                                                             int id = query(po);
    if(b[now].tag != 0) ans.A += ans.B * b[now].tag, ans.B = 0;
                                                                             if(id >= 0) v.pb(mp(DIS(id, now), mp(id, now)));
    return ans;
                                                                             update(po, x[now].A + x[now].B, now);
  }
REP(i, 1, n + 1) cin >> x[i];
Build(1, 1, n);
update(1, 1, n, l, r, v);
                                                                        void Build(){
                                                                          BuildEdge();
                                                                           for (int i = 0; i < n; ++ i) swap(x[i].A, x[i].B);
cout << query(1, 1, n, l, r).A << endl;</pre>
                                                                           BuildEdge();
                                                                           for (int i = 0; i < n; ++ i) x[i].A *= -1;
12.3 Stone Merge
                                                                          BuildEdge();
int n, x[MAX], ans = 0;
                                                                           for (int i = 0; i < n; ++ i) swap(x[i].A, x[i].B);
                                                                           BuildEdge();
vector<int> v;
int DFS(int now) {
                                                                        int solveKruskal(){
  int val = v[now] + v[now + 1];
  ans += val;
                                                                           ds.init();
                                                                           sort(ALL(v));
  v.erase(v.begin() + now);
  v.erase(v.begin() + now);
                                                                           int res = 0;
                                                                           for (int i = 0; i < v.size(); ++ i) {
  int dis = v[i].A;</pre>
  int id = 0;
  for (int i = now - 1; i >= 0; -- i)
    if(v[i] >= val) { id = i + 1; break; }
                                                                             PII tmp = v[i].B;
  v.insert(v.begin() + id, val);
                                                                             if(ds[tmp.A] != ds[tmp.B]){
  while(id \Rightarrow 2 && v[id - 2] \Leftarrow v[id]) {
                                                                               ds.Union(tmp.A, tmp.B);
    int dis = v.size() - id;
                                                                               res += dis;
```

```
    return res;
    |}
    int32_t main(){
        IOS;
        cin >> n;
        for (int i = 0; i < n; ++ i) cin >> x[i].A >> x[i].B;
        Build();
        int ans = solveKruskal();
        cout << ans << endl;
        return 0;
}</pre>
```

#### 12.5 K Cover Tree

```
int n, k, dp[MAX], ans;
vector<int> v[MAX];
void DFS(int now, int fa) {
  if(v[now].size() == 1 && v[now][0] == fa)
    return dp[now] = -1, void();
  int sml = INF, big = -INF;
  for(auto to : v[now]) if(to != fa) {
    DFS(to, now);
    sml = min(sml, dp[to]);
    big = max(big, dp[to]);
  if(sml == -k) dp[now] = k, ans ++;
  else if(big - 1 >= abs(sml)) dp[now] = big - 1;
else dp[now] = sml - 1;
int32_t main() {
  IOS;
  cin >> n >> k;
  REP(i, 2, n + 1) {
    int a, b; cin >> a >> b;
    v[a].pb(b); v[b].pb(a);
  if(k == 0) cout << n << endl;
    DFS(0, 0), ans += dp[0] < 0;
    cout << ans << endl;
  return 0;
```

## 12.6 M Segments' Maximum Sum

```
-----Greedy-
int n, m, fr[MAX], ba[MAX];
int v[MAX], idx = 1;
set<PII> cc;
void erase(int id) {
 if(id == 0) return;
  int f = fr[id], b = ba[id];
  ba[fr[id]] = b, fr[ba[id]] = f;
 cc.erase(mp(abs(v[id]), id));
int32_t main() {
  cin >> n >> m;
  int sum = 0, pos = 0, ans = 0;
  for (int i = 0; i < n; ++ i) {
    int tmp; cin >> tmp;
    if(tmp == 0) continue:
    if((tmp >= 0 \&\& sum >= 0) || (tmp <= 0 \&\& sum <= 0)) {}
      sum += tmp;
      if(sum > 0) ans += sum, pos ++;
      v[idx ++] = sum, sum = tmp;
  if(sum) v[idx ++] = sum;
  if(sum > 0) ans += sum, pos ++;
  REP(i, 0, idx) {
    fr[i + 1] = i;
    ba[i] = i + 1;
    if(i) cc.insert(mp(abs(v[i]), i));
  ba[idx - 1] = 0;
  while(pos > m) {
    auto tmp = cc.begin();
    int val = (*tmp).A, id = (*tmp).B;
    cc.erase(tmp);
    if(v[id] < 0 \&\& (fr[id] == 0 || ba[id] == 0)) continue;
    if(v[id] == 0) continue;
ans -= val, pos --;
    v[id] = v[fr[id]] + v[id] + v[ba[id]];
    cc.insert(mp(abs(v[id]), id));
```

```
erase(fr[id]), erase(ba[id]);
        cout << ans << endl;
       return 0;
}
                              -----Aliens-----
int n, k, x[MAX];
PII dp[MAX], rd[MAX]; // max value, times, can be buy, times
int judge(int now) {
        dp[1] = mp(0, 0), rd[1] = mp(-x[1], 0);
        REP(i, 2, n + 1) {
               dp[i] = max(dp[i - 1], mp(rd[i - 1].A + x[i] - now, rd[i - 1].A + x[i] - now, rd[i] - now, rd[i - 1].A + x[i] - now, rd[i - 1].A + x[i] - now, rd[i - 1].A + x[i] - now, rd[i] - now, rd[
               rd[i] = max(rd[i - 1], mp(dp[i - 1].A - x[i])
                                                                                                                                                                                     , dp[i -
                               1].B));
       }
        return dp[n].B;
int32_t main() {
        IOS;
        cin >> n >> k;
        n ++;
        for (int i = 2; i <= n + 1; ++ i)
              cin >> x[i];
        for (int i = 1; i <= n; ++ i)
               x[i] += x[i - 1];
         if(judge(0) <= k) cout << dp[n].A << endl;</pre>
        else {
              int l = 0, r = 10000000000000L;
while(r - l > 1) {
                      int mid = l + ((r - l) \gg 1), res = judge(mid);
                      if(res == k) return cout << dp[n].A + dp[n].B * mid <<</pre>
                                    endl, 0;
                      else if(res < k) r = mid;</pre>
                     else if(res > k) l = mid;
               judge(l);
              cout \ll dp[n].A + k * l \ll endl;
        return 0;
}
```

## 12.7 Minimum Enclosing Cycle

```
#define pdd pair<double, double>
#define F first
#define S second
pdd a[maxn];
mt19937 rng(chrono::steady_clock::now().time_since_epoch().
      count());
double dis(pdd p1, pdd p2) {
  return hypot(p1.F - p2.F, p1.S - p2.S);
inline double sq(double x) {
  return x * x;
pdd external(pdd p1, pdd p2, pdd p3) {
  double a1 = p1.F - p2.F, a2 = p1.F - p3.F;
  double b1 = p1.S - p2.S, b2 = p1.S - p3.S;
  double c2 = (sq(p1.F) - sq(p3.F))
  + sq(p1.S) - sq(p3.S)) / 2;

double dd = a1 * b2 - a2 * b1;

return make_pair((c1 * b2 - c2 * b1) / dd

, (a1 * c2 - a2 * c1) / dd);
}
int main() {
  cin >> n;
  for (int i = 0; i < n; ++ i)
     cin >> a[i].F >> a[i].S;
  shuffle(a, a + n, rng);
  pdd center = a[0];
  double r = 0;
  for (int i = 0; i < n; ++ i) {
     if (dis(center, a[i]) <= r) continue;</pre>
     center = a[i], r = 0;
     for (int j = 0; j < i; ++ j) {
       if (dis(center, a[j]) <= r) continue;</pre>
       center.F = (a[i].F + a[j].F) / 2;
center.S = (a[i].S + a[j].S) / 2;
       r = dis(center, a[i]);
```

```
for (int k = 0; k < j; ++ k) {
    if (dis(center, a[k]) <= r) continue;
    center = external(a[i], a[j], a[k]);
    r = dis(center, a[i]);
    }
}

cout << fixed << setprecision(10) << r << endl;
cout << center.F << " " << center.S << "\n";
return 0;
}</pre>
```

## 12.8 Rotating Sweep Line

```
PII p[maxn];
int n, idx[maxn], pos[maxn];
vector<PII> v;
inline PII operator + (PII x, PII y) {
  return make_pair(x.F + y.F, x.S + y.S); }
inline PII operator - (PII x, PII y) {
return make_pair(x.F - y.F, x.S - y.S); }
inline long long cross(PII x, PII y) {
  return 111 * x.F * y.S - 111 * x.S * y.F; }
inline int cmp(PII x, PII y) {
 x = p[x.S] - p[x.F];

y = p[y.S] - p[y.F];
  return cross(x, y) > 0;
int32_t main() {
  cin.tie(0), cout.sync_with_stdio(0);
  cin >> n >> wnt, wnt += wnt;
for (int i = 1; i <= n; ++ i)
  cin >> p[i].F >> p[i].S;
  sort(p + 1, p + 1 + n);
  for (int i = 1; i <= n; ++ i)
     idx[i] = i, pos[i] = i;
  for (int i = 1; i \le n; ++ i)
     for (int j = i + 1; j \le n; ++ j)
       v.emplace_back(i, j);
  sort(v.begin(), v.end(), cmp);
  for(auto line : v) {
     int fr = pos[line.F], ba = pos[line.S], now;
     if(fr > ba) swap(fr, ba);
     // [TODO] points:
     // p[idx[
                    1]] more farther
     // p[idx[
                    2]] farther
                  fr]] ... p[idx[ba]]
     // p[idx[
     // p[idx[n - 1]] farther
     // p[idx[n - 0]] more farther
     swap(idx[fr], idx[ba]);
     swap(pos[line.F], pos[line.S]);
  }
     return 0;
```

## 12.9 Hilbert Curve