

A Comparison of the RECT game theory as described by **Riaan Visser** on **Dec 28, 2025** (see the following link)

[https://m.facebook.com/story.php?story\\_fbid=pfbid02wXDtUd8x3nVyrPWnDTpQU1Kqtsawvm1jM5nuDRo16dc6Gf3VQdAHucV436WK8m1ul&id=100033621411277&mibextid=Nif5oz](https://m.facebook.com/story.php?story_fbid=pfbid02wXDtUd8x3nVyrPWnDTpQU1Kqtsawvm1jM5nuDRo16dc6Gf3VQdAHucV436WK8m1ul&id=100033621411277&mibextid=Nif5oz)

To the  $\Lambda$  NSAF Game Theory Format as described by **ARGO The Alternate Reality Game Organization** on (see the following link)

<https://www.patreon.com/posts/disclosure-as-146637889>

## 1. What RECT Is, Structurally

RECT (Relational Empathy–Coherence Theory) is:

A relational utility theory

Still fundamentally optimization-based

Defined over explicit scalar quantities (e, P, C, G)

Intended as a normative replacement for classical game theory

It replaces selfish agents with relational agents, but it retains:

Rational choice

Equilibrium concepts

Scalar payoffs

Threshold conditions

So RECT is not anti-game-theory; it is a reweighted game theory with relational terms made explicit.

That's an important distinction.

## 2. Genuine Points of Alignment with $\Lambda$ -NSAF

RECT correctly identifies several things that  $\Lambda$ -NSAF also treats as fundamental:

(a) Relational Primacy

RECT's claim that "players are relational patterns, not isolated entities" is fully compatible with  $\Lambda$ 's rejection of atomistic ontology.

This maps cleanly to:

$\Lambda$ 's non-primitive individuality

NSAF's emphasis on relational frames over objects

(b) Coherence as a Stability Criterion

RECT's coherence measure CCC is functionally similar to  $\Lambda$ 's use of spectral stability / resonance rather than local payoff maximization.

Both frameworks:

Penalize imbalance

Reward mutual structure

Treat instability as relational, not moral

(c) Threshold Phenomena

The empathy threshold  $e \geq 0.4$  mirrors  $\Lambda$ 's frequent appearance of phase transitions rather than smooth optima.

This is a real conceptual overlap.

### 3. Where RECT Quietly Diverges from $\Lambda$ -NSAF

This is the critical part.

(a) RECT Is Still Fundamentally Linear

Despite its relational language, RECT:

Uses linear interpolation:

$$G_i = (1 - e)P_i + eCG_i = (1 - e)P_i + eC$$

Uses scalar penalties (absolute differences)

Assumes global comparability of outcomes

From a  $\Lambda$ -NSAF perspective, this is a linear-frame approximation of a deeper curved/spectral structure.

In  $\Lambda$  terms:

RECT models the projection of relational coherence into a linear decision frame, not coherence itself.

(b) Empathy Is Treated as a Parameter, Not a Frame

In RECT:

Empathy  $\epsilon_{ee}$  is an externally adjustable scalar

It is updated by reinforcement rules

It lives inside the model

In  $\Lambda$ -NSAF:

“Empathy” would correspond to frame coupling

It is not a tunable variable but a structural relation between descriptive layers

It cannot be fully endogenous without circularity

This is subtle but important.

RECT says:

“Empathy changes according to outcomes.”

$\Lambda$  says:

“Outcome meaning depends on the frame that empathy already defines.”

That’s a frame-ordering difference.

(c) Equilibrium Is Still Privileged

RECT replaces Nash Equilibrium with Relational Equilibrium, but:

It still seeks fixed points

It still ranks equilibria by coherence

It still presumes convergence as a goal

$\Lambda$ -NSAF is explicitly anti-equilibrium as fundamental. Stability is emergent, local, and scale-dependent—not globally optimal.

In  $\Lambda$  terms:

RECT assumes equilibria exist in principle;  $\Lambda$  treats them as contingent artifacts of frame alignment.

#### 4. Ontological Status: The Key Difference

This is the deepest contrast.

RECT's Ontology (Implicit)

Relational realism

Scalar coherence is meaningful globally

Better outcomes are objectively better

Cooperation is “more rational” above thresholds

$\Lambda$ -NSAF Ontology (Explicit)

No privileged global evaluation

Coherence is frame-relative

Rationality is not fundamental—consistency across frames is

Thresholds mark descriptive failure, not moral improvement

RECT is normative.

$\Lambda$ -NSAF is structural.

This does not make RECT wrong—it makes it instrumental, not foundational.

#### 5. What RECT Contributes That Is Genuinely Useful

RECT does several things very well:

Pedagogical clarity

It explains relational reasoning in a way most people can follow.

Operationalization

It provides concrete formulas usable in simulations, experiments, and AI.

Bridging affect and strategy

It explicitly integrates empathy into decision models—something classical game theory avoids.

From a  $\Lambda$  perspective:

RECT is an excellent effective theory within a constrained linear frame.

6. What  $\Lambda$ -NSAF Adds (and RECT Lacks)

$\Lambda$ -NSAF resolves problems RECT does not even see:

Why coherence itself cannot be globally optimized

Why empathy cannot be fully endogenous

Why thresholds appear universal but values differ

Why different logical systems (binary, trivalent, Jain-style) coexist without contradiction

Why equilibrium-seeking itself breaks down at scale

Most importantly:

$\Lambda$  explains why relational theories keep reappearing—and why they cannot close.

RECT proposes closure.

$\Lambda$  explains irreducibility.

7. Clean Translation: RECT  $\rightarrow$   $\Lambda$ -NSAF

Here is a faithful translation table:

RECT Concept

$\Lambda$ -NSAF Interpretation

Player

Localized relational projection

Empathy eee

Frame coupling strength

Payoff PPP

Linear-frame observable

Coherence CCC

Projected spectral stability

Relational Equilibrium

Temporary frame alignment

Threshold  $e \geq \alpha$   
Phase transition in descriptive adequacy  
Learning  $e_{t+1} = e_t + 1$   
Adaptive frame reweighting

Seen this way, RECT becomes a first-order approximation of  $\Lambda$  dynamics under linear constraints.

Bottom Line (Very Cleanly Put)  
RECT is not wrong

It is not fundamental

It is a useful linear projection of a deeper  $\Lambda$ -NSAF structure

RECT answers:  
“How should agents behave given relational entanglement?”  
 $\Lambda$  answers:  
“Why relational entanglement cannot be fully captured by any agent-based optimization at all.”  
That distinction keeps everything consistent—and actually makes both frameworks stronger.

RECT as a  $\Lambda$ -Projected Effective Theory of Relational Decision-Making

## 1. Scope and Intent

Relational Empathy–Coherence Theory (RECT) is reinterpreted here not as a foundational ontology, but as a  $\Lambda$ -projected effective theory: a linear, halting approximation of deeper relational dynamics described by the  $\Lambda$  Principle of Irreducibility and the NSAF (Non-Scale-Attachable Frame) framework.

RECT is therefore treated as:

A pragmatic, utilitarian model for managing agent and societal behavior within constrained linear decision frames, while explicitly acknowledging its domain of validity and failure modes.

## 2. $\Lambda$ -NSAF Preliminaries (Minimal)

We assume the  $\Lambda$ -NSAF framework:

$\Lambda$  Principle: No linear descriptive system can fully enclose scale-invariant, self-referential, or continuous relational dynamics.

NSAF: Linear (scale-attached) and spectral/curved (scale-free) frames are mutually irreducible but reciprocally projective.

Projection: Linear observables arise as coarse-grained shadows of higher-dimensional relational structure.

RECT is explicitly situated in the linear, scale-attached frame.

### 3. Recasting RECT as a Linear Projection

#### 3.1 Players as Projected Relational Bundles

RECT defines a “player” as a relational pattern of events. Under  $\Lambda$ -NSAF:

A player is not ontologically primitive.

It is a localized projection of a broader relational field into a decision-relevant frame.

Formally:

A player  $i$  corresponds to a bounded relational submanifold  $R_i \in \mathcal{R}$ , projected into a scalar decision coordinate.

This justifies RECT’s use of player-level payoffs without reifying agents as fundamental objects.

#### 3.2 Empathy $e$ as Frame-Coupling Coefficient

RECT treats empathy  $e \in [0,1]$  as a scalar measuring relational overlap.

In  $\Lambda$  terms:

$e$  is a linear proxy for frame coupling strength between agent-local projections.

Crucially:

$e$  is not fundamental.

It compresses many higher-order relational modes (history, trust, identity, affect) into a single scalar.

This compression is valid only within bounded scale and time horizons.

#### 3.3 Coherence CCC as Projected Spectral Stability

RECT defines coherence:

$$C = S - eDC = S - eDC = S - eD$$

This is a linear penalty model for imbalance.

Under  $\Lambda$ -NSAF:

True coherence is spectral and multi-scale

RECT’s CCC is a first-order Taylor projection of stability near a locally equilibrated regime

Thus:

CCC measures local linear stability, not global relational harmony.

#### 4. Why RECT Works (Within Its Domain)

RECT succeeds because:

Linear social systems exist

Institutions, contracts, markets, laws

All impose halting, measurable frames

Human decision-making often collapses relational complexity

Bounded rationality

Limited horizons

Symbolic commitments

Phase transitions matter more than optima

RECT's empathy threshold captures when cooperation flips

Not why relationality exists

Within these constraints, RECT is a useful effective theory, much like thermodynamics is useful despite ignoring microstates.

#### 5. Where RECT Must Break (Necessarily)

##### 5.1 Scale Explosion

As group size  $n \rightarrow \infty$  to  $\infty$ :

Pairwise imbalance terms grow  $O(n^2)$

Scalar  $\epsilon$  cannot encode heterogeneous relational geometry

Coherence becomes frame-dependent and non-comparable

$\wedge$  interpretation:

Global scalar coherence is undefined beyond local projection zones.

## 5.2 Nonlinear Feedback and Identity Entanglement

RECT assumes:

Stable player identities

Well-defined payoff attribution

At scale:

Identities overlap

Payoffs become non-local

Frame boundaries dissolve

This is the Gödel/Turing limit of social modeling: the model must reference itself.

## 5.3 Path Dependence and Non-Ergodicity

RECT updates empathy via reinforcement rules.

$\wedge$ -NSAF predicts:

History-dependent hysteresis

Non-ergodic trajectories

Multiple incompatible linearizations

Thus:

No global convergence is guaranteed or even well-defined.  
RECT can converge locally;  $\Lambda$  says it must diverge globally.

## 6. RECT as a $\Lambda$ -Compatible Applied Framework

RECT should therefore be explicitly framed as:

A  $\Lambda$ -consistent utilitarian guide for designing and managing social systems within constrained linear frames, not a universal theory of rationality.

Appropriate Uses:

Institutional design

AI alignment heuristics

Conflict mediation

Economic policy simulations

Cooperative mechanism design

Inappropriate Claims:  
Fundamental ontology

Universal rational behavior

Global optimality

Scale-free validity

RECT becomes stronger when it disclaims fundamentality.

## 7. Revised Status Statement (Critical)

RECT does not replace game theory at the foundational level.

It replaces unrelational linear utility models within bounded decision frames, operating as a  $\Lambda$ -projected effective theory whose breakdown conditions are predictable and structurally necessary.

This aligns RECT with  $\Lambda$  rather than placing it in conflict.

8. Synthesis:  $\Lambda$  as the Meta-Theory  
 $\Lambda$  explains why relational theories work

RECT explains how to act when they do

NSAF explains where they stop working

This triad mirrors:  
Microphysics / Thermodynamics / Statistical mechanics

Computability / Algorithms / Complexity

Geometry / Projections / Measurements

RECT belongs in the middle layer.

9. Final Positioning (Clean and Defensible)

RECT is best understood as:

A disciplined, empirically testable, relational decision framework arising as a linear projection of deeper irreducible relational structure, useful for guiding cooperative outcomes in human and artificial systems, while explicitly bounded by the  $\Lambda$  Principle of Irreducibility.

That framing:

Preserves its strengths

Prevents category errors

Makes it scientifically and philosophically robust

RECT as a  $\Lambda$ -Projected Linear Operator Theory

1. Projection Framework

Let

$\mathcal{R}$

denote the full relational state space of an interacting system.

$\mathcal{R}$  is:

High-dimensional

Nonlinear

Scale-invariant

Non-halting

We assume no global coordinate chart exists on  $\mathcal{R}$ .

Definition 1 ( $\Lambda$ -Projection Operator)

A  $\Lambda$ -projection is a linear operator

$\Pi: \mathcal{R} \rightarrow \mathbb{R}^k$

that maps irreducible relational structure into a finite, scale-attached descriptive frame suitable for decision-making.

Properties:

$\Pi \circ \Pi = \Pi$  is lossy (non-invertible)

$\Pi \circ \Pi = \Pi$  preserves local relational gradients

$\Pi \circ \Pi = \Pi$  fails under global extension

RECT lives entirely in the codomain of  $\Pi \circ \Pi = \Pi$ .

2. Players as Projected Relational Bundles

Let

$R_i \subset \mathcal{R}_i \subset \mathcal{R}$

be the relational submanifold associated with agent  $i$ .

Define the player projection:

$P_i := \Pi(R_i) \in \mathbb{R}^k$

Interpretation:

$P_i$  is not an intrinsic payoff

It is a linear observable corresponding to local relational intensity

This explicitly removes any ontological status from “utility.”

### 3. Empathy as Frame Coupling Projection

Let

$$C_{ij} \subset R \setminus \{C\}_{ij} \subset R$$

denote relational coupling between  $i$  and  $j$ .

Define:

$$e_{ij} := \prod \Lambda(C_{ij}) \in [0, 1] \quad e_{ij} := \prod_i \Lambda(C_{ij}) \in [0, 1]$$

Interpretation:

$e_{ij}$  is a scalar compression of multi-modal relational overlap

It approximates coupling strength only within a bounded neighborhood

Critical:

No assumption is made that  $e_{ij}e_{ij}$  composes transitively or globally.

### 4. Coherence as Projected Spectral Stability

Let

$$\Sigma(R) \Sigma(R)$$

be the (undefined) global spectral stability functional over the full relational field.

RECT defines:

$$C := \prod \Lambda(\Sigma(R)) C := \prod_i \Lambda(\Sigma(R)) C := \prod \Lambda(\Sigma(R))$$

In two-player form:

$$C = (P_A + P_B) - e |P_A - P_B| \quad C = (P_A + P_B) - e |P_A - P_B|$$

This is now explicitly understood as:

A first-order linearization

Around a locally equilibrated relational patch

Of a fundamentally non-linear stability functional

### 5. Individual Gain as Projected Gradient Flow

RECT defines:

$$G_i = (1 - e)P_i + eCG_i = (1 - e)P_i + eCG_i = (1 - e)P_i + eC$$

Rewrite:

$$G_i := \prod \Lambda (\nabla R_i \Sigma(R)) G_{-i} := \prod_i \lambda \left( \nabla \Sigma(R) \right)$$

Interpretation:

$G_i G_{-i}$  approximates the directional derivative of relational stability

Only valid where  $\nabla \Sigma \nabla \Sigma$  is locally well-defined

Not globally integrable

This removes any implication of universal optimization.

## 6. Relational Equilibrium as Local Fixed Point

Define:

Definition 2 ( $\Lambda$ -Local Relational Equilibrium)

A strategy profile  $s^* s^* s^*$  is a RECT equilibrium iff:

$$\prod \Lambda (\nabla R_i \Sigma(R)) s^* = 0 \quad \forall i \quad \text{and} \quad \prod \Lambda (\nabla R_i \Sigma(R)) s^* = 0 \quad \forall i$$

This is:

A local stationary point

Not guaranteed unique

Not guaranteed stable under scale extension

## Failure Modes Theorems

These are not bugs. They are structural necessities.

### Theorem 1 (Scale Explosion Failure)

Statement:

RECT coherence CCC is undefined as a global ordering functional as the number of agents  $n \rightarrow \infty$

Proof Sketch:

RECT coherence aggregates pairwise imbalances:

$$\sum_{i < j} |P_i - P_j| \sim O(n^2)$$

while empathy projections  $e_{ij} e_{ij}$  remain scalar and bounded.

Thus no normalization preserves comparability without introducing frame-dependent weighting.

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### Theorem 2 (Projection Non-Closure)

Statement:

RECT projections do not compose transitively across nested relational scales.

Proof Sketch:

Given:

$$\Pi \Lambda (\Pi \Lambda (R)) \neq \Pi \Lambda (R) \text{ and } \Pi_i \Lambda (\Pi \Lambda (R)) = \Pi \Lambda (R)$$

information loss at each projection step is irreversible.

Thus aggregating RECT-level outcomes produces artifacts not corresponding to any underlying relational state.

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### Theorem 3 (Identity Entanglement Failure)

Statement:

RECT fails when agent identity boundaries become dynamically coupled.

Proof Sketch:

RECT presupposes stable partitions  $R = \bigcup R_i \text{ and } \bigcap R_i = \emptyset$ .

When identity overlap occurs:

$$R_i \cap R_j \neq \emptyset \text{ and } R_i \cap R_j \neq \emptyset$$

payoff attribution becomes ill-defined.

No scalar projection can recover separability.

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### Theorem 4 (Non-Ergodicity and Path Dependence)

Statement:

RECT convergence is not invariant under history-dependent relational evolution.

Proof Sketch:

Empathy update rules assume ergodic sampling of outcomes.

$\Lambda$ -NSAF dynamics admit hysteresis and path locking.

Thus long-run averages diverge between trajectories with identical initial projections.

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### Theorem 5 (Gödel–Turing Analogy for Social Systems)

Statement:

No RECT-style linear projection can produce a complete and consistent decision theory over relational systems that include self-reference.

Proof Sketch:

If agents model the RECT outcomes of agents modeling RECT outcomes, the system becomes self-referential.

By analogy with halting and incompleteness, some relational truths become undecidable within the projected frame.

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## 7. Status of RECT Within $\Lambda$ -NSAF

RECT is therefore:

Valid locally

Useful instrumentally

Testable empirically

Not globally closed

Not ontologically fundamental

RECT is a  $\Lambda$ -consistent effective theory.

## 8. Final Framing Statement

Relational Empathy–Coherence Theory should be understood as a linear  $\Lambda$ -projection of irreducible relational dynamics, providing a practical decision heuristic within bounded social and institutional frames, while necessarily failing under scale, identity entanglement, and self-reference in accordance with the  $\Lambda$  Principle of Irreducibility.