§ 3 The Stack ADT

1. ADT

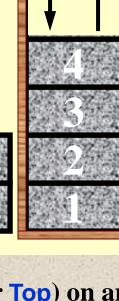
A stack is a Last-In-First-Out (LIFO) list, that is, an ordered list in which insertions and deletions are made at the top only.

Objects: A finite ordered list with zero or more elements.

Operations:

- Int IsEmpty(Stack S);
- Stack CreateStack();
- DisposeStack(Stack S);
- MakeEmpty(Stack S);
- Push(ElementType X, Stack S);
- ElementType*Top(Stack S);
- pop(Stack S);





Note: A Pop (or Top) on an empty stack is an error in the stack ADT.

Push on a full stack is an implementation error but not an ADT error.

2. Implementations

Linked List Implementation (with a header node)



② S->Next = TmpCell

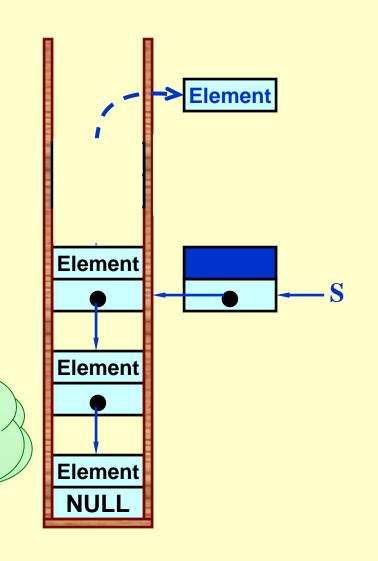
Top: return S->Next->Element

Pop: ① FirstCell = S->Next

② S->Next = S->Next->Next

③ free (FirstCell)





> Array Implementation

Note: ① The stack model must be well encapsulated. That is, no part of your code, except for the stack routines, can attempt to access the Array or TopOfStack variable.
② Error check must be done before Push or Pop (Top).

Read Figures 3.38-3.52 for detailed implementations of stack operations.

3. Applications

***** Balancing Symbols



Check if parenthesis (), brackets [], and braces { } are balanced.

```
Algorithm {
  Make an empty stack S;
                                               T(N) = O(N)
  while (read in a character c) {
                                            where N is the length
    if (c is an opening symbol)
                                              of the expression.
       Push(c, S);
                                                  This is an
    else if (c is a closing symbol) {
                                              on-line algorithm.
       if (S is empty) { ERROR; exit; }
       else { /* stack is okay */
         if (Top(S) doesn't match c) { ERROR, exit; }
         else Pop(S);
       } /* end else-stack is okay */
    } /* end else-if-closing symbol */
  } /* end while-loop */
  if (S is not empty) ERROR;
```

*** Postfix Evaluation**

[Example] An infix expression: a + b * c - d / e

A prefix expression: -+a*bc/de

A postfix expression: a b c + d e /

Reverse Polish notation

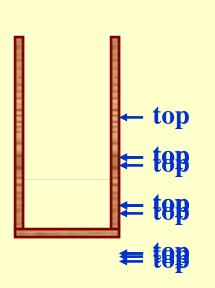
operand

the highest precedence

operator with

operator

[Example] 62/3-42*+=8



Get token: 6 (operand)	Get token: 2 (operand)
Get token: / (operator)	Get token: 3 (operand)
Get token: – (operator)	Get token: 4 (operand)
Get token: 2 (operand)	Get token: * (operator)
Get token: + (operator)	Pop: 8

T(N) = O(N). No need to know precedence rules.

* Infix to Postfix Conversion

[Example]
$$a+b*c-d = abc*+d-$$

Note:

- > The order of operands is the same in infix and postfix.
- higher precedence appear before those lence.

Isn't that simple?

Get example... + (plus)

Get token: c (operand)

Get token: c (operand)

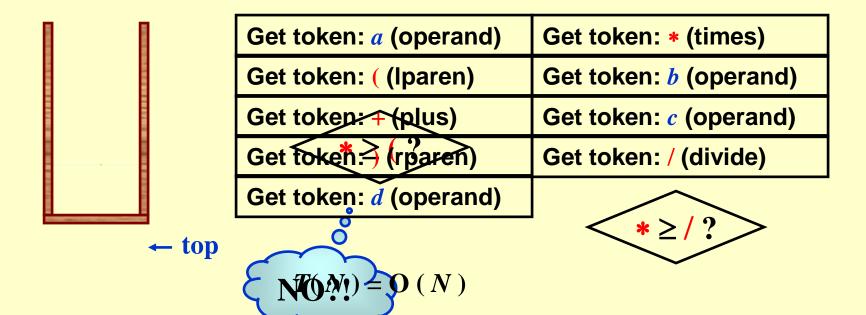
Get token: d (operand)

Wait till



[Example]
$$a * (b + c) / d = abc + * d /$$

Output: a b c + * d



Solutions:

- ① Never pop a (from the stack except when processing a).
- ② Observe that when (is not in the stack, its precedence is the highest; but when it is in the stack, its precedence is the lowest. Define in-stack precedence and incoming precedence for symbols, and each time use the corresponding precedence for comparison.

Note: a-b-c will be converted to ab-c. However, 2^2^3 (2^2^3) must be converted to 223^2 , not 22^3 since exponentiation associates right to left.

/* a bad use of recursion */

```
fp
             Recursion can always be completely removed.
                                                                      nents
           Non recursive programs are generally faster than
                     equivalent recursive programs.
              However, recursive programs are in general
                 much simpler and easier to understand.
                                                                .1e.
void PrintL
                                      void PrintList ( List L )
                List L)
  if ( L != N\ /L ) {
                                      top: if ( L != NULL ) {
    PrintEle /nent ( L->Element );
                                            PrintElement ( L->Element );
    PrintList( L->next );
                                            L = L->next;
                                            goto top; /* do NOT do this */
```

} /* compiler removes recursion */

§ 4 The Queue ADT

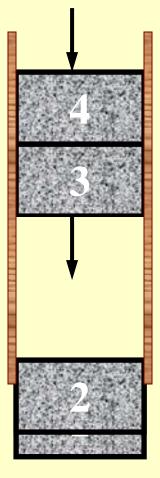
1. ADT

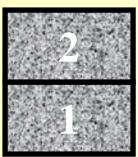
A queue is a First-In-First-Out (FIFO) list, that is, an ordered list in which insertions take place at one end and deletions take place at the opposite end.

Objects: A finite ordered list with zero or more elements.

Operations:

- rint IsEmpty(Queue Q);
- Queue CreateQueue();
- DisposeQueue(Queue Q);
- MakeEmpty(Queue Q);
- Enqueue(ElementType X, Queue Q);
- ElementType Front(Queue Q);
- Dequeue(Queue Q);





2. Array Implementation of Queues

(Linked list implementation is trivial)

```
struct QueueRecord {
             Capacity; /* max size of queue */
        int
             Front; /* the front pointer */
        int
        int Rear; /* the rear pointer */
             Size; /* Optional - the current size of queue */
        int
        ElementType *Array; /* array for queue elements */
};
```

Job Scheduling in an Operating System (Example)



Front

Rear

Enqueue Job 1	Enqueue Job 2	Enqueue Job 3	Dequeue Job 1
Enqueue Job 4	Enqueue Job 5	Enqueue Job 6	Dequeue Job 2
Enqueue Job 7	Enqueue Job 8		

Rear

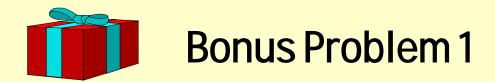
[1]

Front

Circular Queue:

[0][5] E Job Job 6 **Question:** Job Why is the queue [4] announced full while there is Job Job still a free space left? [2] The queue is full

Note: Adding a Size field can avoid wasting one empty space to distinguish "full" from "empty". Do you have any other ideas?



LRU-K

(2 points)

Due: Monday, June 17th, 2024 at 10:00pm

The problem can be found and submitted at https://pintia.cn/