

Today

Mon: Midterm  
in class

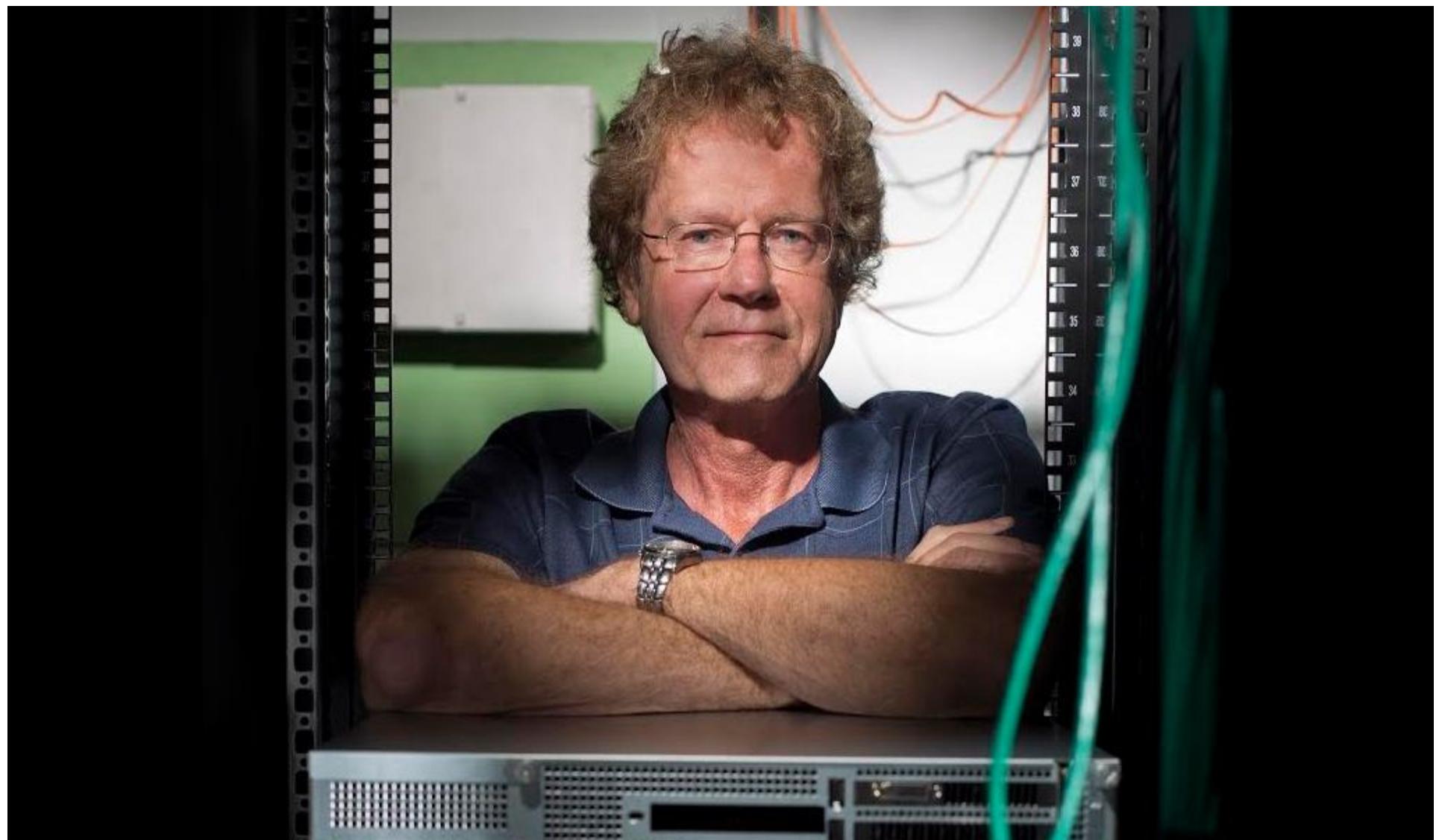
Distributed Systems

\* Basics

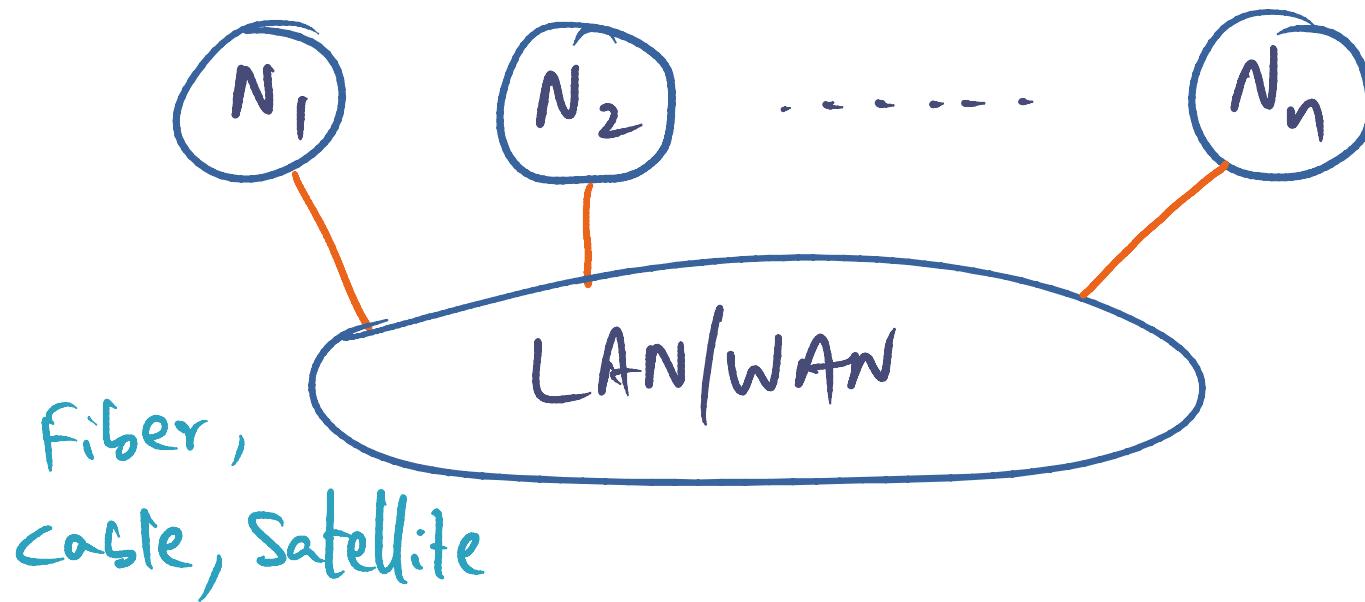
- \* Lamport clock
  - Logical
- \* Example of using Logical clock
  - Distr. M.E.
- \* Physical clock

Friday

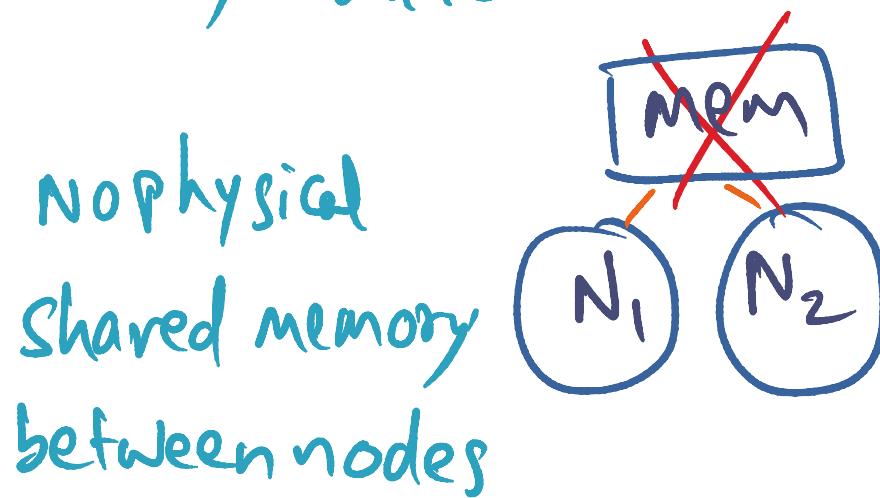
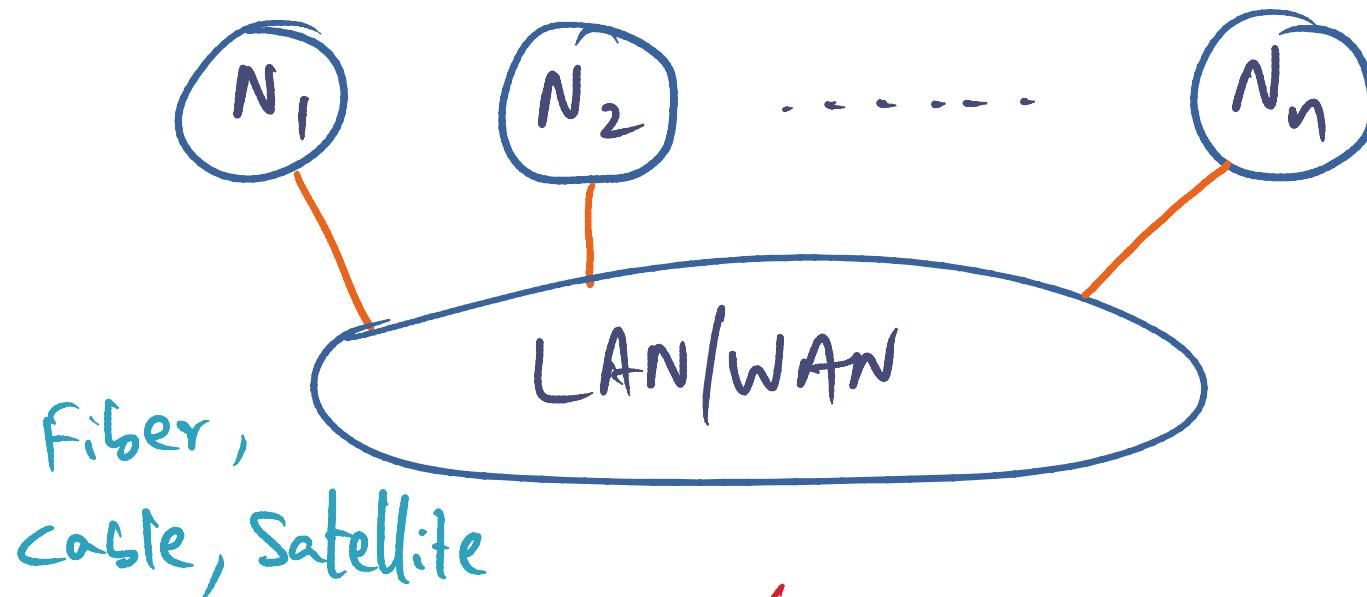
\* Townhall



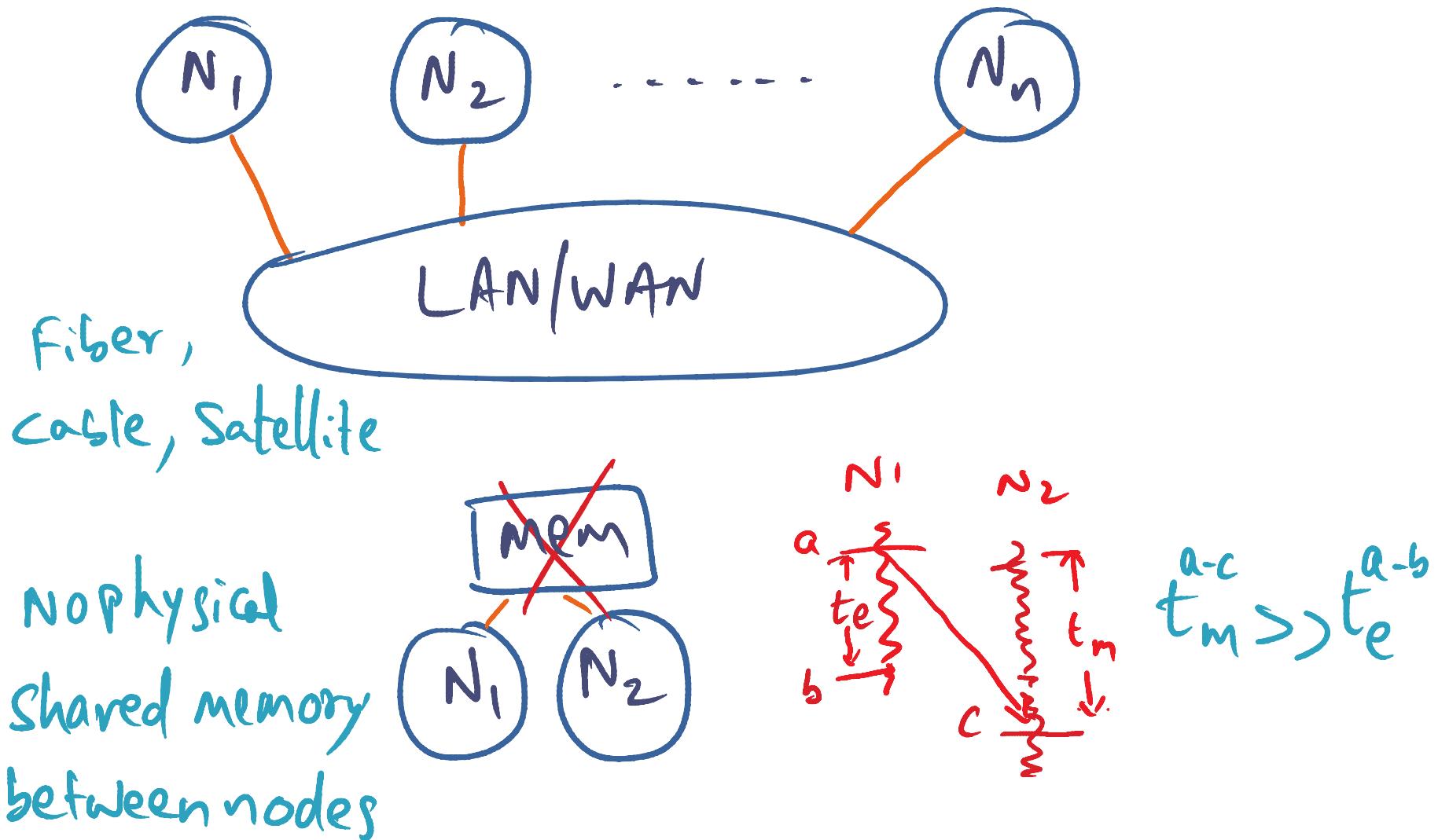
# Distributed Systems Definition



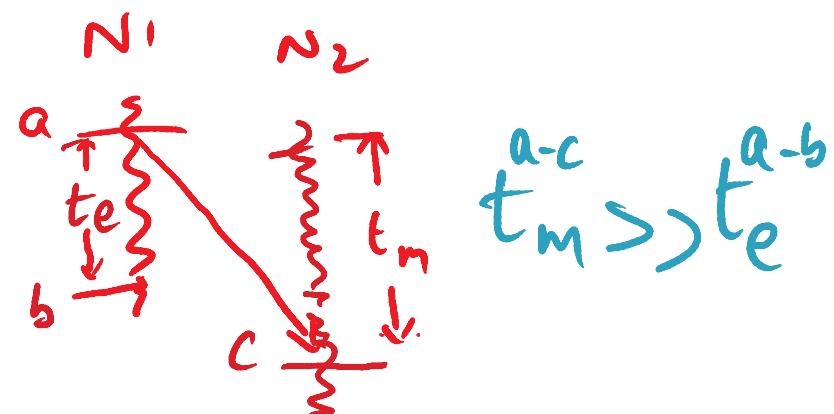
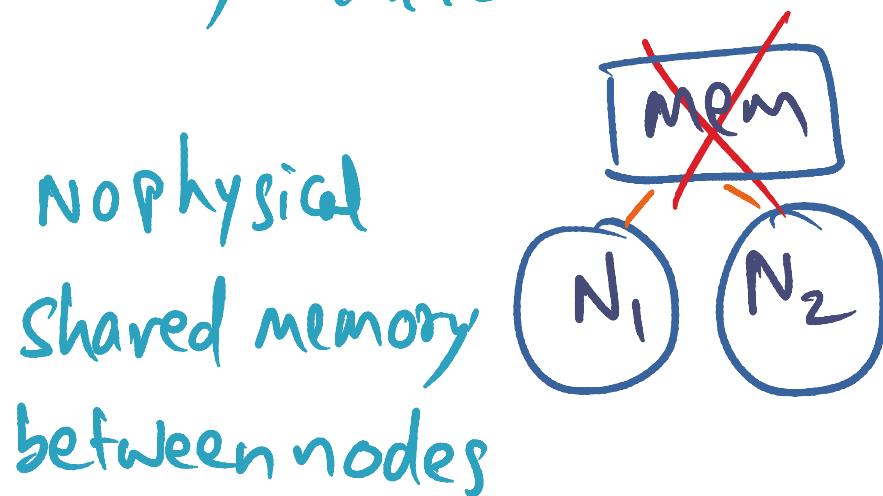
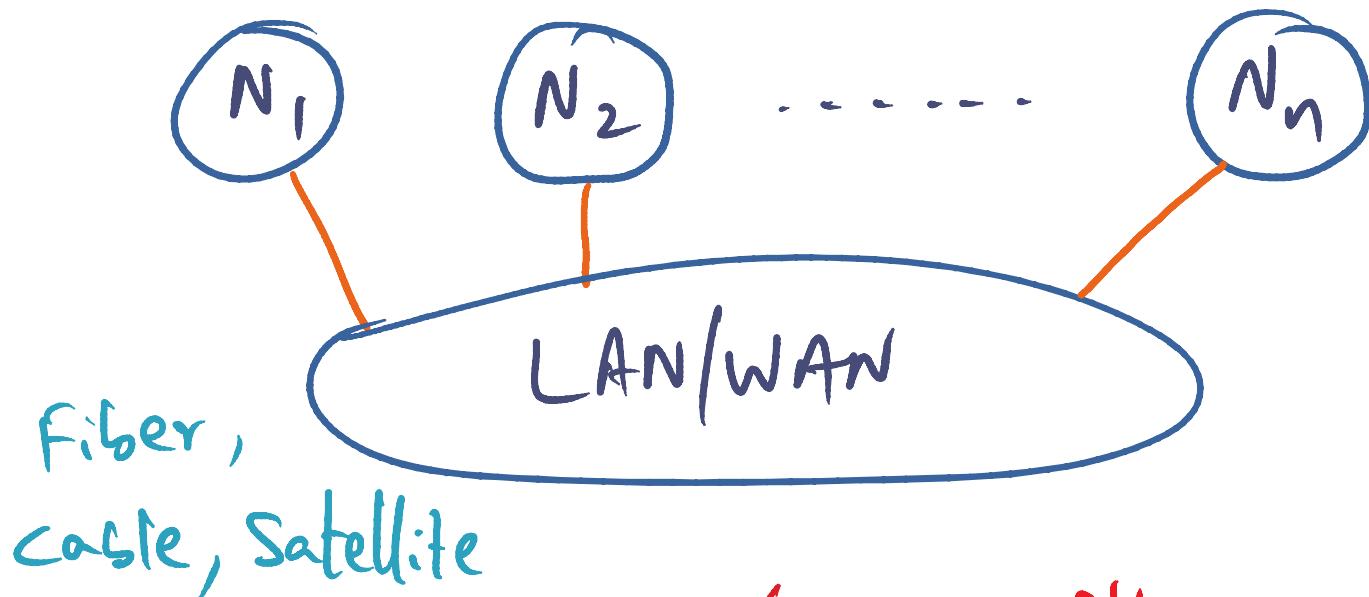
# Distributed Systems Definition



# Distributed Systems Definition

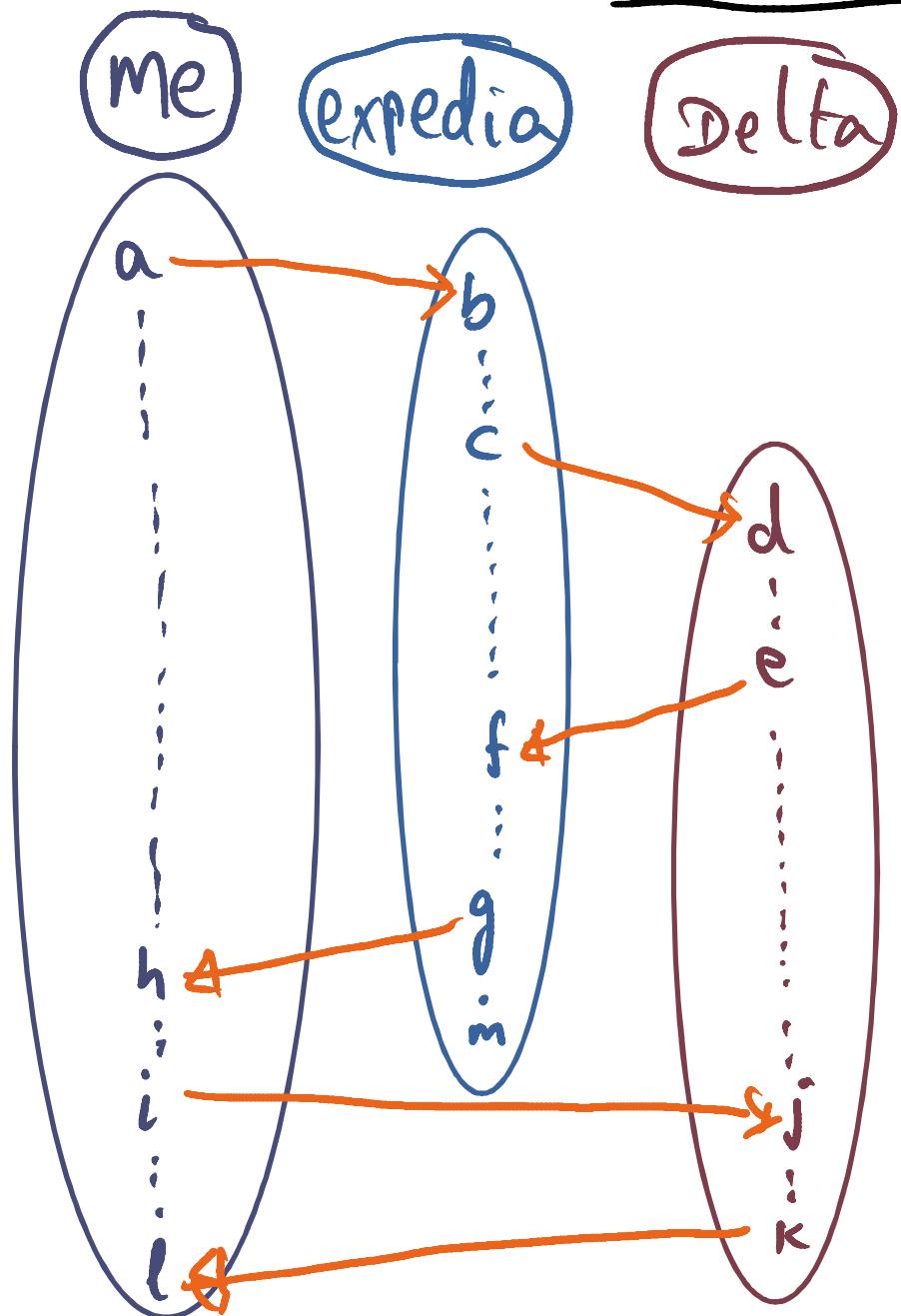


# Distributed Systems Definition

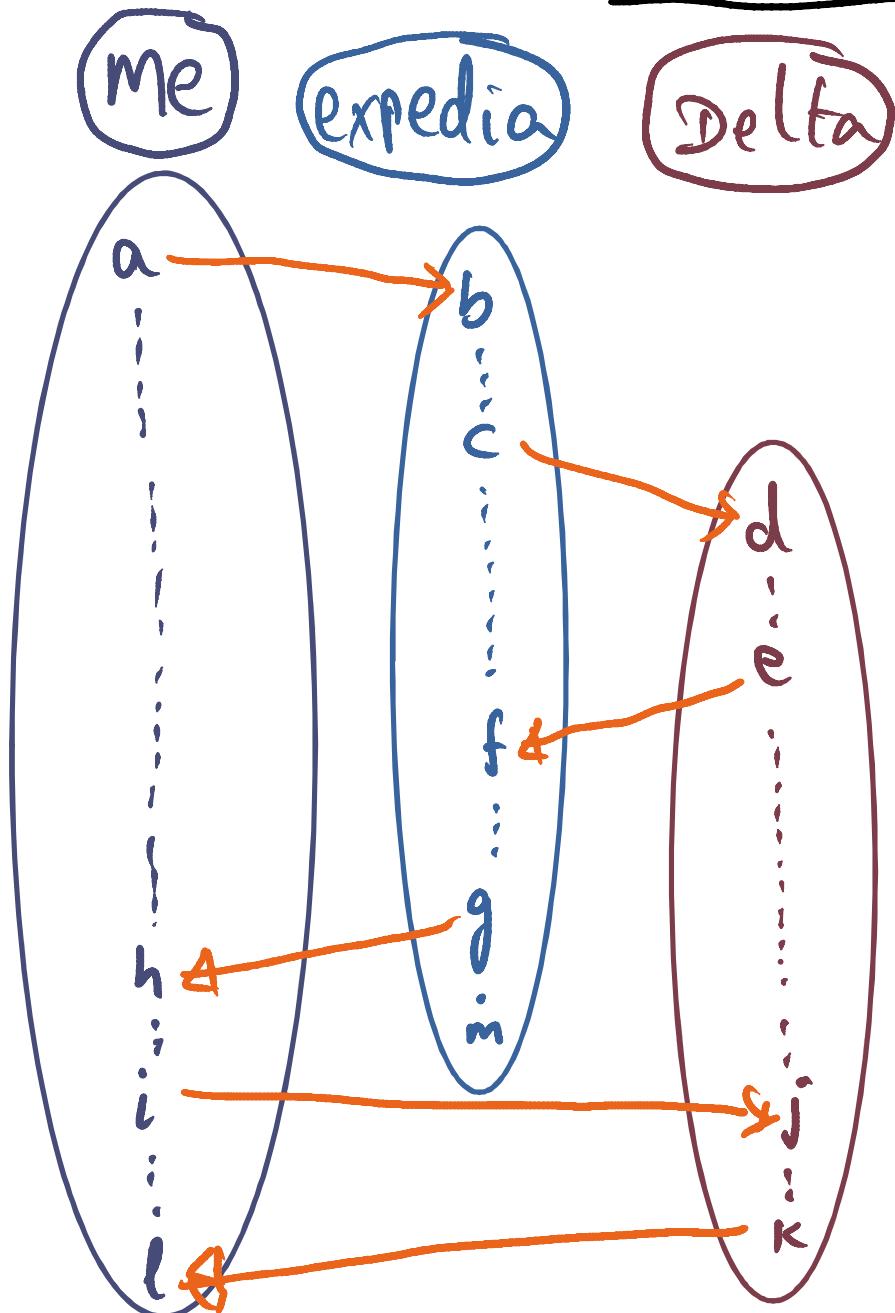


Even a cluster is a  
distributed system!

## A fun Example



## A fun Example



Beliefs!

- Processes Sequential



events totally ordered

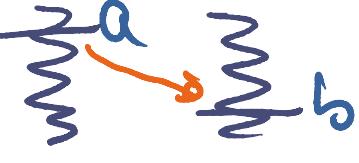
$h \rightarrow i$ ,  $f \rightarrow g$ ,  $d \rightarrow e \dots$

- send before receive



$a \rightarrow b$ ,  $e \rightarrow f$ , ...

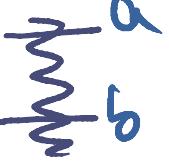
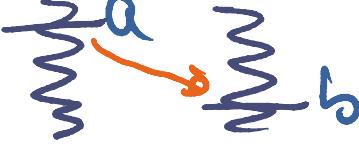
## "Happened Before" Relation

$a \rightarrow b \Rightarrow$  either  or 

 Same process

 Communication

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$a \rightarrow b \Rightarrow$  either  or 

 Same process

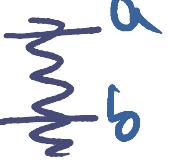
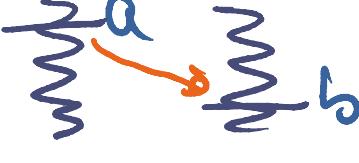
 Communication

Transitivity of "happened before"

$a \rightarrow b \Rightarrow a \rightarrow c$

$b \rightarrow c$

## "Happened Before" Relation

$a \rightarrow b \Rightarrow$  either  or 

  
Same  
process

  
Communication

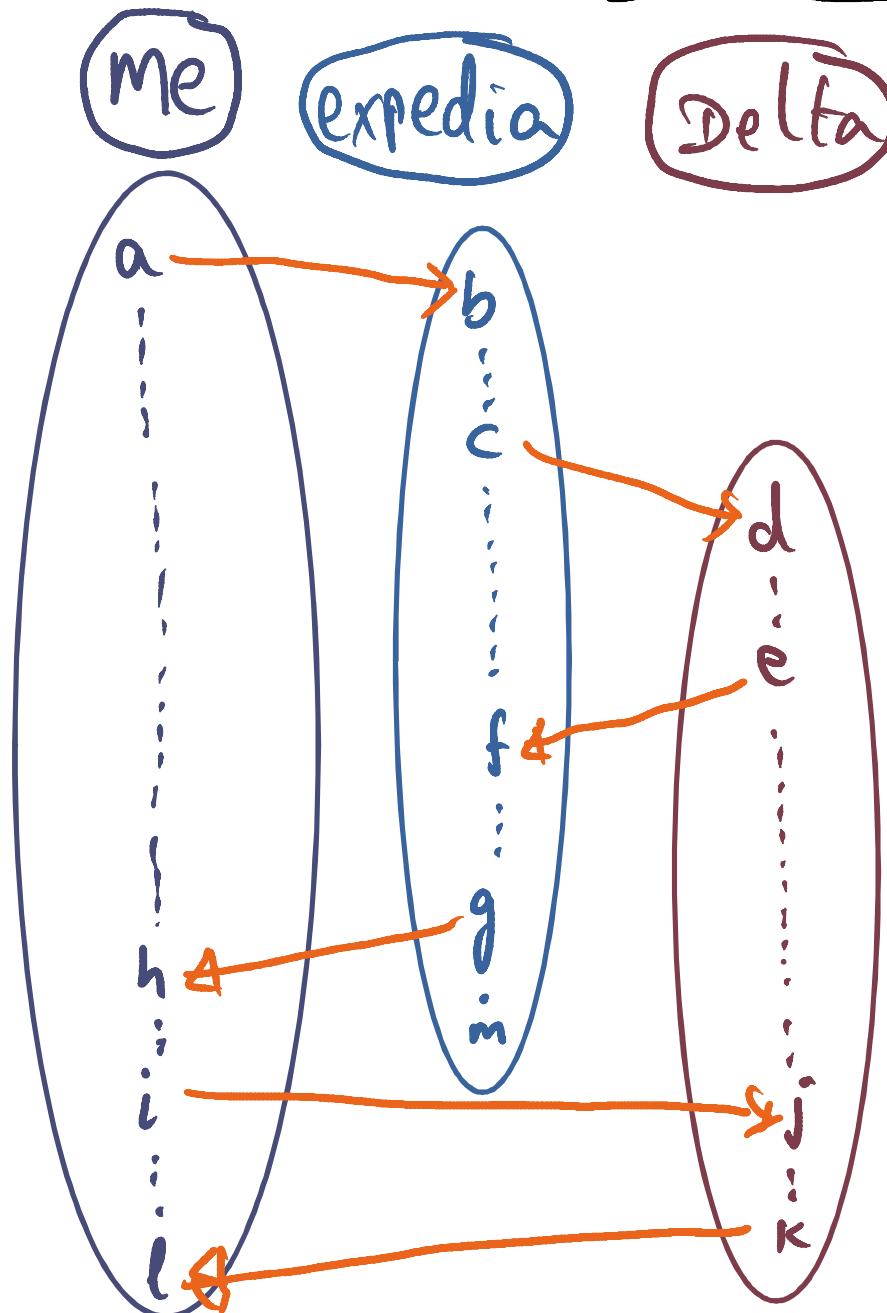
Transitivity of "happened before"

$a \rightarrow b \Rightarrow a \rightarrow c$

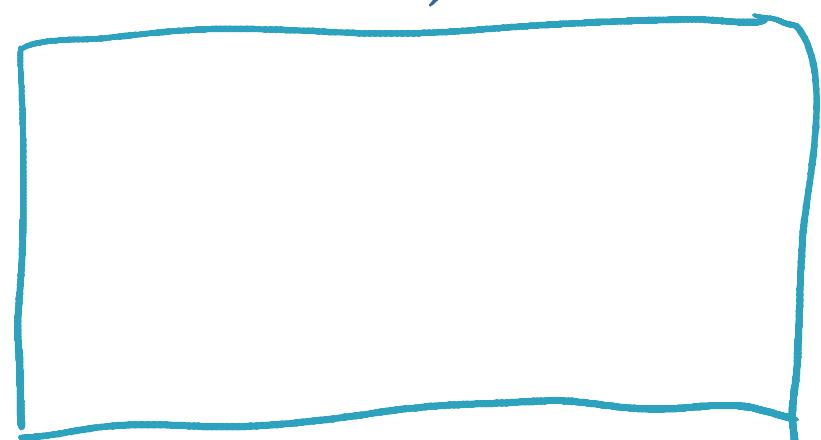
$b \rightarrow c$

Concurrent events   
 $a \parallel b$

# Question



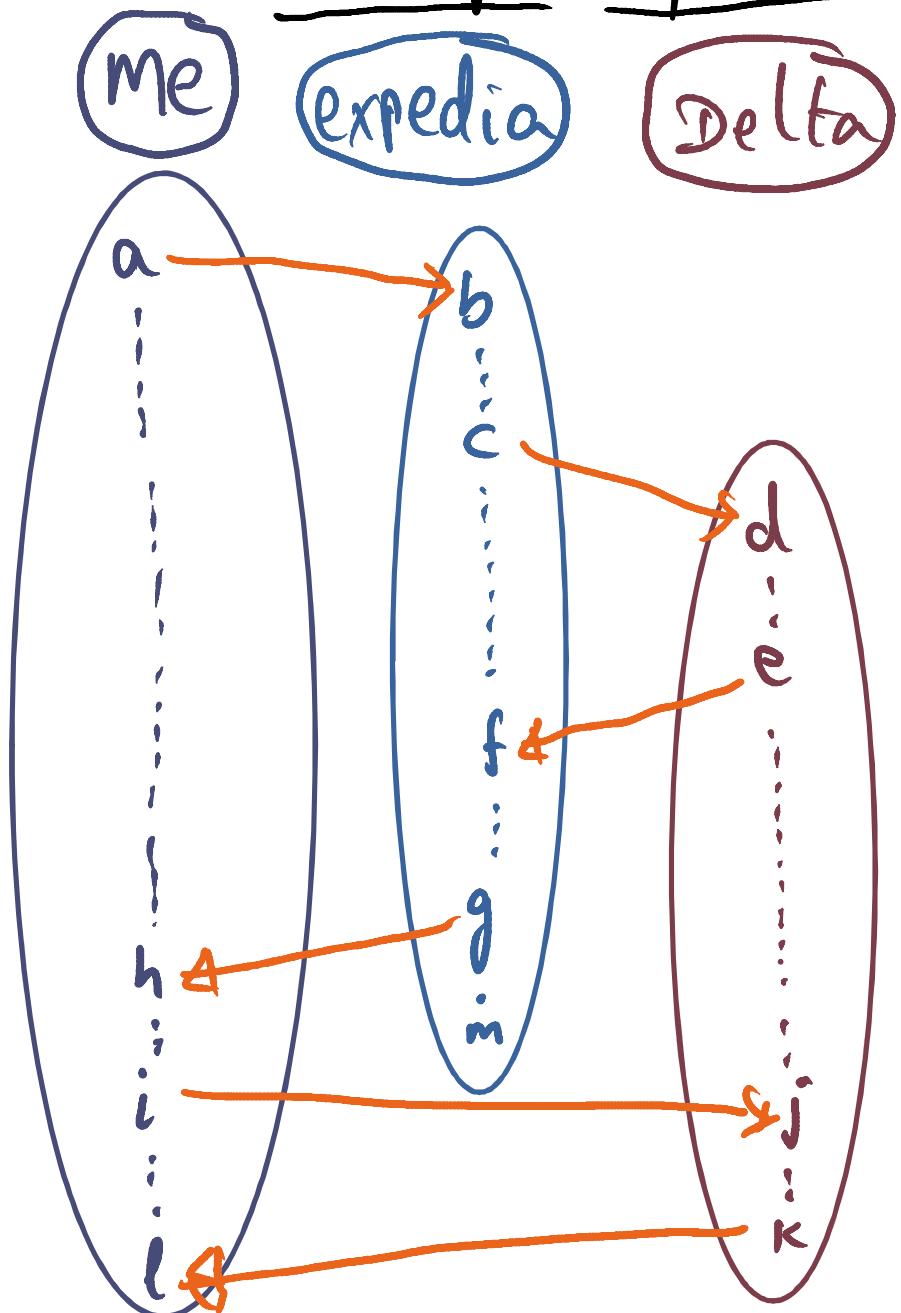
i) Identify all the events connected by  $\Rightarrow$



ii) Identify all || events



# Example of Event Ordering with $\rightarrow$



Events connected by  $\rightarrow$

$$\begin{array}{ll} a \rightarrow b \rightarrow i \rightarrow l & a \rightarrow b \quad i \rightarrow j \\ b \rightarrow c \rightarrow f \rightarrow g \rightarrow m & c \rightarrow d \quad k \rightarrow l \\ & e \rightarrow f \\ d \rightarrow e \rightarrow j \rightarrow k & g \rightarrow h \end{array}$$

Transitive  $\rightarrow$

$$a \rightarrow e, d \rightarrow m, \dots$$

conCurrent events ||

$$\begin{array}{ll} h || m & m || j \\ i || m & m || k \\ l || m & \end{array}$$

# Lamport's Logical clock

Each node

- \* its own events
- \* its communication events

Lamport's Logical clock

\* monotonic increase of own event times

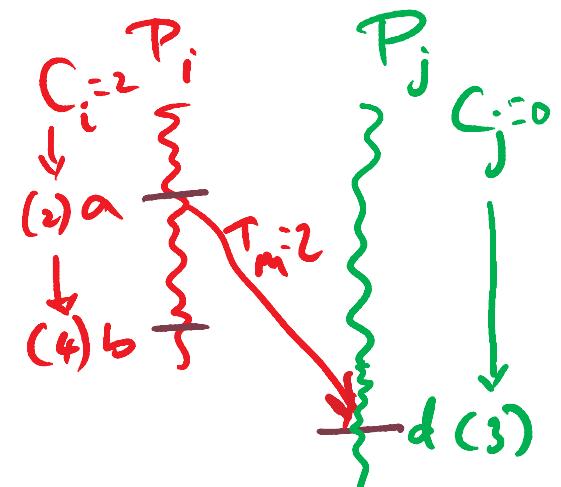
Condition 1:  $C_i(a) < C_i(b)$

\* message receipt time greater than send time

Condition 2:  $C_i(a) < C_j(d)$

$\Rightarrow$  choose  $C_j(d) = \max(C_i(a) + 1, C_j)$

\* timestamp of concurrent events?



## Logical clock Conditions

### Clock Conditions

\* monotonic increase of own event-times

$$\text{Condition 1: } C_i(a) < C_i(b)$$

\* message receipt time greater than send time

$$\text{Condition 2: } C_i(a) < C_j(d)$$

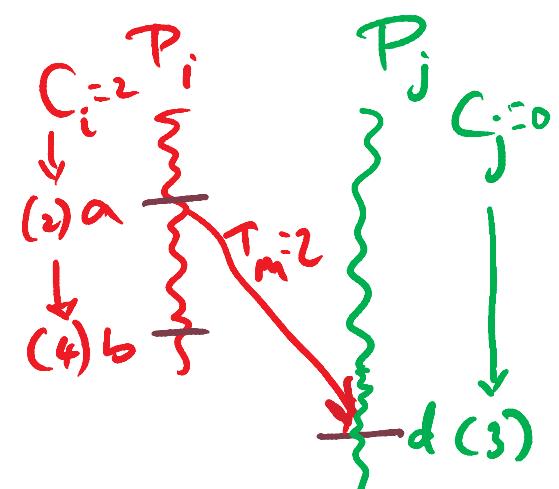
$$\Rightarrow \text{choose } C_j(d) = \max(C_i(a)++, C_j)$$

\* concurrent events (b and d)

arbitrary timestamps

$$C(x) < C(y)$$

$$\not\Rightarrow x \rightarrow y$$



## Lamport's Total Order

Condition for  $\Rightarrow$

$a \Rightarrow b$  iff

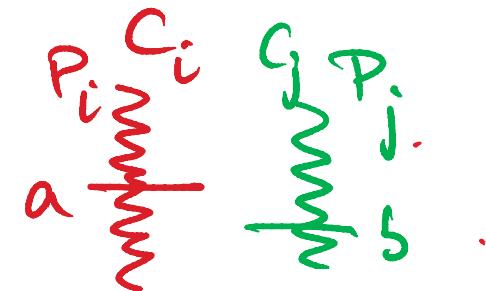
$$c_i(a) < c_j(b)$$

or

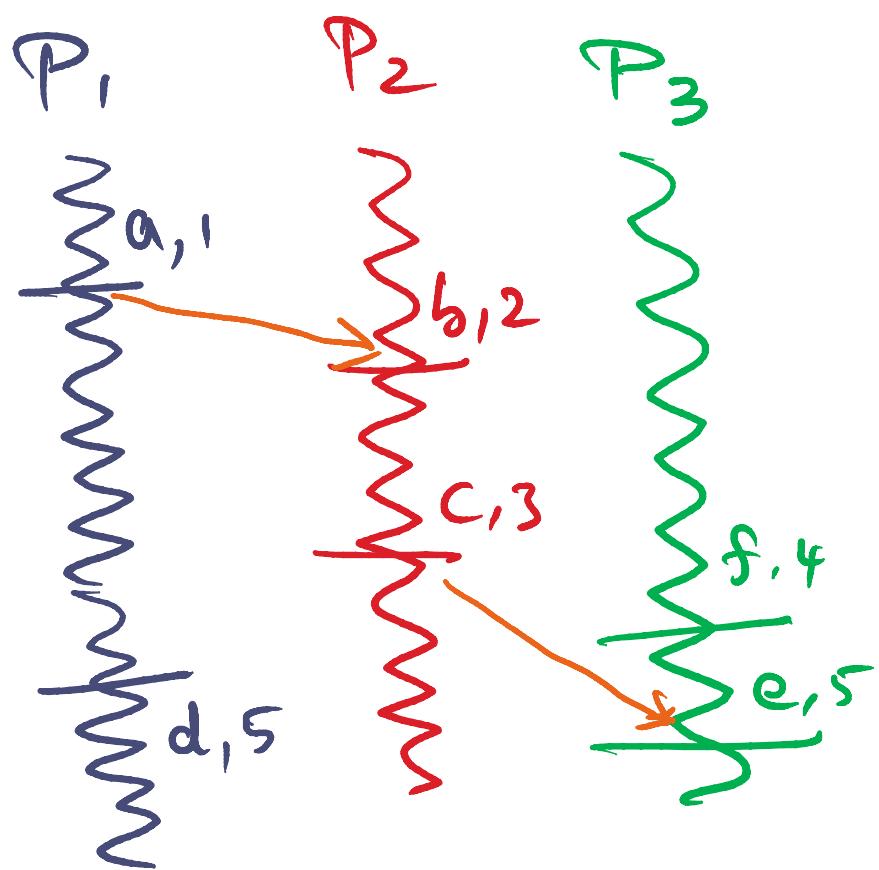
$$c_i(a) = c_j(b) \text{ and } p_i \ll p_j$$

( $\ll$  arbitrary "well known" condition  
to break a tie)

No single total order

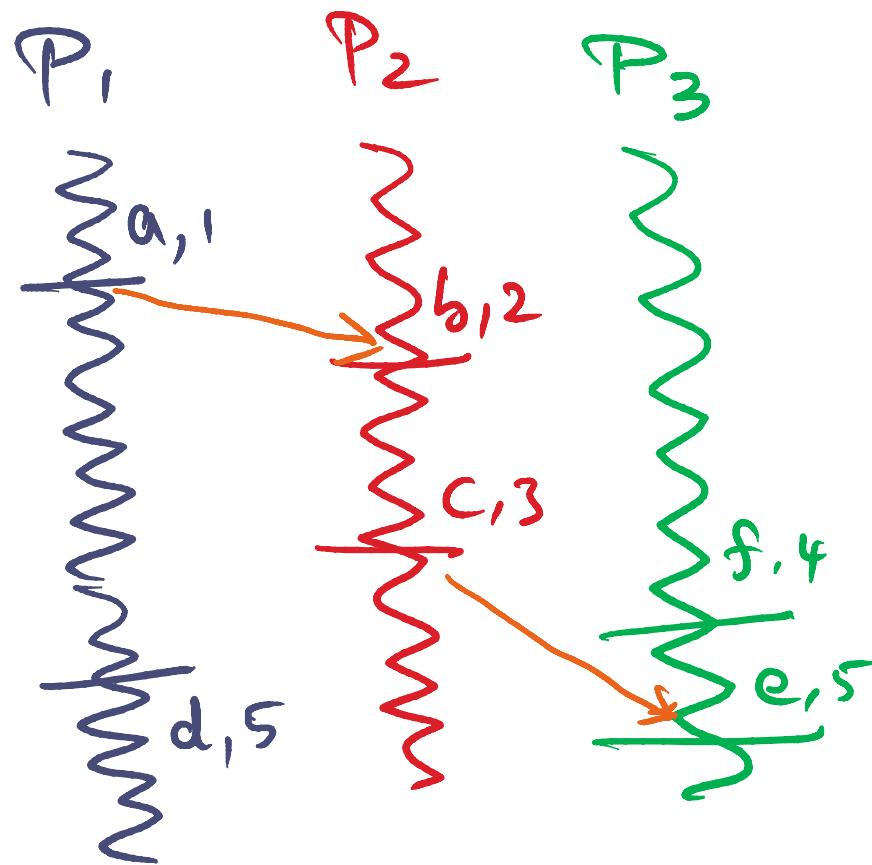


## Question



What is the total order  
using Process ID to  
break the tie?

## Question/Solution



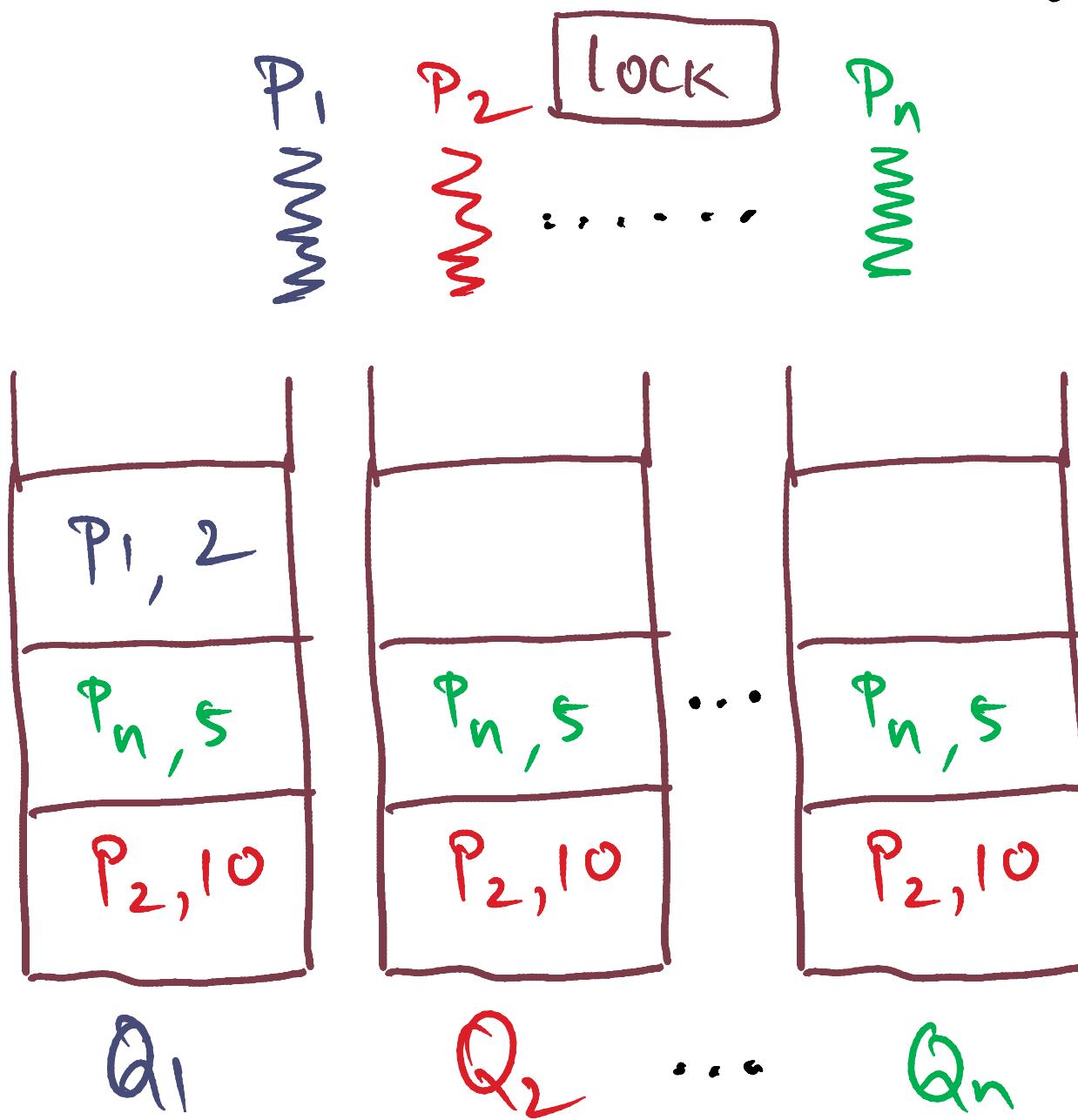
What is the total order  
using Process ID to  
break the tie?

Partial orders by →  
 $a \rightarrow b \rightarrow c \rightarrow e; f \rightarrow e$   
concurrent events ||  
 $d \parallel \{b, c, f, e\}; f \parallel \{a, d, b, c\}$

Total order respecting  
timestamps + PID ⇒

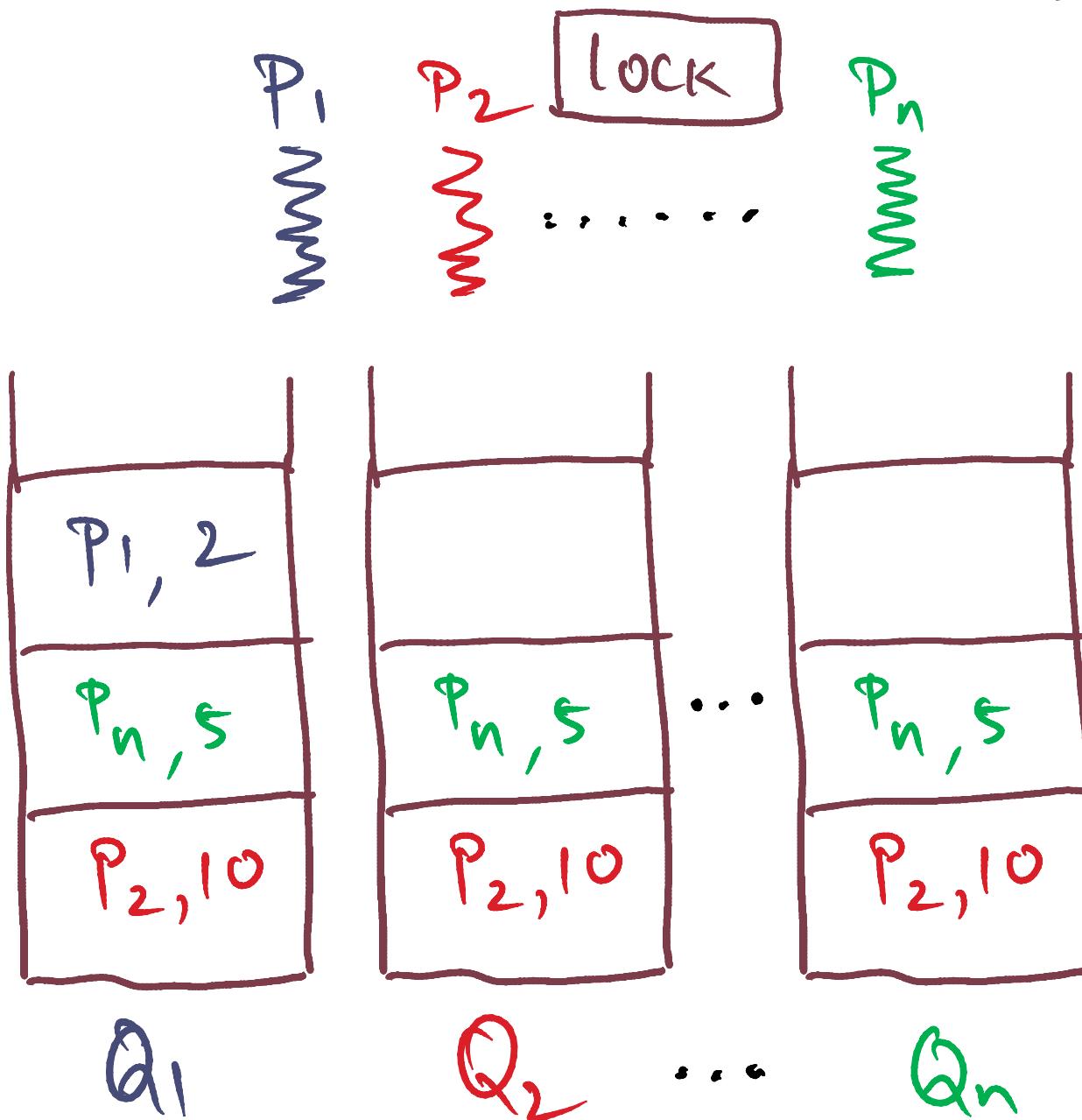
a b c f d e

# Distributed M.E. lock algorithm

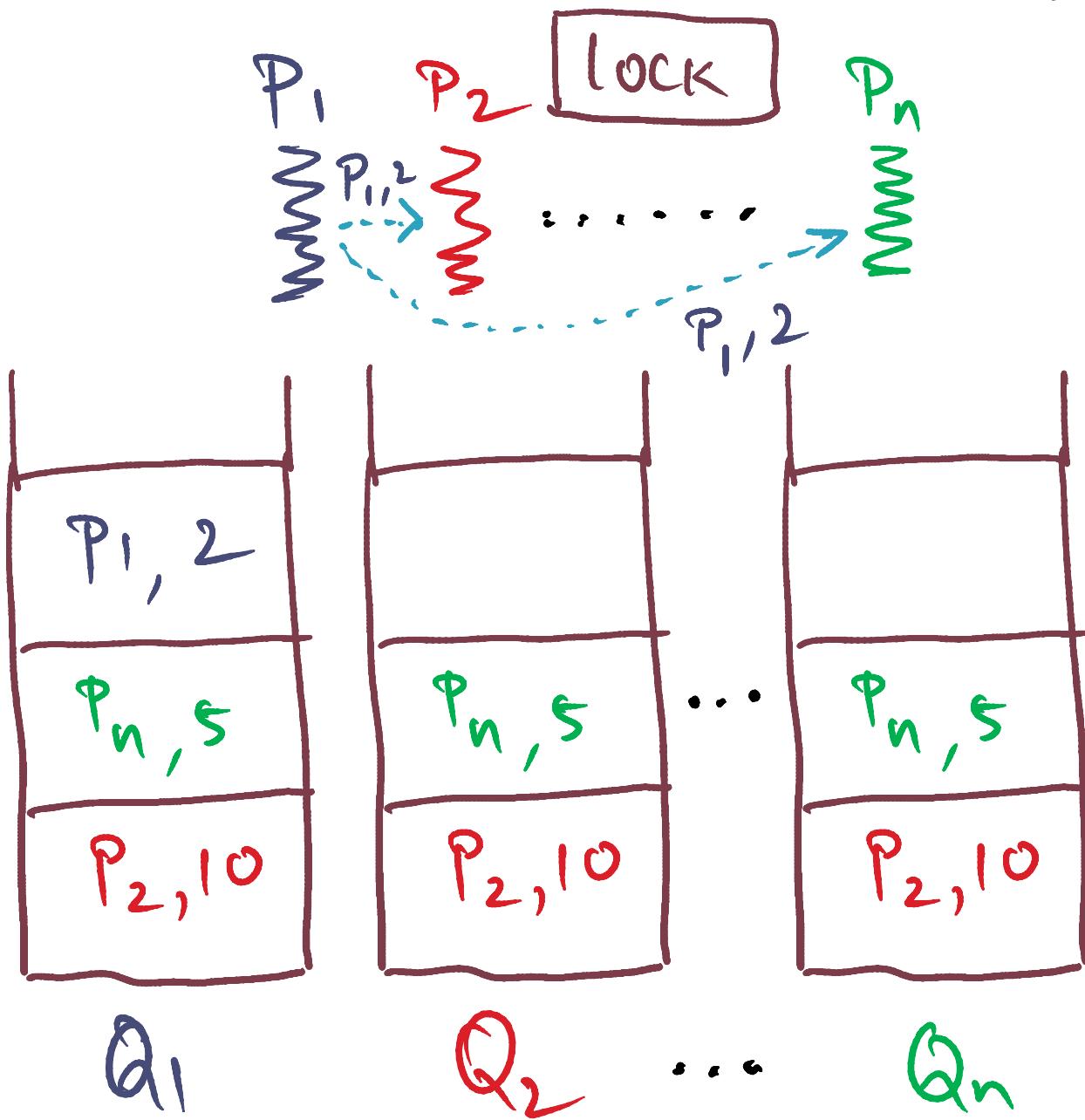


## Distributed M.E. lock algorithm

Possible ?

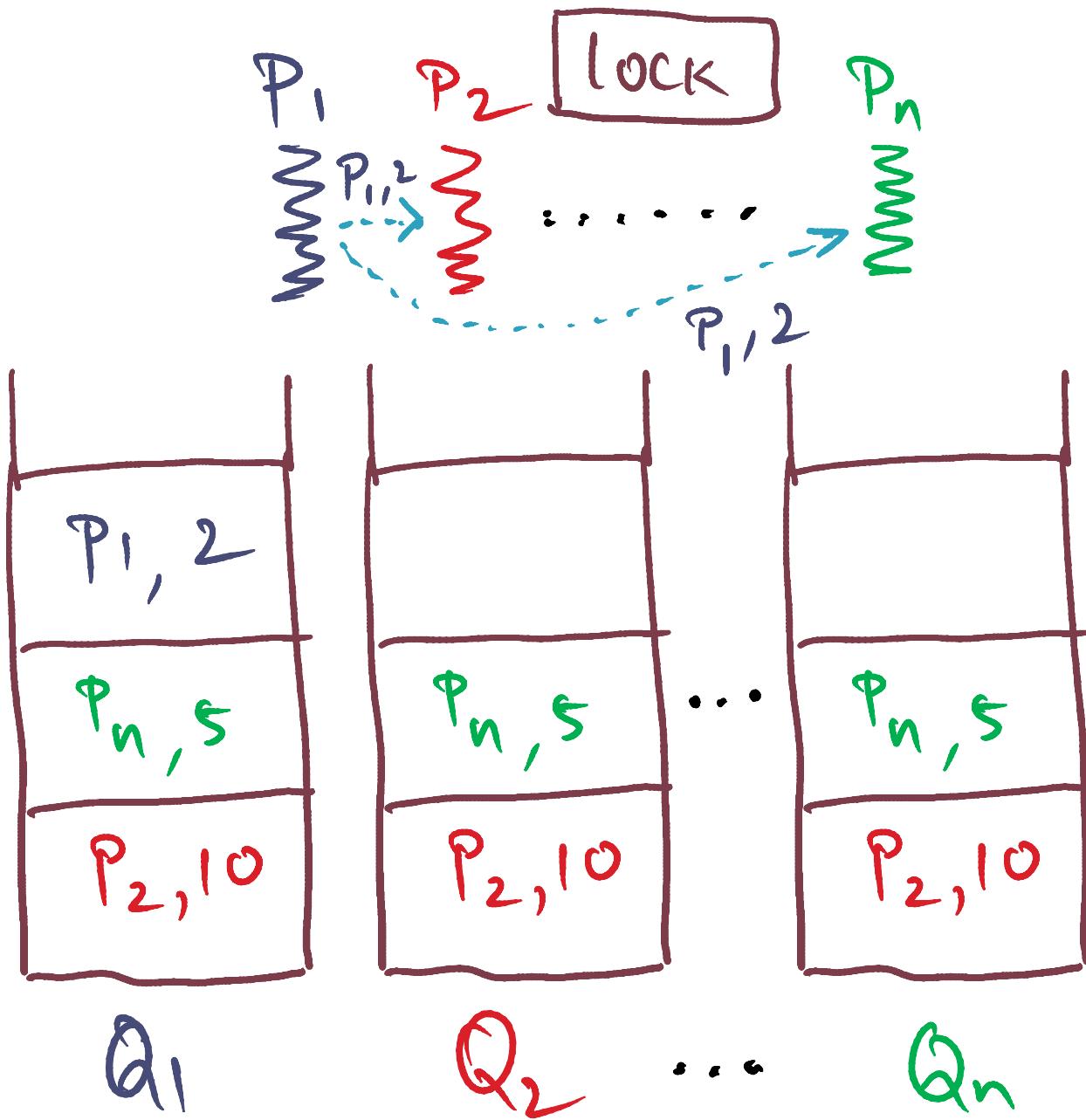


## Distributed M.E. lock algorithm



Possible ?  
\*  $P_i$ 's msg in transit  
†  $P_i$  received  $P_2$ 's &  $P_n$ 's subsequently

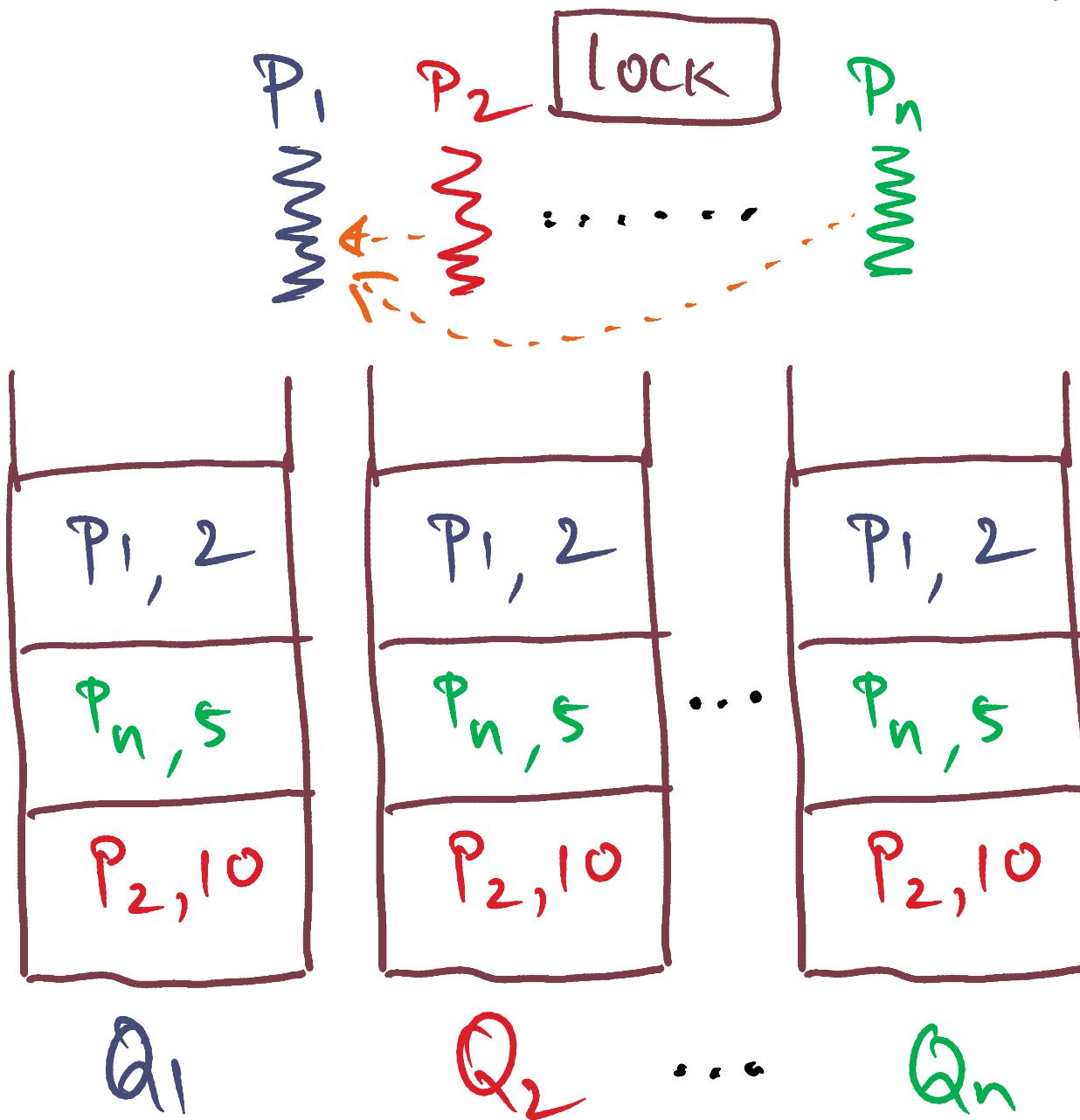
## Distributed M.E. lock algorithm



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\*  $P_i$ 's msg in transit  
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Do I have it?

## Distributed M.E. lock algorithm



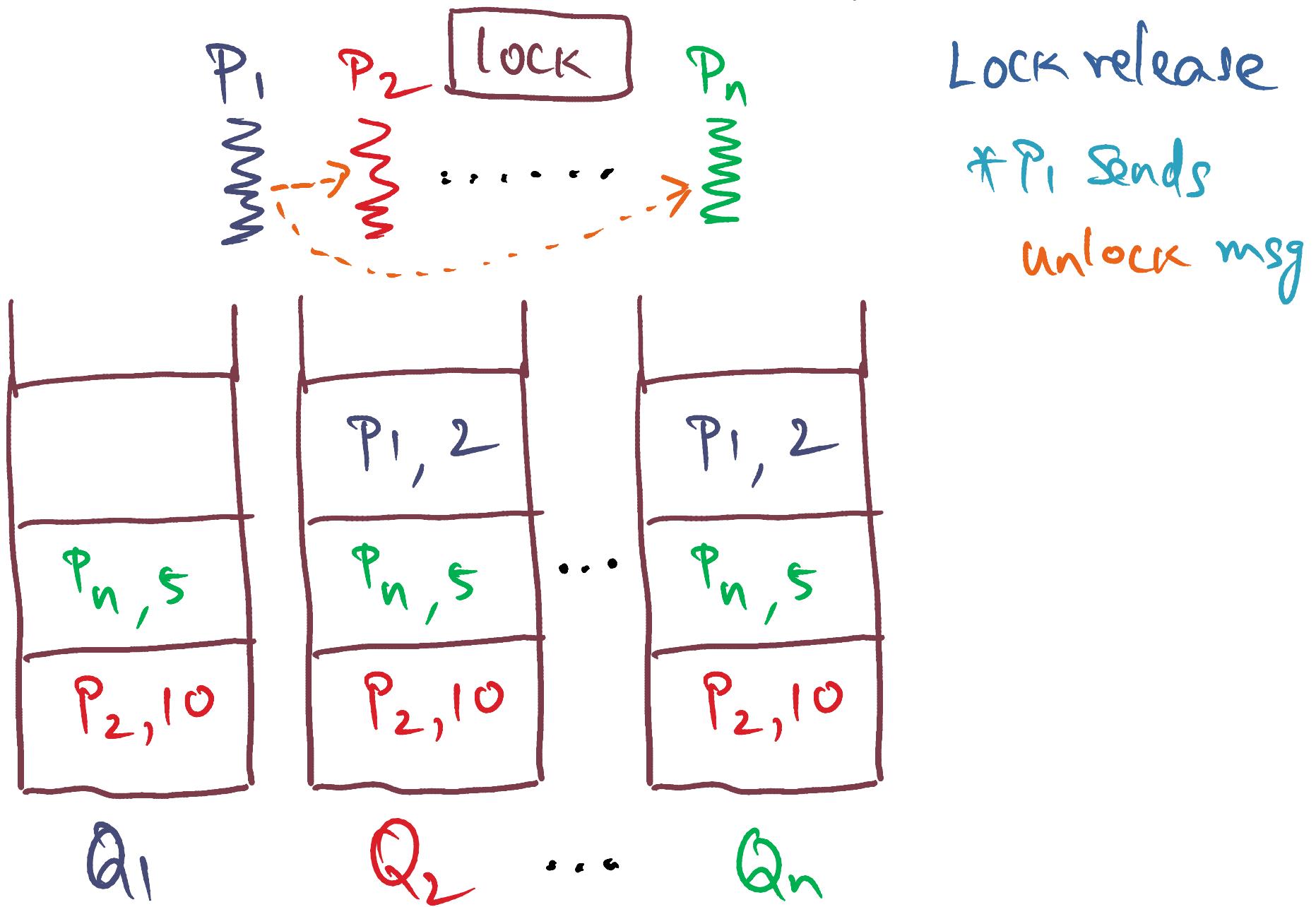
Possible ?

- \*  $P_i$ 's msg in transit
- \*  $P_i$  received  $P_2$ 's &  $P_n$ 's subsequently

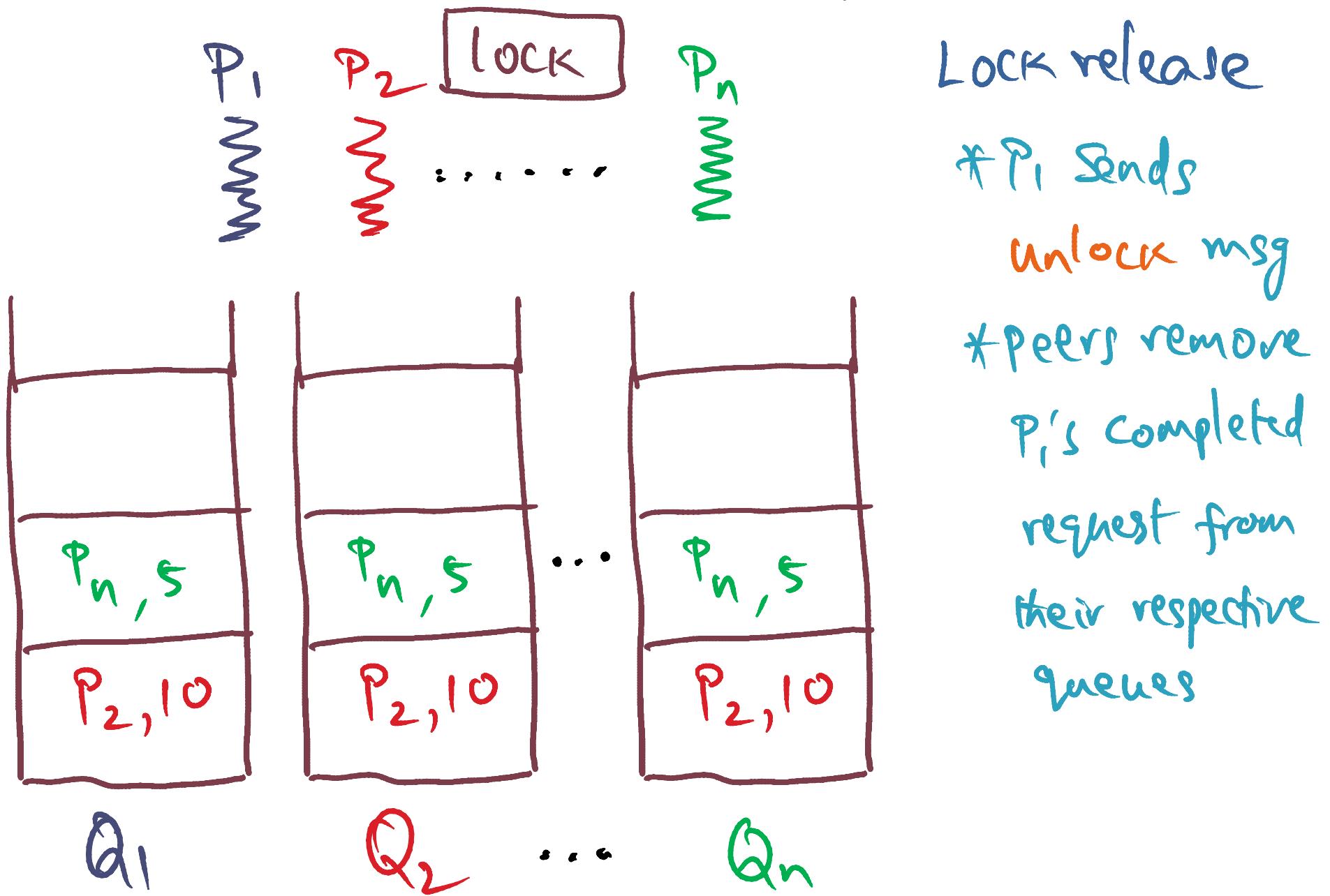
Do I have it?

- \* top of my Q
- \* ACK from others or later lock reqs

# Distributed M.E. lock algorithm



# Distributed M.E. lock algorithm



## Distributed M.E. lock algorithm

Correctness 2

- \* msgs arrive in order
- \* no message loss
- \* Q's totally ordered  $\Rightarrow$  by Lamport's  
Logical clocks plus PID to break ties

## Distributed M.E. lock algorithm

Correctness ?

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Logical clocks plus PID to break ties

message complexity ?

## Message Complexity

LOCK(L)  $\Rightarrow$  N-1 req msgs

⋮  
N-1 ACK msgs

unlock(L)  $\Rightarrow$  N-1 unlock msgs

Total  $3(N-1)$

## Message Complexity

LOCK(L)  $\Rightarrow$  N-1 req msgs

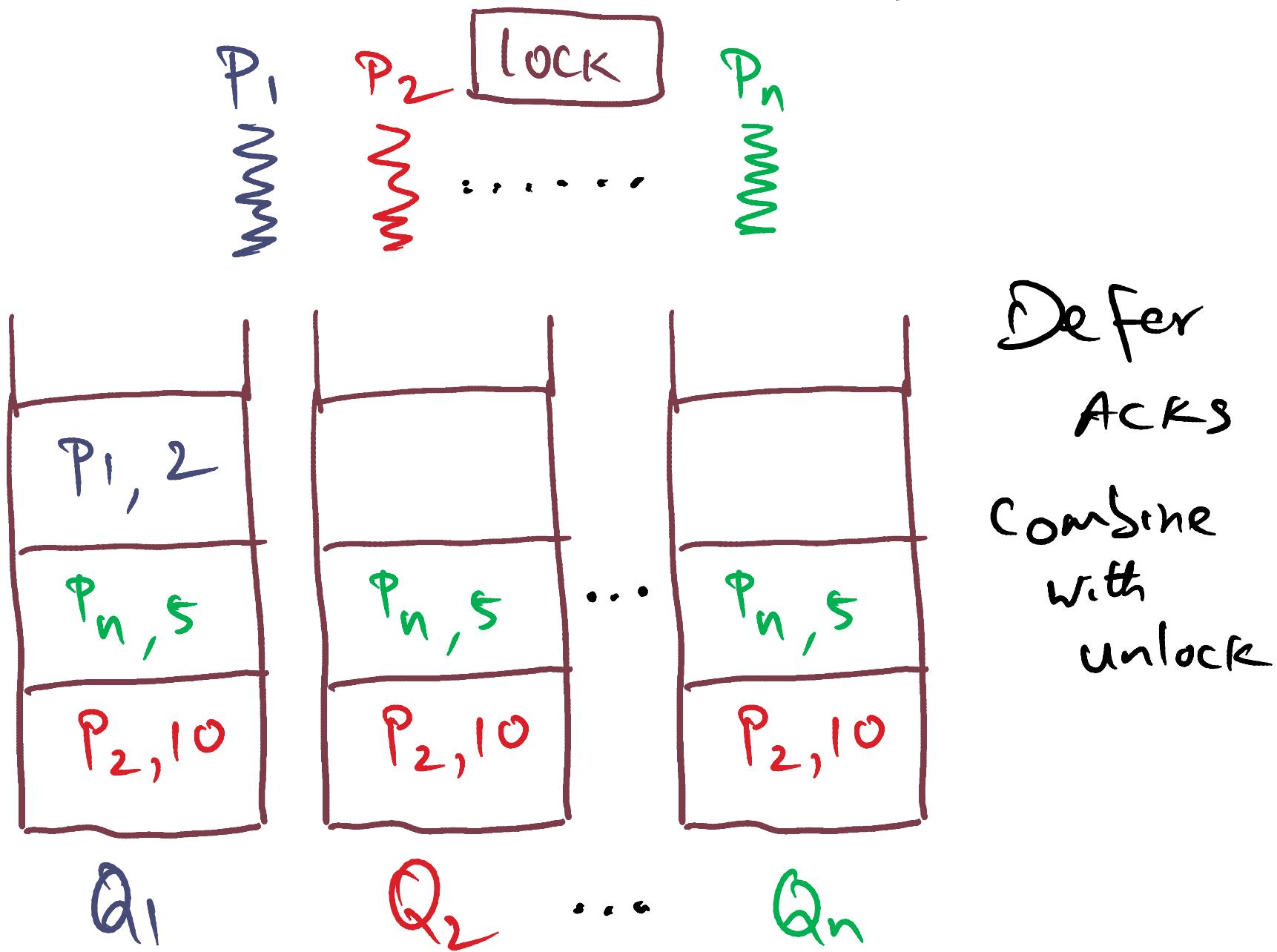
⋮  
N-1 ACK msgs

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Total  $3(N-1)$

Can we do better?

# Distributed M.E. lock algorithm



## Message Complexity

LOCK(L)  $\Rightarrow$  N-1 req msgs

⋮  
N-1 ACK msgs

unlock(L)  $\Rightarrow$  N-1 unlock msgs

Total  $3(N-1)$

Can we do better?

\* defer ACKS if my req precedes yours

$\Rightarrow$  combine with unlock  $\Rightarrow 2(N-1)$

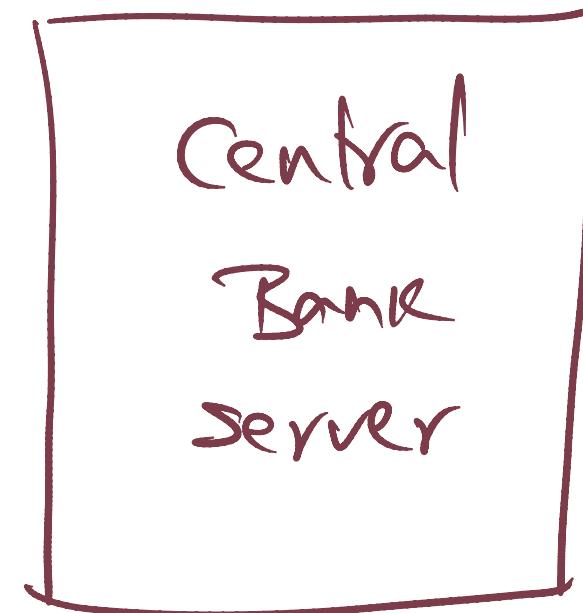
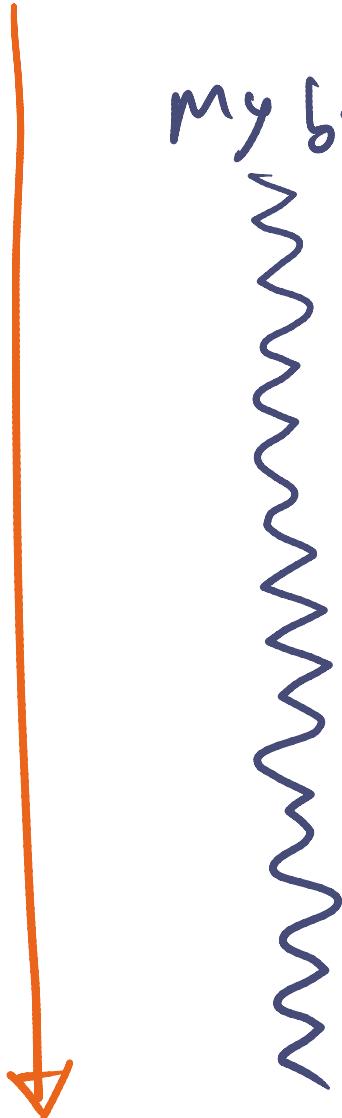
## Real world scenario

real time

my branch

your branch

Out of band  
me  you



## Real world scenario

real time

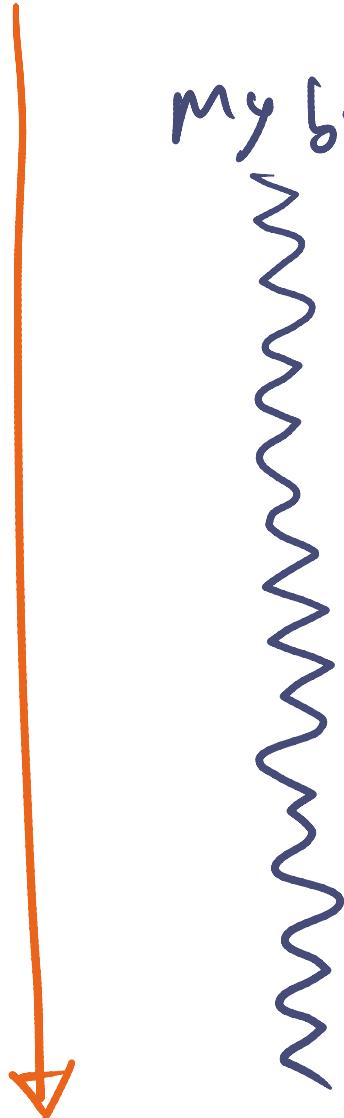
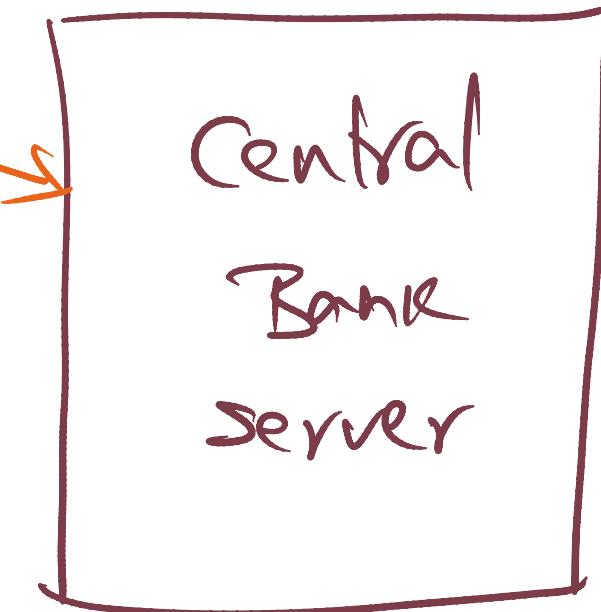
my branch

your branch

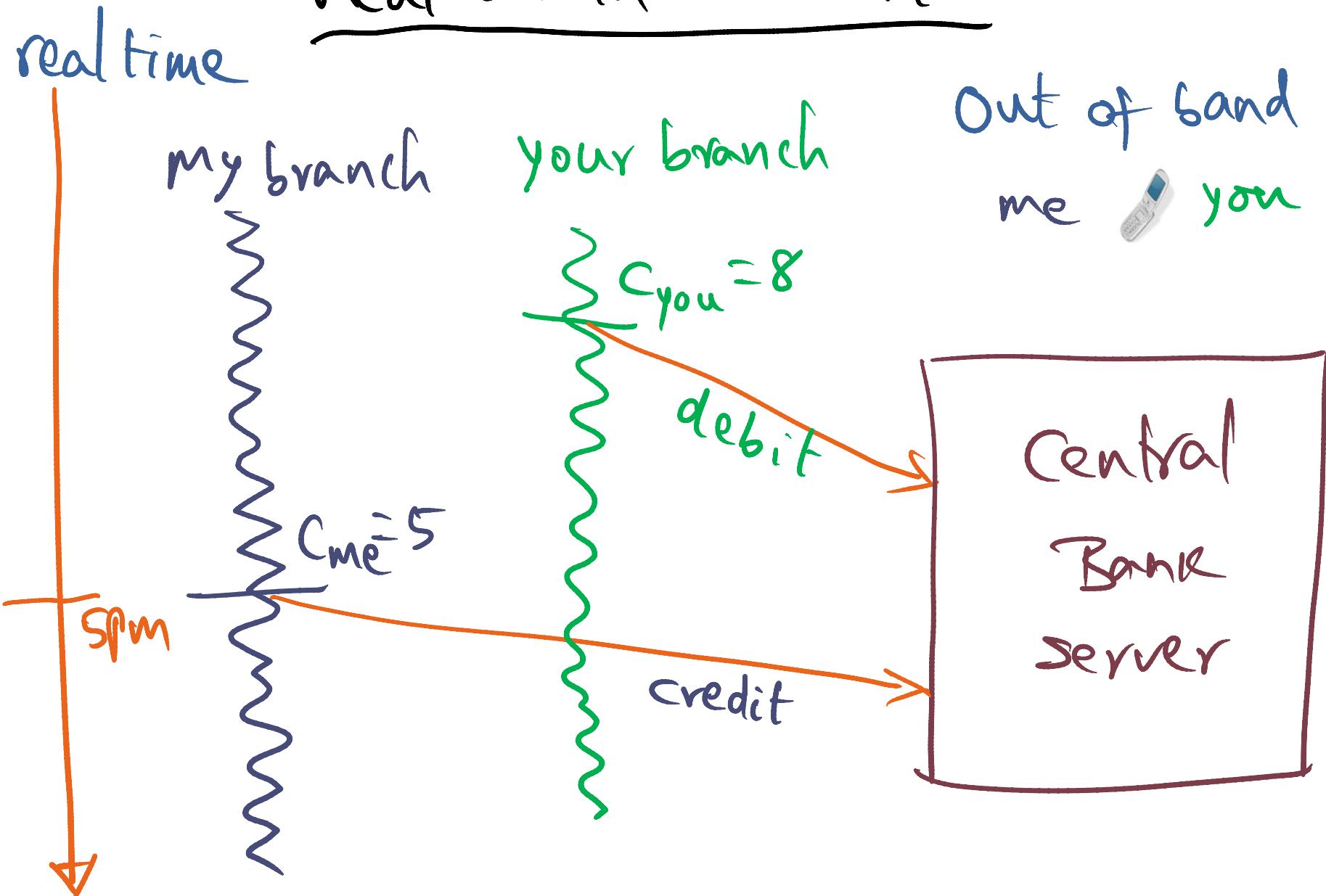
Out of band  
me  you

$c_{you} = 8$

debit

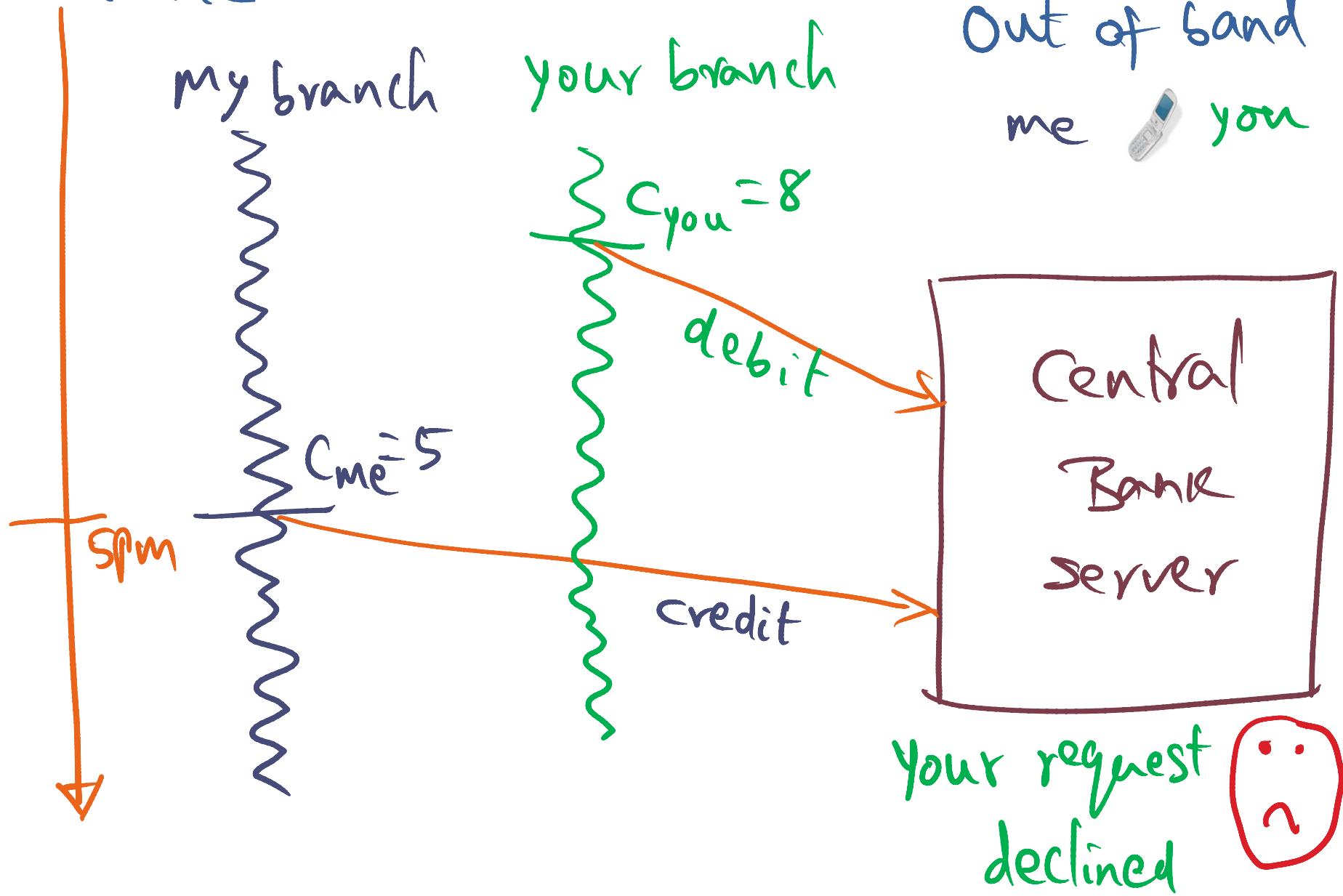


## Real world scenario



## Real world scenario

real time



# Lamport's Physical clock

$a \rightarrow b$

$$\Rightarrow c_i(a) < c_j(b)$$

$$c_i(t) \xrightarrow{a} \begin{cases} p_i \\ p_j \end{cases} \quad \left. \begin{array}{l} c_i(t) \\ c_j(t) \end{array} \right\} s_j(t)$$

Physical clock conditions :

1) PC1 (bound on individual clock drift)

$$\left( \frac{\frac{dc_i(t)}{dt}}{1} - 1 \right) < \kappa \quad \forall i; (\kappa \ll 1)$$

2) PC2 (bound on mutual drift)

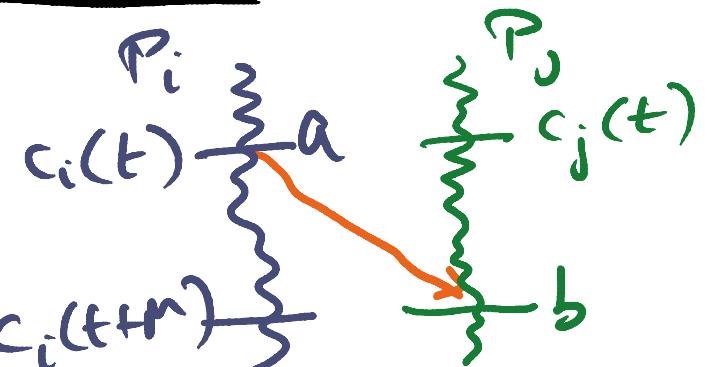
$$\forall i, j: |c_i(t) - c_j(t)| < \epsilon$$

## IPC time and clock drift

Let  $\mu$  be lower bound on IPC

To avoid anomalies if

a on  $P_i \mapsto b$  on  $P_j$



1)  $c_i(t+\mu) - c_j(t) > 0$

2)  $c_i(t+\mu) - c_i(t) > \mu(1-\kappa)$

(difference equation formulation of PC1) ~~PC2~~

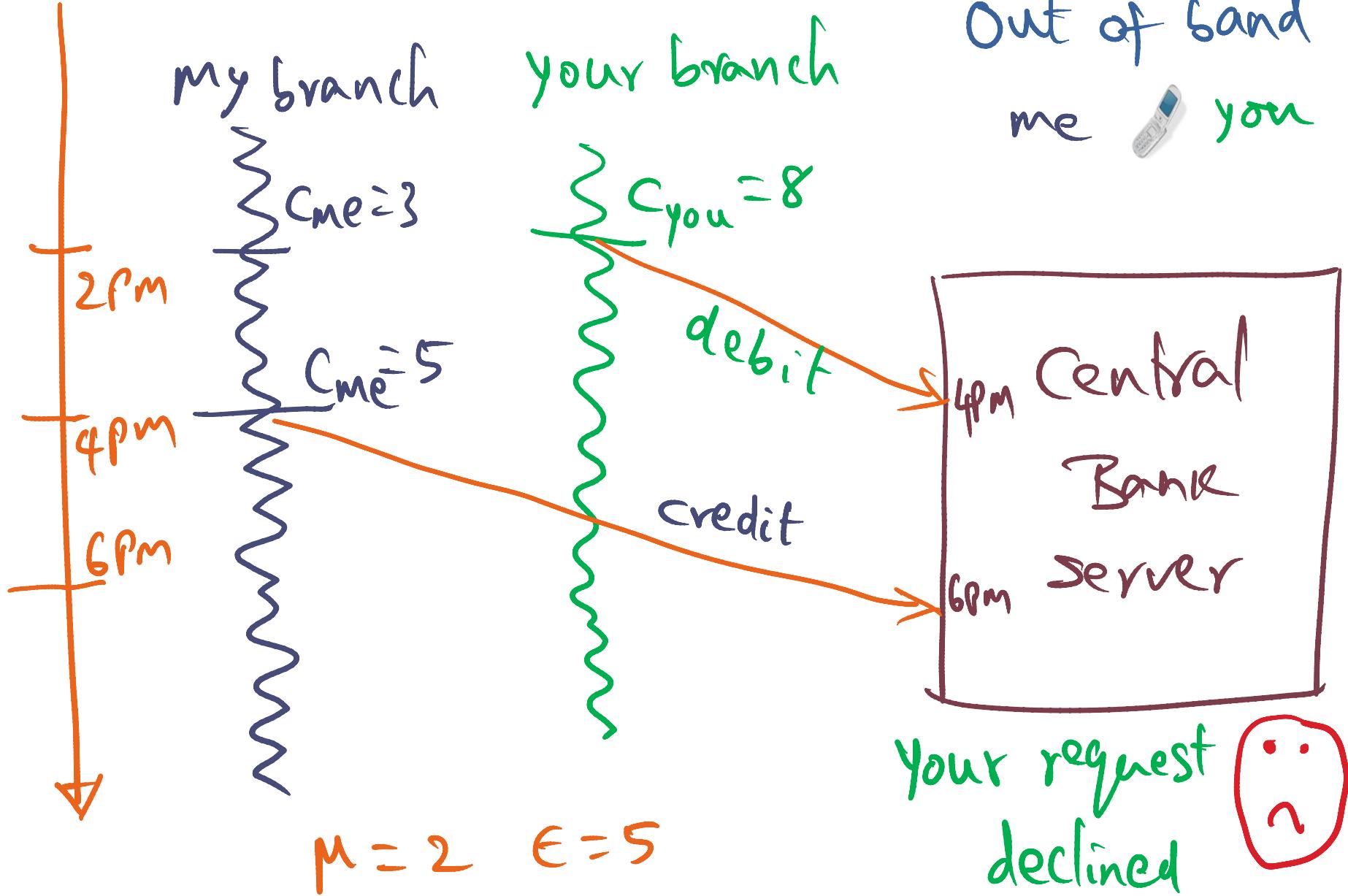
Using ① + ② and sound  $\in$  on mutual drift

$$\mu \geq \epsilon / (1 - \kappa)$$

to avoid anomalies

## Real world scenario

real time



## Real world scenario

