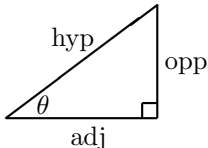


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<p>DEFINITION</p> <p><i>absolute value</i></p> <p>CALCULUS I</p>	<p>THEOREM</p> <p><i>properties of absolute values</i></p> <p>CALCULUS I</p>
<p>DEFINITION</p> <p><i>equation of a line in various forms</i></p> <p>CALCULUS I</p>	<p>DEFINITION</p> <p><i>equation of a circle</i></p> <p>CALCULUS I</p>
<p>DEFINITION</p> <p>sin, cos, tan</p> <p>CALCULUS I</p>	<p>DEFINITION</p> <p>sec, csc, tan, cot</p> <p>CALCULUS I</p>
<p>DEFINITION</p> <p><i>midpoint formula</i></p> <p>CALCULUS I</p>	<p>DEFINITION</p> <p><i>function</i></p> <p>CALCULUS I</p>

<p>The solutions or roots of the quadratic equation $ax^2 + bx + c = 0$ are given by</p> $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$	<p>These flashcards and the accompanying \LaTeX source code are licensed under a Creative Commons Attribution–NonCommercial–ShareAlike 2.5 License. For more information, see creativecommons.org. You can contact the author at:</p> <p style="text-align: center;">jasonu at physics utah edu</p> <p style="text-align: center;">File last updated on Wednesday 17th May, 2017, at 09:03</p>										
<ol style="list-style-type: none"> $ab = a b$ $\left \frac{a}{b}\right = \frac{ a }{ b }$ $a + b \leq a + b$ $a - b \geq a - b$ 	$ x = \begin{cases} x & x \geq 0 \\ -x & x < 0 \end{cases}$										
<p>The equation of a circle centered at (h, k) with radius r is:</p> $(x - h)^2 + (y - k)^2 = r^2$	<table> <tr> <th>Form</th><th>Equation</th></tr> <tr> <td>point–slope</td><td>$y - y_1 = m(x - x_1)$</td></tr> <tr> <td>slope–intercept</td><td>$y = mx + b$</td></tr> <tr> <td>two point</td><td>$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1}(x - x_1)$</td></tr> <tr> <td>standard</td><td>$Ax + By + C = 0$</td></tr> </table>	Form	Equation	point–slope	$y - y_1 = m(x - x_1)$	slope–intercept	$y = mx + b$	two point	$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1}(x - x_1)$	standard	$Ax + By + C = 0$
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$\sec \theta = \frac{1}{\cos \theta} \quad \csc \theta = \frac{1}{\sin \theta}$ $\tan \theta = \frac{\sin \theta}{\cos \theta} \quad \cot \theta = \frac{\cos \theta}{\sin \theta}$	<div style="display: flex; align-items: center;">  <div style="margin-left: 20px;"> $\sin \theta = \frac{\text{opp}}{\text{hyp}}$ $\cos \theta = \frac{\text{adj}}{\text{hyp}}$ $\tan \theta = \frac{\text{opp}}{\text{adj}}$ </div> </div>										
<p>A function is a mapping that associates with each object x in one set, which we call the domain, a single value $f(x)$ from a second set which we call the range.</p>	<p>If $P(x_1, y_1)$ and $Q(x_2, y_2)$ are two points, then the mid-point of the line segment that joins these two points is given by:</p> $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$										

<p>DEFINITION</p> <p><i>even and odd functions</i></p> <p>CALCULUS I</p>	<p>DEFINITION</p> <p><i>limit</i></p> <p>CALCULUS I</p>
<p>DEFINITION</p> <p><i>one-sided limit</i></p> <p>CALCULUS I</p>	<p>THEOREM</p> <p><i>limit exists iff both the right-handed and left-handed limits exist and are equal</i></p> <p>CALCULUS I</p>
<p>THEOREM</p> <p><i>main limit theorem (part 1)</i></p> <p>CALCULUS I</p>	<p>THEOREM</p> <p><i>main limit theorem (part 2)</i></p> <p>CALCULUS I</p>
<p>THEOREM</p> <p><i>squeeze theorem</i></p> <p>CALCULUS I</p>	<p>THEOREM</p> <p><i>two special trigonometric limits</i></p> <p>CALCULUS I</p>
<p>DEFINITION</p> <p><i>point-wise continuity</i></p> <p>CALCULUS I</p>	<p>THEOREM</p> <p><i>composition limit theorem</i></p> <p>CALCULUS I</p>

<p>If a function $f(x)$ is defined on an open interval containing c, except possibly at c, then the limit of $f(x)$ as x approaches c equals L is denoted</p> $\lim_{x \rightarrow c} f(x) = L$ <p>The above equality holds if and only if for any $\varepsilon > 0$ there exists a $\delta > 0$ such that</p> $0 < x - c < \delta \Rightarrow f(x) - L < \varepsilon$	<p>even $f(-x) = f(x)$ for all x e.g. $x^2, \cos(x)$</p> <p>odd $f(-x) = -f(x)$ for all x e.g. $x, \sin(x)$</p>
$\lim_{x \rightarrow c} f(x) = L \Leftrightarrow \lim_{x \rightarrow c^+} f(x) = \lim_{x \rightarrow c^-} f(x) = L$	<p>right-handed limit</p> $\lim_{x \rightarrow c^+} f(x) = L$ <p>iff for any $\varepsilon > 0$ there exists a δ such that</p> $0 < x - c < \delta \Rightarrow f(x) - L < \varepsilon$
<p>Let f, g be functions that have limits at c, and let n be a positive integer.</p> <p>7. $\lim_{x \rightarrow c} \frac{f(x)}{g(x)} = \frac{\lim_{x \rightarrow c} f(x)}{\lim_{x \rightarrow c} g(x)}$ if $\lim_{x \rightarrow c} g(x) \neq 0$</p> <p>8. $\lim_{x \rightarrow c} [f(x)]^n = [\lim_{x \rightarrow c} f(x)]^n$</p> <p>9. $\lim_{x \rightarrow c} \sqrt[n]{f(x)} = \sqrt[n]{\lim_{x \rightarrow c} f(x)}$ provided that $\lim_{x \rightarrow c} f(x) > 0$ when n is even.</p>	<p>Let k be a constant, and f, g be functions that have limits at c.</p> <ol style="list-style-type: none"> $\lim_{x \rightarrow c} k = k$ $\lim_{x \rightarrow c} x = c$ $\lim_{x \rightarrow c} kf(x) = k \lim_{x \rightarrow c} f(x)$ $\lim_{x \rightarrow c} [f(x) + g(x)] = \lim_{x \rightarrow c} f(x) + \lim_{x \rightarrow c} g(x)$ $\lim_{x \rightarrow c} [f(x) - g(x)] = \lim_{x \rightarrow c} f(x) - \lim_{x \rightarrow c} g(x)$ $\lim_{x \rightarrow c} [f(x) \cdot g(x)] = \lim_{x \rightarrow c} f(x) \cdot \lim_{x \rightarrow c} g(x)$
$\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$ $\lim_{x \rightarrow 0} \frac{1 - \cos x}{x} = 0$	<p>Suppose f, g and h are functions which satisfy the inequality $f(x) \leq g(x) \leq h(x)$ for all x near c, (except possibly at c). Then</p> $\lim_{x \rightarrow c} f(x) = \lim_{x \rightarrow c} h(x) = L \Rightarrow \lim_{x \rightarrow c} g(x) = L$
<p>If $\lim_{x \rightarrow c} g(x) = L$ and f is continuous at L, then</p> $\lim_{x \rightarrow c} f(g(x)) = f(\lim_{x \rightarrow c} g(x)) = f(L)$	<p>Let f be defined on an open interval containing c, then we say that f is point-wise continuous at c if</p> $\lim_{x \rightarrow c} f(x) = f(c)$

<p>DEFINITION</p> <p><i>continuity on an interval</i></p> <p>CALCULUS I</p>	<p>DEFINITION</p> <p><i>derivative</i></p> <p>CALCULUS I</p>
<p>DEFINITION</p> <p><i>equivalent form for the derivative</i></p> <p>CALCULUS I</p>	<p>THEOREM</p> <p><i>differentiability and continuity</i></p> <p>CALCULUS I</p>
<p>THEOREM</p> <p><i>constant and power rules</i></p> <p>CALCULUS I</p>	<p>THEOREM</p> <p><i>differentiation rules</i></p> <p>CALCULUS I</p>
<p>THEOREM</p> <p><i>derivatives of trig functions</i></p> <p>CALCULUS I</p>	<p>THEOREM</p> <p><i>chain rule</i></p> <p>CALCULUS I</p>
<p>THEOREM</p> <p><i>generalized power rule</i></p> <p>CALCULUS I</p>	<p>DEFINITION</p> <p><i>notation for higher-order derivatives</i></p> <p>CALCULUS I</p>

<p>The derivative of a function f is another function f' (read “f prime”) whose value at x is</p> $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ <p>provided the limit exists and is not ∞ or $-\infty$.</p>	<p>A function f is said to be continuous on an open interval iff f is continuous at every point of the open interval.</p> <p>A function f is said to be continuous on a closed interval $[a, b]$ iff</p> <ol style="list-style-type: none">1. f is continuous on (a, b) and2. $\lim_{x \rightarrow a^+} f(x) = f(a)$ and3. $\lim_{x \rightarrow b^-} f(x) = f(b)$																																			
<p>If the function f is differentiable at c, then f is continuous at c.</p>	$f'(c) = \lim_{x \rightarrow c} \frac{f(x) - f(c)}{x - c}$																																			
<p>Let f and g be functions of x and k a constant.</p> <ol style="list-style-type: none">1. scalar product rule $(kf)' = kf'$2. sum rule $(f + g)' = f' + g'$3. difference rule $(f - g)' = f' - g'$4. product rule $(fg)' = f'g + fg'$5. quotient rule $\left(\frac{f}{g}\right)' = \frac{f'g - g'f}{g^2}$	$\begin{array}{ll} f(x) = k & f'(x) = 0 \\ f(x) = x & f'(x) = 1 \\ f(x) = x^n & f'(x) = nx^{n-1} \end{array}$																																			
<p>Let $u = g(x)$ and $y = f(u)$. If g is differentiable at x, and f is differentiable at $u = g(x)$, then the composite function $(f \circ g)(x) = f(g(x))$ is differentiable at x and</p> $(f \circ g)'(x) = f'(g(x))g'(x)$ <p>In Leibniz notation</p> $\frac{dy}{dx} = \frac{dy}{du} \frac{du}{dx}$	$\begin{array}{l} (\sin x)' = \cos x \\ (\cos x)' = -\sin x \\ (\tan x)' = \sec^2 x \\ (\cot x)' = -\csc^2 x \\ (\sec x)' = \sec x \tan x \\ (\csc x)' = -\csc x \cot x \end{array}$																																			
<table><tr><th>Derivative</th><th>$f'(x)$</th><th>y'</th><th>D</th><th>Leibniz</th></tr><tr><td>first</td><td>$f'(x)$</td><td>y'</td><td>$D_x y$</td><td>$\frac{dy}{dx}$</td></tr><tr><td>second</td><td>$f''(x)$</td><td>y''</td><td>$D_x^2 y$</td><td>$\frac{d^2 y}{dx^2}$</td></tr><tr><td>third</td><td>$f'''(x)$</td><td>y'''</td><td>$D_x^3 y$</td><td>$\frac{d^3 y}{dx^3}$</td></tr><tr><td>fourth</td><td>$f^{(4)}(x)$</td><td>$y^{(4)}$</td><td>$D_x^4 y$</td><td>$\frac{d^4 y}{dx^4}$</td></tr><tr><td>\vdots</td><td>\vdots</td><td>\vdots</td><td>\vdots</td><td>\vdots</td></tr><tr><td>nth</td><td>$f^{(n)}(x)$</td><td>$y^{(n)}$</td><td>$D_x^n y$</td><td>$\frac{d^n y}{dx^n}$</td></tr></table>	Derivative	$f'(x)$	y'	D	Leibniz	first	$f'(x)$	y'	$D_x y$	$\frac{dy}{dx}$	second	$f''(x)$	y''	$D_x^2 y$	$\frac{d^2 y}{dx^2}$	third	$f'''(x)$	y'''	$D_x^3 y$	$\frac{d^3 y}{dx^3}$	fourth	$f^{(4)}(x)$	$y^{(4)}$	$D_x^4 y$	$\frac{d^4 y}{dx^4}$	\vdots	\vdots	\vdots	\vdots	\vdots	nth	$f^{(n)}(x)$	$y^{(n)}$	$D_x^n y$	$\frac{d^n y}{dx^n}$	<p>If f is a differentiable function and n is an integer, then the power of the function</p> $y = [f(x)]^n$ <p>is differentiable and</p> $\frac{dy}{dx} = n[f(x)]^{n-1} f'(x)$
Derivative	$f'(x)$	y'	D	Leibniz																																
first	$f'(x)$	y'	$D_x y$	$\frac{dy}{dx}$																																
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<p>THEOREM</p> <p><i>extreme value theorem</i></p> <p>CALCULUS I</p>	<p>THEOREM</p> <p><i>intermediate value theorem</i></p> <p>CALCULUS I</p>
<p>DEFINITION</p> <p><i>critical point</i> <i>stationary point</i> <i>singular point</i></p> <p>CALCULUS I</p>	<p>DEFINITION</p> <p><i>increasing</i> <i>decreasing</i> <i>monotonic</i></p> <p>CALCULUS I</p>
<p>THEOREM</p> <p><i>monotonicity theorem</i></p> <p>CALCULUS I</p>	<p>DEFINITION</p> <p><i>concave up</i> <i>concave down</i></p> <p>CALCULUS I</p>
<p>THEOREM</p> <p><i>concavity theorem</i></p> <p>CALCULUS I</p>	<p>DEFINITION</p> <p><i>inflection point</i></p> <p>CALCULUS I</p>
<p>DEFINITION</p> <p><i>local maximum</i> <i>local minimum</i> <i>local extremum</i></p> <p>CALCULUS I</p>	<p>THEOREM</p> <p><i>first derivative test</i></p> <p>CALCULUS I</p>

<p>If the function f is continuous on the closed interval $[a, b]$ and v is any value between the minimum and maximum of f on $[a, b]$, then f takes on the value v.</p>	<p>If the function f is continuous on the closed interval $[a, b]$, then f has a maximum value and a minimum value on the interval $[a, b]$.</p>
<p>A function f defined on the interval I is</p> <ul style="list-style-type: none"> • increasing on $I \Leftrightarrow$ for every $x_1, x_2 \in I$ $x_1 < x_2 \Rightarrow f(x_1) < f(x_2)$ • decreasing on $I \Leftrightarrow$ for every $x_1, x_2 \in I$ $x_1 < x_2 \Rightarrow f(x_1) > f(x_2)$ <p>The function f is said to be monotonic on I if f is either increasing or decreasing on I.</p>	<p>If f is a function defined on an open interval containing the point c, we call c a critical point of f iff either</p> <ul style="list-style-type: none"> • $f'(c) = 0$ or • $f'(c)$ does not exist <p>Furthermore when $f'(c) = 0$ we call c a stationary point of f, and when $f'(c)$ does not exist we call c a singular point of f.</p>
<p>Suppose f is differentiable on an open interval I, then if f' is increasing on I we say that f is concave up on I.</p> <p>If f' is decreasing on I we say that f is concave down on I.</p>	<p>Suppose f is differentiable on an open interval I, then</p> <ul style="list-style-type: none"> • $f'(x) > 0$ for each $x \in I \Rightarrow f$ is increasing on I • $f'(x) < 0$ for each $x \in I \Rightarrow f$ is decreasing on I
<p>Let f be continuous at c, then the ordered pair $(c, f(c))$ is called an inflection point of f if f is concave up on one side of c and concave down on the other side of c.</p>	<p>Let f be twice differentiable on the open interval I.</p> <ul style="list-style-type: none"> • $f''(x) > 0$ for each $x \in I \Rightarrow$ f is concave up on I • $f''(x) < 0$ for each $x \in I \Rightarrow$ f is concave down on I
<p>Let f be differentiable on an open interval (a, b) that contains c.</p> <ol style="list-style-type: none"> 1. $f'(x) > 0 \ \forall x \in (a, c)$ and $f'(x) < 0 \ \forall x \in (c, b) \Rightarrow f(c)$ is a local maximum of f. 2. $f'(x) < 0 \ \forall x \in (a, c)$ and $f'(x) > 0 \ \forall x \in (c, b) \Rightarrow f(c)$ is a local minimum of f. 3. If $f'(x)$ has the same sign on both sides of c, then $f(c)$ is not a local extremum. 	<p>Let the function f be defined on an interval I containing c. We say f has a local maximum at c iff there exists an interval (a, b) containing c such that $f(x) \leq f(c)$ for all $x \in (a, b)$.</p> <p>We say f has a local minimum at c iff there exists an interval (a, b) containing c such that $f(x) \geq f(c)$ for all $x \in (a, b)$.</p> <p>A local extremum is either a local maximum or a local minimum.</p>

THEOREM	THEOREM
<i>second derivative test</i>	<i>mean value theorem</i>
CALCULUS I	CALCULUS I
CALCULUS I	CALCULUS I
CALCULUS I	CALCULUS I
CALCULUS I	CALCULUS I
CALCULUS I	CALCULUS I

<p>If f is continuous on a closed interval $[a, b]$ and differentiable on its interior (a, b), then there is at least one point c in (a, b) such that</p> $\frac{f(b) - f(a)}{b - a} = f'(c)$ <p>or equivalently</p> $f(b) - f(a) = f'(c)(b - a)$	<p>Let f be twice differentiable on an open interval containing c, and suppose $f'(c) = 0$.</p> <ol style="list-style-type: none">1. If $f''(c) < 0$, then f has a local maximum at c.2. If $f''(c) > 0$, then f has a local minimum at c.3. If $f''(c) = 0$, then the test fails.