

# Assignment 4

Emil Hafeez (eh2928)

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```
knee_df =  
  read_csv(  
    "./data/Knee.csv") #load in df  
  
## Parsed with column specification:  
## cols(  
##   Below = col_double(),  
##   Average = col_double(),  
##   Above = col_double()  
## )
```

## Problem 1

In the context of ANOVA models, prove the partitioning of the total variability (sum of squares).

$$\sum_{i=1}^k \sum_{j=1}^{n_i} (y_{ij} - \bar{y})^2 = \sum_{i=1}^k \sum_{j=1}^{n_i} (y_{ij} - \bar{y}_i)^2 + \sum_{i=1}^k \sum_{j=1}^{n_i} (\bar{y}_i - \bar{y})^2 \quad (1)$$

We assume that the samples are drawn independently from the underlying populations, that the distributions of the error terms are normal, and that the variances of the  $k$  populations are equal (and thus that the variance of the outcome does not depend on the sample).

Let  $n$  be the total number of observations

Let  $\bar{y}$  be the mean from the  $i^{th}$  group

Let  $\bar{\bar{y}}$  be the grand mean, such that  $\bar{\bar{y}} = \frac{\sum_{i=1}^k \sum_{j=1}^{n_i} y_{ij}}{n}$