Assignment 4

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```
knee_df =
   read_csv(
        "./data/Knee.csv") #load in df

## Parsed with column specification:
## cols(
## Below = col_double(),
## Average = col_double(),
## Above = col_double()
## above = col_double()
```

Problem 1

In the context of ANOVA models, prove the partitioning of the total variability (sum of squares).

$$\sum_{i=1}^{k} \sum_{j=1}^{n_i} (y_{ij} - \overline{\bar{y}})^2 = \sum_{i=1}^{k} \sum_{j=1}^{n_i} (y_{ij} - \bar{y}_l)^2 + \sum_{i=1}^{k} \sum_{j=1}^{n_i} (\bar{y}_i - \overline{\bar{y}})^2$$
(1)

We assume that the samples are drawn independently from the underlying populations, that the distributions of the error terms are normal, and that the variances of the k populations are equal (and thus that the variance of the outcome does not depend on the sample).

Let n be the total number of observations Let \bar{y} be the mean from the i^{th} group. Let \bar{y}_i be the grand mean, such that $\bar{\bar{y}} = \frac{\sum_{i=1}^k \sum_{j=1}^{n_i} y_{ij}}{n}$ Let $\bar{\bar{y}}$