

Capital Controls and Free Trade Agreements

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The views expressed here do not necessarily reflect the position of the Bank of England.

Trade & Financial Openness: Not Always Aligned

- *Bretton Woods*: Free trade promoted, but capital controls widely used
- *Post-Bretton Woods*: Increased trade and more financial openness
- *Recent Years*:
 - Growing protectionism (China-US trade war; Brexit; export restrictions post-Covid)
 - More sanguine views on capital controls (IMF's Integrated Policy Framework) and increasing 'macroprudential FX regulation'

How does conduct of capital controls change in a world with less free trade?

This Paper: Trade-Finance Nexus

- Optimal capital controls \leftrightarrow free trade agreements (FTAs) / import tariffs
 - How does trade policy influence optimal capital controls?
 - How do domestic welfare gains, and spillovers, from capital controls depend on trade policy?
- Simple theoretical framework: two-country endowment economy (Home and Foreign) with terms-of-trade externality
 - Ramsey planner (Unilateral & Nash) maximises welfare, manipulating interest rates and relative prices using capital flow taxes and:
 - i. with FTA in place; or
 - ii. absent FTA, with optimal import tariff

► Related Literature

Key Findings

Cannot separate discussions of **capital controls** and **trade protectionism**.

1. Policy prescriptions around **trade** and **financial** openness interlinked.
 - **With FTA**, optimal capital controls stabilise balance of payments
 - **Without FTA**, optimal capital controls and tariffs stabilise terms of trade/real exchange rate
2. Accounting for strategic interactions across countries:
 - **Capital controls** more prevalent in the absence of a FTA
 - **Capital control wars** more prevalent if intertemporal elasticity low, **tariff wars** if intratemporal elasticity low
3. In **absence of FTA**, **domestic gains from optimal capital controls are small**, but **spillovers are large**

Model

Model-in-a-Slide

- Countries: Home H and Foreign F (*). Goods: 1 and 2.
- Time: $t = 0, 1, \dots, \infty$. No uncertainty. Zero assets at $t = 0$
- Preferences: $U_0 = \sum_{t=0}^{\infty} \beta^t u(C_t)$, where $\beta \in (0, 1)$, C_t aggregate consumption, and $u(C) = \frac{C^{1-\sigma}-1}{1-\sigma}$ with $\sigma > 0$
- Households consume both goods 1 and 2:

$$C_t \equiv g(\mathbf{c}_t) = \left[\alpha_1^{\frac{1}{\phi}} c_{1,t}^{\frac{\phi-1}{\phi}} + (1 - \alpha_1)^{\frac{1}{\phi}} c_{2,t}^{\frac{\phi-1}{\phi}} \right]^{\frac{\phi}{\phi-1}}$$

where $\mathbf{c}_t = [c_{1,t}, c_{2,t}]$, $\alpha_1 \in (0.5, 1]$, and $\phi > 0$ is ‘elasticity of trade’

- Country endowments: $\mathbf{y}_t^{(*)} = [y_{1,t}^{(*)}, y_{2,t}^{(*)}]$
- Real Exchange Rate $Q = \frac{P^*}{P}$ and Terms of Trade $S = \frac{p_2}{p_1}$

Key Friction: Terms-of-Trade Externality

- Large countries affect prices when making consumption decisions,
i.e. $\frac{dC^*}{dC} \neq 0$, $\frac{dc_1^*}{dc_1} \neq 0$ [Geanakoplos and Polemarchakis, 1986]

⇒ Planner incentives to exercise monopoly/monopsony power [Costinot et al, 2014]

- **Inter-temporal:**

Faster growth → Larger future trade surplus (ie future seller)

→ Incentive to increase future consumption

→ Promote domestic saving today (eg capital inflow tax)

- **Intra-temporal:**

Faster gr. of good sold abroad → Incentive to increase future price

→ If home bias, can increase consumption

→ Promote saving today (eg inflow tax) /
increase good cons. in future (eg tariffs)

Unilateral Home Planner: **With** and **Without** Free Trade

Optimal Unilateral Policy: Setup

- Home country sets capital flow taxes to maximise welfare of domestic representative agent
- Primal Approach:** Home planner chooses $\{c_t\}$ in order to maximise welfare of representative agent U_0 , taking as given:

- Foreign consumer maximising U_0^* subject to intertemporal budget constraint

$$\sum_{t=0}^{\infty} p_t \cdot (c_t^* - y_t^*) \leq 0$$

where $p_t = [p_{1,t}, p_{2,t}]$ is vector of world prices

► Foreign Maximisation

- Goods market clearing

$$y_{1,t} + y_{1,t}^* = c_{1,t} + c_{1,t}^*, \quad y_{2,t} + y_{2,t}^* = c_{2,t} + c_{2,t}^*$$

- Prevailing trade agreement

► FTA Problem

► nFTA Problem

Optimal Allocations **with** FTA

With FTA [Costinot, Lorenzoni, Werning, 2014]

- 1 FOC + 1 Instrument

$$\underbrace{\frac{d\mathcal{L}}{dC}}_{FOC=0} = \frac{\partial \mathcal{L}}{\partial c_1} \underbrace{c'_1(C)}_{FTA} + \frac{\partial \mathcal{L}}{\partial c_2} \underbrace{c'_2(C)}_{FTA}$$

- $u'(C_t) = \mu \mathcal{M} \mathcal{B}_t^{FTA}$, where RHS

reflects price of cons., Δ

inter-temporal price, and Δ

intra-temporal price

- Choose C given FTA

\Rightarrow Trade off $\frac{\partial \mathcal{L}}{\partial c_1}$ and $\frac{\partial \mathcal{L}}{\partial c_2}$, with c_1 and c_2 constrained by FTA

Optimal Allocations **with** and **without** FTA

With FTA [Costinot, Lorenzoni, Werning, 2014]

- 1 FOC + 1 Instrument

$$\underbrace{\frac{d\mathcal{L}}{dC}}_{FOC=0} = \frac{\partial \mathcal{L}}{\partial c_1} \underbrace{c'_1(C)}_{FTA} + \frac{\partial \mathcal{L}}{\partial c_2} \underbrace{c'_2(C)}_{FTA}$$

- $u'(C_t) = \mu \mathcal{MB}_t^{FTA}$, where RHS reflects price of cons., Δ inter-temporal price, and Δ intra-temporal price

- Choose C given FTA

\Rightarrow Trade off $\frac{\partial \mathcal{L}}{\partial c_1}$ and $\frac{\partial \mathcal{L}}{\partial c_2}$, with c_1 and c_2 constrained by FTA

Without FTA

- ★ 2 FOCs + 2 Instruments

$$\frac{d\mathcal{L}}{dC} = \underbrace{\frac{\partial \mathcal{L}}{\partial c_1}}_{FOC=0} c'_1(C) + \underbrace{\frac{\partial \mathcal{L}}{\partial c_2}}_{FOC=0} c'_2(C)$$

- ★ $u'(c_{i,t}) = \mu \mathcal{MB}_{i,t}^{nFTA}$ for $i = 1, 2$, where RHS reflects price of cons., Δ inter-temporal price, and Δ intra-temporal price

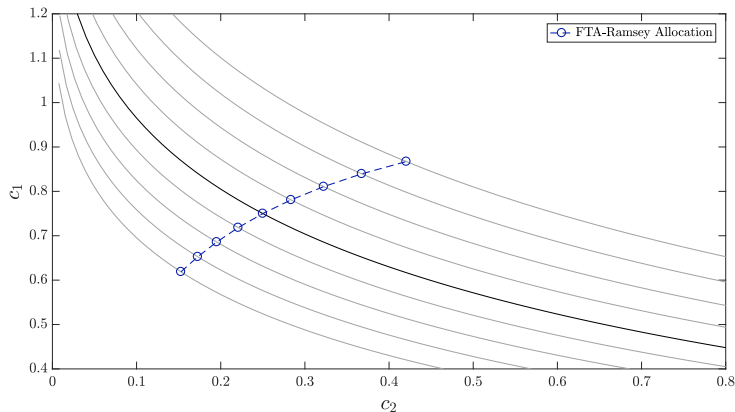
- ★ Choose c_1 and c_2 , given $C = g(\mathbf{c})$

$\Rightarrow C$ optimal for Home planner and can violate FTA constraint

Allocations with a Free Trade Agreement

Feasible combinations of $\{c_1, c_2\}$ given F

FTA $\Rightarrow H$ cannot impose good-specific taxes $\Rightarrow (c_t, c_t^*)$ is Pareto efficient

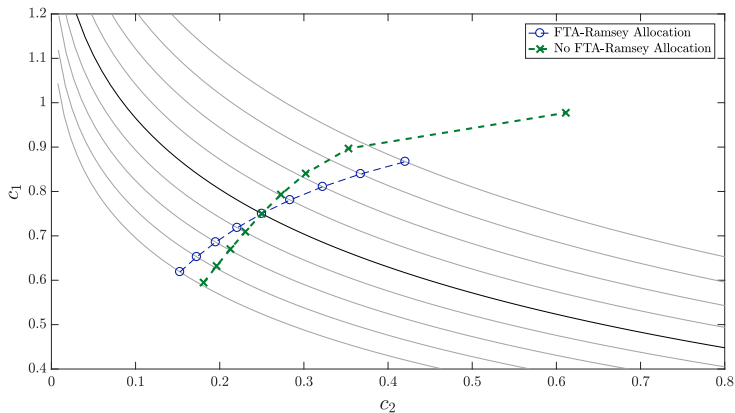


Note: $\phi = 1.5$, $\alpha_1 = \alpha_2^* = 0.75$, $y_1 = \alpha_1 \pm 0.25$, $y_2 = \alpha_2$, $y_i^* = 1 - y_i$ for $i = 1, 2$.

Relaxing the Free Trade Agreement

Feasible combinations of $\{c_1, c_2\}$ given F

No FTA $\Rightarrow H$ sets optimal import tariffs \Rightarrow unconstrained by Pareto frontier



Note: $\phi = 1.5$, $\alpha_1 = \alpha_2^* = 0.75$, $y_1 = \alpha_1 \pm 0.25$, $y_2 = \alpha_2$, $y_i^* = 1 - y_i$ for $i = 1, 2$.

Relaxing the FTA can Increase Home Welfare

Proposition

Suppose goods preferences are symmetric, $\alpha_1 = \alpha_2^*$ and $\alpha_2 = \alpha_1^*$:

- (i) In general: $C^{nFTA} \geq C^{FTA}$
- (ii) When $C^{nFTA} > C^{FTA}$: optimal nFTA allocation violates Pareto frontier
- (iii) $C^{nFTA} = C^{FTA}$ when endowments are proportional to preferences, i.e.
 $y_1 \propto \alpha_1$, $y_2 \propto \alpha_2$, $y_1^* \propto \alpha_1^*$ and $y_2^* \propto \alpha_2^*$

► Graph

What Drives Optimal Policy?

Simulation: Growing Endowment of Home-Bias Good

Non-linear model simulation with AR(1) endowments (persistence ρ)

[► Details](#)

Implement allocation with **capital inflow tax** ($\theta_t < 0$) and **import tariff** ($\tau_t > 0$)

- Initial H endowments:

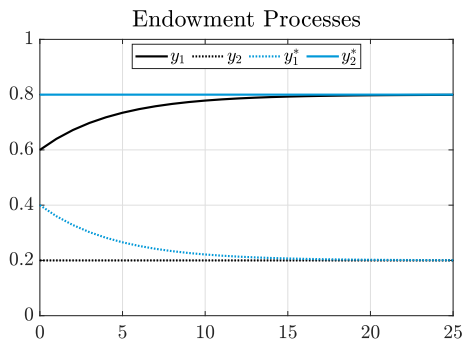
$$y_{1,0} = 0.75\bar{y}_1, \text{ and } y_{2,0} = \bar{y}_2$$

- No aggregate uncertainty:

$$y_{i,t}^* = 1 - y_{i,t} \quad \forall i, t$$

- $\sigma = 2$, $\beta = 0.96$, $\phi = 1.5$, $\rho = 0.8$

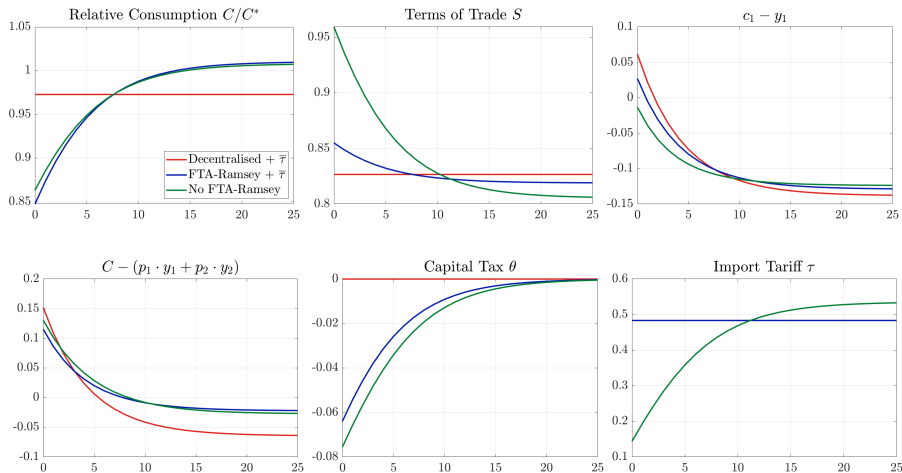
- $\alpha_1 = \alpha_2^* = 0.6$ and $\bar{y}_1 = \bar{y}_2^* = 0.8$



Equalise model steady states (via exogenous tax) to focus on welfare gains along transition path

[► Details](#)

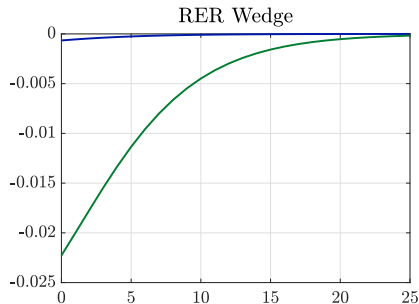
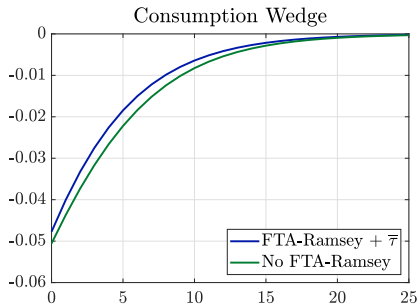
FTA: Stabilise TOT/RER; No-FTA: Stabilise Exports



Tariffs \uparrow RER Misalignment $\Rightarrow \uparrow$ Capital Controls

Why is the capital tax higher absent FTA?

$$-\ln(\tau_t) = \underbrace{-\sigma (\tilde{C}_t - \tilde{C}_{t+1} + \tilde{C}_{t+1}^* - \tilde{C}_t^*)}_{\equiv \ln(\Theta_t / \Theta_{t+1})} + (\tilde{Q}_t - \tilde{Q}_{t+1})$$



► Alternative Simulation

Strategic Planners: **With** and **Without** Free Trade

Optimal Policy at Nash Equilibrium

Both countries max. dom. welfare, taking other's optimisation as given

⇒ Optimally choose **capital controls** $\{\theta, \theta^*\}$ and **import tariffs** $\{\tau, \tau^*\}$ (no FTA).

- Optimality conditions trade off marginal benefits to each country
- **Globally sub-optimal**: cooperation (+ no intervention) is optimal from global perspective

Key results:

- ★ **Capital controls** are larger in the **absence of an FTA** in response to both types of shocks [▶ Graphs](#)
- ★ **Capital control wars** more substantial as $\sigma \uparrow$ whilst **tariff wars** more substantial as $\phi \downarrow$ [▶ Graphs](#)

How Prevalent Are Capital Controls?

- Simulation: $\sigma_y = 5\%$ (annual) [Benigno and Thoenissen, 2008]; uncorrelated shocks
- Complete specialisation, i.e. H endowed with good 1 ($\bar{y}_1 = 1, \bar{y}_2 = 0$)

Nash $\times 10^{-3}$	Decentralised	FTA-Ramsey	nFTA-Ramsey
$\text{var}(y_i)$	8.5	8.5	8.5
$\text{var}(Q)$	0.20	0.17	0.032
$\text{var}(S)$	5.0	4.2	0.80
$\text{var}(BoP)$	1.1	0.23	0.46
$\text{cov}(C, C^*)$	2.6	2.1	1.7
$\text{var}(\theta)$		1.1	1.9
$\text{var}(\theta^*)$		1.1	1.9
$\text{var}(\tau)$			2.9
$\text{var}(\tau^*)$			2.9

Note: Median estimates from 100 model simulations, each with simulation length $T = 100$.

Global Welfare and Cross-Border Spillovers

Spillovers Dwarf Domestic Gains, esp. with Tariffs

- ★ *Unilateral*: Welfare gain in H small relative to loss in F , esp. without FTA
- ★ *Nash*: Losses from policy wars
⇒ really big with capital control and tariff wars

Welfare Difference Rel. Dec. (utils) :	H	F	Global $\sum_{H,F}$
Experiment 1			
with FTA (Unilateral)	+0.029	-0.042	-0.012
without FTA (Unilateral)	+0.50	-0.77	-0.27
with FTA (Nash)	-0.02	-0.02	-0.04
without FTA (Nash)	-0.44	-0.34	-0.78

Conclusions

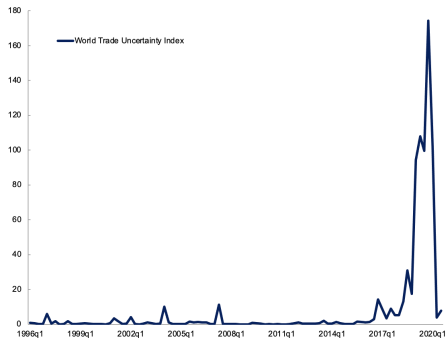
Conclusions

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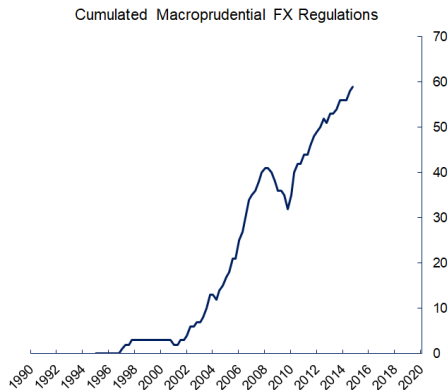
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Appendix

Trade & Financial Openness: Not Always Aligned



Source: World Trade Uncertainty Index. Ahir, Bloom and Furceri (2018).



Source: Ahnert, Forbes, Friedrich and Reinhardt (2020).

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Related Literature

Non-Exhaustive

- **Capital Controls:** Costinot, Lorenzoni and Werning (2014); Bianchi (2011); Farhi and Werning (2016); ...
- **Trade Policy:** Lerner (1936); Broda, Limao and Weinstein (2008); Costinot and Werning (2019); Corsetti and Bergin (2020); ...
- **Integrated Policy Analysis:** Ostry et al. (2010); Basu et al. (2020); Auray, Deveraux and Eyquem (2020) ...

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Foreign Consumer Maximisation

- Representative Foreign consumer problem:

$$\max_{\{\mathbf{c}_t^*\}} U_0^* = \sum_{t=0}^{\infty} \beta^t U^*(C_t^*) \quad \text{s.t.} \quad \sum_{t=0}^{\infty} \mathbf{p}_t \cdot (\mathbf{c}_t^* - \mathbf{y}_t^*) \leq 0$$

⇒ Optimality conditions:

$$\beta^t U^{*'}(C_t^*) \nabla g_c^*(\mathbf{c}_t^*) = \lambda^* \mathbf{p}_t$$

$$\sum_{t=0}^{\infty} \mathbf{p}_t \cdot (\mathbf{c}_t^* - \mathbf{y}_t^*) = 0$$

$$\text{where } \nabla g_c^*(\mathbf{c}_t) = \left[\frac{\partial g^*(\mathbf{c}_t^*)}{\partial c_{1,t}^*}, \frac{\partial g^*(\mathbf{c}_t^*)}{\partial c_{2,t}^*} \right]$$

Unilateral Home Planning Problem

With FTA [Costinot, Lorenzoni & Werning, 2014]

$$\max_{\{C_t, \mathbf{c}_t\}} \sum_{t=0}^{\infty} \beta^t u(C_t) \quad (\text{P-FTA})$$

$$\text{s.t.} \quad \sum_{t=0}^{\infty} \rho(C_t) \cdot [\mathbf{c}_t - \mathbf{y}_t] = 0 \quad (\text{IC})$$

$$\mathbf{c}_t = \mathbf{c}_t(C_t), \quad \mathbf{c}_t^* = \mathbf{c}_t^*(C_t) \quad (\text{FTA})$$

where $\rho(C_t) \equiv \beta^t u^{*'}(C_t^*) \nabla g_c^*(\mathbf{c}_t^*(C_t))$

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Unilateral Home Planning Problem

Without FTA

$$\max_{\{C_t, \mathbf{c}_t\}} \sum_{t=0}^{\infty} \beta^t u(C_t) \quad (\text{P-nFTA})$$

$$\text{s.t.} \quad \sum_{t=0}^{\infty} \rho(C_t) \cdot [\mathbf{c}_t - \mathbf{y}_t] = 0 \quad (\text{IC})$$

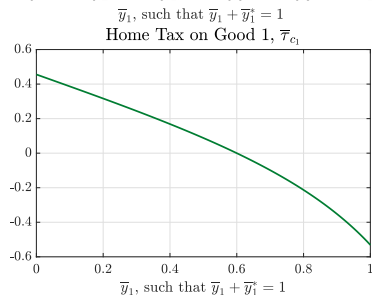
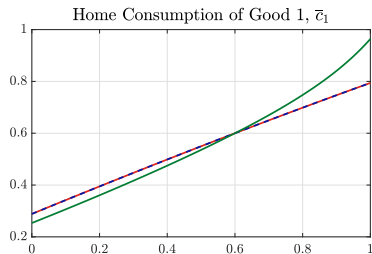
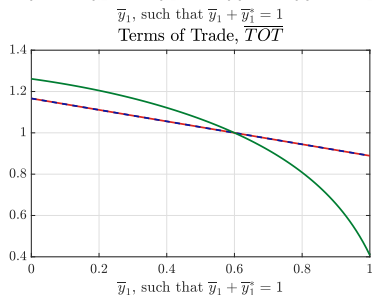
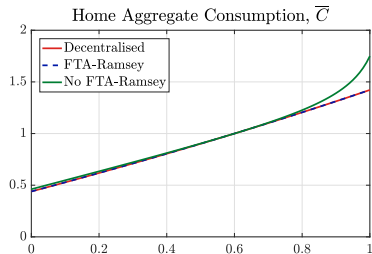
~~$$\mathbf{c}_t = \mathbf{c}_t(C_t), \quad \mathbf{c}_t^* = \mathbf{c}_t^*(C_t)$$~~

$$C_t = g(\mathbf{c}_t) \quad (\text{nFTA})$$

where $\rho(C_t) \equiv \beta^t u^{*'}(C_t^*) \nabla g_c^*(\mathbf{c}_t^*(C_t))$

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Steady State Allocations



Note: $\phi = 1.5$, $\alpha_1 = \alpha_2^* = 0.6$, $\alpha_1^{(*)} + \alpha_2^{(*)} = 1$, $y_2^{(*)} = \alpha_2^{(*)}$.

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Model Solution: 1-Good Example

- For simplicity, suppose each country is endowed with a single good
- Endowment processes for $H \{y_t\}_{t=0}^T$ and $F \{y_t^*\}_{t=0}^T$ **fully deterministic**, where T refers to length of simulation
- Ramsey problem has $T + 2$ FOCs: $T + 1$ w.r.t. c_t and 1 w.r.t. the multiplier μ_0

$$c_t^{-\sigma} = \mu_0 \left[c_t^{*- \sigma} - \sigma c_t^{*- \sigma - 1} (y_t - c_t) \right] \quad \text{for } t = 0, 1, \dots, T$$

$$0 = \sum_{t=0}^T \beta^t c_t^{*- \sigma} (y_t - c_t)$$

- In addition we have market clearing in each period:

$$c_t + c_t^* = y_t + y_t^* \quad \text{for } t = 0, 1, \dots, T$$

$\Rightarrow 2T + 3$ equations in $2T + 3$ unknowns: $\{c_t\}_{t=0}^T$, $\{c_t^*\}_{t=0}^T$ and μ_0 .

Model Solution: Taking to MATLAB

Using vector notation, take $\mathbf{y} = [y_0, y_1, \dots, y_T]'$ and $\mathbf{y}^* = [y_0^*, y_1^*, \dots, y_T^*]'$ as inputs, then use `fsolve` on

$$\mathbf{c}^{-\sigma} = \mu_0 \left[\mathbf{c}^{*-\sigma} - \sigma \mathbf{c}^{*-\sigma-1}(\mathbf{y} - \mathbf{c}) \right]$$

$$\mathbf{c} + \mathbf{c}^* = \mathbf{y} + \mathbf{y}^*$$

$$0 = \mathbf{x}'(\mathbf{y} - \mathbf{c}), \quad \text{where } \mathbf{x} = \mathbf{b} \odot \mathbf{c}^{*-\sigma}$$

where $\mathbf{b} = [\beta^0, \beta^1, \dots, \beta^T]'$

► Back

Model Solution

- Model solved non-linearly
- Endowment processes specified as AR(1) with no aggregate uncertainty:

$$y_{i,t} = (1 - \rho_y)y_{i,0} + \rho_y y_{i,t}, \quad \forall t > 0 \text{ and } i = 1, 2$$

$$\mathbf{y}_t = [y_{1,t}, y_{2,t}], \quad \mathbf{y}_t^* = [1 - y_{1,t}, 1 - y_{2,t}]$$

- Different steady-state allocations across model variants:
 - FTA: no steady-state welfare gains from capital controls
 - w/out FTA: optimal import tariffs deliver steady-state welfare gains

⇒ Compare three model variants, with **first-best steady state**:

1. Decentralised + Steady-State Goods Tax $\bar{\tau}_1$
2. FTA-Ramsey + Steady-State Goods Tax $\bar{\tau}_1$
3. No FTA-Ramsey

★ Focus on **welfare gains along transition path** – **Explicit WTO arrangement**

Implementation

★ Capital taxation:

$$\frac{u'(C_{t+1})}{u'(C_t)}(1 - \theta_t) = \frac{u'(C_{t+1}^*)}{u'(C_t^*)} \frac{Q_t}{Q_{t+1}}$$

$\theta_t < 0$ denotes a tax on current consumption relative to future consumption,
or **tax on capital inflows**

★ Import tariff:

$$\frac{\alpha_1}{1 - \alpha_1} \frac{c_{1,t}}{c_{2,t}} = \left[\frac{p_{1,t}}{p_{2,t}(1 + \tau_t)} \right]^{-\phi}$$

important. where $\tau_t > 0$ denotes **import tariff**

- Implementation not unique [Chari and Kehoe, 1999], but policy-relevant

Experiment #2: F Pursues ' F -First' Production

- Share of good 2 falls, on impact, in H , and rises in F :

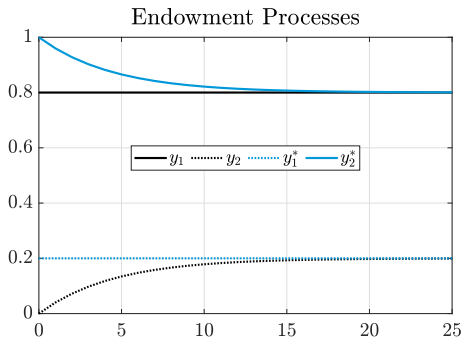
$$y_{1,0}^* = \bar{y}_1^*$$

$$y_{2,0}^* = 1.25\bar{y}_2^*$$

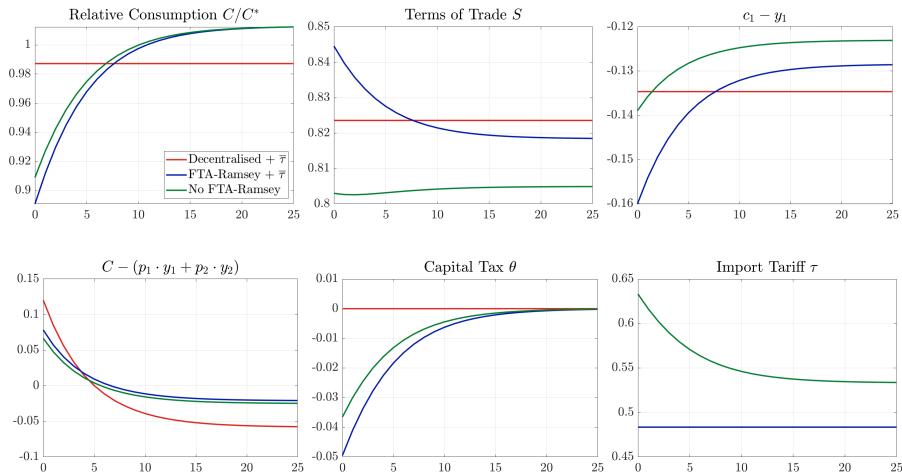
- No aggregate uncertainty $\forall t$:

$$y_{1,t} = 1 - y_{1,t}^*$$

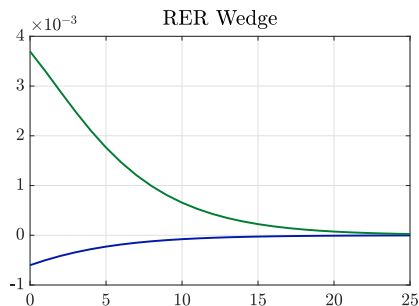
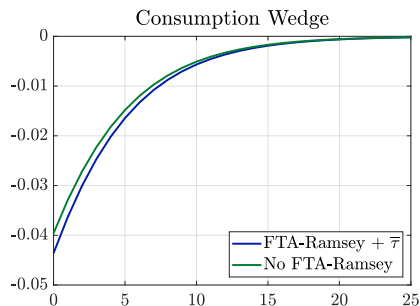
$$y_{2,t} = 1 - y_{2,t}^*$$



Experiment #2: Macro Dynamics

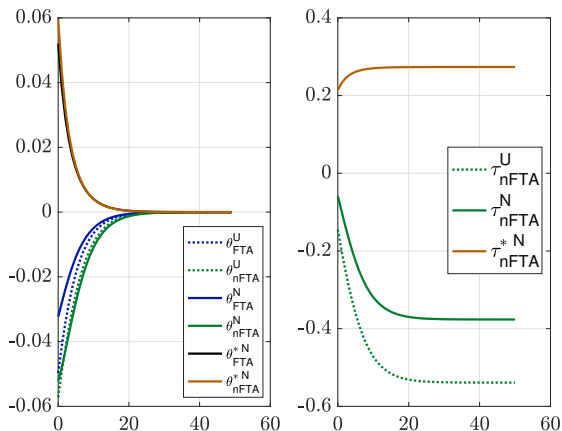


Experiment #2: Capital Tax Decomposition



- ★ Real exchange rate moves in opposite direction, lower capital controls needed
- ★ Trade policy disentangles C growth and Q growth

Figure: Experiment 1 (NASH) – Rising Home Endowment of H Goods



Notes: Optimal capital controls and taxes. "U" subscript denotes unilateral optimal policy result (for Home). "N" denotes Nash outcome.

Capital Control and Tariff Wars

$$\Delta^R = \frac{1 - \theta_t}{1 - \theta_t^*}, \quad \Delta^{p_F} = \frac{1 - \tau_t}{1 - \tau_t^*},$$

Figure: Difference in cost of borrowing and cost of F - goods across countries

