

Project report : Probabilistic programming

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1 Discrete inference by enumeration

1.1 Overview

Simon : Draft phase

We build our language in Ocaml with a library offering a recursive structure and then allow the use of syntactic sugar to improve use comfort. For this first approach, we restrain ourselves to discrete distributions with a finite support. All of this is found in the “finite” sublibrary.

1.2 A recursive structure

Our approach is centered on the introduction of a “model” type, which we inductively defined as follows :

$$Model_1 ::= return\ e \mid (assume\ b),\ Model_2 \mid a = sample(d)\ in\ Model_2 \mid (factor\ i),\ Model_2 \quad (1)$$

With e an expression, b an expression that has type `bool`, i an expression that has type `int`, d an expression that has the type of a distribution, and a a variable name. We require that every expression be well formed with regard to free variables. ie all of their free variables are bound by the time they are encountered in the tree this forms either by normal Ocaml code or by a sample.

When we move to code, this gives the AST (Abstract Syntax Tree) from figure 1.

```
type 'a t =  
| Return : 'a -> 'a t  
| Assume : (bool * 'a t) -> 'a t  
| Factor : (Prob.t * 'a t) -> 'a t  
| Sample : ('a Dist.t * ('a -> 'b t)) -> 'b t
```

Figure 1: Type definition for finite distributions

Note that the construction found in our models is existential. **Simon : Let Emile word this.**

Perhaps more interesting, we can see how this can be used to define an example model (see figure 2). Please note that the bindings happening in samples in equation 1 are replace by functions here, which will be called during evaluation. This approach will present multiples advantages and inconvenient in the rest of this project.

As shown in figure 2 this code is not very convenient to use. We will see in subsection 1.4 how we used syntactic sugar to improve on this.

1.3 Recursive evaluation

List all cases quickly. Explain main idea of cartesian product. Continuation for sample.

```

let funny_bernoulli_ugly =
  Model.(
    Sample
      ( sample (Dist.bernoulli_int ~p:0.5)
        , fun a ->
          Sample
            ( sample (Dist.bernoulli_int ~p:0.5)
              , fun b ->
                Sample
                  ( sample (Dist.bernoulli_int ~p:0.5)
                    , fun (c : int) -> Assume (a = 1 || b = 1, Return (a + b + c))
                  )
                )
              )
            )
          )
    )

```

Figure 2: A first code example with an unwieldly syntax

1.4 Syntactic sugar

Yada. Show snippets of example code.

2 Metropolis Hasting

2.1 Writing continuous distributions

A continuous distribution is either a finite distribution or a pair (sample, logpdf). We implement only one mode of inference for these distributions, Metropolis Hasting. This is found in the continuous sublibrary.

2.2 General theory

Simon : Re-discuss this first

2.3 We already have continuations

Because of the way we wrote the previous logic, it can be followed loosely here while still allowing easy access to continuation.

3 The tests

Simon : Not now