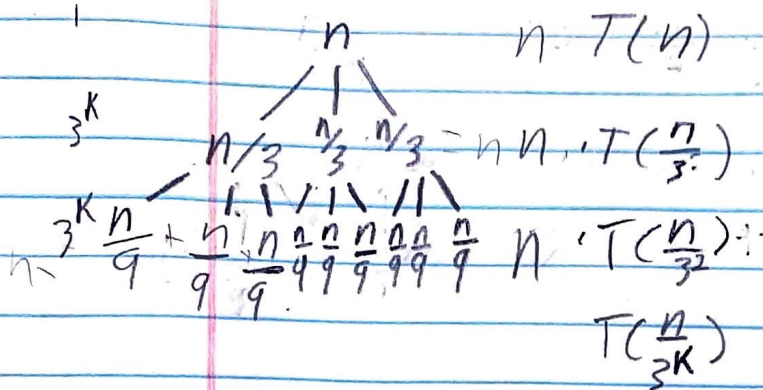


1. $T(n) = 3T(n/3) + n$



$1 = \frac{n}{3^k} \rightarrow n \log_3 n = k$

Sub Method

$$\begin{aligned} T(n) &= 3T(n/3) + n \\ &= 3cn/3 \log_3(n/3) + n \\ &= cn \log_3 n - cn \log_3 3 + n \\ &= cn \log_3 n - cn + n \\ &= cn \log_3 n \end{aligned}$$

2. $2T(n/4) + 1$

$a=2$ $n^{\log_4 2} = n^{0.5}$

$b=4$

$f(n) = 1 = n^0$

According to the master theorem
The answer is $\Theta(n^{0.5}) = T(n)$

2. $2T(n/4) + \sqrt{n}$

$a=2$ $n^{\log_4 2} = n^{0.5}$

$b=4$

$f(n) = \sqrt{n} = n^{1/2}$

According to the master theorem
Then
 $T(n) = \Theta(n^{0.5} \log(n^{0.5}))$

2. $2T(n/4) + n$

$a=2$ $n^{\log_4 2} = n^{0.5}$

$b=4$

$f(n) = n = n^1$

According to the master theorem
Then
 $T(n) = \Theta(n^1)$

2. $2T(n/4) + n^2$

$a=2$ $n^{\log_4 2} = n^{0.5}$

$b=4$

$f(n) = n^2$

According to the master theorem
Then
 $T(n) = \Theta(n^2)$