

Emotion Inertia Analysis

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```
feelings_initial <- load("feelings_initial.RData")
ls()
```

```
## [1] "dat"                "feelings_initial" "Iaro_wide"        "Ineg_wide"
## [5] "Ipos_wide"
```

```
summary(feelings_initial)
```

```
##      Length      Class      Mode  
##           4 character character
```

```
str(dat)
```

```
## 'data.frame':    16380 obs. of  9 variables:  
## $ subj      : Factor w/ 156 levels "f001","f002",...: 1 1 1 1 1 1 1 1 1 1 ...  
## $ trial.num: int   1 2 3 4 5 6 7 8 9 10 ...  
## $ trial.val: Factor w/ 3 levels "neg","neu","pos": 3 1 1 3 3 2 2 1 1 3 ...  
## $ sex       : Factor w/ 3 levels "male","female",...: 2 2 2 2 2 2 2 2 2 2 ...  
## $ age       : int   19 19 19 19 19 19 19 19 19 19 ...  
## $ ethn      : Factor w/ 7 levels "Asian or Pacific Islander",...: 1 1 1 1 1 1 1 1 1 1 ...  
## $ Ineg      : num   1 4 2 1 1 1 1 3 5 1 ...  
## $ Ipos      : num   3.69 1 1 1 4 ...  
## $ Iaro      : num   2.86 3 2 2 3 ...
```

0.1 Descriptive statistics

```
summary(dat[, c("Ineg", "Ipos", "Iaro")])
```

```
##           Ineg           Ipos           Iaro  
## Min.      :1.000   Min.      :1.000   Min.      :1.000  
## 1st Qu.:1.000   1st Qu.:1.000   1st Qu.:1.000  
## Median :2.000   Median :2.000   Median :3.000  
## Mean    :3.075   Mean    :3.066   Mean    :3.265  
## 3rd Qu.:5.000   3rd Qu.:5.000   3rd Qu.:5.000  
## Max.    :9.000   Max.    :9.000   Max.    :9.000
```

- Mean score of Iaro is higher than the other two

```
# identify NAs  
colSums(is.na(dat))
```

```
##      subj trial.num trial.val      sex      age      ethn      Ineg      Ipos  
##       0         0         0         0         0         0         0         0  
##      Iaro  
##       0
```

There are no NAs in the dataset.

```
# identify outliers using z-score

# Calculate Z-scores for Ineg, Ipos, and Iaro
dat$z_Ineg <- scale(dat$Ineg)
dat$z_Ipos <- scale(dat$Ipos)
dat$z_Iaro <- scale(dat$Iaro)

# Identify outliers (Z-score > 3 or < -3)
outliers_Ineg <- dat[abs(dat$z_Ineg) > 3, ]
outliers_Ineg
```

```
## [1] subj      trial.num trial.val sex      age      ethn      Ineg
## [8] Ipos      Iaro      z_Ineg   z_Ipos   z_Iaro
## <0 rows> (or 0-length row.names)
```

```
outliers_Ipos <- dat[abs(dat$z_Ipos) > 3, ]
outliers_Ipos
```

```
## [1] subj      trial.num trial.val sex      age      ethn      Ineg
## [8] Ipos      Iaro      z_Ineg   z_Ipos   z_Iaro
## <0 rows> (or 0-length row.names)
```

```
outliers_Iaro <- dat[abs(dat$z_Iaro) > 3, ]
outliers_Iaro
```

```
## [1] subj      trial.num trial.val sex      age      ethn      Ineg
## [8] Ipos      Iaro      z_Ineg   z_Ipos   z_Iaro
## <0 rows> (or 0-length row.names)
```

There are no outliers.

0.2 Linear Mixed Effects Model: emotional responses by trial type & demographics

- Each participant has multiple trials, so the trials within a participant are likely correlated
- Data is nested
- Each participant may have their own baseline level of emotional responses
- fixed effects (trial.val, sex, age, ethn) explain the variation between individuals
- random effects (1|subj) explain the correlation of repeated measures within individuals

0.2.1 How different trial types & demographics affect negative emotional response (Ineg)?

```
library(lme4)
```

```
## Loading required package: Matrix
```

```
# Mixed-effects model for predicting Ineg
```

```
model_ineg <- lmer(Ineg ~ trial.val + sex + age + ethn + (1|subj), data = dat)  
summary(model_ineg)
```

```
## Linear mixed model fit by REML ['lmerMod']
```

```
## Formula: Ineg ~ trial.val + sex + age + ethn + (1 | subj)
```

```
## Data: dat
```

```
##
```

```
## REML criterion at convergence: 58969.5
```

```
##
```

```
## Scaled residuals:
```

```
##      Min       1Q   Median       3Q      Max  
## -3.9915 -0.5714 -0.0487  0.5031  5.6660
```

```
##
```

```
## Random effects:
```

```
## Groups   Name      Variance Std.Dev.  
## subj    (Intercept) 0.5259   0.7252  
## Residual                2.0745   1.4403
```

```
## Number of obs: 16380, groups: subj, 156
```

```
##
```

```
## Fixed effects:
```

```
##                                     Estimate Std. Error  
## (Intercept)                        5.218934    0.443816  
## trial.valneu                       -4.076439    0.034381  
## trial.valpos                       -4.086175    0.024311  
## sexfemale                          0.317543    0.121858  
## sexother                          -0.031652    0.747300  
## age                               0.001809    0.021086  
## ethnBlack/African American        -0.060943    0.237892  
## ethnLatino/Hispanic               -0.317652    0.232008  
## ethnOther                         0.138570    0.290750  
## ethnWhite/Caucasian               0.070420    0.155354  
## ethnAmerican Indian/Native American or Alaskan Native -0.692261    0.393608  
## ethnDecline to state              -0.275510    0.543413  
##                                     t value  
## (Intercept)                        11.759  
## trial.valneu                       -118.566  
## trial.valpos                       -168.079  
## sexfemale                          2.606
```

```

## sexother -0.042
## age 0.086
## ethnBlack/African American -0.256
## ethnLatino/Hispanic -1.369
## ethnOther 0.477
## ethnWhite/Caucasian 0.453
## ethnAmerican Indian/Native American or Alaskan Native -1.759
## ethnDecline to state -0.507
##
## Correlation of Fixed Effects:
##          (Intr) trl.vln trl.vlp sexfml sexthr age etB/AA ethL/H ethnOt
## trial.valne -0.019
## trial.valps -0.027 0.354
## sexfemale -0.197 0.000 0.000
## sexother -0.070 0.000 0.000 0.084
## age -0.941 0.000 0.000 0.021 0.059
## ethnBlck/AA -0.026 0.000 0.000 0.072 -0.002 -0.149
## ethnLtn/Hsp 0.065 0.000 0.000 0.072 -0.008 -0.250 0.334
## ethnOther -0.081 0.000 0.000 -0.044 -0.006 -0.038 0.234 0.244
## ethnWht/Ccs -0.091 0.000 0.000 0.107 -0.062 -0.171 0.468 0.496 0.357
## ethAI/NAoAN -0.141 0.000 0.000 0.123 0.012 0.029 0.176 0.178 0.134
## ethnDclntst -0.067 0.000 0.000 0.144 0.010 -0.027 0.139 0.145 0.096
##          ethW/C eIAoAN
## trial.valne
## trial.valps
## sexfemale
## sexother
## age
## ethnBlck/AA
## ethnLtn/Hsp
## ethnOther
## ethnWht/Ccs
## ethAI/NAoAN 0.271
## ethnDclntst 0.211 0.092

```

- Random effects: each participant has a different baseline emotional response
 - (1|subj): represents the random effect
 - * each participant (subj) has a different baseline deviation (intercept).
 - * This accounts for the correlation between multiple trial results from the same participant
- REML score (residual maximum likelihood estimate): assess the model fit
- Fixed Effects:
 - Intercept: Negative trial
 - trial.valneu (Neutral trial): Estimate = -4.08, t = -118.57, a very significant negative value.

- * Compared to the baseline (negative trial), **the neutral trial significantly decreases negative emotions (Ineg)**
- trial.valpos (Positive trial): Estimate = -4.09, t = -168.08, also significant.
 - * **the positive trial also significantly decreases negative emotions** compared to the negative trial
- sexfemale: Estimate = 0.317543, t = 2.606.
 - * **Females have significantly higher negative emotional responses (Ineg)** compared to males
- The effects of age and ethnicity are small and not significant

0.2.2 How different trial types & demographics affect positive emotional response (Ipos)?

```
# Mixed-effects model for predicting Ipos
model_ipos <- lmer(Ipos ~ trial.val + sex + age + ethn + (1|subj), data = dat)
summary(model_ipos)
```

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: Ipos ~ trial.val + sex + age + ethn + (1 | subj)
## Data: dat
##
## REML criterion at convergence: 60034.7
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -3.8302 -0.5834 -0.0294  0.5335  5.4659
##
## Random effects:
## Groups Name Variance Std.Dev.
## subj (Intercept) 0.5687 0.7541
## Residual 2.2138 1.4879
## Number of obs: 16380, groups: subj, 156
##
## Fixed effects:
##
## Estimate Std. Error
## (Intercept) 0.71768 0.46141
## trial.valneu 0.33658 0.03552
## trial.valpos 4.03432 0.02511
## sexfemale 0.20020 0.12669
## sexother -1.13135 0.77693
## age 0.02213 0.02192
## ethnBlack/African American 0.08731 0.24732
## ethnLatino/Hispanic -0.33718 0.24121
## ethnOther -0.01740 0.30228
## ethnWhite/Caucasian 0.13375 0.16151
```

```

## ethnAmerican Indian/Native American or Alaskan Native -0.93997    0.40921
## ethnDecline to state -0.33289    0.56496
## t value
## (Intercept) 1.555
## trial.valneu 9.477
## trial.valpos 160.642
## sexfemale 1.580
## sexother -1.456
## age 1.010
## ethnBlack/African American 0.353
## ethnLatino/Hispanic -1.398
## ethnOther -0.058
## ethnWhite/Caucasian 0.828
## ethnAmerican Indian/Native American or Alaskan Native -2.297
## ethnDecline to state -0.589
##
## Correlation of Fixed Effects:
## (Intr) trl.vln trl.vlp sexfml sexthr age etB/AA ethL/H ethnOt
## trial.valne -0.019
## trial.valps -0.027 0.354
## sexfemale -0.197 0.000 0.000
## sexother -0.070 0.000 0.000 0.084
## age -0.941 0.000 0.000 0.021 0.059
## ethnBlck/AA -0.026 0.000 0.000 0.072 -0.002 -0.149
## ethnLtn/Hsp 0.065 0.000 0.000 0.072 -0.008 -0.250 0.334
## ethnOther -0.081 0.000 0.000 -0.044 -0.006 -0.038 0.234 0.244
## ethnWht/Ccs -0.091 0.000 0.000 0.107 -0.062 -0.171 0.468 0.496 0.357
## ethAI/NAoAN -0.141 0.000 0.000 0.123 0.012 0.029 0.176 0.178 0.134
## ethnDclntst -0.067 0.000 0.000 0.144 0.010 -0.027 0.139 0.145 0.096
## ethW/C eIAoAN
## trial.valne
## trial.valps
## sexfemale
## sexother
## age
## ethnBlck/AA
## ethnLtn/Hsp
## ethnOther
## ethnWht/Ccs
## ethAI/NAoAN 0.271
## ethnDclntst 0.211 0.092

```

- Intercept (negative trial): estimate = 0.72, t-value = 1.56. The effect of negative trial on positive emotions (Ipos) is small.
- trial.valneu: estimate = 0.34, t-value = 9.48. Compared to valneg, the neutral trial significantly increases positive emotions (Ipos).
- trial.valpos: estimate = 4.03, t-value = 160.64. Compared to valneg, the positive trial largely increases positive emotions (Ipos), and the effect is extremely significant.

- `sexfemale`: estimate = 0.20, $t = 1.58$. Females tend to have slightly higher positive emotional responses than males.
- `ethnAmerican Indian/Native American or Alaskan Native`: estimate = -0.94, $t = -2.30$. This ethnicity tends to have significantly lower positive emotional responses compared to the reference group.
- `trial.valneu` and `trial.valpos` have a correlation of 0.354, showing that the effects of neutral and positive trials are somewhat related.

0.2.3 How different trial types & demographics affect arousal emotional response (Iaro)?

```
# Mixed-effects model for predicting Iaro
model_aro <- lmer(Iaro ~ trial.val + sex + age + ethn + (1|subj), data = dat)
summary(model_aro)
```

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: Iaro ~ trial.val + sex + age + ethn + (1 | subj)
## Data: dat
##
## REML criterion at convergence: 59841.3
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -4.4843 -0.6288 -0.1072  0.5760  4.8022
##
## Random effects:
## Groups Name Variance Std.Dev.
## subj (Intercept) 1.593 1.262
## Residual 2.168 1.472
## Number of obs: 16380, groups: subj, 156
##
## Fixed effects:
##
## (Intercept) 2.92802 0.76311
## trial.valneu -2.25913 0.03515
## trial.valpos -0.30058 0.02485
## sexfemale 0.22642 0.20959
## sexother -1.53358 1.28529
## age 0.02904 0.03627
## ethnBlack/African American 0.22313 0.40915
## ethnLatino/Hispanic 0.12385 0.39903
## ethnOther 0.52839 0.50007
## ethnWhite/Caucasian 0.06932 0.26720
## ethnAmerican Indian/Native American or Alaskan Native -0.85245 0.67697
## ethnDecline to state 0.07313 0.93462
## t value
```



```

## (Intercept) 3.837
## trial.valneu -64.279
## trial.valpos -12.095
## sexfemale 1.080
## sexother -1.193
## age 0.801
## ethnBlack/African American 0.545
## ethnLatino/Hispanic 0.310
## ethnOther 1.057
## ethnWhite/Caucasian 0.259
## ethnAmerican Indian/Native American or Alaskan Native -1.259
## ethnDecline to state 0.078
##
## Correlation of Fixed Effects:
##          (Intr) trl.vln trl.vlp sexfml sexthr age      etB/AA ethL/H ethnOt
## trial.valne -0.012
## trial.valps -0.016  0.354
## sexfemale -0.197  0.000  0.000
## sexother -0.070  0.000  0.000  0.084
## age -0.942  0.000  0.000  0.021  0.059
## ethnBlck/AA -0.026  0.000  0.000  0.072 -0.002 -0.149
## ethnLtn/Hsp  0.065  0.000  0.000  0.072 -0.008 -0.250  0.334
## ethnOther -0.081  0.000  0.000 -0.044 -0.006 -0.038  0.234  0.244
## ethnWht/Ccs -0.091  0.000  0.000  0.107 -0.062 -0.171  0.468  0.496  0.357
## ethAI/NAoAN -0.141  0.000  0.000  0.123  0.012  0.029  0.176  0.178  0.134
## ethnDclntst -0.067  0.000  0.000  0.144  0.010 -0.027  0.139  0.145  0.096
##          ethW/C eIAoAN
## trial.valne
## trial.valps
## sexfemale
## sexother
## age
## ethnBlck/AA
## ethnLtn/Hsp
## ethnOther
## ethnWht/Ccs
## ethAI/NAoAN  0.271
## ethnDclntst  0.211  0.092

```

- Intercept (negative trial): estimate = 2.93, t-value = 3.84. The effect of negative trial on arousal (Iaro) is moderate.
- trial.valneu: estimate -2.26, t-value = -64.28. Compared to valneg, the **neutral trial significantly decreases arousal (Iaro)**, which can be expected.
- trial.valpos: estimate = -0.30, t-value = -12.10. Compared to valneg, the **positive trial also significantly decreases arousal (Iaro)**, but the effect is small.
- Other fixed effects are not significant.

0.3 Autoregressive Modeling

0.3.1 Assign 12 inertia scores for each participant

Assign 1 overall inertia score for pos, neg, and aro for each participant:

```
library(dplyr)

##
## Attaching package: 'dplyr'

## The following objects are masked from 'package:stats':
##
##   filter, lag

## The following objects are masked from 'package:base':
##
##   intersect, setdiff, setequal, union

library(purrr)
library(broom)

# Create a function to return inertia (lag-1 beta value)
get_inertia <- function(x) {
  # Create lagged data
  lag_x <- dplyr::lag(x)
  df <- data.frame(current = x, lagged = lag_x)
  df <- na.omit(df)

  # Linear regression: current ~ lagged
  model <- lm(current ~ lagged, data = df)
  coef(model)["lagged"]
}

# find inertia scores for the 3 emotions for each participant
overall_inertia <- dat %>%
  group_by(subj) %>%
  summarise(
    pos_inertia = get_inertia(Ipos),
    neg_inertia = get_inertia(Ineg),
    aro_inertia = get_inertia(Iaro)
  )
overall_inertia

## # A tibble: 156 x 4
##   subj pos_inertia neg_inertia aro_inertia
```

```
##      <fct>      <dbl>      <dbl>      <dbl>
##  1 f001      -0.0956     -0.149     -0.139
##  2 f002       0.0187      0.0682      0.0974
##  3 f003      -0.0855     -0.143      0.0149
##  4 f004       0.0648     -0.0705     0.0150
##  5 f005      -0.0433     -0.0918    -0.0962
##  6 f006      -0.0750      0.160      0.175
##  7 f007       0.0834      0.0245      0.190
##  8 f008      -0.0125     -0.0254     0.00949
##  9 f009       0.0162      0.0865     -0.136
## 10 f010       0.164       0.110      0.0143
## # i 146 more rows
```

For each of the 3 emotional reactions (pos, neg, aro), assign 1 inertia score for each of the 3 trial type (pos, neg, neu)

```
library(tidyr)
```

```
##
## Attaching package: 'tidyr'
```

```
## The following objects are masked from 'package:Matrix':
##
##      expand, pack, unpack
```

```
# For each subj x trial.val x emotion
inertia_long <- dat %>%
  group_by(subj, trial.val) %>%
  summarise(
    pos_inertia = get_inertia(Ipos),
    neg_inertia = get_inertia(Ineg),
    aro_inertia = get_inertia(Iaro),
    .groups = "drop"
  )

# Reshape into wide format: 1 row per participant, 9 inertia scores
inertia_wide <- inertia_long %>%
  pivot_wider(
    names_from = trial.val,
    values_from = c(pos_inertia, neg_inertia, aro_inertia),
    names_glue = "{.value}_{trial.val}"
  )

inertia_wide
```

```
## # A tibble: 156 x 10
```

```
##      subj pos_inertia_neg pos_inertia_neu pos_inertia_pos neg_inertia_neg
##      <fct>          <dbl>          <dbl>          <dbl>          <dbl>
##  1 f001          -0.0233           NA           0.0214          -0.203
##  2 f002          -0.0233          -0.115         -0.00418           0.376
##  3 f003           0.131          -0.0939         -0.127           -0.106
##  4 f004          -0.0732          -0.0111          0.196           0.0689
##  5 f005           0.223          -0.0769          0.0571           0.107
##  6 f006          -0.0883          -0.161          0.239           0.416
##  7 f007          -0.0233          -0.0888          0.0636           0.191
##  8 f008           0.0422          -0.247          0.0363          -0.174
##  9 f009          -0.0560           0.0590          0.0652           0.0603
## 10 f010          -0.0233           0.0577          0.199           0.220
## # i 146 more rows
## # i 5 more variables: neg_inertia_neu <dbl>, neg_inertia_pos <dbl>,
## #   aro_inertia_neg <dbl>, aro_inertia_neu <dbl>, aro_inertia_pos <dbl>
```

```
# Find the reason of NAs
```

```
# Whether there's not enough data for each subj × trial.val group?
```

```
dat %>%
  group_by(subj, trial.val) %>%
  summarise(n = n()) %>%
  filter(n < 5)
```

```
## 'summarise()' has grouped output by 'subj'. You can override using the
## '.groups' argument.
```

```
## # A tibble: 0 x 3
## # Groups:   subj [0]
## # i 3 variables: subj <fct>, trial.val <fct>, n <int>
```

```
# Whether some emotion ratings for certain trial type are always the same?
```

```
dat %>%
  group_by(subj, trial.val) %>%
  summarise(
    Ineg_var = var(Ineg),
    Ipos_var = var(Ipos),
    Iaro_var = var(Iaro)
  ) %>%
  filter(Ineg_var == 0 | Ipos_var == 0 | Iaro_var == 0)
```

```
## 'summarise()' has grouped output by 'subj'. You can override using the
## '.groups' argument.
```

```
## # A tibble: 106 x 5
## # Groups:   subj [80]
##   subj trial.val Ineg_var Ipos_var Iaro_var
##   <fct> <fct>      <dbl>    <dbl>    <dbl>
## 1 f001 neu         0      0.267    0.352
## 2 f001 pos         0      1.61     1.08
## 3 f002 neu         0      1.26     1.35
## 4 f002 pos         0      1.51     1.14
## 5 f005 neu         0      0.267    0.0667
## 6 f007 neu         0      0.0663    0
## 7 f007 pos         0      0.786    0.382
## 8 f013 neu         0      0.0659    0
## 9 f019 neu        0.124    4.92     0
## 10 f020 neu         0      2.52     1.55
## # i 96 more rows
```

- The reason of NAs is not due to insufficient data for each $\text{subj} \times \text{trial.val}$ group
- NAs are also not likely to be caused by zero-variance of some emotion inertia ratings, since NAs from `inertia_wide` are more than the number of $\text{Var} = 0$.

```
# Merge all inertia scores (by subj)
inertia_all <- overall_inertia %>%
  left_join(inertia_wide, by = "subj")
inertia_all
```

```
## # A tibble: 156 x 13
##   subj pos_inertia neg_inertia aro_inertia pos_inertia_neg pos_inertia_neu
##   <fct>    <dbl>    <dbl>    <dbl>    <dbl>    <dbl>
## 1 f001 -0.0956 -0.149 -0.139 -0.0233 NA
## 2 f002  0.0187  0.0682  0.0974 -0.0233 -0.115
## 3 f003 -0.0855 -0.143  0.0149  0.131 -0.0939
## 4 f004  0.0648 -0.0705  0.0150 -0.0732 -0.0111
## 5 f005 -0.0433 -0.0918 -0.0962  0.223 -0.0769
## 6 f006 -0.0750  0.160  0.175 -0.0883 -0.161
## 7 f007  0.0834  0.0245  0.190 -0.0233 -0.0888
## 8 f008 -0.0125 -0.0254  0.00949  0.0422 -0.247
## 9 f009  0.0162  0.0865 -0.136 -0.0560  0.0590
## 10 f010  0.164  0.110  0.0143 -0.0233  0.0577
## # i 146 more rows
## # i 7 more variables: pos_inertia_pos <dbl>, neg_inertia_neg <dbl>,
## #   neg_inertia_neu <dbl>, neg_inertia_pos <dbl>, aro_inertia_neg <dbl>,
## #   aro_inertia_neu <dbl>, aro_inertia_pos <dbl>
```

```
library(ggplot2)
library(dplyr)
library(tidyr)
```

```

library(e1071)    # for skewness
library(psych)    # for describe()

##
## Attaching package: 'psych'

## The following objects are masked from 'package:ggplot2':
##
##      %+%, alpha

# Convert to inertia_long format
inertia_long <- inertia_all %>%
  pivot_longer(-subj, names_to = "inertia_type", values_to = "inertia")

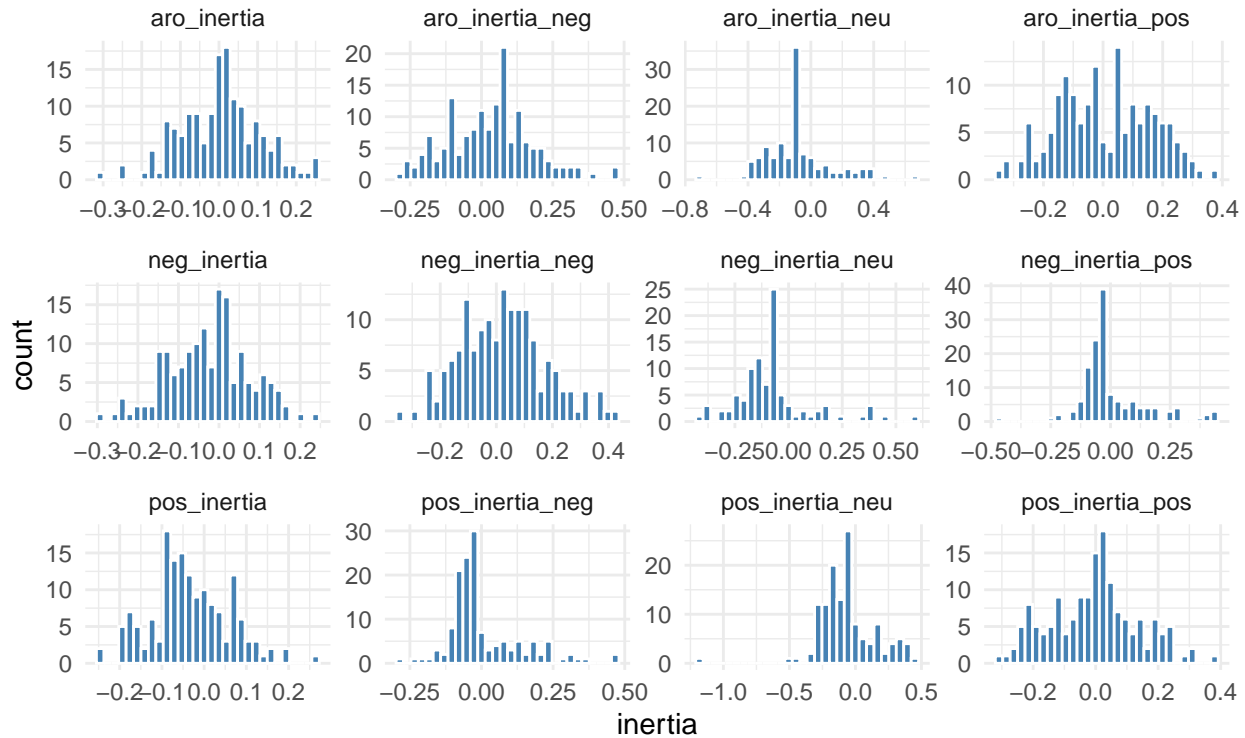
# Distribution & Skewness
inertia_long %>%
  group_by(inertia_type) %>%
  mutate(
    skew = skewness(inertia, na.rm = TRUE),
    normality_p = shapiro.test(inertia)$p.value
  ) %>%
  ggplot(aes(x = inertia)) +
  geom_histogram(bins = 30, fill = "steelblue", color = "white") +
  facet_wrap(~ inertia_type, scales = "free") +
  theme_minimal() +
  labs(title = "Histogram of Inertia Scores across Participants",
        subtitle = "Check for skewness & normality visually")

## Warning: Removed 159 rows containing non-finite outside the scale range
## ('stat_bin()').

```

Histogram of Inertia Scores across Participants

Check for skewness & normality visually



describe_stats for all 3 + 9 = 12 types of inertia

```
describe_stats <- inertia_long %>%
  group_by(inertia_type) %>%
  summarise(
    n = sum(!is.na(inertia)),
    sd = sd(inertia, na.rm = TRUE),
    Q1 = quantile(inertia, 0.25, na.rm = TRUE),
    Q3 = quantile(inertia, 0.75, na.rm = TRUE),
    skewness = skewness(inertia, na.rm = TRUE),
    normality_p = shapiro.test(inertia)$p.value
  )
describe_stats
```

A tibble: 12 x 7

##	inertia_type	n	sd	Q1	Q3	skewness	normality_p
##	<chr>	<int>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
##	1 aro_inertia	156	0.103	-0.0630	0.0666	-0.0809	6.10e- 1
##	2 aro_inertia_neg	156	0.150	-0.0772	0.124	0.230	1.39e- 1
##	3 aro_inertia_neu	117	0.208	-0.182	-0.00947	0.715	3.86e- 5
##	4 aro_inertia_pos	154	0.157	-0.117	0.134	0.0368	1.11e- 1
##	5 neg_inertia	156	0.0998	-0.0890	0.0316	-0.120	8.17e- 1
##	6 neg_inertia_neg	156	0.151	-0.0928	0.117	0.253	4.16e- 1

##	7	neg_inertia_neu	95	0.177	-0.166	-0.0635	1.30	1.30e- 7
##	8	neg_inertia_pos	141	0.139	-0.0694	0.0458	1.08	6.69e-10
##	9	pos_inertia	156	0.0927	-0.0889	0.0276	0.290	2.67e- 1
##	10	pos_inertia_neg	140	0.129	-0.0691	0.0479	1.27	2.32e- 9
##	11	pos_inertia_neu	130	0.216	-0.167	0.0242	-0.399	8.44e- 8
##	12	pos_inertia_pos	156	0.141	-0.119	0.0684	0.0816	1.17e- 1

Inertia scores that are not normal:

- neg_inertia_pos: normality_p = 6.689087e-10; skewness = 1.07982750
 - Under positive stimuli, negative emotion inertia is right-skewed: a few individuals have unusually persistent negative emotions
- pos_inertia_neg: normality_p = 2.318693e-09; skewness = 1.27067898
 - Under negative stimuli, positive emotion inertia is strongly right-skewed: most people have low inertia in positive feelings, with a few showing strong inertia
- pos_inertia_neu: normality_p = 8.436415e-08; skewness = -0.39896752
 - For neutral stimuli, positive emotion inertia is slightly left-skewed
- neg_inertia_neu: normality_p = 1.296106e-07; skewness = 1.29575508
 - For neutral stimuli, negative emotion inertia is strongly right-skewed
- aro_inertia_neu: normality_p = 3.859573e-05; skewness = 0.71497318
 - For neutral stimuli, arousal inertia is right-skewed

0.3.2 Normalize the skewed inertia types

```
# Transform the skewed inertia types to normal
library(bestNormalize)

skewed_vars <- c(
  "neg_inertia_pos", "pos_inertia_neg", "pos_inertia_neu",
  "neg_inertia_neu", "aro_inertia_neu"
)

inertia_long_normalized <- inertia_long %>%
  group_by(inertia_type) %>%
  mutate(
    inertia_trans = if_else(
      inertia_type %in% skewed_vars,
      orderNorm(inertia)$x.t, # transform only these
      inertia # leave others unchanged
    )
  )
```



```
## Warning: There were 6 warnings in 'mutate()'.
## The first warning was:
## i In argument: 'inertia_trans = if_else(...)'.
```

i In group 3: 'inertia_type = "aro_inertia_neu"'.
 ## Caused by warning in 'orderNorm()':
 ## ! Ties in data, Normal distribution not guaranteed
 ## i Run 'dplyr::last_dplyr_warnings()' to see the 5 remaining warnings.

```
inertia_long_normalized
```

```
## # A tibble: 1,872 x 4
## # Groups:   inertia_type [12]
##   subj inertia_type inertia inertia_trans
##   <fct> <chr>          <dbl>          <dbl>
## 1 f001 pos_inertia    -0.0956        -0.0956
## 2 f001 neg_inertia    -0.149         -0.149
## 3 f001 aro_inertia    -0.139         -0.139
## 4 f001 pos_inertia_neg -0.0233         0.244
## 5 f001 pos_inertia_neu NA              NA
## 6 f001 pos_inertia_pos 0.0214         0.0214
## 7 f001 neg_inertia_neg -0.203         -0.203
## 8 f001 neg_inertia_neu NA              NA
## 9 f001 neg_inertia_pos NA              NA
## 10 f001 aro_inertia_neg -0.187         -0.187
## # i 1,862 more rows
```

0.3.3 Compare means and sd of the 12 inertia types

```
# Find mean value of each of the 12 inertia types

inertia_means <- inertia_long_normalized %>%
  group_by(inertia_type) %>%
  summarise(
    mean_inertia = mean(inertia_trans, na.rm = TRUE),
    sd_inertia = sd(inertia_trans, na.rm = TRUE),
    n = sum(!is.na(inertia_trans))
  ) %>%
  arrange(desc(abs(mean_inertia)))

inertia_means
```

```
## # A tibble: 12 x 4
##   inertia_type mean_inertia sd_inertia n
##   <chr>          <dbl>          <dbl> <int>
## 1 pos_inertia    -0.0324         0.0927  156
```

```
## 2 aro_inertia_neg 0.0308      0.150    156
## 3 neg_inertia     -0.0244      0.0998   156
## 4 neg_inertia_neg 0.0242      0.151    156
## 5 aro_inertia_pos 0.00693     0.157    154
## 6 pos_inertia_pos -0.00589     0.141    156
## 7 aro_inertia      0.00482     0.103    156
## 8 neg_inertia_neu -0.0000523   0.998     95
## 9 aro_inertia_neu -0.0000440   0.998    117
## 10 pos_inertia_neg -0.0000328   0.999    140
## 11 neg_inertia_pos -0.00000932  0.999    141
## 12 pos_inertia_neu 0.0000000373  0.999    130
```

- aro_inertia_neu: Extremely high SD (0.998) — arousal inertia under neutral stimuli varies greatly across individuals
- neg_inertia_pos: Negative near-zero mean (-9.32×10^{-6}) but very high variance ($sd = 0.999$);
 - Negative emotion is likely to bounce back after positive stimuli
 - Huge individual differences
- pos_inertia_neg: Negative near-zero mean (-3.28×10^{-5}) but very high variance ($sd = 0.999$);
 - Positive emotion is likely to bounce back after negative stimuli
 - Huge individual differences
- **aro_inertia_neg (mean = 0.031) vs. aro_inertia_pos (mean = 0.007)**
 - participants show slightly greater arousal persistence following negative stimuli ($M = 0.0308$) compared to positive stimuli
 - but the difference is non-significant

```
# check significance for aro_inertia_neg vs. aro_inertia_pos
t.test(inertia_trans ~ inertia_type,
       data = filter(inertia_long_normalized, inertia_type %in% c("aro_inertia_neg", "aro_inertia_pos")))

##
## Welch Two Sample t-test
##
## data:  inertia_trans by inertia_type
## t = 1.3669, df = 306.81, p-value = 0.1727
## alternative hypothesis: true difference in means between group aro_inertia_neg and group aro_inertia_pos
## 95 percent confidence interval:
## -0.01049249  0.05823600
## sample estimates:
## mean in group aro_inertia_neg mean in group aro_inertia_pos
##          0.030804571          0.006932816
```

- **neg_inertia (mean = -0.024) vs. pos_inertia (mean = -0.032):**

```
t.test(inertia_trans ~ inertia_type,
       data = filter(inertia_long_normalized, inertia_type %in% c("neg_inertia", "pos_inertia")))

##
## Welch Two Sample t-test
##
## data: inertia_trans by inertia_type
## t = 0.73868, df = 308.32, p-value = 0.4607
## alternative hypothesis: true difference in means between group neg_inertia and group pos_inertia
## 95 percent confidence interval:
## -0.01340656 0.02952216
## sample estimates:
## mean in group neg_inertia mean in group pos_inertia
## -0.02436017 -0.03241797
```

- Negative emotions appeared to decay slightly more slowly ($M = -0.024$) than positive ones ($M = -0.032$), but the difference is not significant ($p\text{-value} = 0.461$)
- on average, both emotional valences exhibited similarly rapid decay, and individual variability may overshadow any consistent group-level differences
- neg_inertia_pos (mean = $-9.32e-06$) vs. pos_inertia_neg ($-3.28e-05$):

```
t.test(inertia_trans ~ inertia_type,
       data = filter(inertia_long_normalized, inertia_type %in% c("neg_inertia_pos", "pos_inertia_neg")))

##
## Welch Two Sample t-test
##
## data: inertia_trans by inertia_type
## t = 0.00019662, df = 278.99, p-value = 0.9998
## alternative hypothesis: true difference in means between group neg_inertia_pos and group pos_inertia_neg
## 95 percent confidence interval:
## -0.2345872 0.2346341
## sample estimates:
## mean in group neg_inertia_pos mean in group pos_inertia_neg
## -9.318999e-06 -3.275277e-05
```

- Interpretation: Emotions tend to reset quickly when the stimulus is the opposite, potentially due to contrast effects or attentional shifts, meaning that people are likely to be affected by opposite stimuli
- no statistically significant difference ($p = 0.9998$)

0.3.4 Compare emotional inertia types (pos_inertia, neg_inertia, aro_inertia) by demographics

```
# Pivot transformed inertia data to wide format

inertia_wide_trans <- inertia_long_normalized %>%
  select(subj, inertia_type, inertia_trans) %>%
  tidyr::pivot_wider(
    names_from = inertia_type,
    values_from = inertia_trans
  )

# Extract demographic info from your original dat

demo_info <- dat %>%
  select(subj, sex, age, ethn) %>%
  distinct()

# Merge the transformed inertia data with demographics
inertia_full <- inertia_wide_trans %>%
  left_join(demo_info, by = "subj")
inertia_full

## # A tibble: 156 x 16
##   subj pos_inertia neg_inertia aro_inertia pos_inertia_neg pos_inertia_neu
##   <fct>      <dbl>      <dbl>      <dbl>          <dbl>          <dbl>
## 1 f001    -0.0956    -0.149    -0.139          0.244           NA
## 2 f002     0.0187     0.0682     0.0974          0.244          -0.184
## 3 f003    -0.0855    -0.143     0.0149          0.935          -0.145
## 4 f004     0.0648    -0.0705     0.0150         -0.779           0.535
## 5 f005    -0.0433    -0.0918    -0.0962          1.49           0.0579
## 6 f006    -0.0750     0.160     0.175          -1.08          -0.581
## 7 f007     0.0834     0.0245     0.190           0.244          -0.0869
## 8 f008    -0.0125    -0.0254     0.00949         0.641          -1.10
## 9 f009     0.0162     0.0865    -0.136          -0.434           0.724
## 10 f010     0.164      0.110     0.0143          0.244           0.699
## # i 146 more rows
## # i 10 more variables: pos_inertia_pos <dbl>, neg_inertia_neg <dbl>,
## #   neg_inertia_neu <dbl>, neg_inertia_pos <dbl>, aro_inertia_neg <dbl>,
## #   aro_inertia_neu <dbl>, aro_inertia_pos <dbl>, sex <fct>, age <int>,
## #   ethn <fct>

# Inertia types by Sex (mean)

# By sex
inertia_full %>%
```

```
group_by(sex) %>%
summarise(across(starts_with("pos_inertia"):starts_with("aro_inertia"), ~mean(., na.rm = TRUE)))
```

```
## Warning: There was 1 warning in 'summarise()'.
## i In argument: 'across(...)'.
## Caused by warning in 'x:y':
## ! numerical expression has 4 elements: only the first used
```

```
## # A tibble: 3 x 4
##   sex      pos_inertia neg_inertia aro_inertia
##   <fct>      <dbl>      <dbl>      <dbl>
## 1 male      -0.0206      -0.0241     -0.0107
## 2 female    -0.0432      -0.0245      0.0188
## 3 other      0.0144      -0.0339     -0.0359
```

```
library(dplyr)
library(tidyr)
library(purrr)

# Transform into long_format
inertia_sex_long <- inertia_full %>%
  filter(!is.na(sex)) %>%
  pivot_longer(
    cols = starts_with("pos_inertia"):starts_with("aro_inertia"),
    names_to = "inertia_type",
    values_to = "inertia_trans"
  ) %>%
  filter(!is.na(inertia_trans))
```

```
## Warning in x:y: numerical expression has 4 elements: only the first used
```

```
# Check for normality using Shapiro test
normality_test <- inertia_sex_long %>%
  group_by(inertia_type, sex) %>%
  filter(n() >= 3) %>% # Keep groups with sample size >= 3
  summarise(
    n = n(),
    shapiro_p = shapiro.test(inertia_trans)$p.value,
    skewness = e1071::skewness(inertia_trans, na.rm = TRUE),
    .groups = "drop"
  ) %>%
  mutate(normal = ifelse(shapiro_p >= 0.05, "Yes", "No"))

normality_test
```

```
## # A tibble: 6 x 6
##   inertia_type sex      n shapiro_p skewness normal
##   <chr>         <fct> <int>    <dbl>    <dbl> <chr>
## 1 aro_inertia  male     72     0.520  -0.226  Yes
## 2 aro_inertia  female   83     0.637  -0.0532 Yes
## 3 neg_inertia  male     72     0.819   0.0121 Yes
## 4 neg_inertia  female   83     0.645  -0.198  Yes
## 5 pos_inertia  male     72     0.767   0.182  Yes
## 6 pos_inertia  female   83     0.185   0.409  Yes
```

```
# Check for significant difference by sex with ANOVA
```

```
inertia_sex_long %>%
  group_by(inertia_type) %>%
  summarise(
    aov_model = list(aov(inertia_trans ~ sex)),
    .groups = "drop"
  ) %>%
  mutate(tidy_result = map(aov_model, tidy)) %>%
  unnest(tidy_result) %>%
  filter(term == "sex") %>%
  select(inertia_type, statistic, p.value)
```

```
## # A tibble: 3 x 3
##   inertia_type statistic p.value
##   <chr>          <dbl>    <dbl>
## 1 aro_inertia    1.68      0.190
## 2 neg_inertia    0.00487  0.995
## 3 pos_inertia    1.28      0.280
```

- On average, males showed higher positive emotion inertia ($M = -0.021$) than females ($M = -0.043$)
- one-way ANOVA revealed that these differences were not statistically significant ($p = .280$)
- differences in negative inertia ($p = .995$) and arousal inertia ($p = .190$) across sex groups were also not significant

```
# By ethnicity (mean)
```

```
inertia_full %>%
  group_by(ethn) %>%
  summarise(across(starts_with("pos_inertia"):starts_with("aro_inertia"), ~mean(., na.rm = TRUE))
```

```
## Warning: There was 1 warning in 'summarise()'.
## i In argument: 'across(...)'.
## Caused by warning in 'x:y':
## ! numerical expression has 4 elements: only the first used
```

```
## # A tibble: 7 x 4
##   ethn                                pos_inertia neg_inertia aro_inertia
##   <fct>                                <dbl>      <dbl>      <dbl>
## 1 Asian or Pacific Islander          -0.0460    -0.0169     0.00867
## 2 Black/African American             0.00711    -0.0267    -0.00710
## 3 Latino/Hispanic                   -0.0172    -0.0306     0.00750
## 4 Other                             -0.0102    -0.0207     0.0640
## 5 White/Caucasian                   -0.0373    -0.0327    -0.00488
## 6 American Indian/Native American or Alaska~ -0.0393     0.0856     0.0272
## 7 Decline to state                  -0.0831     0.00606     0.0983
```

- **American Indian/Native American or Alaskan Native:** the only group with positive `neg_inertia` -> tend to stay in negative states longer
- **Black/African American:** the only group with `pos_inertia` -> tend to stay in positive states longer (which is unexpected)
- **White/Caucasian:** the only group with negative inertia across all three emotions -> tend to bounce back quickly overall (emotionally adaptive).
 - This may reflect greater access to resources, social safety nets, and less exposure to systemic stressors for White people.
- **Both “Other” and “Decline to state” have much higher `aro_inertia` than others.**
 - This may suggest that the people who are less confident or more confused about their identities are likely to face heightened stress, social vigilance, or lack of belonging—all known to elevate arousal.
- But these patterns **did not reach statistical significance**

```
# By ethnicity (check for significance)

library(tidyr)
library(dplyr)
library(purrr)
library(broom)

inertia_ethn_long <- inertia_full %>%
  filter(!is.na(ethn)) %>%
  pivot_longer(
    cols = matches("inertia"),
    names_to = "inertia_type",
    values_to = "inertia_trans"
  ) %>%
  filter(!is.na(inertia_trans))

# Check for significant between-group difference using ANOVA

ethn_anova <- inertia_ethn_long %>%
  group_by(inertia_type) %>%
```

```

summarise(
  aov_model = list(aov(inertia_trans ~ ethn)),
  .groups = "drop"
) %>%
mutate(tidy_result = map(aov_model, tidy)) %>%
unnest(tidy_result) %>%
filter(term == "ethn") %>%
select(inertia_type, statistic, p.value)

ethn_anova

```

```

## # A tibble: 12 x 3
##   inertia_type      statistic p.value
##   <chr>           <dbl>   <dbl>
## 1 aro_inertia      0.901   0.496
## 2 aro_inertia_neg  0.823   0.553
## 3 aro_inertia_neu  1.78    0.110
## 4 aro_inertia_pos  0.895   0.501
## 5 neg_inertia      0.976   0.444
## 6 neg_inertia_neg  0.371   0.896
## 7 neg_inertia_neu  2.44    0.0317
## 8 neg_inertia_pos  2.52    0.0243
## 9 pos_inertia      0.828   0.550
## 10 pos_inertia_neg 0.703   0.648
## 11 pos_inertia_neu 0.656   0.685
## 12 pos_inertia_pos 0.805   0.568

```

- neg_inertia_neu: $p = 0.0317$
- neg_inertia_pos: $p = 0.0243$

```

# post-hoc: check which groups have the difference using TukeyHSD

# neg_inertia_neu
neg_inertia_neu_model <- aov(inertia_trans ~ ethn,
  data = filter(inertia_ethn_long, inertia_type == "neg_inertia_neu"))

TukeyHSD(neg_inertia_neu_model)

```

```

##   Tukey multiple comparisons of means
##     95% family-wise confidence level
##
## Fit: aov(formula = inertia_trans ~ ethn, data = filter(inertia_ethn_long, inertia_type == "neg_inertia_neu"))
##
## $ethn
##
## Black/African American-Asian or Pacific Islander

```

```

diff
0.69182884

```


## Latino/Hispanic-Asian or Pacific Islander	1.38296700
## Other-Asian or Pacific Islander	0.59868053
## White/Caucasian-Asian or Pacific Islander	0.70583536
## American Indian/Native American or Alaskan Native-Asian or Pacific Islander	1.33966690
## Decline to state-Asian or Pacific Islander	0.20305352
## Latino/Hispanic-Black/African American	0.69113816
## Other-Black/African American	-0.09314831
## White/Caucasian-Black/African American	0.01400652
## American Indian/Native American or Alaskan Native-Black/African American	0.64783806
## Decline to state-Black/African American	-0.48877532
## Other-Latino/Hispanic	-0.78428647
## White/Caucasian-Latino/Hispanic	-0.67713164
## American Indian/Native American or Alaskan Native-Latino/Hispanic	-0.04330009
## Decline to state-Latino/Hispanic	-1.17991348
## White/Caucasian-Other	0.10715483
## American Indian/Native American or Alaskan Native-Other	0.74098638
## Decline to state-Other	-0.39562701
## American Indian/Native American or Alaskan Native-White/Caucasian	0.63383154
## Decline to state-White/Caucasian	-0.50278184
## Decline to state-American Indian/Native American or Alaskan Native	-1.13661338
##	lwr
## Black/African American-Asian or Pacific Islander	-1.08766914
## Latino/Hispanic-Asian or Pacific Islander	0.12467191
## Other-Asian or Pacific Islander	-0.73594296
## White/Caucasian-Asian or Pacific Islander	-0.03373238
## American Indian/Native American or Alaskan Native-Asian or Pacific Islander	-1.61129665
## Decline to state-Asian or Pacific Islander	-1.93048961
## Latino/Hispanic-Black/African American	-1.29840106
## Other-Black/African American	-2.13181935
## White/Caucasian-Black/African American	-1.69535600
## American Indian/Native American or Alaskan Native-Black/African American	-2.68129781
## Decline to state-Black/African American	-3.12068832
## Other-Latino/Hispanic	-2.38830427
## White/Caucasian-Latino/Hispanic	-1.83411638
## American Indian/Native American or Alaskan Native-Latino/Hispanic	-3.12548100
## Decline to state-Latino/Hispanic	-3.49154916
## White/Caucasian-Other	-1.13241244
## American Indian/Native American or Alaskan Native-Other	-2.37313508
## Decline to state-Other	-2.74968156
## American Indian/Native American or Alaskan Native-White/Caucasian	-2.27537678
## Decline to state-White/Caucasian	-2.57818865
## Decline to state-American Indian/Native American or Alaskan Native	-4.66769521
##	upr
## Black/African American-Asian or Pacific Islander	2.4713268
## Latino/Hispanic-Asian or Pacific Islander	2.6412621
## Other-Asian or Pacific Islander	1.9333040
## White/Caucasian-Asian or Pacific Islander	1.4454031
## American Indian/Native American or Alaskan Native-Asian or Pacific Islander	4.2906305

## Decline to state-Asian or Pacific Islander	2.3365966
## Latino/Hispanic-Black/African American	2.6806774
## Other-Black/African American	1.9455227
## White/Caucasian-Black/African American	1.7233690
## American Indian/Native American or Alaskan Native-Black/African American	3.9769739
## Decline to state-Black/African American	2.1431377
## Other-Latino/Hispanic	0.8197313
## White/Caucasian-Latino/Hispanic	0.4798531
## American Indian/Native American or Alaskan Native-Latino/Hispanic	3.0388808
## Decline to state-Latino/Hispanic	1.1317222
## White/Caucasian-Other	1.3467221
## American Indian/Native American or Alaskan Native-Other	3.8551078
## Decline to state-Other	1.9584275
## American Indian/Native American or Alaskan Native-White/Caucasian	3.5430399
## Decline to state-White/Caucasian	1.5726250
## Decline to state-American Indian/Native American or Alaskan Native	2.3944684
##	p adj
## Black/African American-Asian or Pacific Islander	0.9023234
## Latino/Hispanic-Asian or Pacific Islander	0.0216906
## Other-Asian or Pacific Islander	0.8243852
## White/Caucasian-Asian or Pacific Islander	0.0713795
## American Indian/Native American or Alaskan Native-Asian or Pacific Islander	0.8161324
## Decline to state-Asian or Pacific Islander	0.9999516
## Latino/Hispanic-Black/African American	0.9410264
## Other-Black/African American	0.9999994
## White/Caucasian-Black/African American	1.0000000
## American Indian/Native American or Alaskan Native-Black/African American	0.9970374
## Decline to state-Black/African American	0.9977155
## Other-Latino/Hispanic	0.7584408
## White/Caucasian-Latino/Hispanic	0.5741655
## American Indian/Native American or Alaskan Native-Latino/Hispanic	1.0000000
## Decline to state-Latino/Hispanic	0.7198705
## White/Caucasian-Other	0.9999726
## American Indian/Native American or Alaskan Native-Other	0.9911554
## Decline to state-Other	0.9986965
## American Indian/Native American or Alaskan Native-White/Caucasian	0.9944937
## Decline to state-White/Caucasian	0.9902699
## Decline to state-American Indian/Native American or Alaskan Native	0.9588499

- significant difference in `neg_inertia_neu` between Latino/Hispanic-Asian ($M = \dots$) and Pacific Islander ($M = \dots$)

```
# neg_inertia_pos
neg_inertia_pos_model <- aov(inertia_trans ~ ethn,
  data = filter(inertia_ethn_long, inertia_type == "neg_inertia_pos"))

TukeyHSD(neg_inertia_pos_model)
```

```

## Tukey multiple comparisons of means
## 95% family-wise confidence level
##
## Fit: aov(formula = inertia_trans ~ ethn, data = filter(inertia_ethn_long, inertia_type == "I")
##
## $ethn
##
## diff
## Black/African American-Asian or Pacific Islander -0.64260793
## Latino/Hispanic-Asian or Pacific Islander 0.31865580
## Other-Asian or Pacific Islander -0.89275521
## White/Caucasian-Asian or Pacific Islander -0.03248153
## American Indian/Native American or Alaskan Native-Asian or Pacific Islander -0.87381348
## Decline to state-Asian or Pacific Islander 0.44137562
## Latino/Hispanic-Black/African American 0.96126373
## Other-Black/African American -0.25014728
## White/Caucasian-Black/African American 0.61012640
## American Indian/Native American or Alaskan Native-Black/African American -0.23120556
## Decline to state-Black/African American 1.08398355
## Other-Latino/Hispanic -1.21141101
## White/Caucasian-Latino/Hispanic -0.35113733
## American Indian/Native American or Alaskan Native-Latino/Hispanic -1.19246929
## Decline to state-Latino/Hispanic 0.12271982
## White/Caucasian-Other 0.86027368
## American Indian/Native American or Alaskan Native-Other 0.01894172
## Decline to state-Other 1.33413083
## American Indian/Native American or Alaskan Native-White/Caucasian -0.84133196
## Decline to state-White/Caucasian 0.47385715
## Decline to state-American Indian/Native American or Alaskan Native 1.31518911
##
## lwr
## Black/African American-Asian or Pacific Islander -1.6424471
## Latino/Hispanic-Asian or Pacific Islander -0.6085569
## Other-Asian or Pacific Islander -2.1173032
## White/Caucasian-Asian or Pacific Islander -0.6766360
## American Indian/Native American or Alaskan Native-Asian or Pacific Islander -2.4227577
## Decline to state-Asian or Pacific Islander -1.6796036
## Latino/Hispanic-Black/African American -0.1610530
## Other-Black/African American -1.6283305
## White/Caucasian-Black/African American -0.2925399
## American Indian/Native American or Alaskan Native-Black/African American -1.9042566
## Decline to state-Black/African American -1.1292549
## Other-Latino/Hispanic -2.5378476
## White/Caucasian-Latino/Hispanic -1.1726307
## American Indian/Native American or Alaskan Native-Latino/Hispanic -2.8231577
## Decline to state-Latino/Hispanic -2.0586718
## White/Caucasian-Other -0.2863063
## American Indian/Native American or Alaskan Native-Other -1.7973564
## Decline to state-Other -0.9892855
## American Indian/Native American or Alaskan Native-White/Caucasian -2.3294033

```

## Decline to state-White/Caucasian	-1.6030831
## Decline to state-American Indian/Native American or Alaskan Native	-1.1943874
##	upr
## Black/African American-Asian or Pacific Islander	0.3572313
## Latino/Hispanic-Asian or Pacific Islander	1.2458685
## Other-Asian or Pacific Islander	0.3317927
## White/Caucasian-Asian or Pacific Islander	0.6116730
## American Indian/Native American or Alaskan Native-Asian or Pacific Islander	0.6751308
## Decline to state-Asian or Pacific Islander	2.5623549
## Latino/Hispanic-Black/African American	2.0835805
## Other-Black/African American	1.1280360
## White/Caucasian-Black/African American	1.5127927
## American Indian/Native American or Alaskan Native-Black/African American	1.4418454
## Decline to state-Black/African American	3.2972220
## Other-Latino/Hispanic	0.1150256
## White/Caucasian-Latino/Hispanic	0.4703561
## American Indian/Native American or Alaskan Native-Latino/Hispanic	0.4382191
## Decline to state-Latino/Hispanic	2.3041114
## White/Caucasian-Other	2.0068537
## American Indian/Native American or Alaskan Native-Other	1.8352399
## Decline to state-Other	3.6575472
## American Indian/Native American or Alaskan Native-White/Caucasian	0.6467394
## Decline to state-White/Caucasian	2.5507974
## Decline to state-American Indian/Native American or Alaskan Native	3.8247656
##	p adj
## Black/African American-Asian or Pacific Islander	0.4682202
## Latino/Hispanic-Asian or Pacific Islander	0.9464785
## Other-Asian or Pacific Islander	0.3119936
## White/Caucasian-Asian or Pacific Islander	0.9999990
## American Indian/Native American or Alaskan Native-Asian or Pacific Islander	0.6246782
## Decline to state-Asian or Pacific Islander	0.9959664
## Latino/Hispanic-Black/African American	0.1456406
## Other-Black/African American	0.9981132
## White/Caucasian-Black/African American	0.4049371
## American Indian/Native American or Alaskan Native-Black/African American	0.9996011
## Decline to state-Black/African American	0.7641887
## Other-Latino/Hispanic	0.0978488
## White/Caucasian-Latino/Hispanic	0.8601370
## American Indian/Native American or Alaskan Native-Latino/Hispanic	0.3083842
## Decline to state-Latino/Hispanic	0.9999980
## White/Caucasian-Other	0.2784172
## American Indian/Native American or Alaskan Native-Other	1.0000000
## Decline to state-Other	0.6046372
## American Indian/Native American or Alaskan Native-White/Caucasian	0.6222010
## Decline to state-White/Caucasian	0.9933425
## Decline to state-American Indian/Native American or Alaskan Native	0.7022672

- No pairwise group differences are significant for neg_inertia_pos

```
# Inertia types by Age (continuous)
```

```
inertia_full %>%  
  summarise(across(  
    starts_with("pos_inertia"):starts_with("aro_inertia"),  
    ~ cor(., age, use = "complete.obs")  
  ))
```

```
## Warning: There was 1 warning in 'summarise()'.  
## i In argument: 'across(...)'.  
## Caused by warning in 'x:y':  
## ! numerical expression has 4 elements: only the first used
```

```
## # A tibble: 1 x 3  
##   pos_inertia neg_inertia aro_inertia  
##       <dbl>       <dbl>       <dbl>  
## 1    -0.0107    -0.128      0.0286
```

- As age increases, neg_inertia (-0.128) decreases more than pos_inertia (-0.011).
 - Negative emotions drop fast with increasing age
- Arousal shows a slight increase with age (0.029)

```
# Check for significant difference of inertia by age
```

```
# Run linear models for each inertia type
```

```
model_pos_age <- lm(pos_inertia ~ age, data = inertia_full)  
model_neg_age <- lm(neg_inertia ~ age, data = inertia_full)  
model_aro_age <- lm(aro_inertia ~ age, data = inertia_full)
```

```
# Summarize results
```

```
summary(model_pos_age) # Check p-value for age
```

```
##  
## Call:  
## lm(formula = pos_inertia ~ age, data = inertia_full)  
##  
## Residuals:  
##      Min       1Q   Median       3Q      Max   
## -0.21201 -0.05678 -0.01154  0.05932  0.29782   
##  
## Coefficients:  
##              Estimate Std. Error t value Pr(>|t|)      
## (Intercept) -0.0254125  0.0534826  -0.475   0.635      
## age         -0.0003365  0.0025437  -0.132   0.895      
##
```

```
## Residual standard error: 0.09301 on 154 degrees of freedom
## Multiple R-squared:  0.0001136, Adjusted R-squared:  -0.006379
## F-statistic: 0.0175 on 1 and 154 DF,  p-value: 0.8949
```

```
summary(model_neg_age)
```

```
##
## Call:
## lm(formula = neg_inertia ~ age, data = inertia_full)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.260228 -0.066053  0.007856  0.064214  0.284167
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  0.066412   0.057117   1.163   0.247
## age        -0.004360   0.002717  -1.605   0.111
##
## Residual standard error: 0.09933 on 154 degrees of freedom
## Multiple R-squared:  0.01645, Adjusted R-squared:  0.01006
## F-statistic: 2.576 on 1 and 154 DF,  p-value: 0.1106
```

```
summary(model_aro_age)
```

```
##
## Call:
## lm(formula = aro_inertia ~ age, data = inertia_full)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.30992 -0.06622  0.00302  0.06073  0.24392
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.016067   0.059340  -0.271   0.787
## age          0.001003   0.002822   0.356   0.723
##
## Residual standard error: 0.1032 on 154 degrees of freedom
## Multiple R-squared:  0.0008201, Adjusted R-squared:  -0.005668
## F-statistic: 0.1264 on 1 and 154 DF,  p-value: 0.7227
```

- No statistically significant difference in age
 - pos_inertia: p-value = 0.895
 - neg_inertia: p-value = 0.111
 - aro_inertia: p-value = 0.723

0.3.5 Compare the effect of trial types (pos, neg, neu) by demographics

```
# By sex
inertia_full %>%
  group_by(sex) %>%
  summarise(across(("pos_inertia_neg"):(("aro_inertia_pos")), ~ mean(., na.rm = TRUE)))
```

```
## # A tibble: 3 x 10
##   sex      pos_inertia_neg pos_inertia_neu pos_inertia_pos neg_inertia_neg
##   <fct>          <dbl>          <dbl>          <dbl>          <dbl>
## 1 male            0.126            -0.0479        -0.000842        0.0250
## 2 female          -0.0984             0.0620        -0.0106         0.0239
## 3 other          -0.881            -1.51          0.0190         0.00201
## # i 5 more variables: neg_inertia_neu <dbl>, neg_inertia_pos <dbl>,
## #   aro_inertia_neg <dbl>, aro_inertia_neu <dbl>, aro_inertia_pos <dbl>
```

- pos_inertia_neg: male(0.1255) vs. female(-0.0984)
 - Females tend to lose positive emotions quickly in response to negative stimuli
- neg_inertia_pos: male (-0.0489) vs. female(0.0297)
 - Females are more likely to retain negative emotions even with positive stimuli
 - > showing difficulty to let go of negativity
- This may partly explain why females are more likely to get depression
- But **none of these differences reached statistical significance** based on one-way ANOVAs

```
# Check for significant difference by sex
inertia_vars <- c("pos_inertia_neg", "pos_inertia_neu", "pos_inertia_pos",
  "neg_inertia_neg", "neg_inertia_neu", "neg_inertia_pos",
  "aro_inertia_neg", "aro_inertia_neu", "aro_inertia_pos",
  "pos_inertia", "neg_inertia", "aro_inertia")

# lapply ANOVA to each variable & get p-value
anova_results <- lapply(inertia_vars, function(var) {
  formula <- as.formula(paste(var, "~ sex"))
  model <- aov(formula, data = inertia_full)
  summary(model)[[1]][["Pr(>F)"]][1]
})

anova_df <- data.frame(
  variable = inertia_vars,
  p_value = unlist(anova_results)
)
```

```
anova_df$significance <- cut(anova_df$p_value,
                             breaks = c(-Inf, 0.001, 0.01, 0.05, 1),
                             labels = c("***", "**", "*", "ns")) # ns = not significant

print(anova_df)
```

```
##           variable    p_value significance
## 1 pos_inertia_neg 0.2853599          ns
## 2 pos_inertia_neu 0.2618470          ns
## 3 pos_inertia_pos 0.8988783          ns
## 4 neg_inertia_neg 0.9883331          ns
## 5 neg_inertia_neu 0.1754660          ns
## 6 neg_inertia_pos 0.5310370          ns
## 7 aro_inertia_neg 0.2978210          ns
## 8 aro_inertia_neu 0.4516965          ns
## 9 aro_inertia_pos 0.2249770          ns
## 10 pos_inertia 0.2799306          ns
## 11 neg_inertia 0.9951371          ns
## 12 aro_inertia 0.1895052          ns
```

```
# by age
inertia_full %>%
  summarise(across(("pos_inertia_neg"):(("aro_inertia_pos")), ~ cor(., age, use = "complete.obs"))
```

```
## # A tibble: 1 x 9
##   pos_inertia_neg pos_inertia_neu pos_inertia_pos neg_inertia_neg
##           <dbl>           <dbl>           <dbl>           <dbl>
## 1      -0.0459        -0.196           0.0220           0.0270
## # i 5 more variables: neg_inertia_neu <dbl>, neg_inertia_pos <dbl>,
## #   aro_inertia_neg <dbl>, aro_inertia_neu <dbl>, aro_inertia_pos <dbl>
```

```
# Check for statistical significance by age

# use lapply to do cor.test for each variable
cor_results <- lapply(inertia_vars, function(var) {
  test <- cor.test(inertia_full[[var]], inertia_full$age, use = "complete.obs")
  data.frame(variable = var, correlation = test$estimate, p_value = test$p.value)
})

cor_df <- do.call(rbind, cor_results)

cor_df$significance <- cut(cor_df$p_value,
                           breaks = c(-Inf, 0.001, 0.01, 0.05, 1),
                           labels = c("***", "**", "*", "ns"))

print(cor_df)
```


	variable	correlation	p_value	significance	
##	cor	pos_inertia_neg	-0.045855139	0.59058803	ns
##	cor1	pos_inertia_neu	-0.195624318	0.02571326	*
##	cor2	pos_inertia_pos	0.021987216	0.78528023	ns
##	cor3	neg_inertia_neg	0.027043415	0.73753690	ns
##	cor4	neg_inertia_neu	0.070776193	0.49551459	ns
##	cor5	neg_inertia_pos	0.006000111	0.94370514	ns
##	cor6	aro_inertia_neg	0.117301465	0.14474373	ns
##	cor7	aro_inertia_neu	-0.033512493	0.71981814	ns
##	cor8	aro_inertia_pos	-0.016360647	0.84039394	ns
##	cor9	pos_inertia	-0.010658415	0.89493948	ns
##	cor10	neg_inertia	-0.128255400	0.11057296	ns
##	cor11	aro_inertia	0.028637775	0.72267814	ns

- only **pos_inertia_neu** vary significantly by age ($r = -0.20$, $p = .026$)
 - as age increases, positive emotion inertia under neutral conditions tends to decrease
 - **older individuals may be less likely to maintain positive emotions in response to neutral stimuli**

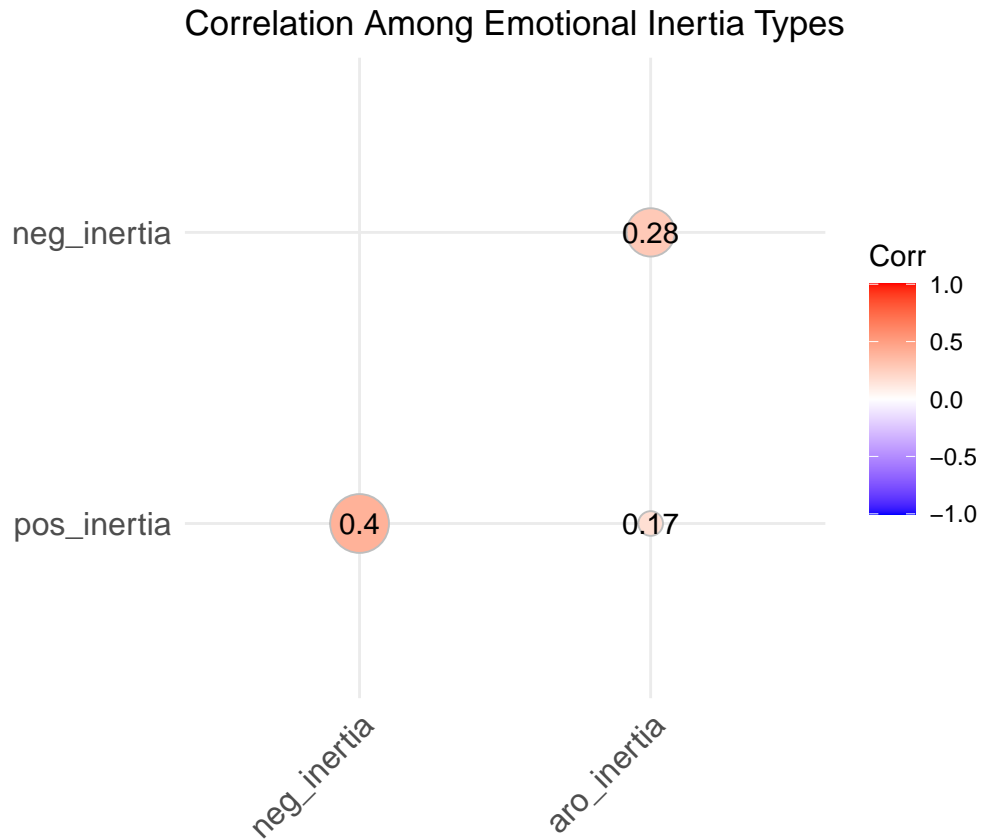
0.3.6 Correlation between inertia types

```
inertia_core <- inertia_full %>%
  select(subj, pos_inertia, neg_inertia, aro_inertia)
cor_matrix <- cor(inertia_core[, -1], use = "complete.obs")
cor_matrix
```

	pos_inertia	neg_inertia	aro_inertia
## pos_inertia	1.0000000	0.4013880	0.1681746
## neg_inertia	0.4013880	1.0000000	0.2784501
## aro_inertia	0.1681746	0.2784501	1.0000000

```
library(ggcorrplot)

ggcorrplot(cor_matrix,
  method = "circle",
  type = "lower",
  lab = TRUE,
  title = "Correlation Among Emotional Inertia Types")
```



- **pos_inertia** and **neg_inertia** have moderate positive correlation ($r = 0.401$): people who tend to hold onto positive emotions also tend to hold onto negative emotions, suggesting emotional stickiness
- **aro_inertia** and **neg_inertia** have small-to-moderate positive correlation ($r = 0.278$): those who hold onto negative emotions also tend to stay aroused longer

0.4 CLPM

0.4.1 Estimate inertia score of positive, negative, and arousal emotions

```
library(lavaan)
```

```
## This is lavaan 0.6-19
## lavaan is FREE software! Please report any bugs.

##
## Attaching package: 'lavaan'

## The following object is masked from 'package:psych':
##
## cor2cov
```

```

library(dplyr)

clpm_data <- dat %>%
  arrange(subj, trial.num) %>%
  group_by(subj) %>%
  mutate(
    Ipos_lag1 = lag(Ipos),
    Ineg_lag1 = lag(Ineg),
    Iaro_lag1 = lag(Iaro)
  ) %>%
  filter(!is.na(Ipos_lag1))

model_inertia <- '
  # Autoregressive (inertia) paths
  Ipos ~ a1 * Ipos_lag1
  Ineg ~ a2 * Ineg_lag1
  Iaro ~ a3 * Iaro_lag1
'

fit <- sem(model_inertia, data = clpm_data)
summary(fit, standardized = TRUE, fit.measures = TRUE)

```

```

## lavaan 0.6-19 ended normally after 28 iterations
##
##      Estimator                      ML
##      Optimization method          NLMINB
##      Number of model parameters          9
##
##      Number of observations          16224
##
## Model Test User Model:
##
##      Test statistic          1402.952
##      Degrees of freedom          6
##      P-value (Chi-square)          0.000
##
## Model Test Baseline Model:
##
##      Test statistic          17555.797
##      Degrees of freedom          12
##      P-value          0.000
##
## User Model versus Baseline Model:
##
##      Comparative Fit Index (CFI)          0.920
##      Tucker-Lewis Index (TLI)          0.841
##

```

```

## Loglikelihood and Information Criteria:
##
##   Loglikelihood user model (H0)          -103647.128
##   Loglikelihood unrestricted model (H1)   -102945.652
##
##   Akaike (AIC)                          207312.257
##   Bayesian (BIC)                        207381.505
##   Sample-size adjusted Bayesian (SABIC)  207352.904
##
## Root Mean Square Error of Approximation:
##
##   RMSEA                                0.120
##   90 Percent confidence interval - lower  0.115
##   90 Percent confidence interval - upper  0.125
##   P-value H_0: RMSEA <= 0.050           0.000
##   P-value H_0: RMSEA >= 0.080           1.000
##
## Standardized Root Mean Square Residual:
##
##   SRMR                                0.082
##
## Parameter Estimates:
##
##   Standard errors                      Standard
##   Information                          Expected
##   Information saturated (h1) model      Structured
##
## Regressions:
##           Estimate  Std.Err  z-value  P(>|z|)  Std.lv  Std.all
##   Ipos ~
##     Ipos_lag1 (a1)    0.200    0.006   33.112    0.000    0.200    0.194
##   Ineg ~
##     Ineg_lag1 (a2)    0.202    0.006   34.422    0.000    0.202    0.196
##   Iaro ~
##     Iaro_lag1 (a3)    0.329    0.006   55.531    0.000    0.329    0.333
##
## Covariances:
##           Estimate  Std.Err  z-value  P(>|z|)  Std.lv  Std.all
##   .Ipos ~~
##     .Ineg             -3.668    0.061  -60.479    0.000   -3.668   -0.540
##     .Iaro              1.199    0.040   29.621    0.000    1.199    0.239
##   .Ineg ~~
##     .Iaro              1.897    0.042   44.857    0.000    1.897    0.376
##
## Variances:
##           Estimate  Std.Err  z-value  P(>|z|)  Std.lv  Std.all
##   .Ipos              6.764    0.075   90.067    0.000    6.764    0.962
##   .Ineg              6.835    0.076   90.067    0.000    6.835    0.962

```

```
##      .Iaro      3.720      0.041      90.067      0.000      3.720      0.889
```

- Positive inertia (0.200) and negative inertia (0.202) are about the same. Negative is slightly higher than positive.
- Arousal inertia (0.329) is much higher than the other two, meaning that arousal emotion is likely to persist.

0.4.2 Cross-lag paths (how one emotion affect another at the next time point)

```
model_clpm <- '
  # Autoregressive (inertia) paths
  Ipos ~ a1 * Ipos_lag1
  Ineg ~ a2 * Ineg_lag1
  Iaro ~ a3 * Iaro_lag1

  # Cross-lagged paths
  Ipos ~ b1 * Ineg_lag1 + b2 * Iaro_lag1
  Ineg ~ c1 * Ipos_lag1 + c2 * Iaro_lag1
  Iaro ~ d1 * Ipos_lag1 + d2 * Ineg_lag1
'

fit_clpm <- sem(model_clpm, data = clpm_data)
summary(fit_clpm, standardized = TRUE, fit.measures = TRUE)
```

```
## lavaan 0.6-19 ended normally after 30 iterations
##
##      Estimator      ML
##      Optimization method      NLMINB
##      Number of model parameters      15
##
##      Number of observations      16224
##
## Model Test User Model:
##
##      Test statistic      0.000
##      Degrees of freedom      0
##
## Model Test Baseline Model:
##
##      Test statistic      17555.797
##      Degrees of freedom      12
##      P-value      0.000
##
## User Model versus Baseline Model:
##
##      Comparative Fit Index (CFI)      1.000
```

```

##    Tucker-Lewis Index (TLI)                                1.000
##
## Loglikelihood and Information Criteria:
##
##    Loglikelihood user model (H0)                            -102945.652
##    Loglikelihood unrestricted model (H1)                    -102945.652
##
##    Akaike (AIC)                                              205921.305
##    Bayesian (BIC)                                           206036.718
##    Sample-size adjusted Bayesian (SABIC)                    205989.049
##
## Root Mean Square Error of Approximation:
##
##    RMSEA                                                    0.000
##    90 Percent confidence interval - lower                    0.000
##    90 Percent confidence interval - upper                    0.000
##    P-value H_0: RMSEA <= 0.050                             NA
##    P-value H_0: RMSEA >= 0.080                             NA
##
## Standardized Root Mean Square Residual:
##
##    SRMR                                                    0.000
##
## Parameter Estimates:
##
##    Standard errors                                          Standard
##    Information                                              Expected
##    Information saturated (h1) model                        Structured
##
## Regressions:
##
##              Estimate  Std.Err  z-value  P(>|z|)  Std.lv  Std.all
## Ipos ~
##   Ipos_lag1 (a1)      0.137    0.011   12.869    0.000    0.137    0.137
## Ineg ~
##   Ineg_lag1 (a2)      0.143    0.011   12.894    0.000    0.143    0.143
## Iaro ~
##   Iaro_lag1 (a3)      0.414    0.009   43.903    0.000    0.414    0.414
## Ipos ~
##   Ineg_lag1 (b1)      0.165    0.011   14.920    0.000    0.165    0.166
##   Iaro_lag1 (b2)      0.010    0.012    0.795    0.427    0.010    0.008
## Ineg ~
##   Ipos_lag1 (c1)      0.173    0.011   16.158    0.000    0.173    0.172
##   Iaro_lag1 (c2)     -0.008    0.013   -0.650    0.516   -0.008   -0.007
## Iaro ~
##   Ipos_lag1 (d1)     -0.043    0.008   -5.289    0.000   -0.043   -0.053
##   Ineg_lag1 (d2)     -0.063    0.008   -7.507    0.000   -0.063   -0.078
##
## Covariances:

```

```
##              Estimate Std.Err z-value P(>|z|) Std.lv Std.all
## .Ipos ~~
## .Ineg      -3.425    0.058 -59.271   0.000   -3.425   -0.526
## .Iaro       1.218    0.040  30.743   0.000    1.218    0.249
## .Ineg ~~
## .Iaro       1.886    0.041  45.562   0.000    1.886    0.383
##
## Variances:
##              Estimate Std.Err z-value P(>|z|) Std.lv Std.all
## .Ipos        6.482    0.072  90.067   0.000    6.482    0.974
## .Ineg        6.549    0.073  90.067   0.000    6.549    0.975
## .Iaro        3.700    0.041  90.067   0.000    3.700    0.860
```

- Arousal inertia (0.414) is much higher than positive inertia (0.137) and negative inertia (0.143)
- Ipos ~ Ineg_lag1 (0.165): negative emotion predicts positive emotion in the next moment, which might reflect emotional rebound
- Ineg ~ Ipos_lag1 (0.173): positive emotion enhances negative emotion in the next moment, which might reflect emotional mix or trial order effect
- Iaro ~ Ipos_lag1 (-0.043): positive emotion decreases arousal at the later stage
- Iaro ~ Ineg_lag1 (-0.063): negative emotion decreases arousal at the later stage
- Ipos ~ Iaro_lag1 and Ineg ~ Iaro_lag1 are not significant
- Conclusion:
 - **Both positive and negative emotions predict more of the opposite in the next moment**
 - **Arousal is reduced by both positive and negative emotions**
 - * maybe a sign of emotional rebound or recovery
 - * more likely to be a result of individual differences (some people are more responsive than others) under random trials within an experimental context, where individuals have “regression to the mean”. This might not be the case in real/natural context

0.4.3 Difference in paths by sex

```
# Group by sex
```

```
fit_clpm_sex <- sem(model_clpm,
                    data = clpm_data,
                    group = "sex")
```

```
## Warning: lavaan->lavParTable():
## using a single label per parameter in a multiple group setting implies
```

```
## imposing equality constraints across all the groups; If this is not
## intended, either remove the label(s), or use a vector of labels (one for
## each group); See the Multiple groups section in the man page of
## model.syntax.
```

```
summary(fit_clpm_sex, standardized = TRUE, fit.measures = TRUE)
```

```
## lavaan 0.6-19 ended normally after 161 iterations
##
## Estimator ML
## Optimization method NLMINB
## Number of model parameters 54
## Number of equality constraints 18
##
## Number of observations per group:
## female 8632
## other 104
## male 7488
##
## Model Test User Model:
##
## Test statistic 70.669
## Degrees of freedom 18
## P-value (Chi-square) 0.000
## Test statistic for each group:
## female 19.632
## other 30.323
## male 20.714
##
## Model Test Baseline Model:
##
## Test statistic 17419.660
## Degrees of freedom 36
## P-value 0.000
##
## User Model versus Baseline Model:
##
## Comparative Fit Index (CFI) 0.997
## Tucker-Lewis Index (TLI) 0.994
##
## Loglikelihood and Information Criteria:
##
## Loglikelihood user model (H0) -102756.204
## Loglikelihood unrestricted model (H1) -102720.870
##
## Akaike (AIC) 205584.409
## Bayesian (BIC) 205861.402
```



```

## Sample-size adjusted Bayesian (SABIC)      205746.996
##
## Root Mean Square Error of Approximation:
##
## RMSEA                                     0.023
## 90 Percent confidence interval - lower      0.018
## 90 Percent confidence interval - upper      0.029
## P-value H_0: RMSEA <= 0.050                1.000
## P-value H_0: RMSEA >= 0.080                0.000
##
## Standardized Root Mean Square Residual:
##
## SRMR                                     0.011
##
## Parameter Estimates:
##
## Standard errors                          Standard
## Information                              Expected
## Information saturated (h1) model          Structured
##
##
## Group 1 [female]:
##
## Regressions:
##           Estimate Std.Err z-value P(>|z|) Std.lv Std.all
## Ipos ~
##   Ipos_lag1 (a1)    0.136   0.011  12.796   0.000   0.136   0.136
## Ineg ~
##   Ineg_lag1 (a2)    0.137   0.011  12.379   0.000   0.137   0.137
## Iaro ~
##   Iaro_lag1 (a3)    0.408   0.009  43.375   0.000   0.408   0.413
## Ipos ~
##   Ineg_lag1 (b1)    0.163   0.011  14.827   0.000   0.163   0.164
##   Iaro_lag1 (b2)    0.005   0.012   0.385   0.700   0.005   0.004
## Ineg ~
##   Ipos_lag1 (c1)    0.167   0.011  15.630   0.000   0.167   0.166
##   Iaro_lag1 (c2)   -0.009   0.012  -0.705   0.481  -0.009  -0.007
## Iaro ~
##   Ipos_lag1 (d1)   -0.045   0.008  -5.657   0.000  -0.045  -0.058
##   Ineg_lag1 (d2)   -0.065   0.008  -7.826   0.000  -0.065  -0.083
##
## Covariances:
##           Estimate Std.Err z-value P(>|z|) Std.lv Std.all
## .Ipos ~~
##   .Ineg             -3.913   0.087 -44.726   0.000  -3.913  -0.549
##   .Iaro              1.264   0.058  21.802   0.000   1.264   0.241
## .Ineg ~~
##   .Iaro              2.077   0.061  34.120   0.000   2.077   0.395

```

```

##
## Intercepts:
##           Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##   .Ipos          2.204   0.057  38.710   0.000   2.204   0.818
##   .Ineg          2.299   0.057  40.163   0.000   2.299   0.850
##   .Iaro          2.366   0.043  55.253   0.000   2.366   1.118
##
## Variances:
##           Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##   .Ipos          7.090   0.108  65.696   0.000   7.090   0.977
##   .Ineg          7.158   0.109  65.696   0.000   7.158   0.978
##   .Iaro          3.866   0.059  65.696   0.000   3.866   0.863
##
##
## Group 2 [other]:
##
## Regressions:
##           Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##   Ipos ~
##     Ipos_lag1 (a1)   0.136   0.011  12.796   0.000   0.136   0.132
##   Ineg ~
##     Ineg_lag1 (a2)   0.137   0.011  12.379   0.000   0.137   0.134
##   Iaro ~
##     Iaro_lag1 (a3)   0.408   0.009  43.375   0.000   0.408   0.356
##   Ipos ~
##     Ineg_lag1 (b1)   0.163   0.011  14.827   0.000   0.163   0.213
##     Iaro_lag1 (b2)   0.005   0.012   0.385   0.700   0.005   0.004
##   Ineg ~
##     Ipos_lag1 (c1)   0.167   0.011  15.630   0.000   0.167   0.121
##     Iaro_lag1 (c2)  -0.009   0.012  -0.705   0.481  -0.009  -0.005
##   Iaro ~
##     Ipos_lag1 (d1)  -0.045   0.008  -5.657   0.000  -0.045  -0.048
##     Ineg_lag1 (d2)  -0.065   0.008  -7.826   0.000  -0.065  -0.093
##
## Covariances:
##           Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##   .Ipos ~~
##     .Ineg          -1.115   0.287  -3.881   0.000  -1.115  -0.412
##     .Iaro          -0.095   0.175  -0.541   0.589  -0.095  -0.053
##   .Ineg ~~
##     .Iaro          1.072   0.258   4.149   0.000   1.072   0.445
##
## Intercepts:
##           Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##   .Ipos          1.176   0.144   8.159   0.000   1.176   0.815
##   .Ineg          2.231   0.192  11.631   0.000   2.231   1.155
##   .Iaro          1.197   0.127   9.441   0.000   1.197   0.900
##

```

```

## Variances:
##               Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##      .Ipos           2.003   0.278   7.211   0.000   2.003   0.962
##      .Ineg           3.667   0.508   7.211   0.000   3.667   0.983
##      .Iaro           1.581   0.219   7.211   0.000   1.581   0.894
##
##
## Group 3 [male]:
##
## Regressions:
##               Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##      Ipos ~
##      Ipos_lag1 (a1)   0.136   0.011  12.796   0.000   0.136   0.136
##      Ineg ~
##      Ineg_lag1 (a2)   0.137   0.011  12.379   0.000   0.137   0.137
##      Iaro ~
##      Iaro_lag1 (a3)   0.408   0.009  43.375   0.000   0.408   0.402
##      Ipos ~
##      Ineg_lag1 (b1)   0.163   0.011  14.827   0.000   0.163   0.163
##      Iaro_lag1 (b2)   0.005   0.012   0.385   0.700   0.005   0.004
##      Ineg ~
##      Ipos_lag1 (c1)   0.167   0.011  15.630   0.000   0.167   0.166
##      Iaro_lag1 (c2)  -0.009   0.012  -0.705   0.481  -0.009  -0.007
##      Iaro ~
##      Ipos_lag1 (d1)  -0.045   0.008  -5.657   0.000  -0.045  -0.055
##      Ineg_lag1 (d2)  -0.065   0.008  -7.826   0.000  -0.065  -0.079
##
## Covariances:
##               Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##      .Ipos ~~
##      .Ineg          -2.915   0.075 -38.669   0.000  -2.915  -0.500
##      .Iaro           1.155   0.054  21.448   0.000   1.155   0.256
##      .Ineg ~~
##      .Iaro           1.651   0.056  29.644   0.000   1.651   0.365
##
## Intercepts:
##               Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##      .Ipos           2.062   0.053  39.082   0.000   2.062   0.844
##      .Ineg           2.033   0.053  38.352   0.000   2.033   0.830
##      .Iaro           2.178   0.040  54.163   0.000   2.178   1.083
##
## Variances:
##               Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##      .Ipos           5.821   0.095  61.188   0.000   5.821   0.975
##      .Ineg           5.849   0.096  61.188   0.000   5.849   0.976
##      .Iaro           3.504   0.057  61.188   0.000   3.504   0.867

```

- Most of the paths are similar between men and women

- Only arousal inertia for women is slightly higher than men

```
# Check for significant difference between men and women
```

```
model_clpm_free <- '
  # Inertia paths
  Ipos ~ c(a1f, a1m, a1o)*Ipos_lag1
  Ineg ~ c(a2f, a2m, a2o)*Ineg_lag1
  Iaro ~ c(a3f, a3m, a3o)*Iaro_lag1

  # Cross-lag
  Ipos ~ c(b1f, b1m, b1o)*Ineg_lag1 + c(b2f, b2m, b2o)*Iaro_lag1
  Ineg ~ c(c1f, c1m, c1o)*Ipos_lag1 + c(c2f, c2m, c2o)*Iaro_lag1
  Iaro ~ c(d1f, d1m, d1o)*Ipos_lag1 + c(d2f, d2m, d2o)*Ineg_lag1
'
```

```
fit_free <- sem(model_clpm_free, data = clpm_data, group = "sex")
```

```
# Whether there's significant difference between sex in at least one path
anova(fit_clpm_sex, fit_free)
```

```
##
## Chi-Squared Difference Test
##
##           Df      AIC      BIC  Chisq Chisq diff    RMSEA Df diff Pr(>Chisq)
## fit_free      0 205550 205965   0.000
## fit_clpm_sex 18 205584 205861 70.669      70.669 0.023261      18 3.482e-08 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

- This shows that at least one or more paths (inertia or cross-lag) differ between males and females

```
# Check which paths are significantly different
```

```
lavTestScore(fit_clpm_sex)
```

```
## $test
##
## total score test:
##
##      test      X2 df p.value
## 1 score 68.394 18      0
##
## $uni
```

```
##
## univariate score tests:
##
##      lhs op    rhs      X2 df p.value
## 1 .p1. == .p28.  0.493  1  0.483
## 2 .p1. == .p55.  3.462  1  0.063
## 3 .p2. == .p29.  3.167  1  0.075
## 4 .p2. == .p56.  1.512  1  0.219
## 5 .p3. == .p30. 10.313  1  0.001
## 6 .p3. == .p57. 17.559  1  0.000
## 7 .p4. == .p31.  3.800  1  0.051
## 8 .p4. == .p58.  1.048  1  0.306
## 9 .p5. == .p32.  0.254  1  0.614
## 10 .p5. == .p59.  0.120  1  0.729
## 11 .p6. == .p33.  1.387  1  0.239
## 12 .p6. == .p60.  1.372  1  0.241
## 13 .p7. == .p34.  0.082  1  0.775
## 14 .p7. == .p61.  0.722  1  0.396
## 15 .p8. == .p35.  0.353  1  0.552
## 16 .p8. == .p62.  3.460  1  0.063
## 17 .p9. == .p36.  0.131  1  0.717
## 18 .p9. == .p63.  2.193  1  0.139
```

- .p3. vs. .p30. and .p3. vs. .p57. are significant ($p < 0.05$)

```
# Understand which paths are them
```

```
pe <- parameterEstimates(fit_clpm_sex, standardized = TRUE)
pe[c(3, 30, 57), c("lhs", "op", "rhs", "group", "est", "std.all")]
```

```
##      lhs op      rhs group  est std.all
## 3 Iaro ~ Iaro_lag1      1 0.408  0.413
## 30 Iaro ~ Iaro_lag1      2 0.408  0.356
## 57 Iaro ~ Iaro_lag1      3 0.408  0.402
```

- females (0.413) and males (0.402) are significantly different in arousal inertia
- females (0.413) and other (0.356) are also significantly different in arousal inertia