Embedded Domain Specific Languages (DSL): Evaluation with Dependencies

Dr. Bruno Oliveira, Boya Peng The University of Hong Kong

General Purpose Languages (GPLs) [1]:

- Pros: Great for generality
- Cons: Takes a lot of effort to establish a suitable context for a particular domain

Domain Specific Languages (DSLs) [2]:

- More concise
- Can be written more quickly
- Easier to maintain
- Easier to reason about

DSLs

Standalone DSLs:

- Entirely separate ecosystem: compiler, editor, etc
- Reinvention of standard language features
- Common within object-oriented circle

Embedded DSLs:

- Existing facilities and infrastructures of the host environment can be used
- Popular within function programming circle

Embedded DSLs within Functional Languages

- Core FP feature can be very helpful in defining embedded DSLs
 - e.g. Algebraic datatypes, higher-order functions
- Define our DSL in Haskell

DSL for Parallel Prefix Circuits

- Prefix computation:
 - Associative binary operator:
 - Inputs: $X_1, X_2, ..., X_n$ (width: n > 0)
 - Outputs: $X_1, X_1 \bullet X_2, \ldots, X_1 \bullet X_2 \bullet \cdots \bullet X_n$

Parallel prefix circuit: performs prefix computation in parallel

DSL for Parallel Prefix Circuits

Example:

• Input: X₁, X₂, X₃, X₄

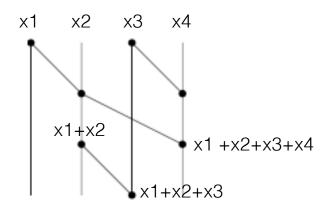


Figure 1. The Brent-Kung parallel prefix circuit of width 4

• Output: X_1 , $X_1 \bullet X_2$, $X_1 \bullet X_2 \bullet X_3$, $X_1 \bullet X_2 \bullet X_3 \bullet X_4$

DSL for Parallel Prefix Circuits

Algebraic Datatype:

```
data Circuit =
Identity Int
| Fan Int
| Above Circuit Circuit
| Beside Circuit Circuit
| Stretch [Int] Circuit
```

```
Stretch [Int] Circuit
```

• Identity n: e.g. Identity 4



• Fan n: e.g. Fan 4



- Beside x y: horizontal composition,
 - e.g. Beside (Fan 2) (Identity 1)

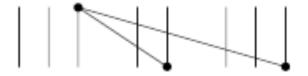


 Above x y: vertical composition, x, y are two circuits with the same width

• e.g. Above (Beside (Fan 2) (Identity 1)) (Beside (Identity 1) (Fan 2))



- Stretch ws x: ws is a list of n integers, width of x = n
 - e.g. Stretch [3, 2, 3] (Fan 3)



The Expression Problem

 "The goal is to define a datatype by cases, where one can add new cases to the data type and new functions over the data type, without recompiling existing code, and while retaining static type safety." — Phil Wadler [3]

The Expression Problem

In summary, we want to:

OO language: trivial Functional language: hard

- Add new cases to a datatype modularly
- Add new evaluation functions over a datatype modularly

OO language: hard

Functional language: trivial

Modular definition of datatypes

```
data Circuit =
Identity Int
| Fan Int
| Above Circuit Circuit
| Beside Circuit Circuit
| Stretch [Int] Circuit
```

Stretch [Int] Circuit

```
data CircuitB =
Identity Int
| Fan Int
| Beside CircuitB CircuitB
```

```
data CircuitE =
Above CircuitE CircuitE
| Stretch [Int] CircuitE
```

How to add CircuitE to CircuitB?

Modular definition of datatypes

- Modular Reifiable Matching (MRM) [4]
 - Use a fixpoint of list-of-functors approach to twolevel types

MRM: Adding datatypes

- Two-level types:
 - Functors:

```
data CircuitFB r =
IdentityF Int
| FanF Int
| BesideF r r
deriving Functor
```

data CircuitFE r =
AboveF r r
| StretchF [Int] r
deriving Functor

Fixpoint of list-of-functors:

```
type Circuit = Fix'[CircuitFB, CircuitFE]
```

```
data Circuit =
Identity Int
| Fan Int
| Above Circuit Circuit
| Beside Circuit Circuit
| Stretch [Int] Circuit
```

MRM — Adding evaluation functions

Algebras corresponding to different functors:

```
\label{eq:type CircuitAlgB a = CircuitFB a a base} \textbf{type CircuitAlgE a = CircuitFE a a base} a \textbf{type CircuitAlgE a = CircuitFE a base} a \textbf{type Circui
```

Evaluation with fold [4]:

```
width :: Circuit \rightarrow Int
width = fold (widthAlgB ::: widthAlgE ::: Void)
```

Problem with fold

- The evaluation needs to be compositional:
 - Limitation to expressivity
- Non-compositional (Dependent) evaluation:
 - e.g. wellSized Whether a circuit is well-formed or not depends on the widths of its constituent parts

```
\begin{tabular}{lll} wellSized :: CircuitE $\rightarrow$ Bool & {\bf data} \ CircuitE = \\ wellSized (Above $\times$ y) = & Above \ CircuitE \ CircuitE \\ wellSized $\times$ \&\& \ wellSized $y$ \&\& \ width $\times$ == width $y$ & Stretch [Int] \ CircuitE \\ wellSized $\times$ \&\& \ length \ ws == width $\times$ & wellSized $\times$ \&\& \ length \ ws == width $\times$ & wellSized $\times$ & width $\times$ & wellSized $\times$ & wellSized $\times$ & width $\times$ & wellSized $\times$ & wellSized $\times$ & width $\times$ & width $\times$ & wellSized $\times$ & wellSized $\times$ & wellSized $\times$ & width $\times$ & width $\times$ & wellSized $\times$ & wellSized $\times$ & width $\times$ & wellSized $\times$ & wellSized $\times$ & width $\times$ & wellSized $\times$ & wellSized $\times$ & width $\times$ & wellSized $\times$
```

Our work: Dependent Evaluation with *fold*

- Idea: compose two algebras together, feed it to fold
 - How to compose algebras together modularly?
 - How to allow dependencies?

Composable Algebra

Type class for membership relationship:

```
class i :<: e where
inter :: e \rightarrow i
```

Composition operator:

```
type Compose a b = (a, b)

(⊕) :: CircuitAlg a → CircuitAlg b → CircuitAlg (Compose a b)

(⊕) a1 a2 (AboveF x y) =

(a1 (AboveF (inter x) (inter y)), a2 (AboveF (inter x) (inter y)))

(⊕) a1 a2 (StretchF xs x) =

(a1 (StretchF xs (inter x)), a2 (StretchF xs (inter x)))
```

Composable Algebra: Example

 Compose algebras together:

```
cAlgE :: Compose Width Depth
cAlgE = widthAlgE2 ⊕ depthAlgE
```

Retrieve individual interpretation:

```
gwidth :: (Width2 :<: e) \Rightarrow e \rightarrow Int gwidth = width \circ inter gdepth :: (Depth2 :<: e) \Rightarrow e \rightarrow Int gdepth = depth \circ inter
```

Example algebras:

```
newtype Width = Width { width :: Int }

widthAlgE2 :: CircuitAlgE Width
widthAlgE2 (AboveF x y) = Width (width x)
widthAlgE2 (StretchF ws x) = Width (sum ws)

newtype Depth = Depth { depth :: Int }

depthAlgE :: CircuitAlgE Depth
depthAlgE (AboveF x y) = Depth (depth x + depth y)
depthAlgE (StretchF ws x) = Depth (sum ws)
```

Dependent Interpretation

New form of algebra:

```
type GAlgB r a = CircuitFB r \rightarrow a type GAlgE r a = CircuitFE r \rightarrow a
```

Example of algebras (for CircuitFE):

```
widthAlgE :: (Width :<: r) ⇒ CircuitFE r → Width
widthAlgE (AboveF x y) = Width2 (gwidth x)
widthAlgE (StretchF xs x) = Width2 (sum xs)

newtype WellSized = WellSized { wellSized :: Bool }

wsAlgE :: (Width :<: r, WellSized :<: r) ⇒
    CircuitFE r → WellSized2
wsAlgE (AboveF x y) =
    WellSized2 (gwellSized x && gwellSized y && gwidth x == gwidth y)
wsAlgE (StretchF xs x) =
    WellSized2 (gwellSized x && length xs == gwidth x)</pre>
```

Dependencies

Composition operator:

```
class Comb f where (\oplus) :: (a : <: r, b : <: r) \Rightarrow (f \ r \rightarrow a) \rightarrow (f \ r \rightarrow b) \rightarrow (f \ r \rightarrow (Compose \ a \ b))
instance Comb CircuitFB where (\oplus) \ a1 \ a2 \ (IdentityF \ w) = \\ (a1 \ (IdentityF \ w), a2 \ (IdentityF \ w))
(\oplus) \ a1 \ a2 \ (FanF \ w) = \\ (a1 \ (FanF \ w), a2 \ (FanF \ w))
(\oplus) \ a1 \ a2 \ (BesideF \ x \ y) = \\ (a1 \ (BesideF \ (inter \ x) \ (inter \ y)), a2 \ (BesideF \ (inter \ x) \ (inter \ y)))
instance Comb CircuitFE where (\oplus) \ a1 \ a2 \ (AboveF \ x \ y) = \\ (a1 \ (AboveF \ (inter \ x) \ (inter \ y)), a2 \ (AboveF \ (inter \ x) \ (inter \ y)))
(\oplus) \ a1 \ a2 \ (StretchF \ xs \ x) = \\ (a1 \ (StretchF \ xs \ (inter \ x)), a2 \ (StretchF \ xs \ (inter \ x)))
```

Dependent Interpretation

Composing algebras together:

```
\mathsf{compAlgB} = \mathsf{widthAlgB} \oplus \mathsf{wsAlgB} \qquad \qquad \mathsf{compAlgE} = \mathsf{widthAlgE} \oplus \mathsf{wsAlgE}
```

Evaluation with fold:

```
eval :: Circuit \rightarrow Compose Width WellSize
eval = fold (compAlgB ::: (compAlgE ::: Void))
```

Modularly extensible DSL with dependent interpretations:

- An approach to compose algebras modularly
- Allow dependent interpretations

Contributions

Modularly extensible DSL with dependent interpretations:

- An approach to compose algebras modularly
- Allow dependent interpretations

Thank you!

References

- [1] Jeremy Gibbons, Nicolas Wu. Folding Domain-Specific Languages: Deep and Shallow Embeddings
- [2] Paul Hudak. Domain Specific Languages
- [3] Phil Wadler. The Expression Problem
- [4] Bruno C.d.S. Oliveira, Shin-Cheng Mu, Shu-Hung You. *Modular Reifiable Matching: A List-of-Functors Approach to Two-Level Types*
- [5] http://hspec.github.io/