



# Word translation using word embeddings

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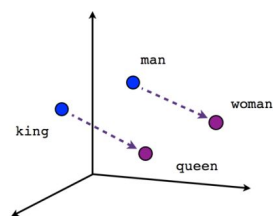
-- DeepL --

# Brief statement of the problem

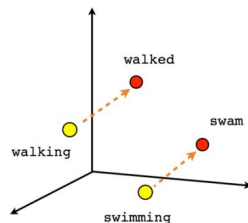
**Goal:** Build a translator from a source language to a target language

ex: fr → en, fr → it ...

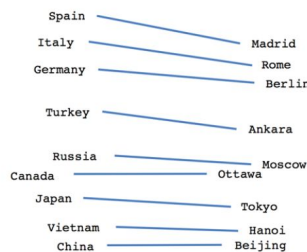
- Idea of the translation :
  - Words used in the same context usually have the same meaning
  - Words can be represented as vectors → Words can be **embedded**



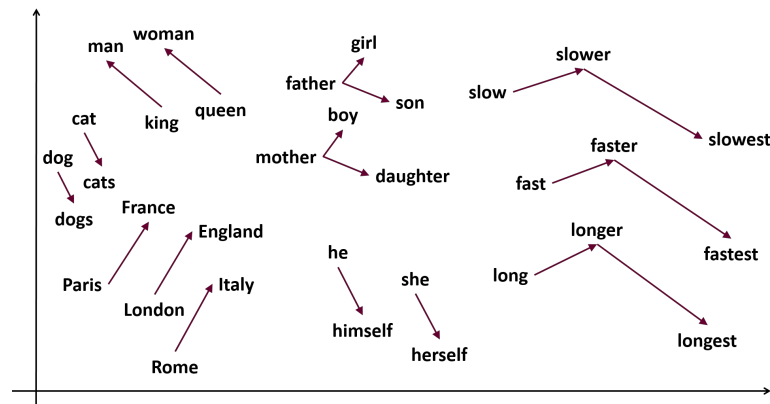
Male-Female



Verb tense



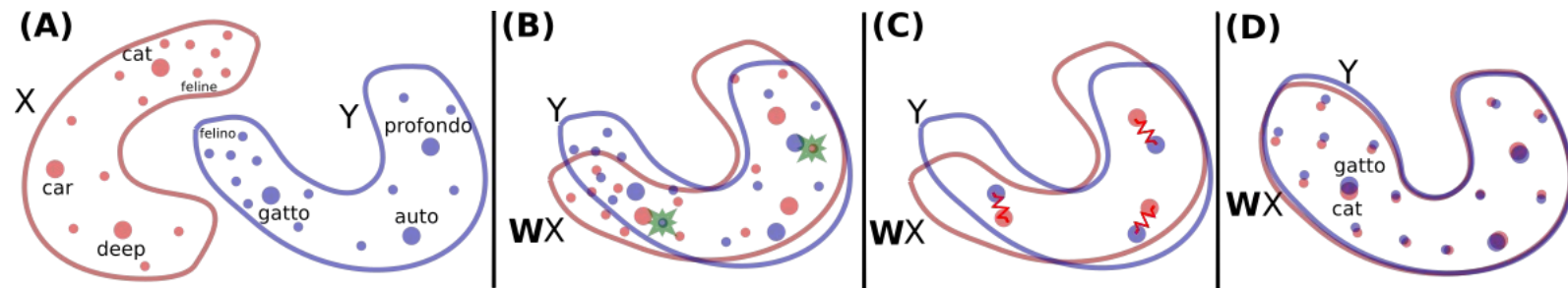
Country-Capital



# Methods

X: set of english word embeddings

Y: set of italian word embeddings



We need to compute the matrix  $W$  that does the translation between the sets

2 ways to do so:

- Supervised, where we need a bilingual dictionary to build  $W$
- Unsupervised, where  $W$  is computed by a GAN

# Supervised

Settings: set of pair of words and their associated vector representation  $\{x_i, z_i\}_{i=1}^n$ , where  $x_i$  is the vector of the word  $i$  in the source language and  $z_i$  the vector of its translation.

*Linear:*

$$\min_W \sum_{i=1}^n \|W x_i - z_i\|^2$$

Solution of this optimization problem (with regularization) is :

$$W = (X X^T - \lambda Id) X^T Z$$

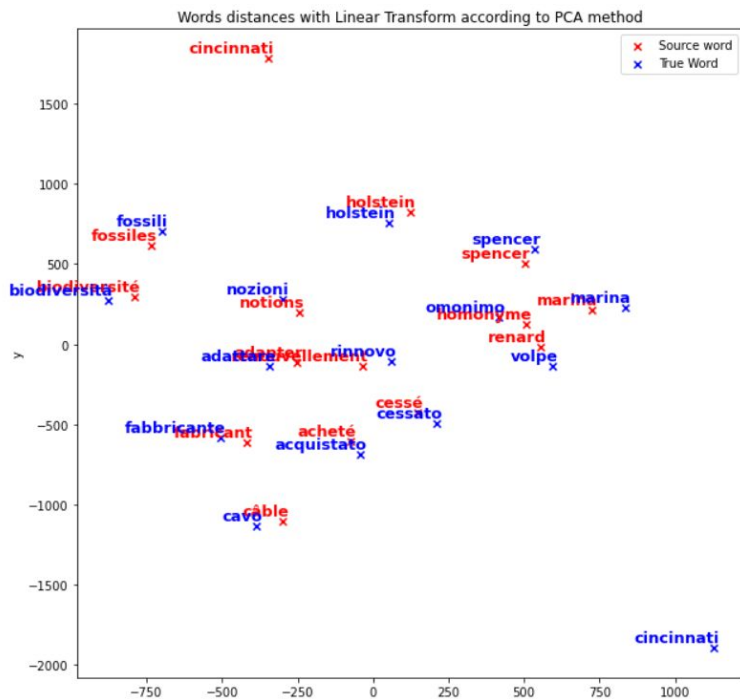
*Orthogonal:*

$$\begin{cases} \min_W \sum_{i=1}^n \|W x_i - z_i\|^2 \\ \min_{\bar{W}} \|W - \bar{W}\| \text{ s.t. } \bar{W}^T \bar{W} = Id \end{cases}$$

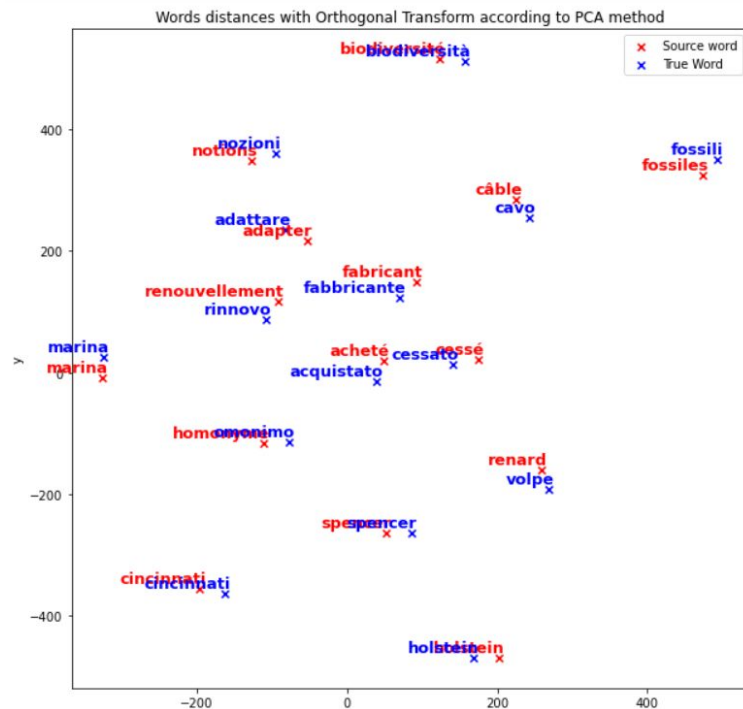
Application of gradient descent and procrustes (through SVD)

# Supervised

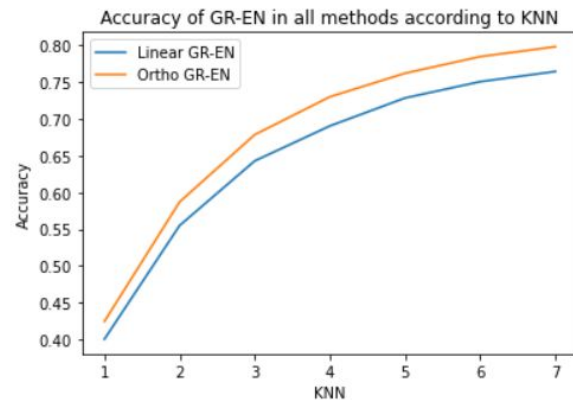
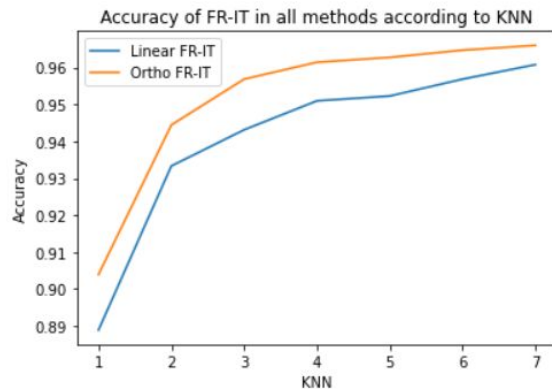
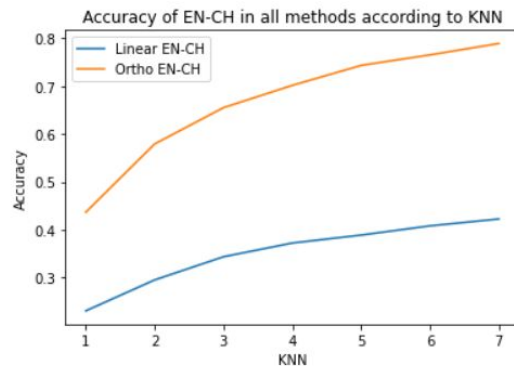
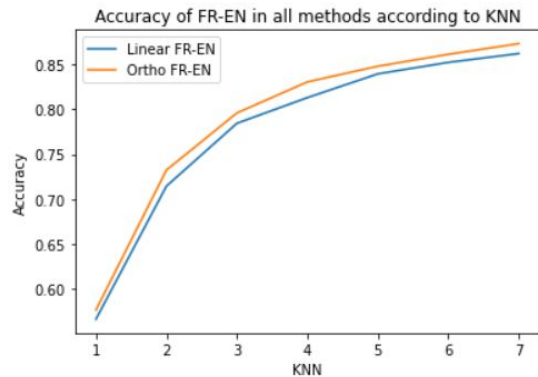
Linear:



Orthogonal:



# Supervised & KNN



# Supervised



	fr-en	en-fr	fr-it	it-fr	en-el	el-en	en-ch
<i>Supervised methods</i>							
Linear - 1-NN	0,57	0,42	0,89	0,78	0,40	0,51	0,23
Linear - 7-NN	0,86	0,87	0,96	0,94	0,76	0,79	0,42
Procrustes - 1-NN	0,57	0,43	0,90	0,79	0,42	0,54	0,43
Procrustes - 7-NN	<b>0,87</b>	<b>0,89</b>	<b>0,97</b>	<b>0,96</b>	<b>0,78</b>	<b>0,82</b>	<b>0,79</b>

Note : with the hubness issue resolved, our en-fr translator has an accuracy of 0.57 for 1-NN and 0.72 for 7-NN

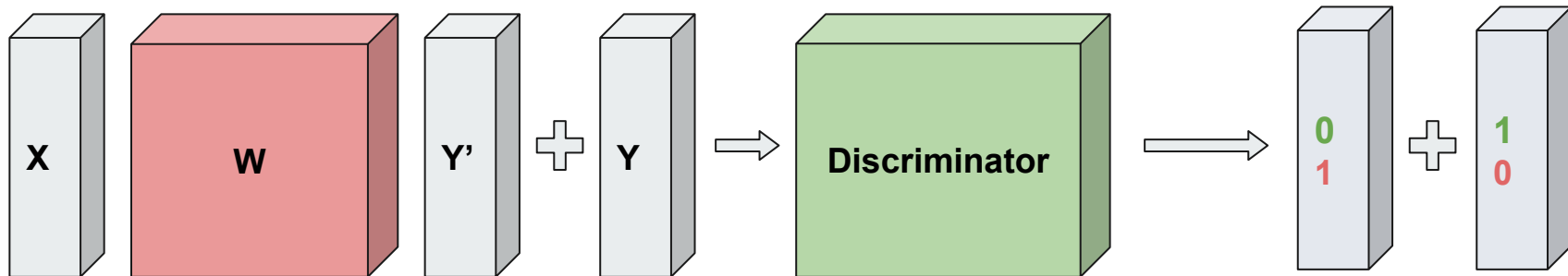
# Unsupervised

Setting: 2 sets of word embeddings ( $X, Y$ ) trained independently on monolingual data. The similarities between monolingual embedding spaces can be exploited to learn mappings between the 2 sets with an adversarial model.

## Minimization Problem

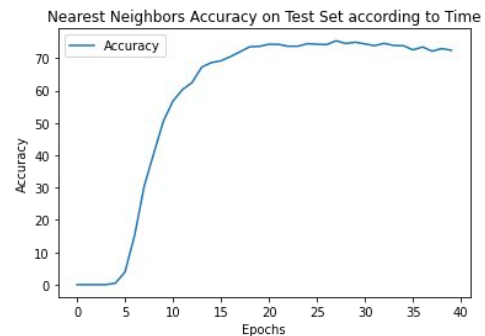
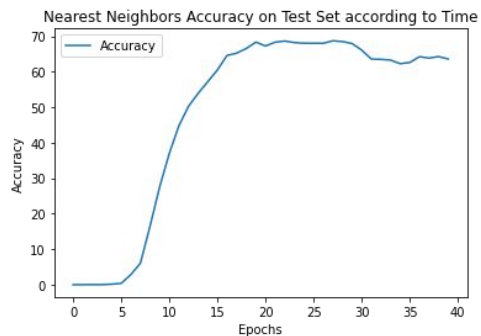
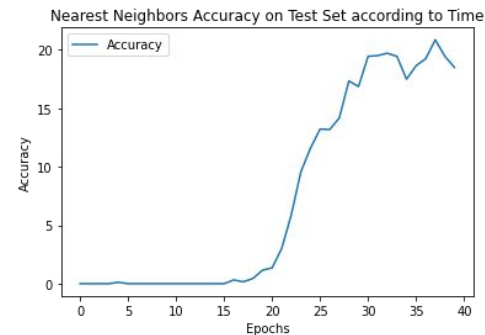
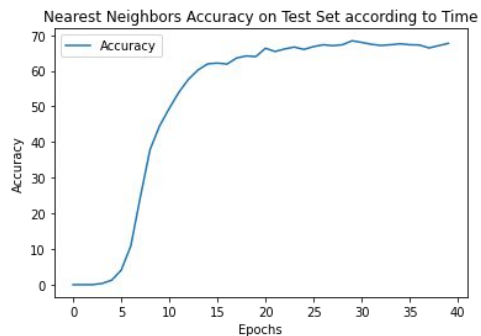
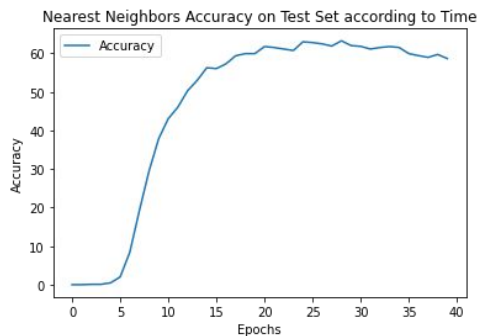
$$W^* = \operatorname{argmin}_{W \in M_d(\mathbb{R})} \|WX - Y\|_F$$

The cosine similarity is used to translate words  
 $t = \operatorname{argmax}_t \cos(Wx_s, y_t)$





# Unsupervised & KNN



# 1-nn accuracies



	fr-en	en-fr	fr-it	it-fr	en-el	en-ch
linear	0,57	0,42	0,89	0,78	0,40	0,23
procrustes	0,57	0,43	0,90	0,79	0,42	0,43
unsupervised	0,73	0,72	0,86	0,84	0,42	0,45