

# Zhang\_Xuan\_Assignment\_4

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## 0.1 Problem

Univariate times series modeling of the S&P 500 over the period 2004-2006.

The data file "stock-treasury-2004\_2006.csv", to be found in the "Data" folder, contains the following:

+ TREAS\_3M: the yield of the 3-month treasury note in percent (i.e 2.1 means 2.1%) + Adjusted close price of ten major stocks: GM, F, UTX, CAT, MRK, PFE, IBM, MSFT, C, XOM + SP: The S&P 500 equity index level at the close of the trading day

### **Do the following:**

Use the pandas read\_csv function to read only the Date and SP columns in a data frame called "sp\_df".

Rename the "SP" column into "ClosePx" in the same read\_csv call.

Compute the close-to-close index returns as:  $r_t = P_{t+1}/P_t - 1$  and add them as a new column "DailyRet".

It is recommended to express all daily returns in basis points (10,000 bps = 100% = 1)

Fit ARIMA models on the DailyRet time series, up to AR order p=2, MA order q=2, and differencing order d=1.

You can reuse the utility function auto\_arima or provide your own.

Display the summary of the best selected model based on the AIC criterion.

Plot the original returns series and the predictions of the best selected model using the model's plot\_predict method.

Run the Jarque-Bera normality test on the residuals of the best selected ARIMA model, and produce the qq plot of the residuals.

Repeat the Jarque-Bera test and the qq plot using the residuals of the white noise model ARMA(0, 0).

Compare the two and comment on whether they are really different.

## 0.2 Solution

<...>

```
In [1]: import pandas as pd
import numpy as np
from mlutils import run_adf_test, auto_arima
import statsmodels.api as sm
```

```
import matplotlib.pyplot as plt
plt.style.use('ggplot')
```

```
sp_df=pd.read_csv("stock-treasury-2004_2006.csv",
                  usecols=[0,12],parse_dates=['Date'],header=0,names=['Date','ClosePx'])
```

```
sp_df.head()
```

```
Out[1]:
```

	Date	ClosePx
0	2004-01-02	1108.48
1	2004-01-05	1122.22
2	2004-01-06	1123.67
3	2004-01-07	1126.33
4	2004-01-08	1131.92

```
In [2]: sp_df = sp_df.assign(DailyRet=10000 * (sp_df.ClosePx / sp_df.ClosePx.shift() - 1))
sp_df.head()
```

```
Out[2]:
```

	Date	ClosePx	DailyRet
0	2004-01-02	1108.48	NaN
1	2004-01-05	1122.22	123.953522
2	2004-01-06	1123.67	12.920818
3	2004-01-07	1126.33	23.672431
4	2004-01-08	1131.92	49.630215

```
In [3]: best_arima, results = auto_arima(sp_df.DailyRet[1:].values, p_max = 2, q_max = 2, d_max = 2)
```

```
D:\anaconda3\lib\site-packages\scipy\signal\signaltools.py:1341: FutureWarning: Using a non-tuple sequence for multidimensional indexing is deprecated; use `tuple` instead of slicing from array.
out_full[ind] += zi
```

```
D:\anaconda3\lib\site-packages\scipy\signal\signaltools.py:1344: FutureWarning: Using a non-tuple sequence for multidimensional indexing is deprecated; use `tuple` instead of slicing from array.
out = out_full[ind]
```

```
D:\anaconda3\lib\site-packages\scipy\signal\signaltools.py:1350: FutureWarning: Using a non-tuple sequence for multidimensional indexing is deprecated; use `tuple` instead of slicing from array.
zf = out_full[ind]
```

```
ARIMA(0, 0, 0) AIC:7578.85 BIC:7587.87
```

```
ARIMA(0, 0, 1) AIC:7579.90 BIC:7593.43
```

```
ARIMA(0, 0, 2) AIC:7578.43 BIC:7596.47
```

```
ARIMA(0, 1, 0) AIC:8054.73 BIC:8063.75
```

```
ARIMA(0, 1, 1) AIC:7577.06 BIC:7590.58
```

```
The computed initial MA coefficients are not invertible
```

```
You should induce invertibility, choose a different model order, or you can
pass your own start_params.
```

```
ARIMA(1, 0, 0) AIC:7580.03 BIC:7593.56
```

```
The computed initial AR coefficients are not stationary
```

```
You should induce stationarity, choose a different model order, or you can
pass your own start_params.
```

```
The computed initial AR coefficients are not stationary
```

```
You should induce stationarity, choose a different model order, or you can
```



```
=====
```

	coef	std err	z	P> z	[0.025	0.975]
const	2.7419	0.315	8.699	0.000	2.124	3.360
ar.L1.y	1.4719	nan	nan	nan	nan	nan
ar.L2.y	-0.4893	nan	nan	nan	nan	nan
ma.L1.y	-1.5372	nan	nan	nan	nan	nan
ma.L2.y	0.5372	nan	nan	nan	nan	nan

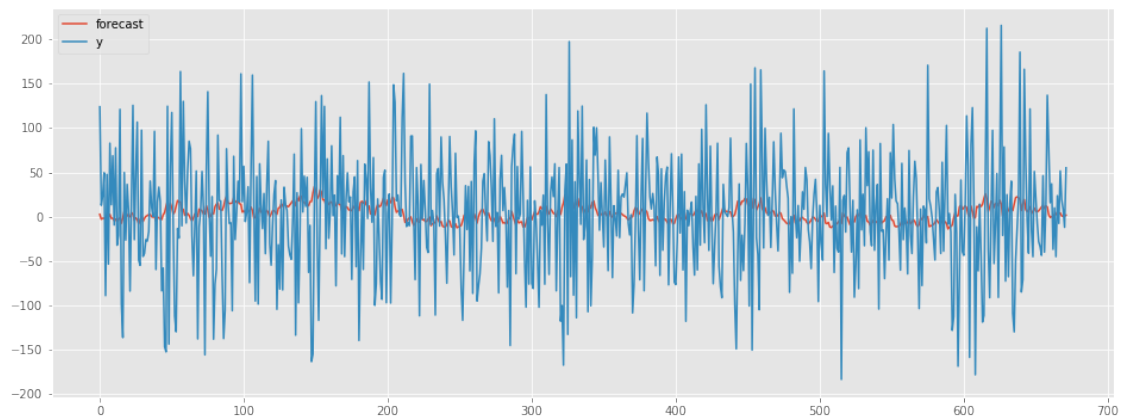
```
=====
Roots
=====
```

	Real	Imaginary	Modulus	Frequency
AR.1	1.0366	+0.0000j	1.0366	0.0000
AR.2	1.9717	+0.0000j	1.9717	0.0000
MA.1	1.0000	+0.0000j	1.0000	0.0000
MA.2	1.8616	+0.0000j	1.8616	0.0000

```
=====
"""
```

```
In [5]: armodel = best_arima['model']
```

```
fig2 = plt.figure(figsize=(16,6))
axx = fig2.add_subplot(111)
armodel.plot_predict(ax = axx);
```



```
In [6]: arresid = armodel.resid
jbres = sm.stats.jarque_bera(arresid)
```

```
print("Jarque-Bera Normality Test on AR Residuals")
print("statistic: {}".format(jbres[0]))
print("p-value: {}".format(jbres[1]))
```

```
print('skew: {}'.format(jbres[2]))
print('kurtosis: {}'.format(jbres[3]))
```

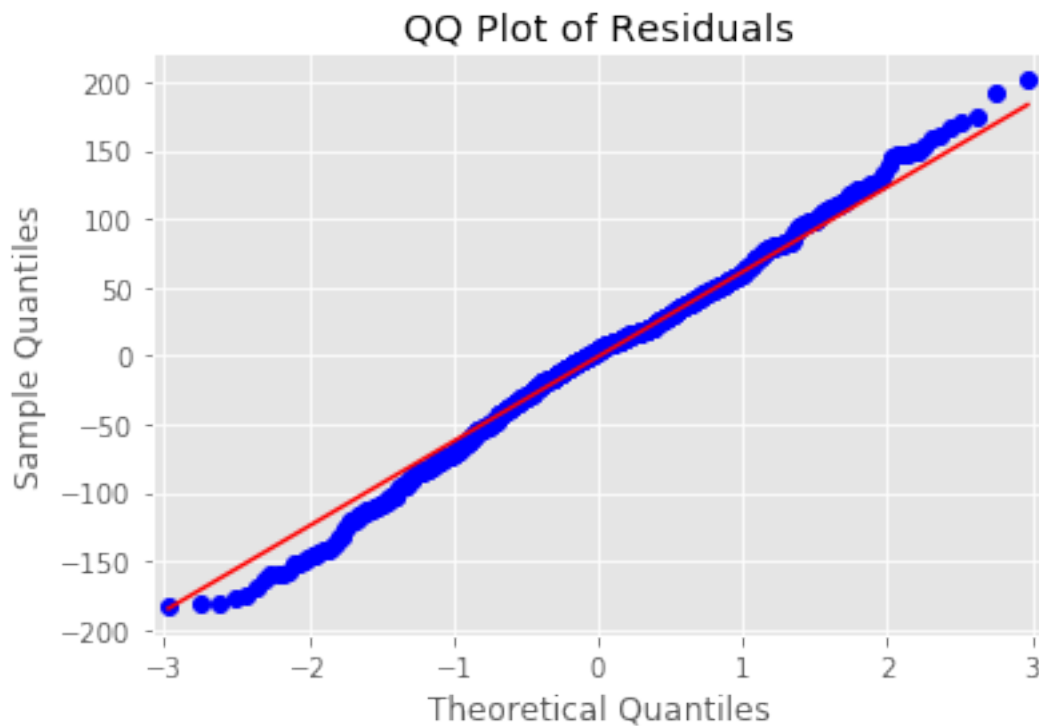
Jarque-Bera Normality Test on AR Residuals  
 statistic: 1.5098564497740838  
 p-value: 0.4700443510061998  
 skew: -0.10713348436248081  
 kurtosis: 3.0895159804068806

```
In [7]: axxx = plt.figure().add_subplot(111)
        sm.graphics.qqplot(arresid, line='q', ax = axxx);
        axxx.set(title = 'QQ Plot of Residuals')
```

D:\anaconda3\lib\site-packages\scipy\stats\stats.py:1713: FutureWarning: Using a non-tuple sequence for multidimensional indexing is deprecated; use `arr[tuple(seq)]` instead of `arr[seq]`. This will raise an error in a future version.

```
return np.add.reduce(sorted[indexer] * weights, axis=axis) / sumval
```

Out[7]: [Text(0.5, 1.0, 'QQ Plot of Residuals')]



```
In [8]: best_arima1, results1 = auto_arima(sp_df.DailyRet[1:].values, p_max = 0, q_max = 0, d_max = 0)
        armodel1 = best_arima1['model']
        arresid1 = armodel1.resid
```

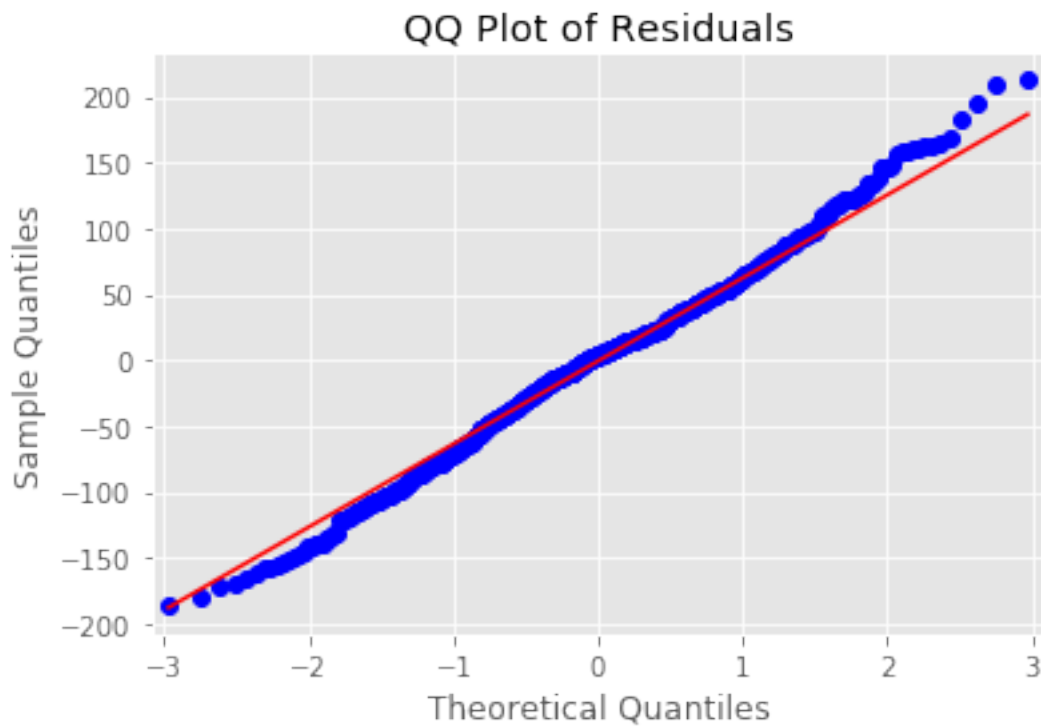
```
ARIMA(0, 0, 0) AIC:7578.85 BIC:7587.87  
Best model params:(0, 0, 0) AIC:7578.85 BIC:7587.87
```

```
In [9]: jbres1 = sm.stats.jarque_bera(arresid1)  
  
print("Jarque-Bera Normality Test on AR Residuals")  
print("statistic: {}".format(jbres1[0]))  
print("p-value: {}".format(jbres1[1]))  
print('skew: {}'.format(jbres1[2]))  
print('kurtosis: {}'.format(jbres1[3]))
```

```
Jarque-Bera Normality Test on AR Residuals  
statistic: 0.6653429629453448  
p-value: 0.717005705127056  
skew: 0.02162822835081098  
kurtosis: 3.1479565058733145
```

```
In [10]: axxx = plt.figure().add_subplot(111)  
sm.graphics.qqplot(arresid1, line='q', ax = axxx);  
axxx.set(title = 'QQ Plot of Residuals')
```

```
Out[10]: [Text(0.5, 1.0, 'QQ Plot of Residuals')]
```



**0.2.1** According to Jarque-Bera Normality Test, the ARIMA(0, 0, 0) is normally distributed, while the ARIMA(2, 0, 2) is not. However, their qq plots are very similar. Therefore, we cannot reject the null hypothesis. Both of them don't have large deviation from normal distribution.