

3.1.1 A)

- a) True ✓ $27 \in A$ b) False ✓ $27 \notin B$ c) True ✓ $100 \in B$ d) False ✓ $E \notin C$ e) $E \subseteq A$ True ✓
 f) $A \not\subseteq C$ False ✓ g) $E \in A$ ~~True~~ False ✓

3.1.2 B)

- a) False ✓ $15 \subset A$ b) ~~False~~ True ✓ $\{15\} \subset A$ c) True ✓ $\emptyset \subset A$ d) True ✓ $A \subseteq A$ e) $\emptyset \in B$ False ✓

3.1.5 c)

- b) $\{3, 6, 9, 12, \dots\} = \{x \in \mathbb{N} : x \geq 3 \text{ and } x \text{ is an integer multiple of } 3\}$
 The cardinality is infinite.

- c) $\{0, 10, 20, 30, \dots, 1000\} = \{x \in \mathbb{N} : x \leq 1000 \text{ and } x \text{ is an integer multiple of } 10\}$
 The cardinality is ~~100~~ 101.

3.2.1 d)

- a) $2 \in X$ True ✓ b) $\{2\} \subseteq X$ True ✓ c) $\{2\} \in X$ False ✓ d) $3 \in X$ False ✓ e) $\{1, 2\} \in X$ True ✓
 f) $\{1, 2\} \subseteq X$ True ✓ g) $\{2, 4\} \subseteq X$ True ✓ h) $\{2, 4\} \in X$ False ✓ i) $\{2, 3\} \subseteq X$ False ✓
 j) $\{2, 3\} \in X$ False ✓ k) $|X| = 7$ False ✓

3.2.4

b) Let $A = \{1, 2, 3\}$. What is $\{X \in P(A) : 2 \in X\}$

$$P(A) = \{\emptyset, \{2\}, \{1\}, \{3\}, \{1, 2\}, \{1, 3\}, \{2, 3\}, \{1, 2, 3\}\}$$

$$\{X \in P(A) : 2 \in X\} = \{2, \{1, 2\}, \{2, 3\}, \{1, 2, 3\}\} \times$$

$$\{X \in P(A) : 2 \in X\} = \{\{2\}, \{1, 2\}, \{2, 3\}, \{1, 2, 3\}\} \checkmark$$

3.3.1

$$c) A \cap C = \{-3, 1, 17\} \checkmark$$

$$d) A \cup (B \cap C) = \{-5, -3, 0, 1, 4, 17\} \checkmark \cup \{-5, 1\}$$

$$e) A \cap B \cap C = \{1\} \checkmark$$

$$\begin{array}{r} 2 \\ \times 25 \\ \hline 125 \end{array}$$

3.3.3

\emptyset

$$\{1\} \checkmark$$

$$a) \bigcap_{i=2}^5 A_i = \{1, 5, 25\} \times \text{ or } A_i \{x \in \mathbb{N} : 0 \leq x \leq 2, \text{ and } x \text{ is a power of } 5\}$$

$$b) \bigcup_{i=2}^5 A_i = \{1, 3, 16, 125\} \quad A_2 \cup A_3 \cup A_4 \cup A_5 = \{1, 2, 5, 4, 1, 16, 125\}$$

$$c) \bigcap_{i=1}^{100} C_i = \{x \in \mathbb{R} : -1/100 \leq x \leq 1/100\} \checkmark$$

$$f) \bigcup_{i=1}^{100} C_i = \{x \in \mathbb{R} : -1 \leq x \leq 1\} \checkmark$$

$$A_i = \{i^0, i^1, i^2, \dots\} \quad A_2 = \{1, 2, 4\} \quad A_3 = \{1, 3, 9\}$$

$$\bigcap_{i=2}^5 A_i$$

3.3.4

$$(b) P(A \cap B)$$

$$A = \{a, b\}$$

$$B = \{b, c\}$$

$$A \cap B = \{b\}$$

$$P(\{b\}) = 2$$

$$P(A \cup B)$$

$$A = \{a, b\}$$

$$B = \{b, c\}$$

$$A \cup B = \{a, b, c\}$$

$$P(A \cup B) = 2^3 = 8$$

$$\{\emptyset, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}, \{a, b, c\}\}$$

$$d) P(A) \cup P(B)$$

$$P(A) = \{\emptyset, \{a\}, \{b\}, \{a, b\}\}$$

$$P(B) = \{\emptyset, \{b\}, \{c\}, \{b, c\}\}$$

$$P(A) \cup P(B) = \{\emptyset, \{a\}, \{b\}, \{c\}, \{a, b\}, \{b, c\}\}$$

3.5.1

$$b) B \times A \times C$$

$$\{\text{foam, tall, whole}\} \in B \times A \times C$$

c) ✓

$\{\text{(foam, non-fat), (foam, whole), (no-foam, non-fat), (no-foam, whole)}\}$

3.5.3

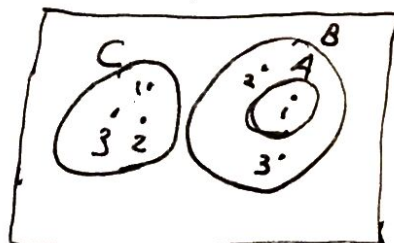
$$b) \mathbb{Z}^2 \subseteq \mathbb{R}^2 : \text{True} \checkmark$$

$$c) \mathbb{Z}^2 \cap \mathbb{Z}^3 = \emptyset : \text{True} \checkmark$$

e) For any three sets A, B, and C, if $A \subseteq B$, then

$$A \times C \subseteq B \times C$$

True ✓



3.5.6

d) xy : where $x \in \{0\} \cup \{0\}^2$ and $y \in \{1\} \cup \{1\}^2$

$$x = \{0, 00\}$$

$$y = \{1, 11\}$$

$$x = \{0, 00\}$$

$$y = \{1, 11\}$$

$$xy = \{01, 011, 001, 0011\}$$

$$xy = 000111$$

$$xy =$$

$$x = \{0, 00\}$$

$$y = \{1, 11\}$$

$$xy = \{01, 011, 001, 0011\}$$

e) xy : $x \in \{aa, ab\}$ and $y \in \{a\} \cup \{a\}^2$

$$x = \{aa, ab\}$$

$$y = \{a, aa\}$$

$$xy = \{a, aa, ab\}$$

$$x = \{aa, ab\}$$

$$y = \{a\} \cup \{a\}^2 = \{a, aa\}$$

$$x = \{aa, ab\}$$

$$y = \{a, aa\}$$

$$xy = aaaaab$$

$$xy = \{aaa, aaaa, aab, aaab\}$$

3.5.7

c) $(A \times B) \cup (A \times C)$

$(A \times B) = \{ab, ac\}$

$(A \times C) = \{aa, ab, ad\}$

$(A \times B) \cup (A \times C) = \{aa, ab, ac, ad\}$

d) $(A \times B) \cap (A \times C)$

$(A \times B) \cap (A \times C) = \{ab\}$

f) $P(A \times B)$

$A \times B = \{ab, ac\}$

$P(A \times B) = \{\emptyset, \{ab\}, \{ac\}, \{aa\}, \{ba\}, \{ca\}, \{bc\}, \{cb\}\}$

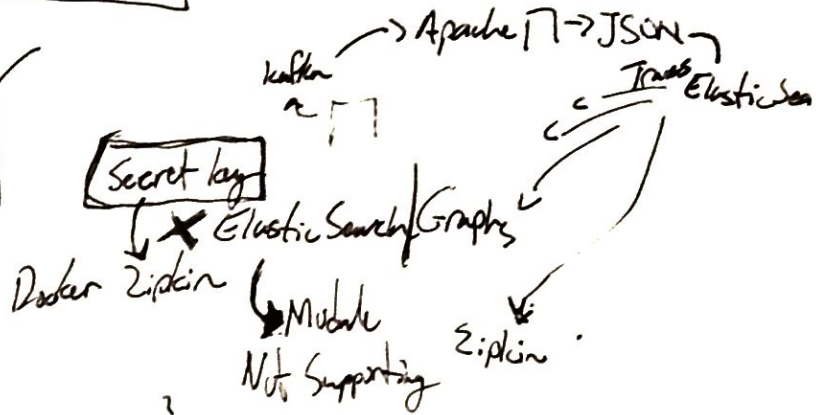
g) $P(A) \times P(B)$

$P(A) = P(\{a\}) = \{\emptyset, \{a\}\}$

$P(B) = P(\{b, c\}) = \{\emptyset, \{b\}, \{c\}, \{bc\}\}$

$P(A) \times P(B) = \{(\emptyset, \emptyset), (\emptyset, \{b\}), (\emptyset, \{c\}), (\emptyset, \{bc\}), (\{a\}, \emptyset), (\{a\}, \{b\}), (\{a\}, \{c\}), (\{a\}, \{bc\})\}$

create page
for Ms. Longmore
Selling Peanut Punch
Irish Moss
Sorel
Ginger Beer



3.5.7

f) $P(A \times B)$

$A = \{a\}$

$B = \{b, c\}$

$A \times B = \{ab, ac\}$

$P(A \times B) = \{ \{ab\}, \{ac\}, \{ba\}, \{bc\} \}$

$P(A \times B) = \{ \{\emptyset\}, \{ab\}, \{ac\}, \{ab, ac\} \}$

↑ This is a Basket

$(a, b) = ab = \text{orange}$

$(a, c) = ac = \text{apple}$

g) $P(A) \times P(B)$

$|P(A)| = 2^n = 2^1 = 2 \quad / \quad P(A) = \{ \{\emptyset\}, \{a\} \}$

$|P(B)| = 2^n = 2^2 = 4 \quad / \quad P(B) = \{ \{\emptyset\}, \{b\}, \{c\}, \{b, c\} \}$

$P(A) \times P(B) = \{ \{\{\emptyset, \emptyset\}\}, \{\{\emptyset, b\}\}, \{\{\emptyset, c\}\}, \{\{\emptyset, b, c\}\}, \{\{a, \emptyset\}\}, \{\{a, b\}\}, \{\{a, c\}\}, \{\{a, b, c\}\} \}$

3.6.2

$$B) (B \cup A) \cup (\bar{B} \cup A) = A$$

$$(B \cup A) \cup (\bar{B} \cup A)$$

$$\times 1 \quad A \cup (B \cup \bar{B}) = \text{Commutative Associative}$$

2.

$$(B \cup A) \cap (\bar{B} \cup A)$$

$$A \cup (B \cap \bar{B}) \rightarrow \text{Distrib.}$$

$$A \cup \emptyset \Rightarrow \text{Complement}$$

$$A \rightarrow \text{Identity}$$



$$C) \overline{A \cap \bar{B}} = \bar{A} \cup B$$

$$\overline{A \cap \bar{B}}$$

$$\bar{A} \cup \bar{\bar{B}} \Rightarrow \text{De Morgan}$$

$$\bar{A} \cup B \rightarrow \text{Double Complement}$$



3.6.3

$$B) A - (B \cap A) = A$$

If $A = \{1\}$ and $B = \{1, 2\}$ by taking the Difference of A away from the intersection of B and A , you are removing the A set $\{1\}$, leaving only elements found in $B \{2\}$.

$$D) (B - A) \cup A = A$$

If $B = \{1, 2\}$ and $A = \{1\}$ by taking the Difference of B from A , you are left with $B - A = \{2\}$. This is then unionized with A to get a set $\{1, 2\}$ which is not equal to $A = \{1\}$.

3.6.4

$$B) A \cap (B - A) = \emptyset$$

$$A \cap (B - A)$$

$$A \cap (B \cap \bar{A}) \rightarrow \text{Subtraction Law}$$

$$A \cap (\bar{A} \cap B) \rightarrow \text{Commutative}$$

$$(A \cap \bar{A}) \cap B \rightarrow \text{Associative}$$

$$\emptyset \cap B \rightarrow \text{Complement}$$

$$\emptyset \rightarrow \text{Domination}$$

~~$$D) A - (B - A)$$~~

$$C) A \cup (B - A) = A \cup B$$

$$A \cup (B - A)$$

$$A \cup (B \cap \bar{A}) \rightarrow \text{Subtraction}$$

$$(A \cup B) \cap (A \cup \bar{A}) \rightarrow \text{Distrib.}$$

$$(A \cup B) \cap U \rightarrow \text{Complement}$$

$$A \cup B \rightarrow \text{Identity}$$