

## Discrete Math: Arguments

Arguments: An "argument" is a sequence of statements. It consists of premises and a conclusion

Example: If John drinks beer, then John drinks alcohol  
John drinks beer.  $\therefore$  (Therefore) John drinks alcohol.

2 premises and 1 conclusion

Arguments can have any number of premises, but the last statement is the conclusion

Logical Form

$p \rightarrow q$   
 $p$   
 $\therefore q$

Want to abstract from arguments, and consider logical form.

Argument Form: A sequence of statement forms. It consists of premises and a conclusion

Argument Form

$p \rightarrow q$   
 $p$   
 $\therefore q$  } Known As Modus Ponens  
Valid If all premises are "T"  
then truth value of conclusion is "T"

# Truth Table for Modus Ponens

P	q	$P \rightarrow q$	P	q
T	T	T	T	T
T	F	F	T	F
F	T	T	F	T
F	F	T	F	F

- Critical Row
- All Premises "T"
- Conclusion is "T"
- Modus Ponens is Valid

Example 2: IF John drinks beer, then John drinks alcohol.  
 John doesn't drink beer.  
 $\therefore$  John doesn't drink alcohol

## Logical Form

$$P \rightarrow q$$

$$\neg P$$

$$\therefore \neg q$$

## Truth Table

P	q	$P \rightarrow q$	$\neg P$	$\neg q$
T	T	T	F	F
T	F	F	F	T
F	T	T	T	F
F	F	T	T	T

- > Critical Rows
- 3rd Row, Premises "T", Conc. "F"
- 3rd Row Not Valid