CS 188 Introduction to Spring 2019 Artificial Intelligence

Written HW 7

Due: Monday 4/1/2019 at 11:59pm (submit via Gradescope).

Leave self assessment boxes blank for this due date.

Self assessment due: Monday 4/8/2019 at 11:59pm (submit via Gradescope)

For the self assessment, fill in the self assessment boxes in your original submission (you can download a PDF copy of your submission from Gradescope – be sure to delete any extra title pages that Gradescope attaches). For each subpart where your original answer was correct, write "correct." Otherwise, write and explain the correct answer. Do not leave any boxes empty.

If you did not submit the homework (or skipped some questions) but wish to receive credit for the self-assessment, we ask that you first complete the homework without looking at the solutions, and then perform the self assessment afterwards.

Policy: Can be solved in groups (acknowledge collaborators) but must be written up individually

Submission: Your submission should be a PDF that matches this template. Each page of the PDF should align with the corresponding page of the template (page 1 has name/collaborators, question 1 begins on page 2, etc.). **Do not reorder, split, combine, or add extra pages.** The intention is that you print out the template, write on the page in pen/pencil, and then scan or take pictures of the pages to make your submission. You may also fill out this template digitally (e.g. using a tablet.)

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Last name	Han
SID	3032325102
Collaborators	

Q1. Probability

- (a) For the following questions, you will be given a set of probability tables and a set of conditional independence assumptions. Given these tables and independence assumptions, write an expression for the requested probability tables. Keep in mind that your expressions cannot contain any probabilities other than the given probability tables. If it is not possible, mark "Not possible."
 - (i) Using probability tables P(A), $P(A \mid C)$, $P(B \mid C)$, $P(C \mid A, B)$ and no conditional independence assumptions, write an expression to calculate the table $P(A, B \mid C)$.

 $P(A, B \mid C) =$ Not possible.

(ii) Using probability tables P(A), $P(A \mid C)$, $P(B \mid A)$, $P(C \mid A, B)$ and no conditional independence assumptions, write an expression to calculate the table $P(B \mid A, C)$.

 $\mathbf{P}(\mathbf{B} \mid \mathbf{A}, \mathbf{C}) = \begin{array}{c} P(A) \ P(B|A) \ P(C|A,B) \ / \ P(A) \ P(B|A) \ P(C|A,B) \end{array} \qquad \bigcirc \quad \text{Not possible.}$

(iii) Using probability tables $P(A \mid B), P(B), P(B \mid A, C), P(C \mid A)$ and conditional independence assumption $A \perp \!\!\! \perp B$, write an expression to calculate the table P(C).

 $\mathbf{P}(\mathbf{C}) = P(A|B) P(C|A)$ One possible.

(iv) Using probability tables $P(A \mid B, C), P(B), P(B \mid A, C), P(C \mid B, A)$ and conditional independence assumption $A \perp \!\!\!\perp B \mid C$, write an expression for P(A, B, C).

P(A, B, C) = Not possible.

Self assessment If correct, write "correct" in the box. Otherwise, write and explain the correct answer.

- (ii) and (iii) needs to include summation symbol. For (ii) add summation symbol in the denominator.
- (b) For each of the following equations, select the *minimal set* of conditional independence assumptions necessary for the equation to be true.
 - (i) $P(A, C) = P(A \mid B) P(C)$

 $\Box A \perp \!\!\!\perp B$

 \Box $A \perp \!\!\!\perp B \mid C$

 \Box $A \perp \!\!\! \perp C$

 \square $A \perp \!\!\!\perp C \mid B$

 \Box $B \perp \!\!\! \perp C$

 \square $B \perp \!\!\!\perp C \mid A$

☐ No independence assumptions needed.

(ii) $P(A \mid B, C) = \frac{P(A) \cdot P(B \mid A) \cdot P(C \mid A)}{P(B \mid C) \cdot P(C)}$

 \square $A \perp \!\!\!\perp B$

 \square $A \perp \!\!\!\perp B \mid C$

 \square $A \perp \!\!\! \perp C$

 \square $A \perp \!\!\!\perp C \mid B$

 \square $B \perp \!\!\! \perp C$

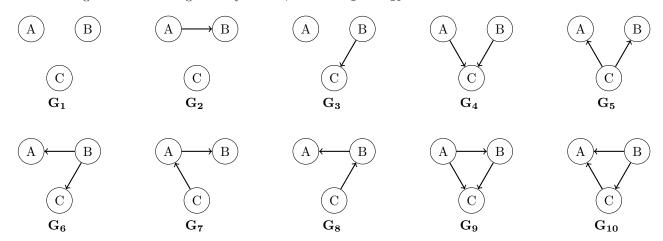
 \square $B \perp \!\!\!\perp C \mid A$

☐ No independence assumptions needed.

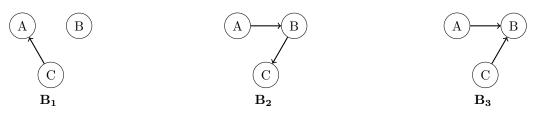
	(iii) P (.	$(\mathbf{A}, \mathbf{B}) = \sum_{\mathbf{c}} \mathbf{P}(\mathbf{A} \mid \mathbf{B}, \mathbf{c}) \ \mathbf{P}(\mathbf{B} \mid \mathbf{c}) \ \mathbf{P}(\mathbf{c})$						
		$\begin{array}{c} A \perp\!\!\!\perp B \\ A \perp\!\!\!\perp B \mid C \\ A \perp\!\!\!\perp C \\ A \perp\!\!\!\perp C \mid B \end{array}$		$\begin{array}{c} B \perp \!\!\! \perp C \\ B \perp \!\!\! \perp C \mid A \\ \mbox{No independence assumptions needed.} \end{array}$				
	(iv) P($\mathbf{A}, \mathbf{B} \mid \mathbf{C}, \mathbf{D}) = \mathbf{P}(\mathbf{A} \mid \mathbf{C}, \mathbf{D}) \ \mathbf{P}(\mathbf{B} \mid \mathbf{A}, \mathbf{C}, \mathbf{D})$						
		$\begin{array}{c} A \perp\!\!\!\perp B \\ A \perp\!\!\!\perp B \mid C \\ A \perp\!\!\!\perp B \mid D \\ C \perp\!\!\!\perp D \end{array}$		$\begin{array}{c} C \perp\!\!\!\perp D \mid A \\ C \perp\!\!\!\perp D \mid B \\ \\ \hbox{No independence assumptions needed.} \end{array}$				
	Self as	sessment If correct, write "correct" in the box. Oth	erwise	e, write and explain the correct answer.				
	1	ect answer is A independent of B and A independent rect answer is B independent of C A.	of C.					
(c)	(i) Ma	rk all expressions that are equal to $P(A \mid B)$, gi	ven	no independence assumptions.				
		$\sum_{c} P(A \mid B, c)$		$\frac{P(A,C B)}{P(C B)}$				
		$\sum_{c} P(A, c \mid B)$		$\frac{P(A C,B) \ P(C A,B)}{P(C B)}$				
		$\frac{P(B A) \ P(A C)}{\sum_{c} P(B,c)}$		None of the provided options.				
		$\frac{\sum_{c} P(A,B,c)}{\sum_{c} P(B,c)}$						
	(ii) Ma	rk all expressions that are equal to $\mathbf{P}(\mathbf{A}, \mathbf{B}, \mathbf{C})$,	given	that $\mathbf{A} \perp \!\!\! \perp \mathbf{B}$.				
		$P(A \mid C) \ P(C \mid B) \ P(B)$		$P(A) \ P(B \mid A) \ P(C \mid A, B)$				
		$P(A) P(B) P(C \mid A, B)$		$P(A,C) P(B \mid A,C)$				
		$P(C) \ P(A \mid C) \ P(B \mid C)$		None of the provided options.				
	$\square P(A) \ P(C \mid A) \ P(B \mid C)$							
	(iii) Mark all expressions that are equal to $P(A, B \mid C)$, given that $A \perp \!\!\! \perp B \mid C$.							
		$P(A \mid C) \ P(B \mid C)$		$\frac{\sum_{c} P(A, B, c)}{P(C)}$				
		$\frac{P(A) \ P(B A) \ P(C A,B)}{\sum_{c} P(A,B,c)}$		$\frac{P(C,A B)\ P(B)}{P(C)}$				
		$P(A \mid B) \ P(B \mid C)$		None of the provided options.				
		$\frac{P(C) \ P(B C) \ P(A C)}{P(C A,B)}$						
	Self assessment If correct, write "correct" in the box. Otherwise, write and explain the correct answer.							
	(i): Correct answer is option 2 and 4 in the first column(ii): Correct answer is option 2 from the first column and 1,2 from the second column.(iii): Correct answer is option 1 from first column and 2 from the second column.							

Q2. Bayes' Nets: Representation

Assume we are given the following ten Bayes' nets, labeled $\mathbf{G_1}$ to $\mathbf{G_{10}}:$



Assume we are also given the following three Bayes' nets, labeled ${\bf B_1}$ to ${\bf B_3}:$



(continued on next page)

					tion d_1 (over A ranteed to be a) can be represer represent \mathbf{d}_1 .	ited by	Bayes' net $\mathbf{B_1}$.	Mark all of	
		$\mathbf{G_1}$		$\mathbf{G_2}$				$\mathbf{G_4}$		G_5	
		G_6		G_7		G_8		G_9		G_{10}	
		None of th	e above.								
	Self assessment If correct, write "correct" in the box. Otherwise, write and explain the correct answer.										
	Correct										
(b)	Assume	we know th:	at a joint d	istribu	tion d ₂ (over A	. B. C) can be represer	ited by	Bayes' net B ₂ .	Mark all of	
					ranteed to be a			red by	Bay os not B ₂ .	man an or	
		G_1		G_2		G_3		G_4		G_5	
		G_6		G_7		G_8		G_9		G_{10}	
		None of th	e above.								
	Self assessment If correct, write "correct" in the box. Otherwise, write and explain the correct answer.										
	Correct	:									
(c)	Assume	we know th	at a joint d	listribu	ition $\mathbf{d_3}$ (over A	A , B , C	C) <i>cannot</i> be rep	oresent	ed by Bayes' net	$\mathbf{B_3}$. Mark	
		_	Bayes' nets		_		ble to represent		_		
		G_1		G_2		G_3		G_4		G_5	
		G_6		G_7		G_8		G_9		G_{10}	
		None of th	e above.								
	Self as	sessment	If correct, wi	rite " co ı	rrect" in the box.	Other	wise, write and ex	plain t	he correct answer.		
	Correct										
(d)	Assume	we know th	at a joint o	listribu	ution $\mathbf{d_4}$ (over \mathbf{A}	A , B , C	C) can be represe	ented b	by Bayes' nets B	$\mathbf{B_1}$, $\mathbf{B_2}$, and	
							eed to be able to			1, 2,	
		G_1		G_2		G_3		$\mathbf{G_4}$		G_5	
		G_6		G_7		G_8		G_9		G_{10}	
		None of th	e above.								
	Self as	sessment	If correct, wi	rite "co	rrect" in the box.	Other	wise, write and ex	plain t	he correct answer.		
	Correc	t									
	331166	•									