

Revision of delayed biological systems with Answer Set Programming

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Abstract. The modeling of biologicals systems relies on background knowledge, deriving either from literature and/or the analysis of biological observations. But with the development of high-throughput data, there is a growing need for methods that are able to automatically revise the existing models with regard to additional observations obtained by biologists. Our research aims at providing a logical approach to revise biological regulatory networks thanks to time series data, *i.e.*, gene expression data depending on time. In this paper, we propose two revision methodologies for models expressed through a timed extension of the Process Hitting framework (which is a restriction, well suited for biological systems, of networks of synchronizing timed automata). The revision methods we introduce aim to make the minimum amount of modifications (addition/deletion of actions between biological components) to a given input model so that the resulting model is most consistent with the observed data. They are implemented in Answer Set Programming, which is a paradigm proven efficient to tackle knowledge representation problems. We illustrate the merits of our methods in a twofold way: (1) we exhibit the benefits of such automatic approaches on a case study consisting of a qualitative model of circadian clock; (2) we lead computational experiments on various benchmarks to show the performances of our algorithms.

Keywords: Answer Set Programming, Process Hitting, dynamic modeling, time-varying genetic networks, network revision

1 Introduction

With both the spread of numerical tools in every part of daily life and the development of new measurement technologies (like DNA microarrays in biology), a large amount of time series data is now produced every day, every minute, every second [12]. This means that the number of experiments - and corresponding data - led on a biological system grows drastically. The newly produced data - as long as the associated noise does not raise an issue with regard to the precision and relevance of the corresponding information - can give us some new

insights on the behavior of a system. This justifies the urge to design efficient revision methods that are able to update previous knowledge on a model with regard to additional information. In other words, there is a strong need for automatic methods that update a given model so that the dynamics of the model is consistent with given observations and a set of criteria (for example, minimize the number of modifications).

Network completion has been the subject of numerous recent works. In [2], the authors targeted the completion of stationary Boolean networks. This method has been further refined along the years. Latest works [14] focus on completion in Time Varying Genetic Networks. These are networks whose topology does not change through time, but the nature of the interactions (activation, inhibition, or no interaction) between components may change at some (finite number of) time points. The completion approach (which, in these authors' papers, refers to both addition and deletion of interactions, making it a synonym of revision) has been successfully applied to biological case-studies, for example the DREAM4 Challenge [16], and the implementation has been improved through heuristics [15]. The method however is limited to acyclic networks.

Logical-based approaches may be also fruitful to network revision. It has been successfully applied to causal networks [11] and molecular networks represented with the SBGN-AF language [22].

Despite being a proper research area, revision is strongly connected to model inference. Starting from an empty model, revision may indeed be used to model from gene expression data. On the reverse, existing inference algorithms may be an inspiration for new revision methodologies. In particular, Answer Set Programming (ASP), a form of declarative programming that has been successively used in many knowledge representation and reasoning tasks [17,3,4] has been proven useful for network reconstruction [8] and inference of metabolic networks [21].

To our knowledge, no works have been led so far in the field of revision of timed models, without any restriction on the structure of the network.

In this paper, we aim to provide a logical approach to tackle the revision of qualitative models of biological dynamic systems, like gene regulatory networks. In our context, we assume the set of interacting components as fixed and we consider potential additions/deletions of interactions between components. The main originality of our work is that we address this problem in a timed setting, with quantitative delays potentially occurring between the moment an interaction activated and the moment its effect is visible. It allows for example to catch delays between the activation of a gene, and the moment the concentration of a gene reaches a qualitative threshold.

During the past decade, there has been a growing interest for the hybrid modeling of gene regulatory networks with delays. These hybrid approaches consider various modeling frameworks. In [13], the authors hybrid Petri nets: the advantage of hybrid with regard to discrete modeling lies in the possibility of capturing biological factors, e.g., the delay for the transcription of RNA polymerase. The merits of other hybrid formalisms in biology have been studied, for instance

timed automata [20] and hybrid automata [1]. Finally, in [7], the authors investigate a direct extension of the discrete René Thomas’ modeling approach by introducing quantitative delays. These delays represent the compulsory time for a gene to turn from a discrete qualitative level to the next (or previous) one. They exhibit the advantage of such a framework for the analysis of mucus production in the bacterium *Pseudomonas aeruginosa*. The approach we propose in this paper inherits from this idea that some models need to capture these timing features.

In order to address the formal checking of dynamical properties within very large BRNs, we previously introduced in [18] a new formalism, named the “*Process Hitting*” (PH), to model concurrent systems having components with a few qualitative levels. Being a particular restriction of asynchronous automata networks or safe Petri nets, Process Hitting can be applied to complex dynamical systems with a very large number of interacting components, where each of these components can be described with a few internal states. In this paper, following recent works enriching (by adding priorities) the expressivity of PH while preserving its efficiency [9], we extend PH with quantitative timing features and exhibit efficient ASP-based approaches to perform network revision.

As readers may not be familiar with PH, we briefly introduce it in section 2, then give in section 3 some preliminary insights about recent translation of PH into ASP presented in [5]. All theoretical and practical notions are then settled to introduce our timed extension of PH, and related completion algorithm in section 4. Then we illustrate the merits of our approach in section 5 by first applying it on a simplified model of mammalian circadian clock [6], then discussing the practical results on a range of benchmarks from bioinformatics literature. Finally, in section 6, we summarize our contribution and give some perspectives for future works.

2 Process Hitting

Definition 1 introduces the Process Hitting(PH) [18] which allows to model a finite number of local levels, called *processes*, grouped into a finite set of components, called *sorts*. A process is noted a_i , where a is the sort’s name, and i is the process identifier within sort a . At any time, exactly one process of each sort is *active*, and the set of active processes is called a *state*.

The concurrent interactions between processes are defined by a set of *actions*. Each action is responsible for the replacement of one process by another of the same sort conditioned by the presence of at most one other process in the current state. An action is denoted by $a_i \rightarrow b_j \uparrow b_k$, which is read as a_i *hits* b_j to make it *bounce* to b_k , where a_i , b_j , b_k are processes of sorts a and b , called respectively *hitter*, *target* and *bounce* of the action. We also call a *self-hit* any action whose hitter and target sorts are the same, that is, of the form: $a_i \rightarrow a_i \uparrow a_k$.

The PH is therefore a restriction of synchronous automata, where each transition changes the local state of exactly one automaton, and is triggered by the local states of at most two distinct automata. This restriction in the form of the

actions was chosen to permit the development of efficient static analysis methods based on abstract interpretation [19].

Definition 1 (Process Hitting). A Process Hitting is a triple $(\Sigma, \mathcal{L}, \mathcal{H})$ where:

- $\Sigma = \{a, b, \dots\}$ is the finite set of sorts;
- $\mathcal{L} = \prod_{a \in \Sigma} \mathcal{L}_a$ is the set of states where $\mathcal{L}_a = \{a_0, \dots, a_{l_a}\}$ is the finite set of processes of sort $a \in \Sigma$ and l_a is a positive integer, with $a \neq b \Rightarrow \mathcal{L}_a \cap \mathcal{L}_b = \emptyset$;
- $\mathcal{H} = \{a_i \rightarrow b_j \uparrow b_k \in \mathcal{L}_a \times \mathcal{L}_b^2 \mid (a, b) \in \Sigma^2 \wedge b_j \neq b_k \wedge a = b \Rightarrow a_i = b_j\}$ is the finite set of actions.

Example 1. The figure 1 represents a $\mathcal{PH}(\Sigma, \mathcal{L}, \mathcal{H})$ with three sorts ($\Sigma = \{a, b, c\}$) and: $\mathcal{L}_a = \{a_0, a_1\}$, $\mathcal{L}_b = \{b_0, b_1\}$, $\mathcal{L}_z = \{z_0, z_1, z_2\}$.

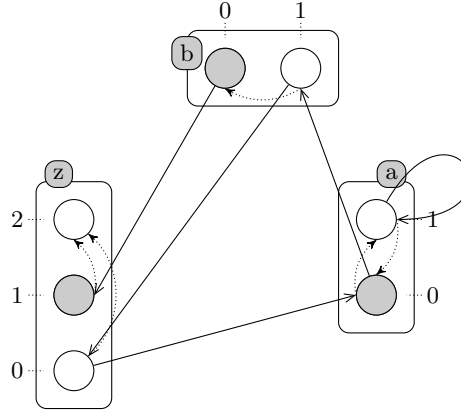


Fig. 1. A PH model example with three sorts: a , b and z (a is either at level 0 or 1, b at either level 0 or 1 and z at either level 0, 1 or 2). Boxes represent the *sorts* (network components), circles represent the *processes* (component levels), and the 5 *actions* that model the dynamic behavior are depicted by pairs of arrows in solid and dotted lines. The grayed processes stand for the possible initial state: $\langle a_1, b_0, z_1 \rangle$.

A state of the networks is a set of active processes containing a single process of each sort. The active process of a given sort $a \in \Sigma$ in a state $s \in \mathcal{L}$ is noted $s[a]$. For any given process a_i we also note: $a_i \in s$ if and only if $s[a] = a_i$. The dynamic of the PH networks is satisfied thanks to the actions. Indeed, the transition from one state s_1 to its successor s_2 is done when there is a playable action (definition 7) at s_1 . After each transition only one sort, or one component, changes its level from one process to another.

We note that during these last years the Process Hitting framework was improved and we added new type of sorts like cooperative sorts and new actions like plural actions, actions with priority and actions with delay.

In some cases it is necessary to represent a reaction of a set of components on one component. For example in the bio-chemical reactions $X \xrightarrow{Y} Z$ or $X + Y \rightarrow Y + Z$, where X is a set of reactives, Y a set of catalysts and Z a set of products. The plural action permits to represent this kind of reactions in PH. The plural is made up of two sets of processes of different sorts, which represent all the hitters and the bonds.

Definition 2 (Plural action). Let $\mathcal{PH} = (\Sigma, \mathcal{L}, \mathcal{H})$ be a process hitting. A plural action is an action noted by: $h = A \rightarrow b_j \uparrow b_k$ with $A \in \mathcal{L}^\diamond \wedge b_j \neq b_k \wedge \text{if } b_i \in A \Rightarrow A = b_i$. We note that \mathcal{L}^\diamond is the set of all the sub-states of \mathcal{L} .

Example 2. We give a simple example to represent a plural action by a cooperation between two biological components (x and y) in order to activate another component (z) and change its level from 0 to 1: $\{x_1, y_1, z_0\} \rightarrow \{x_1, y_1, z_1\}$ and in PH it can be translated by this action: $\{x_1 \wedge y_1\} \rightarrow z_0 \uparrow z_1$.

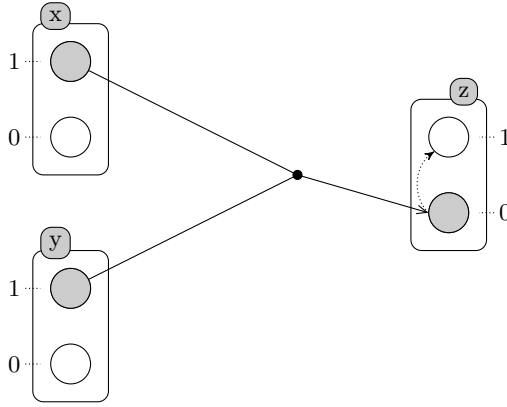


Fig. 2. Representation of a plural action in Process Hitting network: $\{x_1 \wedge y_1\} \rightarrow z_0 \uparrow z_1$.

In some dynamics it is crucial to have information about the delays between two events (two states in PH). The normal actions cannot show this information we just know that the state s_2 will be after s_1 in the next step but it is not possible to know how much time this transition takes time. We propose to add the delay in the action attributes which is responsible of the transition between the two states. That means that this action needs to be played during a specific time so that the system doesn't change the state (definition 3).

Definition 3 (timed plural action). A timed plural action is a plural action with a delay D : $A \xrightarrow{D} b_i \uparrow b_j$ where $D \in \mathbb{R}^+$, $A \in \mathcal{L}^\diamond$, and b_i, b_j where $b_i \neq b_j$ are two processes of the target sort b . If $b_i \in A$, $A = b_i$.

Definition 4 (Process Hitting with timed plural actions). A Process Hitting is a triple $(\Sigma, \mathcal{L}, \mathcal{H}_{tp})$ where:

- $\Sigma = \{a, b, \dots\}$ is the finite set of sorts;
- $\mathcal{L} = \prod_{a \in \Sigma} \mathcal{L}_a$ is the set of states where $\mathcal{L}_a = \{a_0, \dots, a_{l_a}\}$ is the finite set of processes of sort $a \in \Sigma$ and l_a is a positive integer, with $a \neq b \Rightarrow \mathcal{L}_a \cap \mathcal{L}_b = \emptyset$;
- $\mathcal{H}_{tp} = \{A \xrightarrow{D} b_j \uparrow b_k \mid A \in \mathcal{L}^\circ, b_j \neq b_k, b_i \in A \Rightarrow A = b_j\}$ is the finite set of timed plural actions.

Definition 5 (Playable timed plural action). Let $\mathcal{PH} = (\Sigma, \mathcal{L}, \mathcal{H}_{tp})$ be a Process Hitting with timed plural actions and $s \in \mathcal{L}$ a state of PH. We say that the action $h = A \xrightarrow{D} b_i \uparrow b_j$ is playable in state s if and only if $A \subseteq s$ and $b_i \in s$.

Definition 6 (autonomous temporised sort). A sort a is said to be an autonomous temporised sort if and only if $\forall h = A \xrightarrow{D} a_i \uparrow a_j \in \mathcal{H}$ where a_i and a_j are processes of a , we have only $A = \{a_i\}$.

Definition 7 (Successor state). Let $\mathcal{PH} = (\Sigma, \mathcal{L}, \mathcal{H}_{tp})$ be a Process Hitting with timed plural actions and $s \in \mathcal{L}$ be the state of \mathcal{PH} at time t . If there is no action in \mathcal{PH} that is playable in s the state of the system remain s for all $t' > t$ (i.e. steady state). Let $h = A \xrightarrow{D} b_i \uparrow b_j$ be a playable action in s . If there is no temporised sort a , that change its process from $a_i \in A$ to $a_j \notin A$ while playing h in s then the state of \mathcal{PH} at $t + D$ is called a successor of s and is denoted by $(s \cdot h)$, where $(s \cdot h)[b] = b_k$ and $\forall c \in \Sigma, c \neq b \Rightarrow (s \cdot h)[c] = s[c]$.

The PH was chosen for several reasons. First, it is a general framework that, although it was mainly used for biological networks, allows to represent any kind of dynamical model, and converters to several other representations are available (see section). Although an efficient dynamical analysis already exists for this framework, based on an approximation of the dynamics, it is interesting to identify its limits and compare them to the approached we present later in this paper. Finally, the particular form of the actions in a PH model allow to easily represent them in ASP, with one fact per action, as described in the next section. Other representations may have required supplementary complexity; for instance, a labeling would be required if actions could be triggered by a variable number of processes.

The rest of the report focuses on the representation of the previous definitions through ASP than we give the example of Circadian Clock network. Later we propose an approach to resolve the completion problem of PH networks with the use of ASP.

3 PH through ASP

3.1 Answer Set Programming

In this section, we recapitulate the basic elements of ASP. An answer set program is a finite set of rules of the form

$$a_0 \text{ :- } a_1, \dots, a_m, \text{ not } a_{m+1}, \dots, \text{ not } a_n \quad (1)$$

where $n \geq m \geq 0$, a_0 is a propositional atom or \perp , all a_1, \dots, a_n are propositional atoms and the symbol "not" denotes default negation. If $a_0 = \perp$, then Rule (1) is a constraint (in which case a_0 is usually omitted). The intuitive reading of a rule of form (1) is that whenever a_1, \dots, a_m are known to be true and there is no evidence for any of the default negated atoms a_{m+1}, \dots, a_n to be true, then a_0 has to be true as well. Note that \perp can never become true.

In the ASP paradigm, the search of solutions consists in computing answer sets of answer set program. An answer set for a program is defined by Gelfond and Lifschitz [10] as follow. An interpretation I is a finite set of propositional atoms. An atom a is true under I if $a \in I$, and false otherwise. A rule r of form 1 is true under I if $\{a_1, \dots, a_m\} \subseteq I$ and $\{a_{m+1}, \dots, a_n\} \cap I = \emptyset$ implies $a_0 \in I$. An Interpretation I is a model of a program P if each rule $r \in P$ is true under I . Finally, I is an answer set of P if I is a subset-minimal model of P^I , where P^I is defined as the program that results from P by deleting all rules that contain a default negated atom from I , and deleting all default negated atoms from the remaining rules. Programs can yield no answer set, one answer set, or many answer sets. To compute answer sets of an answer set program, we run an ASP solver.

3.2 Translation of PH networks to ASP

PH network is easy to be presented in ASP. Indeed we need only 3 predicates to define the whole network: "sort" to define sorts, "process" for the processes and "action" for the network actions. We will see in example ?? how a PH network is defined with these predicates.

Example 3 (Representation of a PH network in ASP). The representation of the PH network of figure 1 in ASP is the following:

```

1 process("a", 0..1). process("b", 0..1). process("z", 0..2).
2 sort(X) ← process(X,I)
3 action("a",0,"b",1,0). action("a",1,"a",1,0). action("b",1,"z",0,2).
4 action("b",0,"z",1,2). action("z",0,"a",0,1).
```

In line 1 we create the list of processes corresponding to each sort, for example the sort "z" has 3 processes numbered from 0 to 2; this specific predicate will in fact expand into the three following predicates: `process("z", 0)`, `process("z", 1)`, `process("z", 2)`. Line 2 enumerates every sort of the network from the previous information. Finally, all the actions of the network are defined in lines 3 and 4; for example, the first predicate `action("a",0,"b",1,0)` represents the action $a_0 \rightarrow b_1 \uparrow b_0$.

Example 4 (Representation of PH network with plural-timed actions in ASP).

We can take the example at the figure 2 and consider that the action $\{x_1, y_1, z_0\} \xrightarrow{D} \{x_1, y_1, z_1\}$ has a delay "D" and in PH the action becomes: $x_1 \wedge y_1 \rightarrow z_0 \uparrow z_1$. So that the PH network in ASP is:

```

5 process("x", 0..1). process("y", 0..1). process("z", 0..1).
6 action("x",1,"y",1,"z",0,1,D).
```

The number of indegree in this action $i = 2$, there is only 2 hitters. It is possible to have an indegree greater than 2. We will show later that the number of the maximum indegree should be an input for in our algorithm.

The predicator `action` represents the ordinary actions as well as the plural actions. Indeed an ordinary action is a plural action with an indegree 1. Moreover all the ordinary actions are a timed action with a delay equal to 1 unit of time. Each action need at least one step to be played. For example the action `action("a",0,"b",1,0)` is equivalent to `action("a",0,"b",1,0,1)`. So the plural-timed action is a generalized way to represent the actions in a Process Hitting network. Thus in the following part we will consider only plural-timed actions.

4 Completion of PH networks

4.1 Asynchronous and non-deterministic networks

4.2 Formalization

4.3 Algorithm

In this section we propose a simple algorithm to complete Process Hitting networks. This algorithm takes as input a Process Hitting and a chronogram of genes evolutions of this network. Knowing the genes influences (or assuming all possible influences), this algorithm will complete the input network by adding the delayed actions that could have realized the changes observed in the chronogram. Algorithm 1 show the pseudo code of our algorithm. If the observations are perfect, it will generate all possible actions that can realize each change observed. Because of the delayed semantic, it is not possible to decide if an action is correct or not. But we can output the minimal sets of actions necessary to realize the changes observed. If the observation are not perfect, we can merge actions by replacing the one that only differ by their delay by one action where its delay is the average. The intuition is that, in practice, if there is enough observation, the delay of those actions should tend to the real value.

Theorem 1 (Completeness). *Let PH be a Process Hitting, C be a chronogram of the genes of PH and A be the set of actions of PH whose realized the chronogram C . Let PH' be a Process Hitting and A' be the set of actions of PH' such that $A' \subseteq A$. Given PH' and C as input, Algorithm 1 (without step 2) is complete: it will output a set of process hitting S , such that $\exists PH'' \in S$ with A'' the set of actions of PH'' such that $A'' = A' \cup A$.*

Proof. Let's suppose that the algorithm is not complete, then there is an action $a \in A$ that realized C and $a \notin A''$. After step 1.2, PH'' contains all actions that can realized each gene change. Here there is no action $a \in A$ that realized C which is not generated by the algorithm, so $a \in A''$. Then it implies that at step 3, the action a is removed from A'' . But since a realized one the change of C and a is generated at step 1, then it will be present in one of the minimal subset of actions. And a will be in one of the network outputted by the algorithm. \square

Algorithm 1 PH-Completion($PH, Chronogram, Influences, indegree$)

-
- INPUT: a Process Hitting PH , a chronogram C of the genes evolution of PH , the genes influences and a maximal action in-degree i .
 - Let $A := \emptyset$
 - Step 1: For each time where a gene G changes its value from P to P' in C :
 - Let D be the delay since the last time a gene has changed.
 - Generate all actions with delay D which involve all subsets of size i of the genes S_1, \dots, S_n having an influence on G :

$$a := action(S_1, P_1, \dots, S_n, P_n, G, P, P', D)$$

- Add all action a in A
- Step 2 (optional): Merge each action with the same hitters, $S_1, P_1, \dots, S_n, P_n$ and the same target, G, P, P' , into one action where the delay is the average.
- Step 3: Generate S the set of all minimal subsets of actions of A that realize C :

$$\forall A \in S, \nexists A' \in S, A' \subset A$$

- OUTPUT: S a set of completed Process Hitting that realize the chronogram.
-

Theorem 2 (Complexity). *Let PH be a Process Hitting, S be the number of sorts of PH and P be the maximal number of processes of a sort of PH . Let C be a chronogram of the genes of PH over T units of time, such that c is the number of gene change of C . The memory use of our algorithm belongs to $O(T \times P \times i^S \times 2^{T \times P \times i^S})$ that is bound by $O(T \times P^{S+1} \times 2^{T \times P^{S+1}})$. The complexity of completing PH by generating actions from the observations of C with Algorithm 1 belongs to $O(c \times i^S + (T \times P \times i^S)^2 + 2^{2 \times T \times P \times i^S} + c \times 2^{T \times P \times i^S})$ that is bound by $O(2^{3 \times T \times P^{S+1}})$.*

Proof. Let i be the maximal indegree of an action in PH , $0 \leq i \leq P$. Let p be a process of PH and n be the number of sorts that can influence p . There is i^S possible combinations of those process that can hit p , each of those can form an action. There is P process and atmost T possibles delay, so that there are $T \times P \times i^S$ possibles actions, thus at step 1, the memory of our algorithm is bound by $O(T \times P \times i^S)$, which belongs to $O(T \times P^{S+1})$ since $0 \leq i \leq P$. Generating all minimal subset of actions A of PH' that realize C can require to generate at most $2^{T \times P \times i^S}$ set of rules. Thus, the memory of our algorithm belongs to $O(T \times P \times i^S \times 2^{T \times P \times i^S})$ and is bound by $O(T \times P^{S+1} \times 2^{T \times P^{S+1}})$.

Merging the actions at step 2 is polynomial in the number of actions and the complexity of this operation belongs to $O((T \times P \times i^S)^2)$. The complexity of this algorithm belongs to $O(c \times i^S + (T \times P \times i^S)^2)$. Since $0 \leq i \leq P$ and $0 \leq c \leq T$ the complexity of Algorithm 1 is bound by $O(T \times P^S + (T \times P \times P^S)^2) = (T \times P^S + T^2 \times P^{2S+2})$.

Generating all minimal subset of actions A of PH' that realize C can require to generate atmost $2^{T \times P \times i^S}$ set of rules. Each set has to be compared

with the others to keep only the minimal ones, this cost $O(2^{2 \times T \times P \times i^S})$. Furthermore, each set of action has to realize each change of C , it require to check c changes and cost $O(c \times 2^{T \times P \times i^S})$. Finally, the total complexity of completing PH by generating actions from the observations of C belongs to $O(c \times i^S + (T \times P \times i^S)^2 + 2^{2 \times T \times P \times i^S} + c \times 2^{T \times P \times i^S})$ that is bound by $O(T \times P^S + (T \times P^{S+1})^2 + 2^{2 \times T \times P^{S+1}} + T \times 2^{T \times P^{S+1}})$ \square

5 Evaluation

5.1 Application: Circadian clock

5.2 Benchmarks

6 Conclusion and perspectives

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