

Q3:

$$z = a.$$

$$y z \Rightarrow y: a \rightarrow b.$$

$$(y z): b.$$

$$x z \Rightarrow x: a \rightarrow d.$$

$$(x z): d.$$

$$(x z)(y z) \Rightarrow d: b \rightarrow c.$$

$$\therefore x: a \rightarrow b \rightarrow c.$$

$$y: a \rightarrow b.$$

$$z = a.$$

$$(x z)(y z): c.$$

$$S = \text{fun } x \rightarrow (\text{fun } y \rightarrow (\text{fun } z \rightarrow (x z) (y z)))$$

$$S: (x: a \rightarrow b \rightarrow c) \rightarrow (y: a \rightarrow b) \rightarrow (z = a) \rightarrow c.$$

Q4.

For $\text{float} \rightarrow \text{float}$, the calling context promises to supply values of type float , but the function $\text{int} \rightarrow \text{int}$ only know how to deal with int as input, which is only a special case of float ($\text{int} \leq \text{float}$). $\text{int} \rightarrow \text{int}$ does not know how to deal with float , so $\text{int} \rightarrow \text{int}$ is not a subtype of $\text{float} \rightarrow \text{float}$.