

Distribuciones

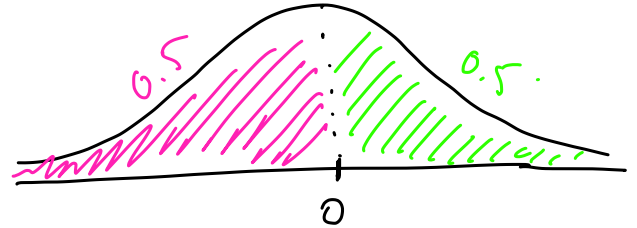
Ejercicio 13



Distribuciones

Si $Z \sim N(0,1)$, hallar el valor de z_0 en cada caso:

- a) $P(Z < z_0) = 0.5$
- b) $P(Z < z_0) = 0.8729$
- c) $P(Z > z_0) = 0.9015$



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Mediana = Mediana = Moda.

a) El valor z_0 que deja
por debajo (y por arriba)
una probabilidad del 50%
es la mediana (= medio)

$$z_0 = 0.$$

Probabilidad acumulada inferior para distribución normal N(0,1)

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μ = Media

σ = Desviación típica

$$P(z \leq z_0) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{z_0} e^{-\frac{z^2}{2}} dz$$



Tipificación: $z_0 = \frac{x - \mu}{\sigma}$

z_0	0,00	0,01	0,02	0,03	0,04	0,05	0,06	0,07	0,08	0,09	z_0
0,0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359	0,0
0,1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753	0,1
0,2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141	0,2
0,3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517	0,3
0,4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879	0,4
0,5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224	0,5
0,6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549	0,6
0,7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852	0,7
0,8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133	0,8
0,9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389	0,9
1,0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621	1,0
1,1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830	1,1
1,2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015	1,2
1,3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177	1,3
1,4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319	1,4
1,5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441	1,5
1,6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545	1,6
1,7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633	1,7
1,8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706	1,8
1,9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767	1,9
2,0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817	2,0
2,1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857	2,1
2,2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890	2,2
2,3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916	2,3
2,4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936	2,4
2,5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952	2,5
2,6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964	2,6
2,7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974	2,7
2,8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981	2,8
2,9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986	2,9
3,0	0.99865	0.99869	0.99874	0.99878	0.99882	0.99886	0.99889	0.99893	0.99896	0.99900	3,0
3,1	0.99903	0.99906	0.99910	0.99913	0.99916	0.99918	0.99921	0.99924	0.99926	0.99929	3,1
3,2	0.99931	0.99934	0.99936	0.99938	0.99940	0.99942	0.99944	0.99946	0.99948	0.99950	3,2
3,3	0.99952	0.99953	0.99955	0.99957	0.99958	0.99960	0.99961	0.99962	0.99964	0.99965	3,3
3,4	0.99966	0.99968	0.99969	0.99970	0.99971	0.99972	0.99973	0.99974	0.99975	0.99976	3,4
3,5	0.99977	0.99978	0.99978	0.99979	0.99980	0.99981	0.99981	0.99982	0.99983	0.99983	3,5
3,6	0.99984	0.99985	0.99985	0.99986	0.99986	0.99987	0.99987	0.99988	0.99988	0.99989	3,6
3,7	0.99989	0.99990	0.99990	0.99991	0.99991	0.99991	0.99992	0.99992	0.99992	0.99992	3,7
3,8	0.99993	0.99993	0.99993	0.99994	0.99994	0.99994	0.99994	0.99995	0.99995	0.99995	3,8
3,9	0.99995	0.99995	0.99996	0.99996	0.99996	0.99996	0.99996	0.99996	0.99997	0.99997	3,9

b) $P(z \leq z_0) = 0.8729$

$z_0 = 1.14$

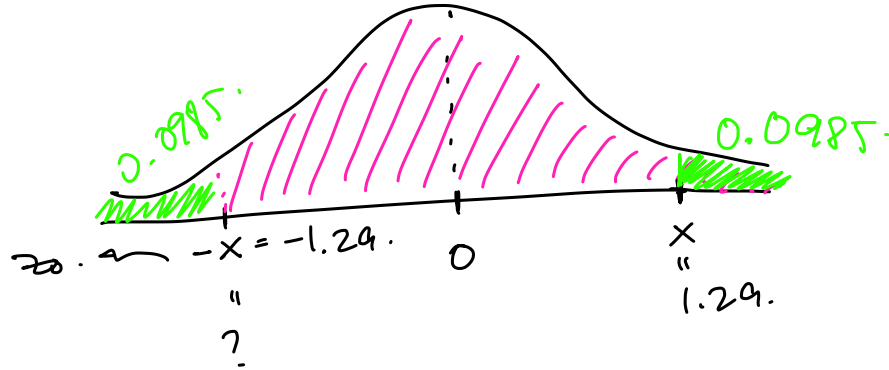
$1-\alpha$	90%	92%	94%	95%	96%	97%	98%	99%
α	10%	8%	6%	5%	4%	3%	2%	1%
$z_{\alpha/2}$	1,645	1,751	1,881	1,960	2,054	2,170	2,326	2,576
z_{α}	1,282	1,405	1,555	1,645	1,751	1,881	2,054	2,326

Siendo:

$1-\alpha$ = Nivel de confianza

α = Nivel de significación

$z_0 = -1.29$
 c) $P(Z > z_0) = 0.9015$
 $1 - P(Z \leq z_0) = 0.9015 \Rightarrow P(Z \leq z_0) = 1 - 0.9015 = 0.0985$



$$P(Z > x) = 0.0985$$

$$1 - P(Z \leq x) = 0.0985$$

$$P(Z \leq x) = 1 - 0.0985 = 0.9015$$

$$\hookrightarrow x = 1.29$$

$$P(Z \geq z_0) = 0.0985.$$

"

$$1 - P(Z < z_0) = 0.0985.$$

$$P(Z \leq z_0) = 1 - 0.0985 = 0.9015.$$

↓
positive.

↓
looker table.

$$z_0 =$$