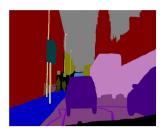
Application of CNN - Image segmentation Numerical Methods for Deep Learning

Image Segmentation

The problem: Given an image $y: R^2 \to R$ compute probability maps for n_c classes, i.e., for $j = 1, \ldots, n_c$

$$P_j: R^2 \to [0,1], \quad \sum_{i=1}^{n_c} P_j = 1$$





 $P_i(x)$ is the probability of a point x to belong to class j.

Setup of Image Segmentation Problem

- ▶ Use a neural network: original image $\rightarrow n_c$ "images"
- Output image represents class probabilities for each pixel
- Loss: average cross entropy for each pixel
- Optimize over network parameters

Simple example: a single layer and linear classification

Image Segmentation with Single-Layer NN

Let $\mathbf{Y}_0 \in \mathbb{R}^{n \times n_f}$ with $n_f = n_1 \cdot n_2 \cdot 3$ $(n_1 \times n_2 \text{ RGB data})$

$$\mathbf{Y}_1 = \sigma(\mathbf{K}(\boldsymbol{\theta})\mathbf{Y}_0 + \mathbf{Bb}).$$

Use 2D convolutions for $K(\theta)$ and assume k output channels, i.e.,

$$\mathbf{K} = egin{pmatrix} \mathbf{K}_{2D}(m{ heta}_{11}) & \mathbf{K}_{2D}(m{ heta}_{12}) & \mathbf{K}_{2D}(m{ heta}_{13}) \\ \mathbf{K}_{2D}(m{ heta}_{21}) & \mathbf{K}_{2D}(m{ heta}_{22}) & \mathbf{K}_{2D}(m{ heta}_{23}) \\ dots & dots & dots \\ \mathbf{K}_{2D}(m{ heta}_{k1}) & \mathbf{K}_{2D}(m{ heta}_{k2}) & \mathbf{K}_{2D}(m{ heta}_{k3}) \end{pmatrix}.$$

Then we have to classify each pixel in \mathbf{Y}_1 using $\mathbf{W} \in \mathbb{R}^{k \times n_c}$. This gives the problem

$$\min_{\mathbf{W},\mathbf{K},\mathbf{b}} E(\mathbf{W} \mathrm{reshape}(\mathbf{Y}_1),\mathbf{P}), \qquad \mathbf{Y}_1 = \sigma(\mathbf{K}(\boldsymbol{\theta})\mathbf{Y}_0 + \mathbf{B}\mathbf{b})$$

Here $\operatorname{reshape}(\mathbf{Y}_1) \in \mathbb{R}^{(n \cdot n_1 \cdot n_2) \times k}$ and E is our cross entropy

References