

$$u(x,t) = (x^3 + x + 1)(3x^4 + 2x + 1)(t^3 + 3t^2 + 1) \\ (t^3 + 3t^2 + 1) \sin x = u; \quad u'_x = (t^3 + 3t^2 + 1) \cos x; \quad u''_{xx} = -(t^3 + 3t^2 + 1) \sin x$$

$$u = (t^3 + 3t^2 + 1)(x^4 + 10x + 3); \quad \text{remember} \quad x \in [0, 1] \\ \text{D}_t u = (\dots)(x^4 + 10x + 3); \quad (1) \\ u_x = (\dots)(4x^3 + 10); \quad u_{xx} = (\dots)(12x^2) \\ \Rightarrow f = (1) - 12x^2(t^3 + 3t^2 + 1)/.$$

$$u_2 \\ 10(t^3 + 3t^2 + 1) = 3 \underbrace{(t^3 + 3t^2 + 1)}_{\beta_1} \underbrace{(t^3 + t^2)}_{\beta_1} - \underbrace{(3t^2(t^3 + 3t^2 + 1))}_{u_1} - (t^3 + 3t^2 + 1)$$

Pr. 2.

$$-14(t^3 + 3t^2 + 1) = 14(t^3 + 3t^2 + 1) \underbrace{(t - 1)}_{\beta_1} - \underbrace{14t(t^3 + 3t^2 + 1)}_{u_2}$$

$$u_0 = x^4 + 10x + 3$$

$$\text{P.S.C.D.}_t u = \left(\frac{t^3 - 2(t)}{\Gamma(4 - 2(t))} + \frac{6t^2 - 2(t)}{\Gamma(3 - 2(t))} \right) \cdot (x^4 + 10x + 3)$$