

Solutions for Homework14

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Abstract

In this document we will show the solutions for problems represented in the given homework for this week.

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1 Task 1

1.1 Problem

In the given graph which represents the movement of a car, answer the following:

- Between which point and point the car accelerate, and between which points it decelerate?
- What is the distance traveled at point C? and what is it at point F?
- Indicate line segments with 0 acceleration, does that mean the car is not moving? Explain.
- What are the values of acceleration and deceleration of the car at each segment?

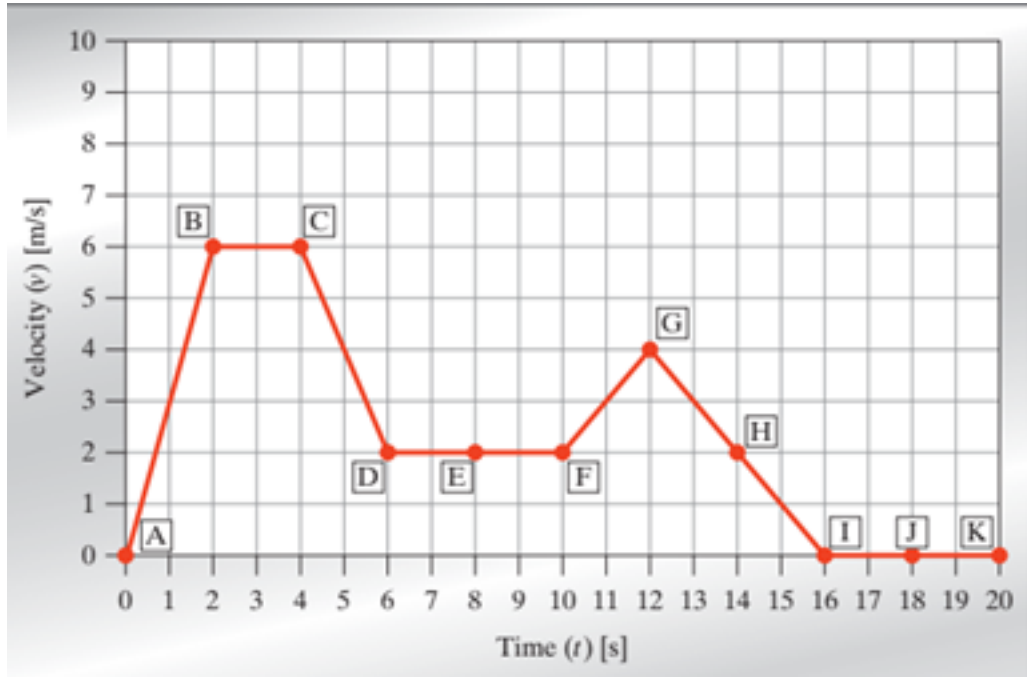


Figure 1: Velocity-Time of the car

1.2 Solution

1. The car accelerates at points:

- $A \rightarrow B$
- $F \rightarrow G$

And it decelerates at points:

- $C \rightarrow D$
- $G \rightarrow I$ ($G \rightarrow H$ & $H \rightarrow I$)

2. To get the distance we can just find the integral from point A (0) to whatever points we want. So to see what the distance traveled at point C is we just have to evaluate

$$\int_A^C v * dt = \int_A^B v * dt + \int_B^C v * dt$$

which is just the area under the graph so from $A \rightarrow B$ we have a right triangle with sides 1×6 which means that the area from that triangle is $\frac{6}{2} = 3$, and from $B \rightarrow C$ we have a rectangle with sides

2×6 so in total the area of the rectangle is 12 meaning that the distance traveled from $A \rightarrow C$ is $3 + 12 = 15m$. To find out the distance traveled from $A \rightarrow F$ we have to solve the following integral:

$$\int_A^F v * dt = \int_A^C v * dt + \int_C^B v * dt + \int_D^F v * dt$$

Since we already know that $\int_A^C v * dt = 15m$ we just have to find the other two integrals, which at the end end up being $15 + \frac{2*4}{2} + 2 * 2 + 2 * 4 = 15 + 4 + 4 + 8 = 31m$

3. The line segments with 0 acceleration are

- $B \rightarrow C$
- $I \rightarrow K$ ($I \rightarrow J$ & $J \rightarrow K$)

This does **NOT** mean that the car isn't moving, this just means that the velocity of the car isn't changing or in other words

$$\frac{dv}{dt} = 0$$

LINE SEGMENT	ACCELERATION VALUE $\left[\frac{m}{s^2}\right]$
$A \rightarrow B$	3
$B \rightarrow C$	0
$C \rightarrow D$	-2
$D \rightarrow E$	0
4. $E \rightarrow F$	0
$F \rightarrow G$	1
$G \rightarrow H$	-1
$H \rightarrow I$	-1
$I \rightarrow J$	0
$J \rightarrow K$	0

2 Task 2

2.1 Problem

An environmental engineer has obtained a bacteria culture from a municipal water sample and allowed the bacteria to grow. The initial count of Bacteria is A, and their growth formula with time being in hours is given by:

$$B = B_0 e^{Ct}$$

A: is the summation of your birthday digits divided by 0.5

C: is the summation of your IUS ID number divided by 50.

- What is B_0 ? And what is its value?
- After how many hours, the amount of Bacteria would be 100000?
- Pick up 4 to 5 points in time and draw the graph of Bacteria growth. (This is done by pen and pencil)
- Use Octave to plot the graph of bacteria growth

2.2 Solution

$$A = \frac{1+4+1+2+2+0+0+2}{0.5} = \frac{12}{0.5} = 24$$
$$C = \frac{2+2+0+3+0+2+2+8+9}{50} = \frac{28}{50} = 0.56$$

1. B_0 is the initial amount of bacteria in our system and since our variable A represents the initial count of bacteria we can conclude that $A = B_0$.
2. To figure this out we simply have to figure out the following equation:

$$24 * e^{0.56 * t} = 100000$$

$$0.56 * t * \ln 24 * e = \ln 100000$$

$$0.56 * t = \frac{\ln 100000}{\ln 24 * e}$$

$$t = \log_{24 * e} 100000 * \frac{1}{0.56}$$

$$t \approx 4.9207[h]$$

3. Using the following code:

```
1 % Clear previous junk
2 clear all;
3 clc;
4
5 % Set up needed variables
6 A = 24;
7 C = 0.56;
8 t = linspace(0,20,10000);
9
10 % Calculate bacterial growth
11 B = A.*exp(C.*t);
12
13 % Plot the graph
14 plot(t,B, 'r*');
15 grid on; legend("Number of ...
    bacteria"); xlabel("Time"); ylabel("Bacteria"); title("Bacterial growth");
```

We get the following graph

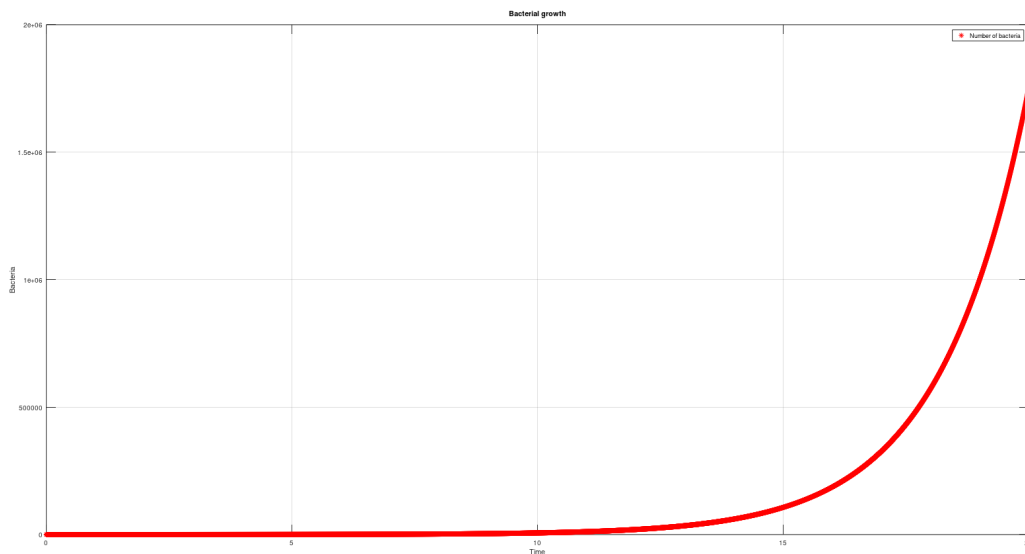


Figure 2: Bacterial growth plot

3 Task 3

3.1 Problem

3.2 Solution

4 Task 4

4.1 Problem

1. Consider the following loop:

```
1 [r,c]=size(D);
2 j=c;
3
4 i=1;
5 while j > 0
6     T(i,1)=D(i,i); T(i,2)=D(i,j);
7     i=i+1; j=j-1;
8 end
```

If we were to run the code and generate the following value for T, $T = [2 \ 11; 7 \ 16]$. What is D

2. What is the output of $M4$ if $M = [1 \ 3 \ 2; 6 \ 0 \ 2]$

```
1 [rows,cols]=size(M);
2 for r=1:1:2*rows
3     for c=1:1:2*cols
4         M4(r,c)=c;
5     end
6 end
```

4.2 Solution

1. If we take a good look at the code we can spot that the first element is always going to be the element on the main diagonal line of the matrix, and the 2nd element will always be the element of the inverse diagonal of the matrix so if we get $T = [2 \ 11; 7 \ 16]$. D must be:

$$D = \begin{bmatrix} 2 & 7 \\ 16 & 11 \end{bmatrix}$$

2. All this code does is take the number of rows and columns, afterwards it makes loops that repeat twice the number of rows and columns. So for a 2×3 . We would have in total 24 iterations. The final output would be:

$$M4 = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 1 & 2 & 3 & 4 & 5 & 6 \\ 1 & 2 & 3 & 4 & 5 & 6 \\ 1 & 2 & 3 & 4 & 5 & 6 \end{bmatrix}$$

5 Task 5

5.1 Problem

Write a program that will ask the user to input his age in year and it will calculate to him his age in days.

5.2 Solution

```
1 % Clear useless junk
2 clear all;
3 clc;
4
5 % Get needed input
6 age = input("Please enter your age in years : ");
7
8 % Print the result
9 printf("You are %d days old", age * 365);
```

6 Task 6

6.1 Problem

Write a program that takes a vector as it's input and returns the maximum, minimum, and mean of the given vector. And it returns how many positive, negative and 0 numbers in the vector as well.

6.2 Solution

```
1 %Clear useless junk
2 clear all;
3 clc;
4
5 % Ask the user to input the vector
6 inputVector = [];
7 while true
8     inputVector(end+1) = input('Please input a value for your vector: ');
9     if !yes_or_no('Do you want to enter another value?');
10         break;
11     endif
12 endwhile
13
14 % display the vector
15 display(inputVector)
16
17 % Find and display the results
18 Max = max(inputVector)
19 min = min(inputVector)
20 mean = mean(inputVector)
21 negValues = sum(inputVector < 0)
22 posValues = sum(inputVector > 0)
23 zeroValues = sum(inputVector == 0)
```

7 Task 7

7.1 Problem

Show how to inscribe a square inside a circle such that all the square's vertices touch the circles' circumference. Then, calculate the area of the square if the circle's area is 628 cm^2

7.2 Solution

The process for inscribing a square inside of a circle goes as follows:

1. Draw a diameter inside the circle
2. Draw another diameter perpendicular to the previous one.
3. The resulting 4 points that touch the circle are now the four vertices of the square.

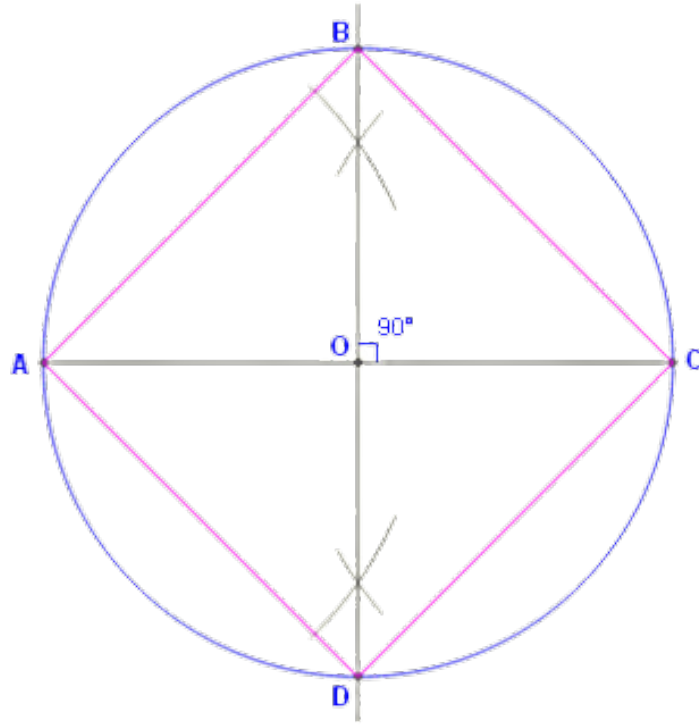


Figure 3: Inscribed square in a circle

As we can see from Figure 3. The diameter of the circle $D = 2r$ is also equal to $D = \sqrt{a^2 + a^2} = \sqrt{2 * a^2}$. Which means the following.

$$D^2 = 2 * a^2 \implies a^2 = A_{\square} = \frac{D^2}{2} \quad (1)$$

$$A_{\circ} = r^2 * \pi = 628[cm^2] \implies r^2 = \frac{628[cm^2]}{\pi} \quad (2)$$

$$r = \sqrt{\frac{628}{\pi}}[cm]$$

$$2r = D = 2 * \sqrt{\frac{628}{\pi}}[cm] \approx 28.277[cm]$$

If we now take the result for our D and substitute it into equation 1. We will get that:

$$A_{\square} \approx \frac{28.277^2}{2} \approx 399.80[cm^2]$$

8 Task 8

8.1 Problem

8.2 Solution

9 Task 9

9.1 Problem

9.2 Solution

10 Task 10

10.1 Problem

10.2 Solution