Math 100 Cheat Sheet

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Abstract

This document contains a set of identities and equations for Math100

Contents

1 Logarithms

1.1 General definition of a logarithm

Logarithms are inverse function of exponential function meaning that if we want to remove an exponent we can apply an logarithm

$$\log_b(a) = c \implies b^c = a$$

1.1.1 Example

Lets say that we want to figure out 2 to the power of what number gives us 524288, or in other words $2^x = 524288$. Well we can approach this problem in two ways, the first way is to apply the definition of the logarithm and phase the problem as such $x = \log_2(524288)$. Or we can do this by placing the both sides of the equation into logarithms as follows $\log_2(2^x) = \log_2(524288) \implies x = \log_2(524288)$.

1.1.2 Domain

$$\log_b(a) = c$$

The logarithm above is valid for the following values:

$$a \in (0, +\infty)$$

$$b \in (0, 1) \cup (1, +\infty)$$

1.2 Logarithm Identities

These are some essential logarithm identities that can be found in many math books:

1. $\ln(a) = \log_e(a)$
2. $\log(a) = \log_{10}(a)$

1.3 Logarithm Rules

There are a lot of rules that can help us when we are dealing with logarithms, some of these rules are:

1. $\log_b(1) = 0$
2. $\log_b(b) = 1$
3. $\log_b(b^x) = x$
4. $\log_b(a^c) = c * \log_b(a)$
5. $\log_b(a) + \log_b(c) = \log_b(a * c)$ ★
6. $\log_b(a) - \log_b(c) = \log_b(\frac{a}{c})$ ★
7. $\log_b(a) = \frac{\log_c(a)}{\log_c(b)}$ ★