

Lab 5: Recursion

Exercise 1 : Greatest Common Divisor using Loop

In this exercise we will implement the Euclidean algorithm for calculating GCD is given below

GCD(a,b) where a and b are integers.

For all a , b with $a > b$ there is a q (quotient) and r (remainder) such that

$$a = qb + r$$

with $r < b$ or $r = 0$

This is calculated repeatedly by making $a=b$ and $b=r$ until $r=0$.

Finally, $GCD=b$.

Example: Let $a = 1071$ and $b = 462$ that is we are searching for $GCD(1071, 462)$ then we will have following steps. Note that b of the current step is used as a in the next step and r of the current step is used b as the next step.

Step k	Equation	Quotient and remainder
0	$1071 = q_0 462 + r_0$	$q_0 = 2$ and $r_0 = 147$
1	$462 = q_1 147 + r_1$	$q_1 = 3$ and $r_1 = 21$
2	$147 = q_2 21 + r_2$	$q_2 = 7$ and $r_2 = 0$; algorithm ends

When r becomes 0 then the b gives you the GCD, which is 21 in this example. $GCD(1071, 462) = 21$

1. Create a class named GCDLoop which has a main method.
2. The class will accept two numbers and return the GCD as shown below

```
> java GCDLoop 90 50  
> 10
```

Exercise 2 : Greatest Common Divisor using Recursion

1. Define the recursive GCD function and the base case for the Euclidean algorithm.
2. Implement the function in a class named GCDRec
3. The class will accept two numbers and return the GCD as shown below

```
> java GCDRec 90 50
```

NOTE: Your lab will **not be graded** if

- Your account name does not have the format described in lab1.pdf
- Your repository name is not lab
- Your files have compilation errors
- You haven't complete the steps described in exercises
- Your added/modified files are not submitted to Bitbucket.
- You have to add commit and push files as described in lab1.pdf