

UNIT II: Linear Data Structures

A Comprehensive Study Guide with Real-Time Examples

Arrays

Arrays are collections of elements stored in contiguous memory locations, accessed by index. Each element can be retrieved in $O(1)$ constant time.

Characteristics:

Fixed Size: Memory allocated at compile time

Homogeneous: All elements must be of the same data type

Random Access: Direct access to any element using index

Contiguous Memory: Elements stored in sequential memory locations

Real-Time Example:

Student Grade Array: A classroom has 30 students with grades stored in an array. To retrieve the 5th student's grade, you directly access `array[4]` in $O(1)$ time. This is efficient for scenarios where you need frequent random access without insertion/deletion.

Advantages and Disadvantages:

Advantages: Fast random access ($O(1)$), memory efficient, cache-friendly

Disadvantages: Fixed size, expensive insertion/deletion ($O(n)$), memory wastage if not fully used

Linked Lists

Linked lists are linear data structures where elements (nodes) are connected via pointers/references. Unlike arrays, they are not stored in contiguous memory.

Singly Linked List

Each node contains data and a pointer to the next node only. The last node points to NULL.

Structure:

Node Structure: [Data | Next Pointer] → [Data | Next Pointer] → [Data | NULL]

Key Operations:

Insertion: $O(n)$ in general, $O(1)$ at head

Deletion: $O(n)$ in general, $O(1)$ at head

Traversal: $O(n)$

Search: $O(n)$

Real-Time Example:

Browser History: When you navigate through web pages, each page visit is a node containing the URL and a pointer to the next visited page. Going back through history is simple as you move through the linked list backwards.

Advantages and Disadvantages:

Advantages: Dynamic size, efficient insertion/deletion at known positions ($O(1)$), no memory wastage

Disadvantages: No random access ($O(n)$), extra memory for pointers, cache-unfriendly

Doubly Linked List

Each node contains data, a pointer to the next node, and a pointer to the previous node. This allows bidirectional traversal.

Structure:

Node: [Prev | Data | Next] \longleftrightarrow [Prev | Data | Next] \longleftrightarrow [Prev | Data | Next]

Key Advantages:

Bidirectional Traversal: Can move forward and backward

Efficient Deletion: No need to traverse to find previous node

Flexible: Better for algorithms requiring backward traversal

Real-Time Example:

Music Playlist: A music player with previous/next buttons implements a doubly linked list. Each song node points to the next and previous tracks, allowing you to navigate both forward and backward through your playlist efficiently.

Circular Linked List

A variant where the last node points back to the first node instead of NULL, forming a circle.

Structure:

Circular: [Data | Next] → [Data | Next] → [Data | Next] ∪ (back to first)

Key Characteristics:

No NULL termination: Last node points to first node

Continuous Traversal: Can traverse indefinitely

Memory Efficient: Single pointer to any node accesses entire list

Real-Time Example:

Round-Robin Scheduling: Operating systems use circular linked lists for CPU scheduling. Each process gets a time slice, and after its turn, the pointer moves to the next process. The circular structure ensures fair rotation among all processes waiting for CPU time.

Another Real-Time Example:

Traffic Light Controller: Traffic lights cycle through Red → Yellow → Green → Red continuously. A circular linked list perfectly represents this where each color node points to the next, and the last (Green) points back to the first (Red).

Stack

A Last-In-First-Out (LIFO) data structure where insertions and deletions occur at the same end called the top.

Key Operations:

Push: Add element to top - $O(1)$

Pop: Remove element from top - $O(1)$

Peek: View top element - $O(1)$

isEmpty: Check if stack is empty - $O(1)$

Implementation:

Array-based: Fixed size, but efficient for known maximum size

Linked List-based: Dynamic size, suitable for variable stack requirements

Real-Time Examples:

1. **Function Call Stack:** When functions call each other in a program, each function call is pushed onto the call stack. When a function returns, it's popped off. If Function A calls Function B which calls Function C, the stack looks like: [A | B | C (top)]. C executes first and returns, then B, then A.
2. **Undo/Redo Mechanism:** Text editors use stacks for undo functionality. Each action (typing, formatting) is pushed onto an undo stack. When you press Ctrl+Z, the most recent action is popped and reversed. Pressing Ctrl+Y pushes it to a redo stack.
3. **Browser Back Button:** Your browsing history uses a stack. Each page visited is pushed onto the stack. Clicking back pops the current page, revealing the previous one.
4. **Expression Evaluation:** Converting infix expressions (A+B) to postfix (AB+) and evaluating them uses stacks. This is fundamental in compiler design.

Queue

A First-In-First-Out (FIFO) data structure where insertions occur at the rear and deletions at the front.

Key Operations:

Enqueue: Add element to rear - $O(1)$

Dequeue: Remove element from front - $O(1)$

Peek: View front element - $O(1)$

isEmpty: Check if queue is empty - $O(1)$

Variants:

Circular Queue: Reuses space, more efficient memory utilization

Priority Queue: Elements dequeued based on priority, not just insertion order

Double-Ended Queue (Deque): Insertion and deletion from both ends

Real-Time Examples:

1. **ATM Queue Management:** Customers arriving at an ATM are added to a queue (enqueue). The customer at the front uses the ATM, and when done, is removed (dequeue). New customers join the rear. This ensures fair FIFO service.
2. **CPU Task Scheduling:** Operating systems queue processes waiting for CPU execution. Processes are added to the ready queue and scheduled in FIFO order, ensuring no process starves indefinitely.
3. **Printer Queue:** Documents sent to a printer are queued. The printer processes documents in the order they were sent, not randomly. First document sent is printed first.
4. **Customer Service:** Call centers use queues. Incoming calls are queued, and agents handle them in FIFO order. When an agent becomes free, the next customer in the queue is served.
5. **Message Broadcasting:** Social media platforms use queues for processing user messages and notifications, ensuring messages are delivered in order.

Applications of Linear Data Structures

Arrays:

Database Records: Store rows of data for fast row access

Image Processing: 2D arrays represent pixel grids

Sparse Matrices: Represent mathematical matrices

Linked Lists:

Dynamic Memory Allocation: Memory allocated as needed

Polynomial Representation: Each term as a node

Symbol Tables: In compilers, store variable information

Stacks:

Compiler Design: Syntax analysis, expression evaluation

Memory Management: Function call stack, local variables

Backtracking Algorithms: Maze solving, N-Queens problem

Queues:

Operating System: Process scheduling, I/O buffer management

Network Protocols: Packet routing, bandwidth management

Simulation: Model real-world systems like hospitals, banks