Rejection method for random number generation



Step by Step Explanation using R

Stimulate Standard Normal Distribution (1/4)

```
fx <- function(x){

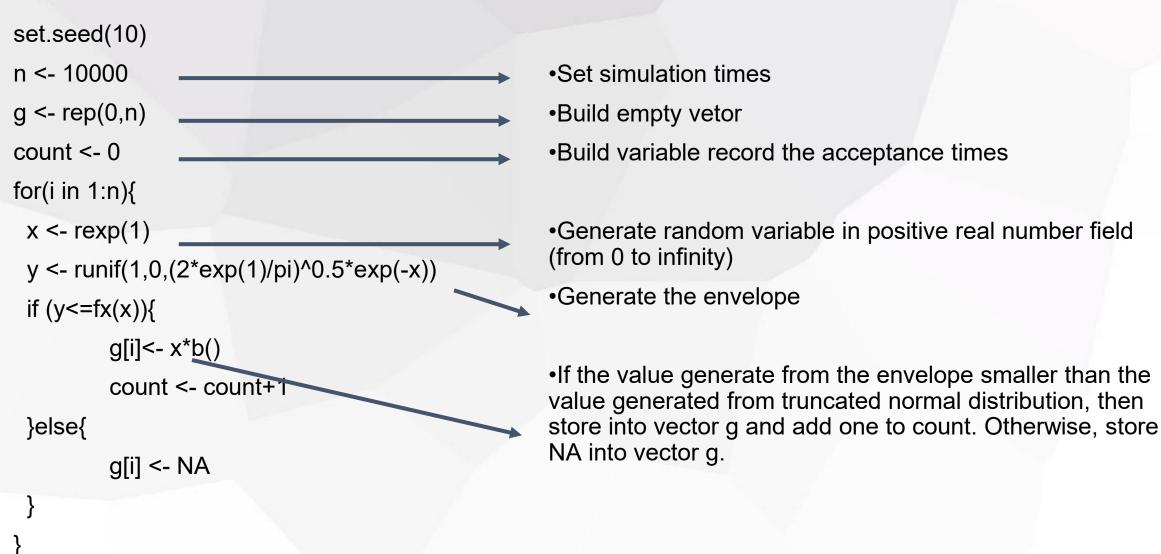
    Build the truncated normal

                                      function (divide Normal Distribution
 return((2/pi)^0.5*exp(-(x^2)/2))
                                      density function by 0.5)

    Build function randomly generating

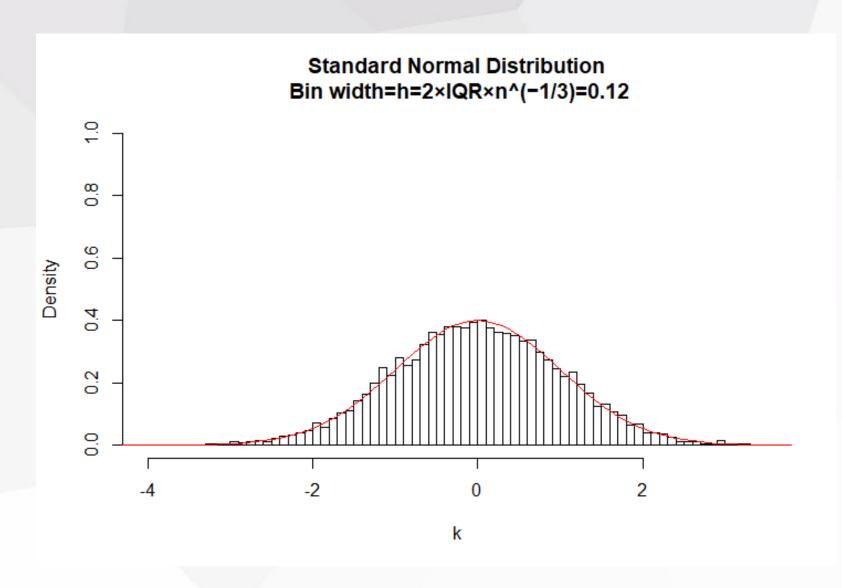
b <- function(){
                                      1 & -1
 k < - rbinom(1,1,0.5)
                                      (relocate half of the accepted data
 if(k==0) return(-1)
                                      to negative side)
 else return(1)
```

Stimulate Standard Normal Distribution (2/4)

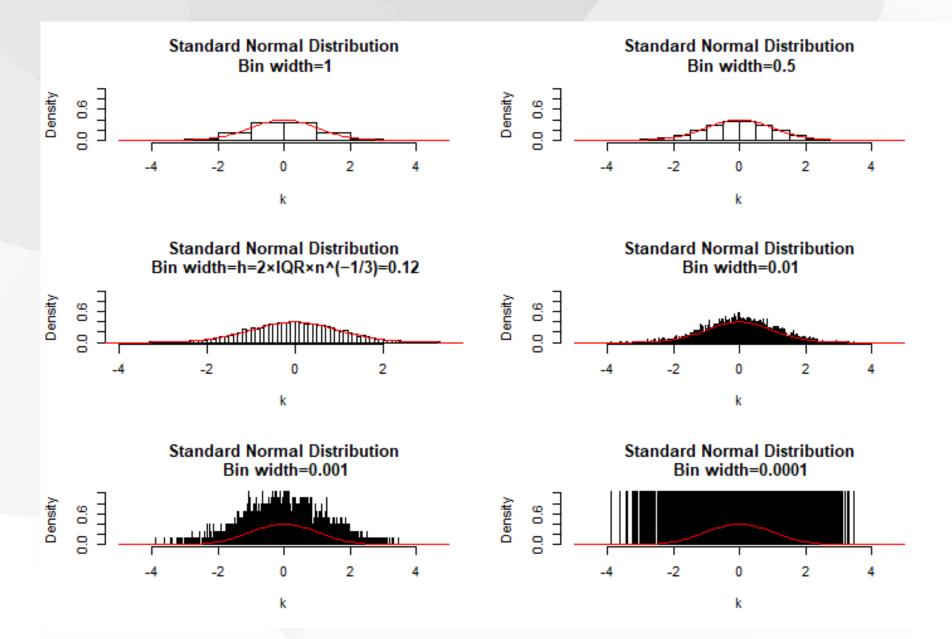


Stimulate Standard Normal Distribution (3/4)

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*Discussion: How to determine bin width?



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- 1. Sturges' formula \longrightarrow $k = \lceil \log_2 n \rceil + 1$
- 1. Doane's Rule
- 1. Scott's Rule

 $h=rac{3.5\hat{\sigma}}{\sqrt[3]{n}}$

$$\log_2(n) + 1 + \log_2(1 + \frac{\sqrt{b}}{\sigma\sqrt{b}})$$
 Where
$$\sqrt{b} = \frac{\sum_{i=1}^n (X_i - \bar{X})^3}{[\sum_{i=1}^n (X_i - \bar{X})^2]^{(3/2)}}$$
 and
$$\sigma\sqrt{b} = \sqrt{\frac{6(n-2)}{(n+1)(n+3)}}.$$

1. Rice's Rule

$$k = \lceil 2\sqrt[3]{n}
ceil$$

1. Freedman-Diaconis rule $\longrightarrow h$

$$h=2 imes \mathrm{IQR} imes n^{-1/3}$$

Application: Stimulate Beta Distribution (1/3)

```
set.seed(10)
n <- 10000 \qquad \qquad \qquad \bullet \text{Set simulation times}
g <- rep(0,n) \qquad \qquad \bullet \text{Build empty vetor}
\text{count } <- 0 \qquad \qquad \bullet \text{Build variable record the acceptance times}
```

```
for(i in 1:n){
 y1<-runif(1,0,1)
 y2 < -runif(1,0,1)
 if (y2 < = 4*(y1*(1-y1))
  g[i]<-y1
   count <- count+1
 }else{
  g[i] <- NA
```

- •Generate random variable from uniform[0,1]
- •Beta distribution with n=m
- •If the value generate randomly from the niform[0,1] smaller than the value generated from Beta distribution, then store into vector g and add one to count. Otherwise, store NA into vector g.

Stimulate Beta Distribution (2/3)

•Rule out the NA in the matrix

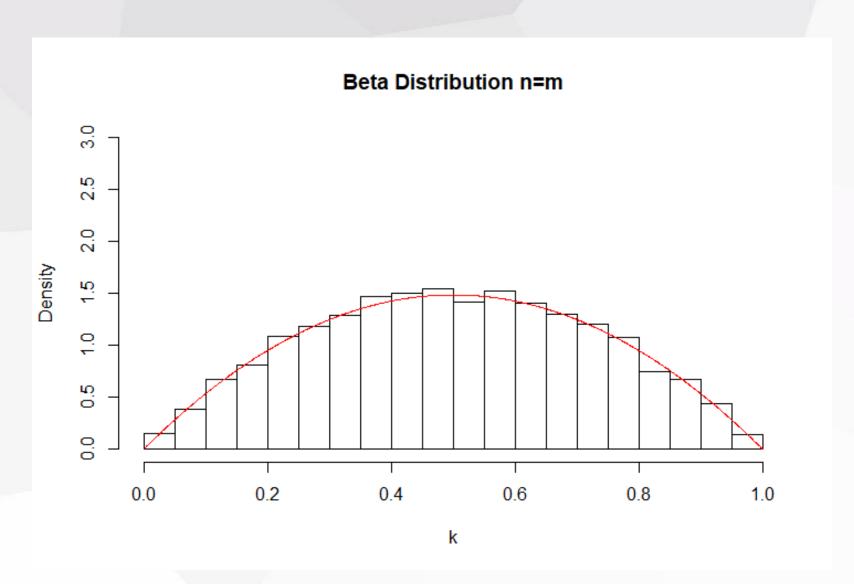
•Determine the bin width with Freedman-Diaconis rule

```
lines(x,5.93*x*(1-x),col="red")
ap_rate= count/n
```

Plot real Beta distribution (n=m)

Count acceptance rate

Stimulate Beta Distribution (3/3)



THANKS!