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Answer to the Q. No. 1

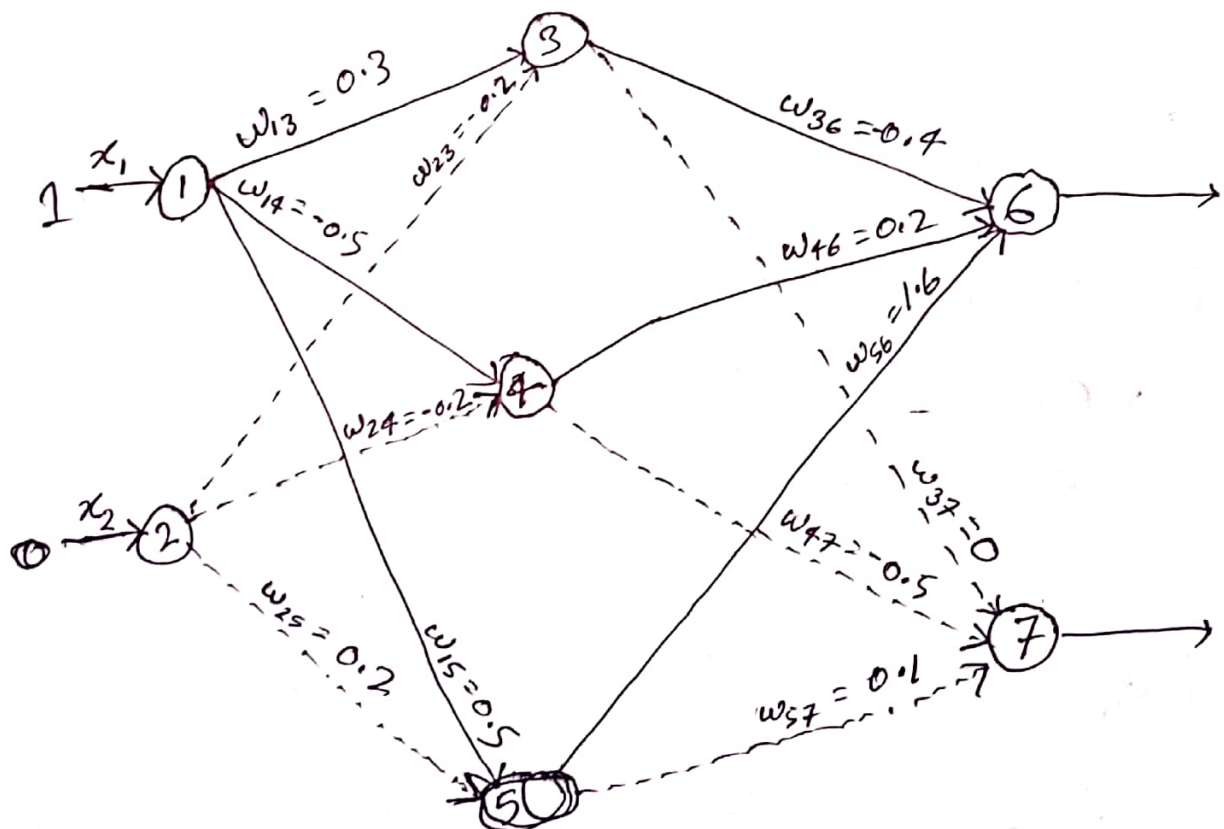
$$w_{13} = 0.3, w_{14} = (12 \times 3) - 0.5 = -0.5, w_{15} = 0.5$$

$$w_{23} = (12 \times 2) - 0.2 = -0.2, w_{24} = (12 \times 4) - 0.2 = -0.2, w_{25} = 0.2$$

$$w_{36} = -0.4, w_{37} = -0.5 + 0.5 = 0, w_{46} = 0.5 - 0.3 = 0.2$$

$$w_{47} = -0.2 - 0.3 = -0.5, w_{56} = (12 \times 5 - 0.4) = 1.6$$

$$w_{57} = 0.1$$



Given,

$$\theta_6 = \theta_7 = \theta_3 = \theta_4 = \theta_5 = 0.2$$

learning rate, $\alpha = 0.1$

(i) Outputs of hidden layer:

$$\begin{aligned}
 y_3 &= \text{sigmoid}(x_1 w_{13} + x_2 w_{23} - \theta_3) \\
 &= \text{sigmoid}(1 \times 0.3 + 0 \times (-0.2) - 0.2) \\
 &= \text{sigmoid}(0.3 - 0.2) = \text{sigmoid}(0.1) \\
 &= \frac{1}{1 + e^{-0.1}} = 0.53
 \end{aligned}$$

$$\begin{aligned}
 y_4 &= \text{sigmoid}(x_1 w_{14} + x_2 w_{24} - \theta_4) \\
 &= \text{sigmoid}(1 \times (-0.5) + 0 \times (-0.2) - 0.2) \\
 &= \text{sigmoid}(-0.5 - 0.2) \\
 &= \text{sigmoid}(-0.7) = \frac{1}{1 + e^{0.7}} = 0.33
 \end{aligned}$$

$$\begin{aligned}
 y_5 &= \text{sigmoid}(x_1 w_{15} + x_2 w_{25} - \theta_5) \\
 &= \text{sigmoid}(1 \times 0.5 + 0 \times 0.2 - 0.2) \\
 &= \text{sigmoid}(0.3) = \frac{1}{1 + e^{-0.3}} = 0.574
 \end{aligned}$$

(ii) Outputs of the output layer:

$$\begin{aligned}
 y_6 &= \text{sigmoid}(y_3 w_{36} + y_4 w_{46} + y_5 w_{56} - \theta_6) \\
 &= \text{sigmoid}(0.53 \times 0.4 + 0.33 \times 0.2 + 0.574 \times 1.6 - 0.2) \\
 &= \text{sigmoid}(0.996) = \frac{1}{1 + e^{-0.996}} = \text{sigmoid}(0.572) \\
 &= 0.73 = \frac{1}{1 + e^{-0.572}} = 0.64
 \end{aligned}$$

$$\begin{aligned}
 y_7 &= \text{sigmoid}(y_3 w_{37} + y_4 w_{47} + y_5 w_{57} - \theta_7) \\
 &= \text{sigmoid}(0.53 \times 0 + 0.33 \times 0.5 + 0.574 \times 0.1 - 0.2) \\
 &= \text{sigmoid}(0.022) \\
 &= 0.51
 \end{aligned}$$

(iii) Update weights:

→ error calculation

$$e_6 = y_{d6} - y_6 = 0 - 0.64 = -0.64$$

$$e_7 = y_{d7} - y_7 = 1 - 0.51 = 0.49$$

→ calculating error gradient:

$$\begin{aligned}
 s_6 &= y_6 [1 - y_6] \times e_6 = 0.64 [1 - 0.64] \times (-0.64) \\
 &= 0.23 \times 0.27 \times (-0.64) \\
 &= -0.147
 \end{aligned}$$

$$\begin{aligned}
 s_7 &= y_7 [1 - y_7] \times e_7 = 0.51 [1 - 0.51] \times 0.49 \\
 &= 0.51 \times 0.49 \times 0.49 \\
 &= 0.122
 \end{aligned}$$

→ new weights:

$$\begin{aligned}
 \Delta w_{36} &= \alpha \times y_3 \times s_6 = 0.1 \times 0.53 \times (-0.147) \\
 &= -0.008
 \end{aligned}$$

$$\Delta W_{37} = \alpha \times y_3 \times s_7 = 0.1 \times 0.53 \times 0.122 = 0.006$$

$$\Delta W_{46} = \alpha \times y_4 \times s_6 = 0.1 \times 0.33 \times (-0.144) = -0.005$$

$$\Delta W_{47} = \alpha \times y_4 \times s_7 = 0.1 \times 0.33 \times 0.122 = 0.004$$

$$\Delta W_{56} = \alpha \times y_5 \times s_6 = 0.1 \times 0.574 \times (-0.144) = -0.008$$

$$\Delta W_{57} = \alpha \times y_5 \times s_7 = 0.1 \times 0.574 \times 0.122 = 0.007$$

∴ Therefore new weights after 1 iteration are,

$$w_{36} = w_{36} + \Delta w_{36} = -0.4 - 0.008 = \cancel{-0.392} - 0.408$$

$$w_{37} = w_{37} + \Delta w_{37} = 0 + 0.006 = 0.006$$

$$w_{46} = w_{46} + \Delta w_{46} = 0.2 - 0.005 = 0.195$$

$$w_{47} = w_{47} + \Delta w_{47} = -0.5 + 0.004 = -0.496$$

$$w_{56} = w_{56} + \Delta w_{56} = 1.6 - 0.008 = 1.592$$

$$w_{57} = w_{57} + \Delta w_{57} = 0.1 + 0.007 = 0.107$$

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