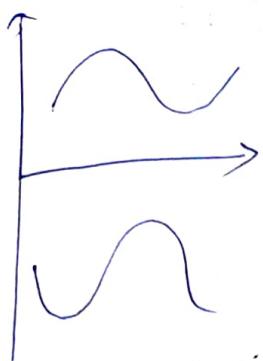
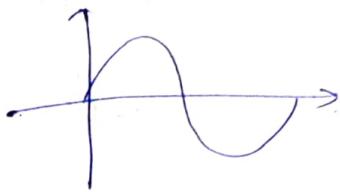


OP - AMP



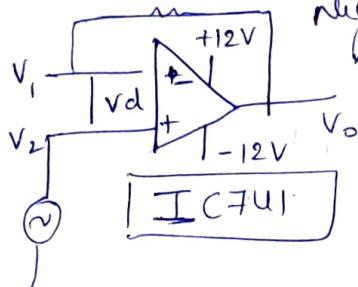
→ Unipolar signal



→ Bipolar signal

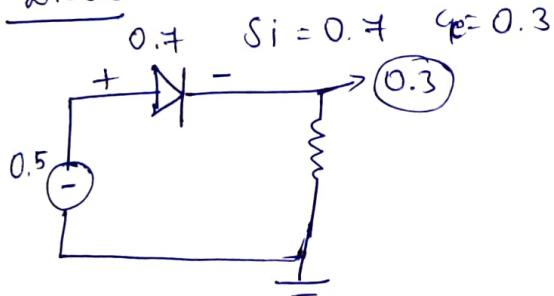
I/p of Op Amp → 50 μAmps

O/p voltage is managed at $1/10^6 \text{ V}$

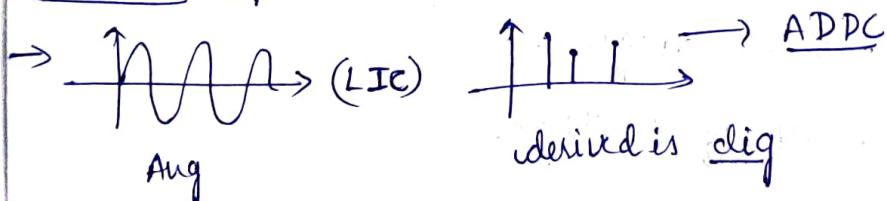


negative feed back for controlling stability of differential I/p's.

Diode



Full wave precision rectifier

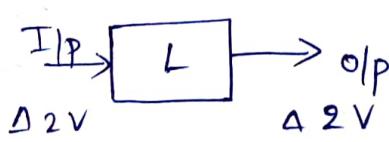


Basic signal is Aug

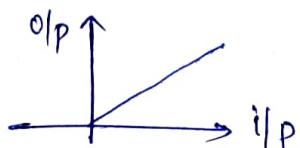
IC: Many components ~~are~~ combined to gather to form IC circuit

Linear system :-

e.g:- or Application
Op AMP



output always depends on I/p.



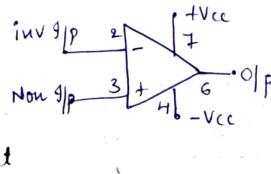
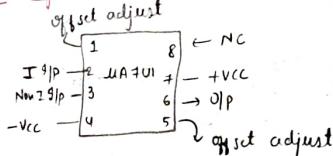
→ Op-AMP converts from Aug to Dig & Dig to Aug

Major App of opAMP → Biomedical app

UNIT-1 CHARACTERISTICS OF OP AMP.

Reference: S Shaliva hanan, VS Ianchima Bhaskaran.
Mc Graw Hill publication 2018

IC symbol



→ practical features
practically

$$(i) A_V = \infty \Rightarrow 2 \times 10^5$$

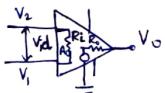
$$B_W = \infty$$

$$\text{Slew rate} = \infty$$

$$R_i = \infty$$

$$R_o = 0$$

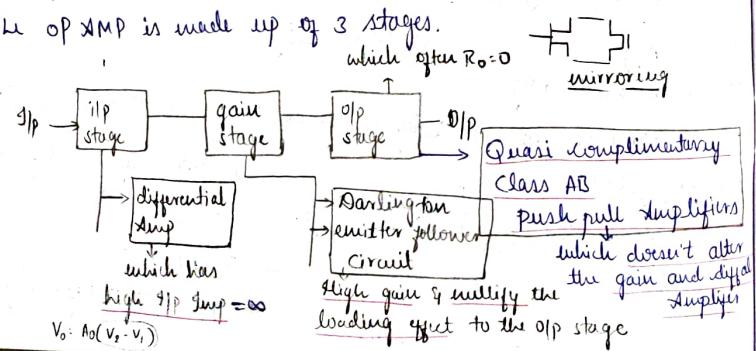
Practical circuit



$$U_o = A_o V_i$$
$$= A_o (V_2 - V_1)$$

Op AMP internal block diagram

The opAMP is made up of 3 stages.



Class A Amplifier = $90^\circ \rightarrow$ conduction angle

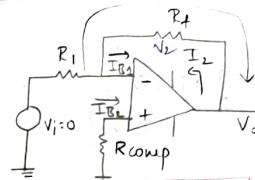
B → 180°

C → $180^\circ - 270^\circ$

AB → $90^\circ + 180^\circ$

DC Performance

(i) I_{IP} bias current : The current which is flowing into opamp is I_{IP} bias current.



If R_{comp} is not present

$$V_o = I_B \cdot R_f$$
$$I_L = 500 \mu A$$

$$R_f = 1 M\Omega$$

$$V_o = 500 mV$$

→ In order to compensate this we

add R_{comp} to produce further more V_o

$$R_{comp} = R_b / R_f$$

$$IB_2 = IB_1 + IB_2$$

P 1 Assume an opamp is having 400 and 300 nA of I_{IP} bias currents. Calculate the I_{IP} bias current and also compensation resistor value when R_f = 100 kΩ and R_b = 1 kΩ.

$$R_{comp} = \frac{R_b R_f}{R_b + R_f} = \frac{1k \times 100k}{(100+1)k} = 0.99k$$

$$IB = \frac{(400 + 300) nA}{2} = 350 nA$$

(ii) I_{IP} offset current and I_{IP} offset voltage

$$I_{os} = |IB_2| - |IB_1| \rightarrow \text{Input offset current}$$

$$I_{IP} \text{ offset volt} = V_o = \left(1 + \frac{R_f}{R_b}\right) V_{os}$$

Op Amp - Active device

Assume an opamp as 500 and 600 nA of i/p currents determine the i/p offset current and V_{OS} when the o/p reduces 200mV of o/p voltage to a resistance of 100kΩ & 1kΩ R_f and R_i respectively.

$$I_{OS} = |500| - |600| = 100 \text{ nA}$$

$$V_O = \left(1 + \frac{R_f}{R_i}\right) V_{OS}$$

$$200 \text{ mV} = \left(1 + \frac{100k}{1k}\right) V_{OS} \Rightarrow 200 = (101) V_{OS}$$

$$\therefore V_{OS} = 1.98 \text{ mV}$$

Total offset voltage

$$V_{OT} = \left(1 + \frac{R_f}{R_i}\right) V_{OS} + R_f I_{OS}$$

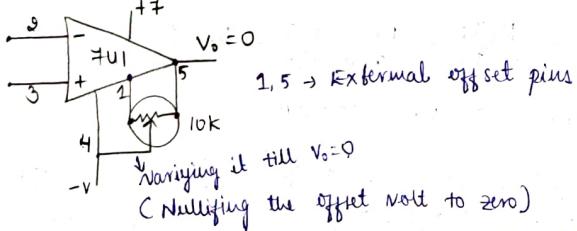
or

$$V_{BAS} = \left(1 + \frac{R_f}{R_i}\right) V_{OS} + R_f I_B$$

offset voltage compensation

(i) Op Amp with null terminals

(ii) Externally connected networks.



Thermal drift: when I_C is undergoing the temperature change it gives variation in characteristics.

$$\frac{\Delta V_{OS}}{\Delta T} \text{ mV/}^\circ\text{C} \quad \frac{\Delta I_{OS}}{\Delta T} \text{ PA/}^\circ\text{C} \quad \frac{\Delta I_B}{\Delta T} \text{ PA/}^\circ\text{C}$$

$$\frac{1}{PURR} = \frac{\text{Max } V_{OS}}{\text{Max } \text{Supply}}$$

Assume R_f = 10kΩ, R_i = 2kΩ, with an i/p offset volt of 5 mV, i/p off set current of 50nA, and a i/p bias current of 200nA at 25°C. Determine the maximum o/p offset voltage of the circuit.

$$\Rightarrow V_{OT} = 30.5 \text{ mV}$$

$$V_{OT} = \left(1 + \frac{R_f}{R_i}\right) V_{OS} + R_f I_{OS} = \left(1 + \frac{10k}{2k}\right) 5 \times 10^{-9} + 10 \times 10^3 \times 50 \times 10^{-9} = 30.5 \text{ mV},$$

$$R_f = 1M\Omega$$

→ An op Amp connected w/ R_i=100k with drift specification

$$\frac{\Delta V_{OS}}{\Delta t} = 30 \text{ mV/}^\circ\text{C} \quad \frac{\Delta I_{OS}}{\Delta t} = 0.20 \text{ PA/}^\circ\text{C}, \text{ assume the O/P volt} = 0 \text{ at } 25^\circ\text{C}$$

cal the max change in o/p volt when the temp raise to 75°C with respect to drift in V_{OS} and drift in I_{OS}.

$$\Delta V_{OS} = 30 \times (75 - 25) = 1500 \text{ mV}$$

$$V_o = \left(1 + \frac{R_f}{R_i}\right) V_{OS} = \left(1 + \frac{1M}{100k}\right)(1.5)$$

$$V_o = 16.5$$

$$\frac{\Delta I_{OS}}{\Delta t} = 0.2 \Rightarrow \Delta I_{OS} = 10 \text{ nA}$$

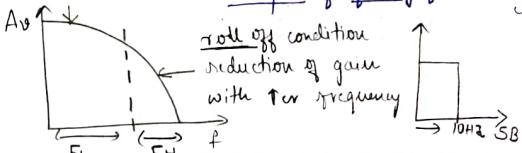
$$\Delta V_{OS} = \Delta I_{OS} \times R_f \\ = 0.01 \text{ V.}$$

$$V_o = \left(1 + \frac{R_f}{R_i}\right) @ 0.01 = 0.11 \text{ V.}$$

$$\text{Max change } V_{o(75)} - V_{o(25)} = 0.11 - 0.10 = 0.01 \text{ V.}$$

AC characteristics

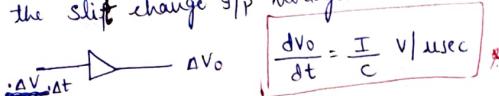
(i) Frequency response. → high pass filter → which allows only high frequency. → low pass frequency filter → which allow only low frequency



(ii) Bandwidth :- The range of frequencies.

$$BW = f_2 - f_1$$

(iii) Slew rate : The maximum change of o/p voltage, when this is the slew change S/P voltage.



* Noises in an op-amp signal

- 2 types of noises
1) Internal noise.
2) External noise.

in op-amps:

- 1) Thermal noise
- 2) shot noise / discrete noise
- 3) 1/f noise / flicking noise
- 4) Burst noise / perform noise.

1. Thermal noise : It is due to increase in temperature of the system.

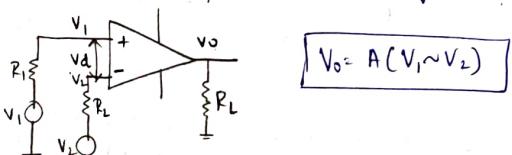
2. shot noise : It is generated due to current flow.

3

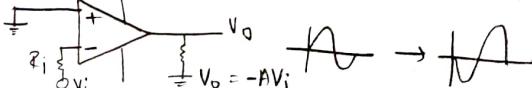
4

* open loop op-Amp configuration

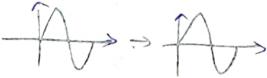
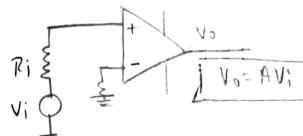
(i) Differential amp → gain of the system is very high.



(ii) Inverting amp :- gives 180° phase shifting.

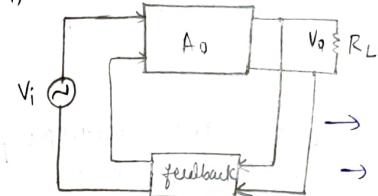


3 Non-inverting op-amp

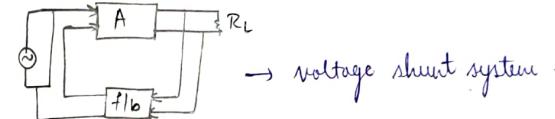


* Closed loop op-amp system.

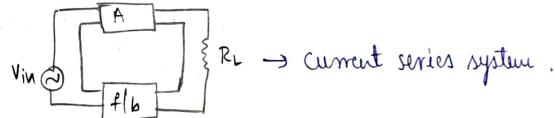
i)



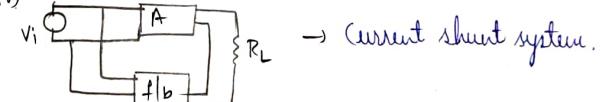
ii)



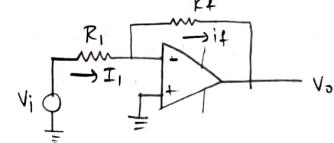
iii)



iv)

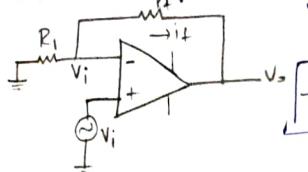


Closed loop (Inverting amp),



$$V_o = -I_f \times R_f$$
$$V_o = -\frac{R_f}{R_i} \times V_i$$
$$\Rightarrow \boxed{\frac{V_o}{V_i} = -\frac{R_f}{R_i}}$$

④ Non-inverting amp

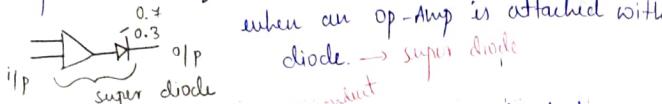


$$V_i = \frac{R_f}{R_1 + R_f} \times V_o$$

$$\frac{V_o}{V_i} = \frac{R_f + R_1}{R_1} = 1 + \frac{R_f}{R_1}$$

Circuits using diodes

→ op-amp does amplification of very low signals.



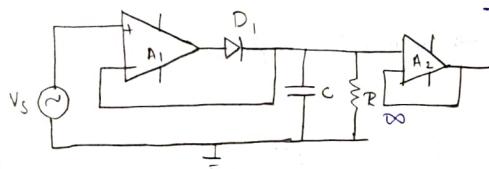
when an op-amp is attached with diode → super diode

diode only has 0V until saturation
where op-amp has high voltage after amplification then
diode has high voltage as compared to saturation voltage.

∴ o/p

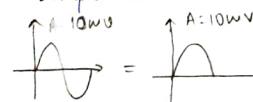
Precision peak detector

The peak detector



② Calculating or calibrating the

Temperature in boilers.



⑤ In this case capacitor should

discharge so Resistor (R) is used.

Application:-

→ Detecting the peak
of the signal.



③ Capacitor will be holding
the gain

④ The input impedance at A2 is
∞ so that capacitor
won't discharge.

To design an ac peak detector.

Design $RC < 10T$ → Time period.

assume $0.01\mu F$

→ Assume, design an ac peak detector circuit $f = 10\text{kHz}$
i/p volt = 25 mV,

$$V_s = 25 \text{ mV} \quad T = 10^{-4} \text{ sec}$$

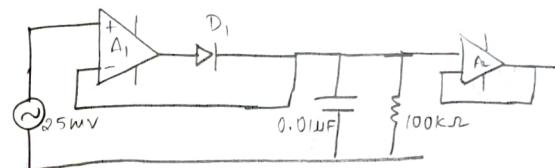
$$R \cdot 0.01 \times 10^6 < 10 \times 10^{-4}$$

$$R < \frac{10^{-3}}{0.01 \times 10^6}$$

$$R < 1 \times 10^5 \Omega = 100 \text{ k}\Omega$$

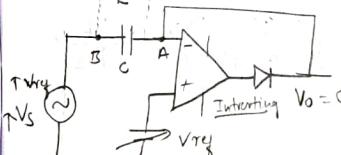
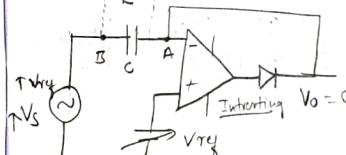
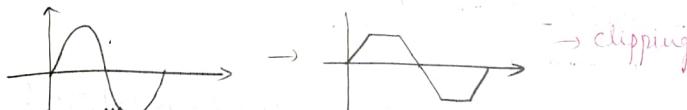
$$\frac{1}{2\pi}$$

$$C = 0.01\mu F$$



Precision clamping

Diodes are basically used for rectification other than that it is used for clamping or clipping.



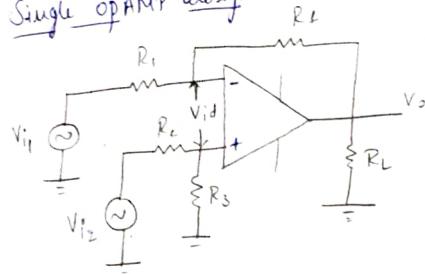
Clamping circuit is the one which shifts the signal by introducing DC voltage

→ DC signal is introduced by using the V_{ref} value.



Op-amp Amplifier

Single OPAMP design



Assuming all the resistors in the circuit to be equal to R , using superposition theorem the output V_{o1} due to the input V_{i1} equal.

$$V_{o1} = \frac{R_f}{R_1} (V_{i1})$$

$$V_o = \frac{R_f}{R} (V_{i1}) \Rightarrow V_{o1} = V_{i1}$$

By grounding input terminal V_{i2} the o/p V_{o2} due to i/p.

$$V_{o2} = -V_{i2}$$

$$V_o = V_{o1} + V_{o2} = V_{i1} - V_{i2}$$

$$\boxed{V_o = V_{i1} - V_{i2}}$$

If we have the variable resistance. Values are not equal the final output $V_o = \left(1 + \frac{R_f}{R_1}\right) \left(\frac{R_3}{R_3 + R_2}\right) V_{i1} - \frac{R_f}{R_2} V_{i2}$

→ calculate the

Diff Mode gain & Common mode gain

Same values are given to both the two i/p signals.

$$\boxed{V_{cm} = \frac{V_{i2} + V_{i1}}{2}}$$

→ Due to the symmetric property of the opamp there will be any mismatch in the o/p voltage even though (should not) a common mode signal is given.

→ Since the system process some abnormalities the response to the +ve and -ve terminals are found to be different.

→ The o/p is not zero even if the common mode signals are given.

→ $\therefore [V_o = A_1 V_{o1} + A_2 V_{o2}]$ then A_1 and A_2 are amplification factors with respect to i/p ① and ②

$\boxed{V_{id} = \text{The differential voltage } V_{id} \text{ is given by } V_{i1} - V_{i2}}$
where V_{i1} w.r.t common mode signal is given by.

$$\boxed{V_{i1} = V_{cm} + \frac{1}{2} V_{id}} \quad \text{and} \quad \boxed{V_{i2} = V_{cm} - \frac{1}{2} V_{id}}$$

• substituting this to o/p eqn

$$\boxed{V_o = A_{dm} V_{id} + A_{cm} V_{cm}}$$

A_{dm} = diff mode gain A_{cm} = common mode gain.

$$\boxed{A_{dm} = \frac{1}{2} (A_1 - A_2)}$$

$$\boxed{A_{cm} = A_1 + A_2}$$

→ For a given CMRR of 10^5 a diff gain of 10^4 . determine the common mode gain.

$$\boxed{CMRR = \frac{A_{dm}}{A_{cm}}}$$

$$10^5 = \frac{10^4}{A_{cm}} \Rightarrow 0.1 \therefore A_{cm} = 0.1$$

→ The two i/p terminals of o/p of op AMP are connected to voltage strength of +705 mV and -700 mV respectively. The differential mode gain of op AMP is 5×10^5 , and CMRR is $\pm 80 \text{ dB}$. calculate the voltage, & % error due to common mode signals.

$$V_1 = +705 \text{ mV} \quad A_d = 5 \times 10^5$$

$$V_2 = -700 \text{ mV} \quad \text{CMRR} = 80 \text{ dB}$$

$$V_o = \text{Adm} V_{id} + \text{Acm} V_{cm}$$

$$V_{id} = V_2 - V_1 = 5 \text{ mV}$$

$$V_{cm} = \frac{V_1 + V_2}{2} = +702.5 \text{ mV}$$

$$V_o = 5 \times 10^5 \times 5 \times 10^{-6} + 50 \times 702.5 \times 10^{-6} \text{ V.}$$

$$= 25 \times 10^{-1} + 0.037125$$

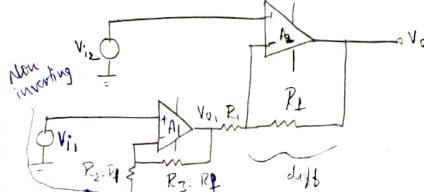
$$V_o = 2.537 \text{ V}$$

$$\text{Ideal voltage: Adm. Vdm} = 2.5 \text{ V}$$

$$\% \text{ ERROR} = \frac{2.537 - 2.5}{2.5} \times 100 = 1.48 \%$$

$$\% \text{ ERROR} = \frac{\text{O/P voltage} - \text{Ideal volt}}{\text{Ideal volt}} \times 100$$

Dual op Amp



To increase the Z_i we are using dual op-Amp

→ Using ideal Op-Amp design the gain of the overall system can be T_{sd} when compared to signal single op-Amp design. the above circuit is split into two parts with op-Amp A₁ acting as non-inverting amplifier and op-Amp A₂ acting as differential amplifier the o/p voltage after of amplifier A₁

$$V_{o1} = \left(1 + \frac{R_3}{R_2}\right) V_{i1}$$

The i/p voltage V_{i2} appears on non-inverting terminal of op-AMP A₂ which process gain of

$$V_o = \left(1 + \frac{R_f}{R_1}\right) V_{i2}$$

V_{o1} appears at the ~~non~~-inverting terminal with an input again of $\left[-\frac{R_f}{R_1} V_{o1} \right]$

∴ By using superposition theorem the final o/p voltage

$$V_o = -\left(\frac{R_f}{R_1}\right) V_{o1} + \left(1 + \frac{R_f}{R_1}\right) V_{i2}$$

Substituting the value of V_{o1} to the above equation

$$V_o = -\left(\frac{R_f}{R_1}\right) \left(1 + \frac{R_3}{R_2}\right) V_{i1} + \left(1 + \frac{R_f}{R_1}\right) V_{i2}$$

If we assume $R_3 = R_f$ and $R_1 = R_2$. final o/p equation.

$$V_o = -\left(\frac{R_f}{R_1}\right) \left(1 + \frac{R_f}{R_2}\right) V_{i1} + \left(1 + \frac{R_f}{R_1}\right) V_{i2}$$

$$V_o = \left(1 + \frac{R_f}{R_1}\right) (V_{i2} - V_{i1})$$

i/p resistance of Dual op-Amp Differential amp

The i/p resistance of the overall system is found by measuring the i/p impedance of each system by considering the one i/p at a time. The i/p impedance for non inverting amplifier R_{ii} is given by $R_{ii} = R_i(1 + A\beta_1)$

where R_i is open loop resistance of the Op-Amp

$$\boxed{\beta_1 = \frac{R_2}{R_2 + R_1}} \quad A - \text{gain.}$$

Similarly, shorting the i/p voltage V_{oi} to ground and the second stage now behaves as non inverting amplifier which has the overall resistance given.

$$\boxed{R_{i2} = R_i(1 + A\beta_2)}$$

$$\boxed{\beta_2 = \frac{R_1}{R_1 + R_2}} \quad R_i - \text{open loop resistance.}$$

→ The overall resistance of the system will be combination of R_{ii} and R_{i2} .

O/p resistance

The o/p impedance of the differential amplifier is same with a minor modification of β value:

$$\boxed{\beta = \frac{1}{A_D}} \quad \text{where } A_D \text{ is the closed loop gain of the differential amplifier}$$

→ The overall output resistance.

$$\boxed{R_{of} = \frac{R_o}{1 + A/A_D}} \quad R_o - \text{open loop resistance}$$

$A - \text{open loop gain of Op Amp}$

Similarly we can calculate the band width of the differential amplifier which is given by BW_{CL} the ratio

of unity gain band width to give closed loop gain.

$$\boxed{BW_{CL} = \frac{A_0 \times f_1}{A_D}}$$

where f_1 is open loop break frequency.

Assume $R_1 = R_3$ which is 560Ω , $R_f = R_2 = 5.6\text{ k}\Omega$ and $V_{oi} = -2\text{ V}$. $R_i = 2\text{ M}\Omega$, and gain $A = 2 \times 10^5$. Determine the voltage gain, i/p resistance and o/p voltage of the diff amp if input to the other terminal of the diff amp is -1 V .

$$V_{oi} = 1 + R_{ii} = R_i(1 + A\beta_1)$$

$$\beta_1 = \frac{R_2}{R_1 + R_2} = \frac{5.6\text{ k}}{560 + 5.6\text{ k}} = 5610 \quad 0.909$$

$$R_{ii} = 2 \times 10^6 (1 + 2 \times 10^5 \times \frac{0.909}{5610})$$

$$R_{ii} = 3.63602 \times 10^{10}$$

$$R_{i2} = R_i(1 + A\beta_2) \quad \beta_2 = \frac{R_1}{R_1 + R_2}$$

$$= 2 \times 10^6 (1 + 2 \times 10^5 \times 0.0909) \quad = \frac{560}{560 + 5.6\text{ k}} = 0.0909.$$

$$V_o = A_D \times V_{id} \quad A_D = 1 + \frac{R_f}{R_i} = 1 + \frac{5.6\text{ k}}{560}$$

$$V_o = -11\text{ V.} \quad = 11$$

Schmitt trigger

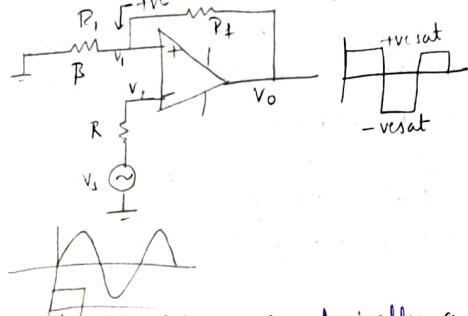
→ which converts the irregular signal to regular signal.

→ And compares the i/p ~~with~~ voltages.

$\beta V_o > V_s \rightarrow$ op amp shifts to +ve sat

$V_{sat} <$ source voltage (12V)

$\beta V_o < V_s \rightarrow$ op amp shifts to -ve sat.



→ A schmitt trigger is basically a comparator circuit which produces a fixed square wave form which oscillates b/w +ve and -ve saturation.

→ At the non inverting terminal due to the presence of voltage divider circuit the feedback fraction of β which is equal to $\frac{R_f}{R_1+R_2}$ is present with output voltage V_o in the non-inverting terminal.

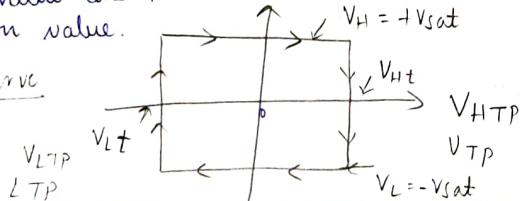
$\therefore V_i = \beta V_o$ where $V_o = \text{closed loop gain} \times \text{input voltage}$

$$V_i = \beta A_f V_s$$

$$V_o = A_f \cdot V_s$$

when $V_i > V_s$ signal the output will continue to be +ve saturation value and when $V_i < V_s$ the output falls to -ve saturation value.

Hysteresis curve



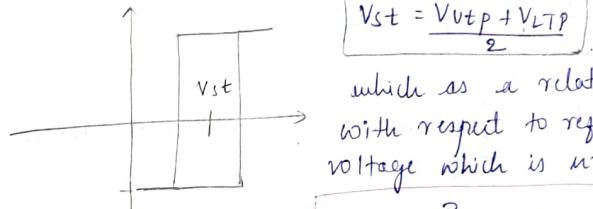
If the i/p exceeds V_{HT} the o/p will be the V_{HT} which shifts from +ve to -ve V_{sat} .

→ similarly if i/p goes below V_{LT} the o/p will be - V_{HT} which shifts from switch from - V_{sat} to + V_{sat} .

Note :- positive voltage source H-curve shifts right.
-ve voltage source H-curve shifts left.

→ internal i/p and o/p characteristics with practical analysis.

For op Amp which is designed as a schmitt trigger with reference voltage the switching pot of the circuit changes from 0 to certain value.



$$V_{st} = \frac{V_{UTP} + V_{LTP}}{2}$$

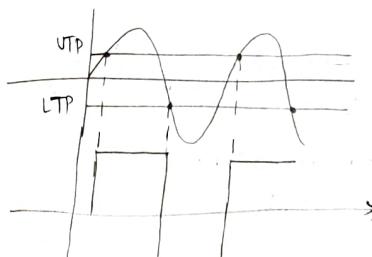
which is a relationship with respect to reference voltage which is vty but.

$$V_{st} = \frac{R_f}{R_1+R_f} \times V_{ref}$$

$$V_{HT} = V_{st} + \frac{R_1}{R_1+R_f} (+V_{sat})$$

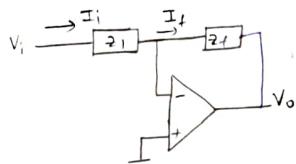
$$V_{LT} = V_{st} + \frac{R_1}{R_1+R_f} (-V_{sat})$$

→ Normal i/p and o/p characteristics.



UNIT-II APPLICATIONS OF OP-AMP

Sign changer / phase inverter.



$$\text{closed loop gain} = -\frac{R_f}{R_1} = -1$$

$$R_f = R_1$$

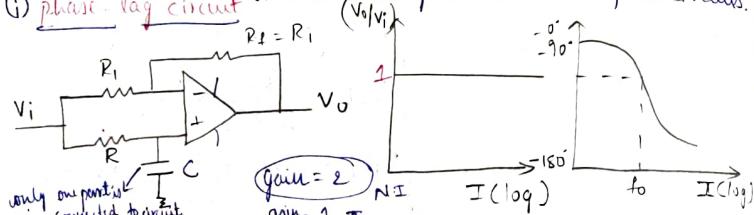
→ whenever sign conversion is required do
 $R_f = R_1 \Rightarrow$ it will be (-180°) change

Scale changer

It doesn't bother on the sign but only on the scale of $\left| \frac{V_o}{V_i} \right|$ where $\left| \frac{R_f}{R_1} \right| \neq 1$

Phase shift circuit

(i) phase lag circuit or Constant delay circuits or All pass circuits.



In phase circuits only imaginary part is considered.

→ Only phase of the signal is considered not magnitude.

→ All kinds of frequency is allowed. (Not like low pass or high pass)

→ Whenever a signal reduces the phase of the signal is called as phase lag signal.

→ To produce the lag we used RC circuit which introduces the lag in the circuits.

→ RC was low pass filter.

$$V_o(j\omega) = -V_i(j\omega) + 2 \frac{1}{j\omega CR} V_i(j\omega)$$

$$= V_i(j\omega) \left(\frac{2}{j\omega CR} - 1 \right)$$

$$= V_i(j\omega) \left(\frac{1 - j\omega CR}{1 + j\omega CR} \right)$$

$$\frac{|V_o(j\omega)|}{|V_i(j\omega)|} = \left| \frac{1 - j\omega CR}{1 + j\omega CR} \right|$$

2-gain & non-inverting terminal.

$$\theta = \tan^{-1}(CR\omega) - \tan^{-1}(CR\omega)$$

$$= -2 \tan^{-1}(CR\omega)$$

$$\omega = 0 \quad \theta = 0^\circ$$

$$\omega = \infty \quad \theta = -180^\circ$$

$$\theta = 2 \tan^{-1}(f/f_0)$$

$$f_0 = \frac{1}{2\pi RC}$$

→ Determine the angle, Output.

Assuming $R_1 = 20\text{k}\Omega$ $R = 39\text{k}\Omega$ $R_f = R_1$ &

$$C = 1\text{nF}, f = 2\text{kHz}$$

$$\theta = 2 \tan^{-1}(f/f_0)$$

$$\theta = 2 \tan^{-1} \left(\frac{2\text{k}}{4080.89} \right)$$

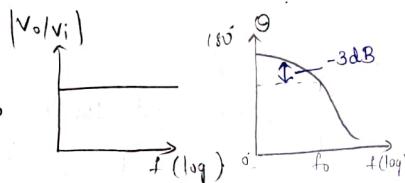
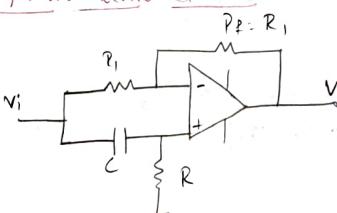
$$\theta = -52.2^\circ$$

$$td \rightarrow T$$

$$\frac{\theta}{360^\circ} = \frac{td}{T} \Rightarrow td = \frac{\theta T}{360^\circ} = \frac{(52.21) \times 5 \times 10^{-4}}{360^\circ}$$

$$td = 7.2513 \times 10^{-5}$$

Phase lead circuits



→ In phase lead circuit we use ~~phase~~ high pass filter to increase the angle.

→ with Capacitor followed by resistor \Rightarrow high pass filter.

→ Not bothered on magnitude and it is constant.

→ One RC component maximally gives 180° phase shift.

→ phase shifts from 180° to 0° anywhere in b/w.

$$V_o(j\omega) = -v_i(j\omega) + 2 \left(\frac{j\omega RC}{1+j\omega RC} \right) v_i(j\omega)$$

Inverting gain = 1
N I gain = 2

$$\left[\frac{V_o(j\omega)}{V_i(j\omega)} = \frac{-1 + j\omega RC}{1 + j\omega RC} \right] \times$$

when ever the difference in real parts phase addition,
difference in imaginary part phase subtraction.

$$\theta = 180^\circ - \tan^{-1}(WRC) - \tan^{-1}(WRC)$$

$$\theta = 180^\circ - 2 \tan^{-1}(WRC)$$

$$\theta = 180^\circ - 2 \tan^{-1}(f/f_0)$$

P Determine a phase angle for phase lead circuit operating with $R_i = 25k\Omega$, $R = 30k\Omega$, $C = 1\text{nF}$, $R_f = R_s$, frequency $f = 5\text{kHz}$

$$\theta = 180^\circ - 2 \tan^{-1}(f/f_0)$$

$$\theta = 180^\circ - 86.60$$

$$\theta = 93.39^\circ$$

$$\begin{aligned} f_0 &= \frac{1}{2\pi RC} \\ &= \frac{1}{2\pi \times 30 \times 10^3 \times 1 \times 10^{-9}} \\ &= 5305.164 \end{aligned}$$

→ Voltage follower:

what ever the input the output should be of same.

$$V_i \xrightarrow{\text{oscilloscope}} |V_i| = |V_o|$$

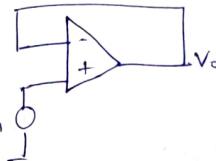
$$V_o \xrightarrow{\text{oscilloscope}}$$

In voltage follower magnitude of the i/p and o/p should be same, so will get same phase angle.

→ To make it possible we have to go through a non-inverting terminal.

$$A_v = 1 + \frac{R_f}{R_i} \quad \text{where } R_i \rightarrow \infty, R_f = 0$$

$$A_v = 1$$



Voltage controlled voltage source

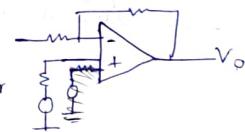
when an output of the circuit depends on the i/p source \rightarrow varc dependent sources.

Design

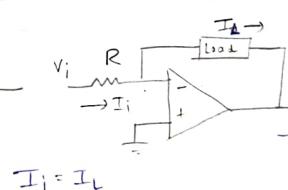
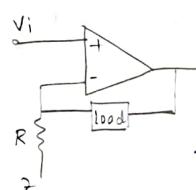
(i) Considering multiplication factor $\rightarrow (K) \Rightarrow$ times.

e.g.: $V_o = K V_i$ Independent of current sources.
dependent

(ii) V_o is independent of I whether it is inverting or non-inverting

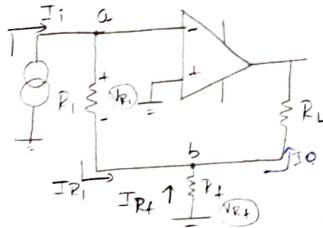


Voltage controlled current source



same current source is going through the circuit
 \rightarrow fixed current source circuits.

Inverting Current amp



$$V_{R1} = V_{RF}$$

$$I_o = I_L = I_{R1} + I_{RF}$$

$$A_i = \frac{I_o}{I_i} = \frac{I_{R1} + I_{RF}}{I_i}$$

$$\boxed{I_{R1} = I_i} \quad \text{**}$$

$$I_{RF} = \frac{V_{RF}}{R_f}$$

$$V_{RF} = V_{R1}$$

$$I_{RF} = \frac{V_{RF}}{R_f} = \frac{I_i R_1}{R_f}$$

$$I_o = I_i + \frac{I_i R_1}{R_f}$$

$$\boxed{I_o = I_i \left(1 + \frac{R_1}{R_f}\right)}$$

$$\boxed{A_i = 1 + \frac{R_1}{R_f}} \quad \text{**}$$

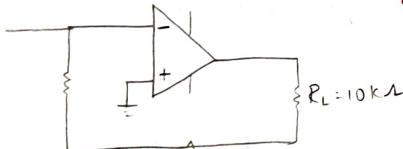
Design an current amplifier for $R_1 = 22\text{ k}\Omega$, $R_f = 1\text{ k}\Omega$, and $R_L = 10\text{ k}\Omega$. input current of 10 mA .

$$\boxed{I_o = I_i \left(1 + \frac{R_1}{R_f}\right)}$$

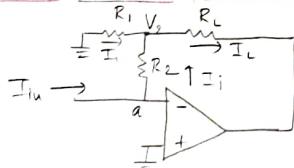
$$10 \times 10^6 \left(1 + \frac{22}{1}\right)$$

$$10 \times 10^6 \times 23$$

$$I_o = 230\text{ mA}$$



Current controlled current source



$$(a) I_o = K_i (I_i)$$

constant

(b) I_i is always independent of load current resistances. The current controlled current source, the op-amp current will be equal to scale version of input current and it is also independent of the load present in the circuit.

\therefore the I_{in} current drawn into the op-amp is zero.

$$I_{in} = I_i$$

Node A is at virtual ground. Voltage at V_2 is given by $\boxed{V_2 = -I_i R_2}$

The current I_i is calculated by:

$$I_i = \frac{0 - V_2}{R_1} =$$

$$I_i = \frac{I_i R_2}{R_1}$$

applying KCL at V_2

$$I_L = I_i + I_i = \frac{I_i R_2}{R_1} + I_i$$

$$\boxed{I_L = I_i \left(1 + \frac{R_2}{R_1}\right)} \quad \text{**}$$

→ Design an work current controlled current source with node voltage $V_2 = 3\text{ V}$, $R_1 = 10\text{ k}$, $R_2 = 5\text{ k}$.

$$\boxed{V_2 = -I_i \times R_2}$$

$$3 = I_i \times 5\text{ k}$$

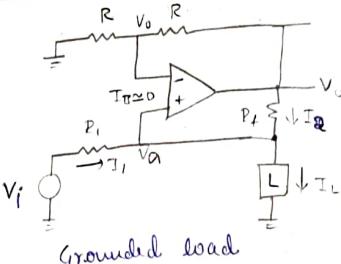
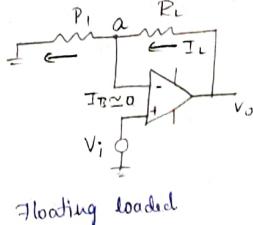
$$\boxed{I_i = 0.6\text{ mA}}$$

$$I_L = 0.6\text{ mA} \left(1 + \frac{1}{2}\right)$$

$$\boxed{I_L = 0.9\text{ mA}} \quad //$$

$$\boxed{I_L = I_i \left(1 + \frac{R_2}{R_1}\right)}$$

Voltage to current converter (Transconductance Amplifier)



A transconductance amplifier with floating node the output current is depending on the input voltage and which is independent of load present in the circuit since $I_B = 0$

The load current $I_L = V_i / R_L$ \rightarrow floating load

In grounded load the analysis slightly differs since the load is connected to ground directly

Applying KCL at node V_a and assuming $R = R_1 = R_f$

$$I_1 + I_2 = I_L$$

$$\frac{V_i - V_a}{R} + \frac{V_o - V_a}{R} = I_L$$

$$V_i - V_a + V_o - V_a = R I_L \Rightarrow V_i + V_o - 2V_a = I_L R$$

$$V_a = \frac{V_i + V_o - I_L R}{2}$$

The gain of the above non-inverting amplifier.

$$1 + \frac{R_f}{R_1} = 1 + \frac{R}{R} = 2$$

The o/p of non inverting amplifier gain times i/p voltage

$$V_o = 2 \times V_a$$

$$V_o = V_i + V_o - I_L R$$

$$V_i = I_L R$$

$$I_L = \frac{V_i}{R}$$

$$\text{The transconductance factor } g_m = \frac{I_L}{V_i} = \frac{1}{R}$$

$$(I_L = V_i \times g_m)$$

\rightarrow Design can transconductance amplifier with floating node having $R_f = 10 \text{ k}\Omega$, $R_1 = 2 \text{ k}\Omega$, $V_i = 0.5 \text{ V}$

$$I_L = \frac{V_i}{R_L} = \frac{0.5}{10 \text{ k}} = 5 \times 10^{-5} \text{ A} = 50 \mu\text{A}$$

$$= \frac{0.5}{2 \times 10^3} = 0.25 \times 10^{-3} \text{ A} = 250 \mu\text{A}$$

$$g_m = \frac{I_L}{V_i} = \frac{0.250 \mu\text{A}}{0.5} = 500 \mu\text{A} = 5 \times 10^{-4} \text{ Siemens}$$

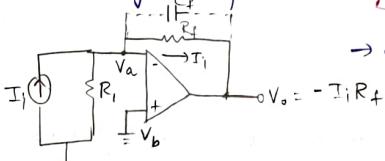
Current to voltage converter

The transresistance amplifier will convert the applied i/p current into a o/p voltage.

O/p voltage is the scaled factor of the input current and independent of the load present.

$\therefore V_o = K I_i$ \therefore where K is called as transresistance factor having a unit of ohms.

The voltage at point V_a ; $V_a = -I_i R_f$



$$\rightarrow \text{The o/p voltage } V_o = K V_a$$

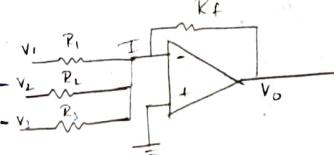
\rightarrow Design a transresistance amplifier o/p volt = 5 v and $I_i = 10 \text{ mA}$

$$V_o = K I_i$$

$$5 = K 10 \text{ mA}$$

$$\Rightarrow K = 500 \text{ ohm}$$

ADDER or summing amplifier:



$$I = \frac{V_1}{R_1} + \frac{V_2}{R_2} + \dots + \frac{V_n}{R_n}$$

$$\boxed{V_0 = -IR_F = -\left[\frac{V_1 R_F}{R_1} + \frac{R_F}{R_2} V_2 + \frac{R_F}{R_3} V_3 + \dots + \frac{R_F}{R_n} V_n\right]}$$

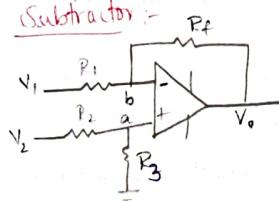
$$\boxed{V_0 = A_1 V_1 + A_2 V_2 + \dots + A_n V_n}$$

→ Design an summing amp for i/p voltage of 2, 3, 4V with equal amount of resistance of 1 kΩ.

$$V_0 = -\left[\frac{R_F}{R_1} (V_1) + \frac{R_F}{R_2} (V_2) + \frac{R_F}{R_3} (V_3)\right]$$

$$= -[2 + 3 + 4] = -9V$$

Subtractor:



$$V_{O1} = -\left(\frac{R_F}{R_1}\right) V_1$$

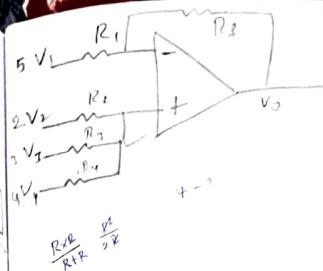
$$V_{O1} = -V_1$$

$$V^I = \frac{R_3}{R_2 + R_3} V_2 = \frac{R}{R+R} V_2 = \frac{V_2}{2}$$

$$V_{O2} = \left(1 + \frac{R_F}{R_1}\right) \frac{V_2}{2}$$

$$\boxed{V_{O2} = V_2}$$

→ Design a subtractor and determine the output voltage with the help of superposition theorem with an input of 2 volts, 3 volts, and 4 volts. all the 3 g/p's are given to Non-inverting terminal and d/p 5V is given to inverting terminal.



$$V^I = \frac{R_4 || R_3}{R_1 || R_3 + R_2} (2) = \frac{R_4}{3R} (2)$$

$$= 2/3$$

$$V^{II} = \frac{R_2 || R_4}{R_1 || R_2 + R_3} (3)$$

$$V^{III} = \frac{R_1}{3R_1} (4)$$

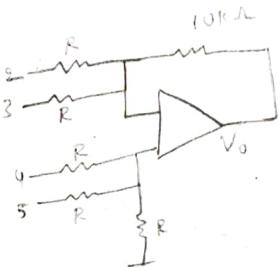
$$= 3/3 = 1V$$

$$= 4/3 V$$

$$V_{O2} = \frac{2}{3} + 1 + \frac{4}{3} = \frac{7}{3} V$$

$$\boxed{V_{O1} = -5V}$$

Calculate the output voltage of adder-subtractor circuit with input voltage 2, 3, 4, 5, volts with a resistance value of $10\text{ k}\Omega$



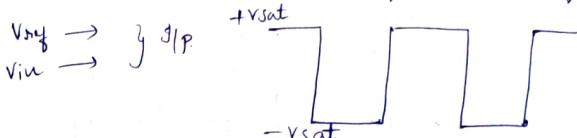
UNIT 1-3 → INVERTING Part

OPAMP AS LINEAR CIRCUITS

Linear circuits: Increment in ΔI_p gives increment in ΔO_p . (There will be a constant relation b/w I_{Op} and O_{Op})

Comparators

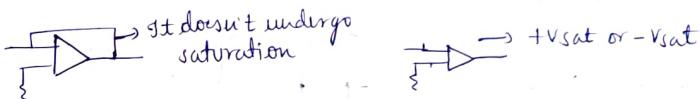
There are also called as square wave generators.



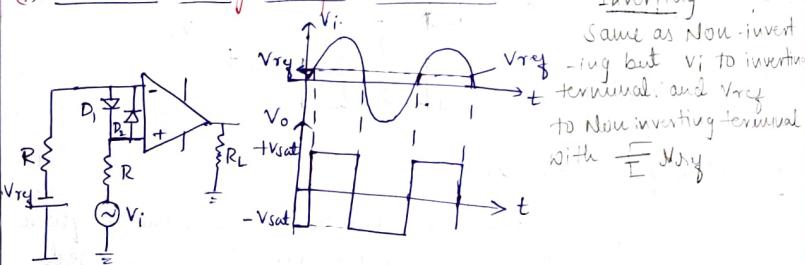
Here opamp has feedback or no feedback so it has only $+V_{sat}$ or $-V_{sat}$

$$V_{in} > V_{sat} \rightarrow +V_{sat}$$

$$V_{in} < V_{sat} \rightarrow -V_{sat}$$



(i) Non-inverting Comparator circuit



Inverting

Same as Non-invert

ing but V_i to invert terminal and V_{ref} to Non-inverting terminal with \ominus sign

Comparators operate in non linear mode which produces output which will be one of the saturation level depending on the comparison between input and reference voltage. The above fig shows the non inverting comparator which compares two input voltage V_{ref} and V_i .

The reference voltage is always a DC voltage and V_{ref} voltage will be a AC signal. Here OP voltage is sinusoidal AC signal.

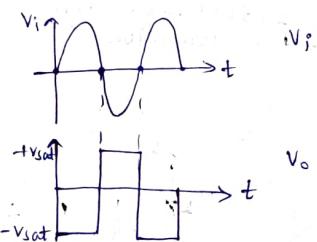
When input voltage V_i is less than V_{ref} then OP of the Op Amp will be at negative saturation, when the OP voltage V_i greater than V_{ref} then OP of the OP Amp will be at +ve sat. This will continue since input voltage continues after every period.

D_1 and D_2 are used for protecting the OP Amp from excessive voltage spikes being generated by reference source.

$$V_i < V_{\text{ref}} \rightarrow V_o \rightarrow -V_{\text{sat}}$$

$$V_i > V_{\text{ref}} \rightarrow V_o \rightarrow +V_{\text{sat}}$$

In inverting comparator V_i is connected to IN terminal and V_{ref} to NI terminal



→ Detect only zero points.

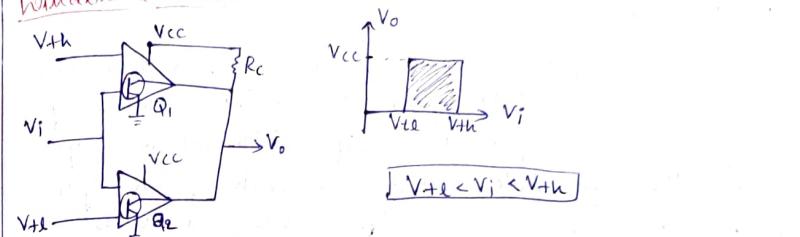
→ Zero crossing detectors are also called as sine to square converters. Here the same comparator circuit is used by making reference voltage to zero.

→ This circuits will detect the zero points and shift the output to either +ve or -ve saturation voltages.

Since the input is given to inverting terminal initially the first zero point will move the output voltage of the

opamp to -ve saturation level. This continues until the circuit detect next zero point which will shift the output to +ve saturation this cycle continues which makes the circuit to operates as sine to square converter.

Window detector



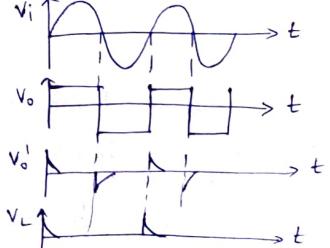
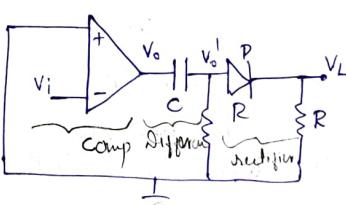
Window detector identifies the unknown input voltage b/w two threshold values V_{tl} and V_{th} .

→ When the input voltage is b/w V_{tl} and V_{th} both the transistor Q_1 and Q_2 are off and the resistor R_C pulls the voltage V_{cc} to the output making V_o to be high.

→ When $V_i > V_{\text{th}}$ transistor Q_1 is ON which makes R_C to be pulled to ground which makes the output equal to zero.

→ Similarly where $V_i < V_{\text{tl}}$ Q_2 is ON which makes the output equal to zero.

Timing Marker signal generator



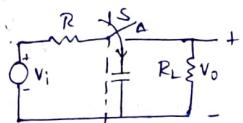
This are used for digital circuit

→ Timing marker signal generator produces trigger pulses
which consists of three parts having

- (i) Comparator
- (ii) Differentiator
- (iii) Rectifier

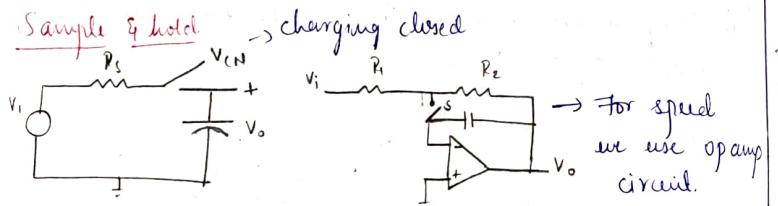
The comparator operates as zero crossing detector, which converts sine wave into square wave, the output of the comparator is fed to a differentiator whose output is V'_1 , the differentiated output consists of two cycle in each period which is rectified using a diode rectifier which produces output V_2 with a single positive spike in each half of the cycle.

Sampling switches



V_g ! Gating signal (Analog signal) \Rightarrow At switch.

Sample & hold



This are also called Analog to digital conversion (ADC)

→ Sample and hold circuits are used in ADC, the circuit is operated using a switch which is controlled by a voltage (V_{CN}). the amount of time duration

decides the charging and discharging of the capacitor
→ Sample and hold circuitries are two time period one is (i) aperture time that is maximum time amount of time for the switch to open.

(ii) Acquisition time which is minimum time required after the sample signal is applied and output reaching the input signal.

→ The opening and closing of the switch is controlled by a RC filter formed using an op-amp for input voltage of V_i , the output voltage $V_o(t)$

$$V_o(t) = -\frac{R_F}{R_i} V_i (1 - e^{-t/R_F C})$$

UNIT - 2 - II part

WAVE FORM GENERATOR'S

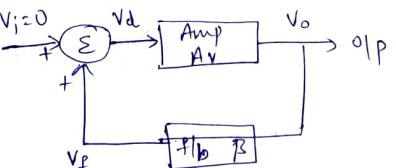
The oscillators which generates wave form without input.

-ve feed back \rightarrow amplifiers

+ve feed back \rightarrow wave form oscillation

(e.g.: square form, triangle

Oscillator is a feed back network consisting of an amplifier and the feed back circuit, the output of the amplifier is fed back to the input through a feed back network, the above fig shows the principle of oscillation with input = 0, the differential voltage V_d is given by summation of $[V_i + V_f] = V_d$



The output voltage V_o is given by voltage gain A_v into V_i

$$V_o = A_v \cdot V_i = A_v (V_i + V_f)$$

Feed back voltage V_f is given feed back factor β

$$V_f = \beta \cdot V_o = \beta \cdot A_v (V_i + V_f)$$

$$\frac{V_o}{V_i} = \frac{A_v}{1 - \beta A_v}$$

The above shown circuit could work as an oscillator, two conditions must be satisfied.

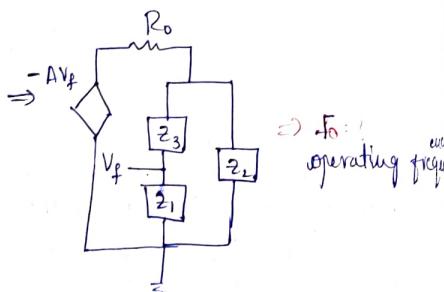
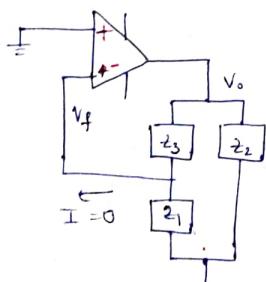
(i) Magnitude of open loop gain at feed back fraction should be equal to one ($|A_v\beta| = 1$)

(ii) The phase angle of open loop gain and feed back factor is 360° or 0° . $|A_v\beta| = 360^\circ$ or 0°

This above two condition is called as barkhausen criterion for sustained oscillation

Sine wave generators

LC - oscillators



LC oscillator is designed using an inverting amplifier and a feed back network which provides a feed back factor β which is equal to

$$\beta = -\frac{V_f}{A V_f}$$

Considering the equivalent circuit having the dependent voltage source and equivalent resistance R_o of the op amp. Analysis is carried out for calculating the operating frequency.

Applying Voltage divider rule to the equivalent circuit we can calculate 1/fb voltage V_f

$$V_f = \frac{z_1}{z_1 + z_2} V_o$$

Similarly the output voltage V_o can be calculated as $\frac{z}{z + R_o} (-AV_f)$ where z is $z = z_2 / (z_1 + z_3)$.

Taking the reciprocal of the overall gain of the system

$$\frac{1}{AV_f} = -\frac{1}{V_o} \frac{z}{z + R_o}$$

Substitute the value of z

$$\frac{1}{AV_f} = -\frac{1}{V_o} \frac{z_2 \times (z_1 + z_3)}{(z + R_o)(z_2 + z_1 + z_3)}$$

$$\frac{1}{AV_f} = -\frac{1}{V_o} \frac{z_1 z_2 + z_2^2}{z_2(z_1 + z_3) + R_o(z_1 + z_2 + z_3)}$$

$$\text{Solving for } \beta, \quad \beta = -\frac{V_f}{AV_f} = -\frac{z_1 z_2}{R_o(z_1 + z_2 + z_3) + z_2(z_1 + z_3)}$$

For an LC Quinable oscillator the 3 impedance z_1 , z_2 , z_3 are purely reactive, that is the real part will be equal to zero, it can be written as.

$$z_i = j x_i \quad i = 1, 2, 3$$

Substituting this to p equation β will become

$$\beta = \frac{x_1 x_2}{j R_o(x_1 + x_2 + x_3) + x_2(x_1 + x_3)}$$

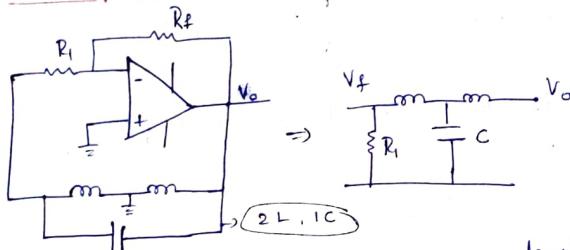
For β to be real the summation of real parts should be equal to zero, which is nothing but $x_1 + x_2 + x_3 = 0$

$$\beta = \frac{x_1}{x_1 + x_3} \quad \beta(w_0) = \frac{x_1}{x_1 + x_3}$$

making x_3 a negligible component so that $x_1 + x_3$ is almost equal to x_2 $\therefore (x_1 + x_3 = x_2)$

$$\beta(w_0) = \frac{x_1}{x_2}$$

Graetz oscillator



Graetz oscillators are sine wave generators which makes use of 2 inductance and one capacitance. In the feed back network the phase shift through the feed back network is 180° with an additional phase shift of 180° being provided by the int. inverting amplifier.

Considering the feedback network the reactance X_1 is

$$X_1 = j\omega L_1 \quad X_2 = j\omega L_2 \quad X_3 = -j/\omega C$$

The operating frequency can be found out using w_0 which is $w_0 = \sqrt{\frac{1}{C(C(L_1 + L_2))}}$

$$\beta(w_0) = \frac{L_1}{L_2}$$

Finally the operating frequency f_0 is given by $\frac{1}{2\pi\sqrt{CL}}$

where $[LT]$ is $L_1 + L_2$ or $L_T = L_1 + L_2 + 2M$ where M is Mutual inductance of coils L_1 and L_2

Colpitts oscillator

$2C, 1L$

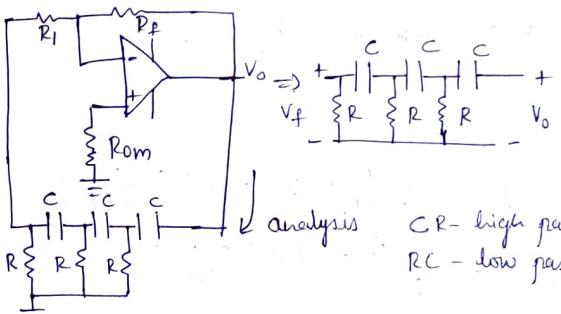
$$\frac{1}{2\pi\sqrt{C_T L}}$$

→ RC - phase shift oscillator.

For smooth and wave form ^{we} will go with RC.

→ basically for sine wave only.

→ only one complex form is present that is C.

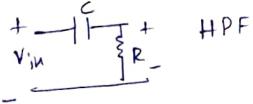


RC phase shift oscillators are used when an application involving low frequency signals are required; LC oscillators are not stable in low frequencies, due to which RC oscillators are used.

RC oscillator contains two stages feed back networks

which provides 180° phase shift and an electrical system consisting of an inverting amplifier providing another 180° phase shift. The equivalent circuit for feedback network is as shown above consisting of R and C components.

Taking a single stage RC network, This behaves as an high pass filter.



The Reactance of the network which contains a capacitive component which is given by $X_C = \frac{1}{\omega C}$

Calculating the gain of the network will get.

$$\frac{V_o}{V_i} = \frac{R}{(R - \frac{j}{\omega C})}$$

Dividing both num and denominator by R we get.

$$\frac{V_o}{V_i} = \frac{1}{(1 - \frac{j}{\omega CR})}$$

The phase angle is given by $\phi = 0 - \tan^{-1}(-\frac{1}{\omega CR})$.

$$\boxed{\phi = \tan^{-1}(\frac{X_C}{R})} \leftarrow \boxed{\phi = \tan^{-1}(\frac{1}{\omega CR})}$$

If X_C = small component then ϕ angle will be equal to zero. ($\phi = 0$)

If R is very small ($\phi = 90^\circ$)

→ Theoretically, by making $R=0$ we achieve 90° of phase shift in each feed back stage, practically, since $R=0$ sustained oscillation

will not be achieved, in order to overcome this third stage of DC component is added to feed back network each providing 90° of phase shift.



Considering the above 3 stage cascade network applying nodal analysis at point V_2

$$V_2 = (-j X_C I_3) + V_o$$

$$V_2 = \left(-j X_C \frac{V_o}{R} \right) + V_o \Rightarrow V_2 = \frac{V_o}{j \omega CR} + V_o$$

$$\boxed{V_2 = V_o \left[1 + \frac{1}{j \omega CR} \right]}$$

Applying KCL at load V_2

$$I_2 = \left(\frac{V_2}{R} \right) + I_3 \quad I_2 = \frac{V_o}{R} \left(1 + \frac{1}{j \omega CR} \right) + \frac{V_o}{R}$$

$$\boxed{I_2 = \frac{V_o}{R} \left[2 + \frac{1}{j \omega CR} \right]}$$

Similarly applying nodal analysis at node V_1

$$\begin{aligned} V_1 &= V_2 + \frac{I_2}{j \omega C} \\ &= V_o \left[1 + \frac{1}{j \omega CR} \right] + \frac{V_o}{R} \left[2 + \frac{1}{j \omega CR} \right] \cdot \frac{1}{j \omega C} \\ &= V_o \left[\left[\frac{1}{j \omega CR} + 1 \right] + \frac{1}{R} \left[\frac{2}{j \omega CR} - \frac{1}{\omega^2 C^2 R^2} \right] \right] \end{aligned}$$

$$V_1 = V_o \left[1 + \frac{3}{j \omega CR} - \frac{1}{\omega^2 C^2 R^2} \right]$$

Applying KCL at V_1 current $I_1 = \frac{V_1}{R} + I_2$

$$I_1 = \frac{V_o}{R} \left[1 + \frac{3}{j\omega CR} - \frac{1}{\omega^2 C^2 R^2} \right] + \frac{V_o}{R} \left[2 + \frac{1}{j\omega CR} \right]$$

$$I_1 = \frac{V_o}{R} \left[3 + \frac{4}{j\omega CR} - \frac{1}{\omega^2 C^2 R^2} \right]$$

Similarly applying nodal analysis for input node
V_{in} is given by $V_{in} = V_1 + \frac{I_1}{j\omega C}$

$$V_{in} = \frac{V_o}{j\omega CR} \left[3 + \frac{4}{j\omega CR} - \frac{1}{\omega^2 C^2 R^2} \right] + V_o \left[1 + \frac{3}{j\omega CR} - \frac{1}{\omega^2 C^2 R^2} \right]$$

$$V_{in} = \frac{V_o}{j\omega CR} \left[\frac{4}{j\omega CR} - \frac{7}{\omega^2 C^2 R^2} \right] \quad \boxed{V_{in} = V_o \left[1 + \frac{6}{j\omega CR} - \frac{5}{\omega^2 C^2 R^2} + \frac{1}{\omega^2 C^2 R^2} \right]}$$

The above equation contains both real part and imaginary part the freq of oscillation is found by equating imaginary part to zero.

$$\frac{6}{j\omega CR} - \frac{1}{\omega^2 C^2 R^2} = 0$$

$$\frac{6}{j\omega CR} = \frac{1}{\omega^2 C^2 R^2} \Rightarrow 6 = \frac{1}{\omega^2 C^2 R^2}$$

$$f = \frac{1}{2\pi RC\sqrt{6}}$$

$$\omega^2 = \frac{1}{\sqrt{6} CR}$$

In the input output relation substitute imaginary part as zero and ω as $\frac{1}{\sqrt{6} CR}$

$$V_{in} = V_o \left[1 + \frac{-5 \times 6 C^2 \times R^2}{\omega^2 \times R^2} \right] \quad \omega^2 = \frac{1}{6 C^2 R^2}$$

$$V_{in} = V_o \left[1 - 30 \right] = \frac{V_o}{V_{in}} = -\frac{1}{29}$$

The gain of the feed back network is $-\frac{1}{29}$ which indicates the phase reversal of 180° , the same reciprocal gain should be provided by the electrical system in order to make the overall gain of the oscillator to be equal to one \therefore The inverting amplifier should be designed with gain $\boxed{\frac{R_F}{R_1} = +29}$

$$\frac{V_o}{V_{in}} = -\frac{R_F}{R_1}$$

$$-\frac{1}{29}$$

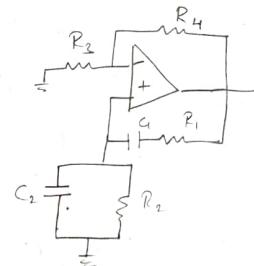
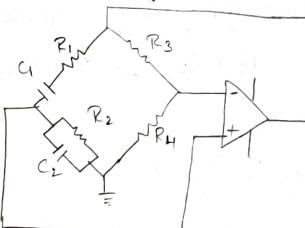
Design an RLC phase shift oscillator for a $f_o = 300$ Hz assuming $C = 0.1 \mu F$

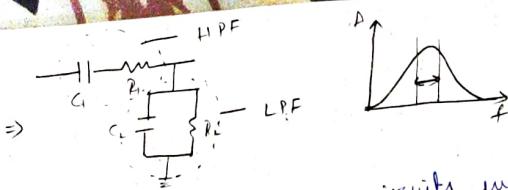
$$f_o = \frac{1}{2\pi RC\sqrt{6}}$$

$$300 = \frac{1}{2 \times 3.14 \times R \times 0.1 \times 10^{-6} \times \sqrt{6}}$$

$$R = 2.1669 k\Omega$$

wien bridge oscillator





- Wein bridge oscillator are circuits which generates frequency in the range of audio signals.
- The circuit consists of two parts: the Wein bridge feed back network and a non-inverting amplifier.
- Since the electrical system doesn't provide any phase shift, the entire 360° phase shift is provided by the feedback network.

Analysing the feedback network it can be visualized as a notch filter whose frequency response is as shown in the fig.

A notch filter allows narrow frequency signals which is made up of combination of high pass filter and a low pass filter. During the resonance frequency the phase angle of the feedback network will be ($\phi = 0$) and the gain is fixed $\left(\frac{V_o}{V_i} = \frac{1}{3}\right)$ or $\boxed{A = \frac{1}{3}}$

This value is called as the feedback factor. $\boxed{\frac{1}{3} = B}$

If $R_1 = R_2$ and $C_1 = C_2$ the Resonance frequency is given by $\boxed{f_r = \frac{1}{2\pi RC}}$ if $R_1 \neq R_2$ & $C_1 \neq C_2$ the Resonant

frequency is given by $\boxed{f_r = \frac{1}{2\pi \sqrt{R_1 R_2 C_1 C_2}}}$

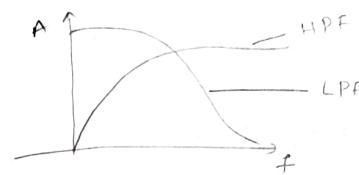
For sustained oscillations

$$\boxed{|AB| = 1}$$

which tells us the gain of the op amp $\boxed{|A|=3}$ since the opamp is config.

as non-inverting amplifiers $\boxed{A = 1 + \frac{R_4}{R_3}}$ which should be equal to 3

$$\frac{R_4}{R_3} = 2 \quad \therefore \boxed{R_4 = 2R_3}$$



Calculate the resonant frequency of a wein bridge oscillator for an $R_1 = R_2 = 10k\Omega$, $C_1 = C_2 = 0.1\mu F$

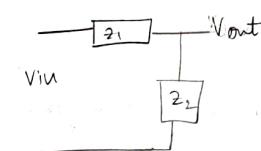
$$f_r = \frac{1}{2\pi \times 10k \times 0.1\mu F}$$

$$\boxed{f_r = \frac{1}{2\pi RC}}$$

$$f_r = 159.23 \text{ Hz}$$

Analysing of feed back

Analysing the feedback network and representing it in terms of impedances the output voltage of the feedback network shown in the above fig can be written as



$$V_{out} = \frac{Z_2}{Z_1 + Z_2} V_{in}$$

$$\boxed{\frac{V_{out}}{V_{in}} = \frac{Z_2}{Z_1 + Z_2}}$$

$$Z_2 = R_2 || C_2 = R_2 \parallel \frac{1}{j\omega C_2}$$

$$\boxed{Z_2 = \frac{R_2}{1 + j\omega C_2 R_2}}$$

$$\boxed{Z_1 = R_1 + \frac{1}{j\omega C_1}}$$

$$A = 1 + \frac{R_4}{R_3}$$

$$= 1 + \frac{\frac{R_2}{1 + j\omega C_2 R_2}}{R_1 + \frac{1}{j\omega C_1}} = \frac{R_1 + j\omega C_1 + \frac{R_2}{1 + j\omega C_2 R_2}}{R_1 + \frac{1}{j\omega C_1}}$$

$$\frac{V_o}{V_i} = \frac{j\omega R_2 C_1}{1 - \omega^2 R_1 R_2 C_1 C_2 + j\omega(R_1 C_1 + R_2 C_2 + R_2 C_1)}$$

At Resonant frequency since the phase shift is equal to zero 0° , the real part of the above equation will be equal to one.

$$\text{Equating Real part} = 1 \quad \omega^2 R_1 R_2 C_1 C_2 = 1$$

$$f_r = \frac{1}{2\pi\sqrt{R_1 R_2 C_1 C_2}}$$

Considering the imaginary part

$$\frac{V_o}{V_i} = \frac{R_2 C_1}{R_1 C_1 + R_2 C_2 + R_2 C_1} = \beta \quad \text{since } R_1 = R_2, C_1 = C_2$$

$$\frac{V_o}{V_i} = \frac{1}{3}$$

Since the sustained oscillations $A\beta = 1$ so $A = \frac{1}{\beta}$

$$A = \frac{R_1 C_1 + R_2 C_2 + R_2 C_1}{R_2 C_1}$$

$$A = \frac{R_1}{R_2} + \frac{C_2}{C_1} + 1 = \frac{R_1}{R_2} + \lambda$$

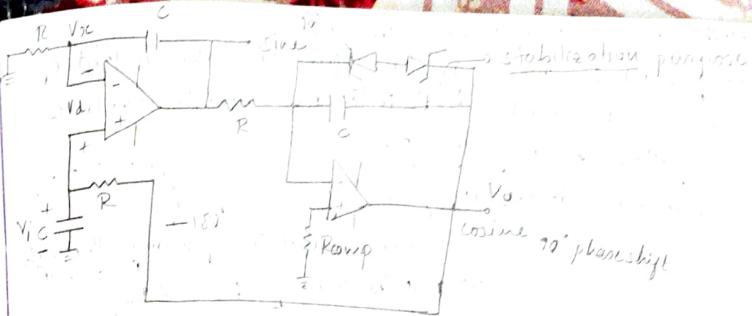
Since it is an non inverting amplifier the gain is given by

$$A = \frac{R_1}{R_2} + \frac{C_2}{C_1} = \frac{R_1}{R_2}$$

Assuming $R_1 = R_2 \quad C_1 = C_2$

$$\frac{R_1}{R_2} = 3$$

Quadrature Oscillations



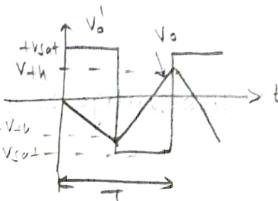
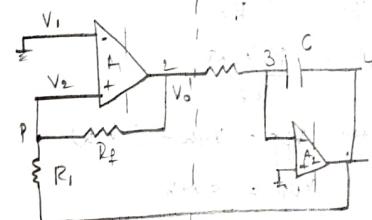
will get same frequency of oscillators with different phase shift.

Sine wave gives 90° phase shift, cosine gives 90° phase and RC gives -180° phase shift.

The overall circuit gives 360° or 0° phase shift.

Water level controller: Analogy, Digital, Mathematical

Triangular wave generator



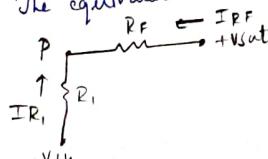
Square wave \rightarrow Integrator \rightarrow triangular wave that generates $V_t + V_h \rightarrow V_o$ voltage that capacitor can hold

triangular wave can be implemented by integrating square wave output generated by switch trigger, in the above circuit op-amp A1 operates as switch trigger and A2 is an integrator A1 compares V_i and V_o and produces square wave accordingly, the operation of overall circuit can be

split into two modes. $V_+ > 0$

During mode 1. V_+ is greater than zero, the output of A_1 is $+V_{sat}$ which fed into A_2 which produces a negative bearing ramp.

The equivalent circuit is given by

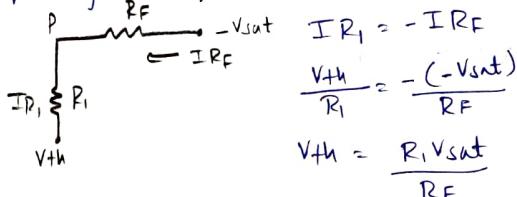


since current flowing through op amp is zero $[IR_1 = -IR_F]$

$$-\frac{V_{th}}{R_1} = -\frac{V_{sat}}{R_F}$$

$$-V_{th} = R_1 \frac{(-V_{sat})}{R_F}$$

During Mode 2 the $V_+ < 0$. A_1 will be at negative $-V_{sat}$ which makes the integrator to produce positive bearing ramp, the equivalent feed back network is given by



$$IR_1 = -IR_F$$

$$\frac{V_{th}}{R_1} = \frac{(-V_{sat})}{R_F}$$

$$V_{th} = R_1 \frac{V_{sat}}{R_F}$$

Peak to Peak Voltage is given by $V_{pp} = V_{th} - (-V_{th})$

$$V_{pp} = 2V_{th}$$

$$V_{pp} = 2 \frac{R_1}{R_F} V_{sat}$$

The period and frequency of the rectangular wave is given by considering the capacitor voltage operating in mode 2, that is input to the integrator is $-V_{sat}$. The instantaneous voltage of capacitor $V_C(t) = \frac{-1}{RC} \int [V_C(t) - V_{th}] dt$

$$V_C(t) = \frac{-1}{RC} \int (-V_{sat}) dt - V_{th}$$

$$V_C(t) = \frac{V_{sat} \cdot t}{RC} - V_{th}$$

$$\text{Considering the period } t = (\pi/2) \Rightarrow V_{th} = \frac{V_{sat} \cdot \pi/2 - V_{th}}{RC}$$

$$V_C(\pi/2) = \frac{V_{sat} \cdot \pi/2}{RC} - \frac{R_1 V_{sat}}{R_F}$$

$$V_{th} = -V_{sat} \left[\frac{\pi}{2RC} - \frac{R_1}{R_F} \right] \Rightarrow 2V_{th} = \frac{V_{sat} \cdot \pi/2}{RC}$$

$$2V_{th} = \frac{V_{sat} \cdot \pi/2}{RC}$$

$$2 \left(\frac{R_1 V_{sat}}{R_F} \right) = \frac{V_{sat} \cdot \pi/2}{RC}$$

$$(T = 1/f)$$

$$T = \frac{4 R C \cdot R_1}{R_F}$$

$$f_o = \frac{R_F}{4 R C R_1}$$

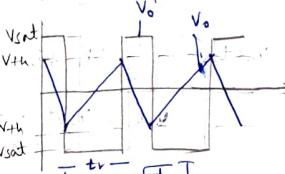
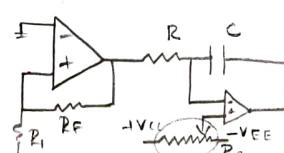
\rightarrow Calculate the time period for an triangular wave with feed back resistance of $10k\Omega$, V_{th} of 3 volts, $R=150k\Omega$, $V_{sat} = 11V$.

$$T = \frac{4 R C \cdot R_1}{R_F} = \frac{4 \times 150k \times 0.1 \mu F}{10k} \times \frac{V_{th} = \frac{R_1 V_{sat}}{R_F}}{2.727k} = 3 = \frac{R_1 \cdot 11}{10k} \\ T = 1.636 \text{ msec}$$

$$\frac{180k}{11} = R_1$$

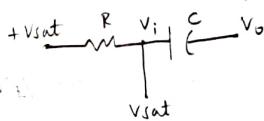
$$(2.727k = R_1)$$

Saw tooth wave generator



Saw tooth wave form is a modified triangular wave with unequal rise and fall time.
The triangular wave is converted into saw tooth by using variable voltage V_{ref} at the non-inverting terminal of op amp A_2 .

Mode 1 - During mode 1 ($V_+ > 0$) output of the op amp A_1 is at positive saturation which is input to the op amp A_2 , the equivalence circuit of the feedback network is given by



At the beginning the output voltage will be V_{th} . The inverting terminal will be at V_{ref} , since, due to the presence of virtual ground concept the inverting terminal will also have same V_{ref} voltage.

→ The initial instantaneous capacitive voltage $V_c(t=0)$

$$V_c(t=0) = V_i - V_o \quad V_i = V_{ref} \\ = V_{ref} - V_{th} \quad V_o = V_{th}$$

→ The instantaneous capacitive voltage $V_c(t) = \frac{1}{C} \int i_c(t) dt + V_c(t=0)$

$$V_{ref} - V_o(t) = \frac{1}{C} \int i_c dt + V_{ref} - V_{th}$$

$$V_{ref} - V_o(t) = \frac{1}{C} \int i_c dt + V_{ref} - V_{th} \quad i_c = \frac{V_{sat} - V_{ref}}{R}$$

$$V_o(t) = -\left[\frac{1}{C} \int i_c dt - V_{th} \right] \\ = V_{th} - \frac{V_{sat} - V_{ref} \cdot t}{RC}$$

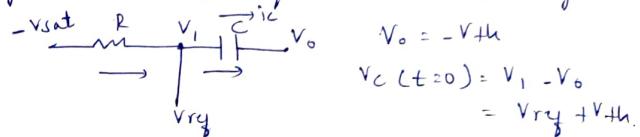
At end of this mode : $t = t_1$ Output voltage will be at

$$V_o(t=t_1) = -V_{th}$$

$$-V_{th} = V_{th} - \frac{V_{sat} - V_{ref} \cdot t_1}{RC}$$

$$t_1 = \frac{2RCV_{th}}{V_{sat} - V_{ref}}$$

During mode 2 : $V_+ < 0$ output of A_1 will be at $-V_{sat}$ (negative saturation) & equivalence circuits is given by



$$V_c(t) = \frac{1}{C} \int i_c(t) dt$$

$$t_2 = \frac{2RCV_{th}}{V_{sat} + V_{ref}}$$

$$T = t_1 + t_2 = \frac{4RCV_{th}V_{sat}}{V_{sat}^2 - V_{ref}^2}$$

$$f = \frac{1}{T} = \frac{V_{sat}^2 - V_{ref}^2}{4RCV_{th}V_{sat}}$$

$$K (\text{Duty cycle}) = \frac{t_1}{T} = \frac{\text{One period}}{\text{Total period}}$$

$$K = \frac{1}{2} \left[1 + \frac{V_{ref}}{V_{sat}} \right]$$