

Crash Introduction to markovchain R package

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Intro

- ▶ The markovchain package (Spedicato 2015) will be introduced.
- ▶ The package is intended to provide S4 classes to perform probabilistic and statistical analysis of Discrete Time Markov Chains (DTMC). See (Brémaud 1999) for a theoretical review of the mathematics underlying the DTMC models.
- ▶ The vignette will show: how to load the package and create a DTMC, how to manage a DTMC, how to perform basic probabilistic analysis, how to fit a DTMC.

- ▶ The package is on Cran since Summer 2013.
- ▶ It requires a recent version of R (≥ 3.0). Since version 0.2 parts of code have been moved to Rcpp (Eddelbuettel 2013).
- ▶ The package won a slot in Google Summer of Code 2015 for optimizing internals and expanding functionalities.

First moves into the markovchain package

Loading the package

- ▶ The package is loaded using

```
library(markovchain) #load the package
```

Creating a DTMC

- ▶ DTMC can be easily create following standard S4 classes syntax. The show method displays it.

```
tmA <- matrix(c(0,0.5,0.5,.5,0,.5,.5,.5,0),nrow = 3,  
              byrow = TRUE) #define the transition matrix  
dtmcA <- new("markovchain",transitionMatrix=tmA,  
            states=c("a","b","c"),  
            name="MarkovChain A") #create the DTMC  
dtmcA
```

```
## MarkovChain A  
## A 3 - dimensional discrete Markov Chain with following  
## a b c  
## The transition matrix (by rows) is defined as follow  
## a b c  
## a 0.0 0.5 0.5  
## b 0.5 0.0 0.5
```

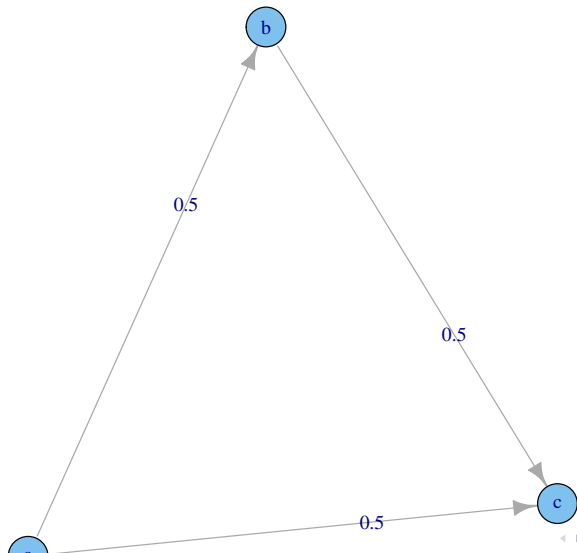
- ▶ Otherwise, it can also be created directly coercing a matrix.

```
dtmcA2<-as(tmA, "markovchain") #using coerce from matrix  
states(dtmcA2) #note default names assigned to states
```

```
## [1] "s1" "s2" "s3"
```


- It is also possible to display a DTMC, using igraph package (Csardi and Nepusz 2006) capabilities

```
plot(dtmcA)
```



Probabilistic analysis

The basic

- ▶ It is possible to access transition probabilities and to perform basic operations.
- ▶ Similarly, it is possible to access the conditional distribution of states, $Pr(X_{t+1}|X_t = s)$

```
dtmcA[2,3] #using [ method
```

```
## [1] 0.5
```

```
transitionProbability(dtmcA,  
                      "b","c") #using specific S4 method
```

```
## [1] 0.5
```

```
conditionalDistribution(dtmcA,"b")
```

```
##    a    b    c
```

```
## 0.5 0.0 0.5
```

- It is possible to simulate states distribution after n-steps

```
initialState<-c(0,1,0)
steps<-4
finalState<-initialState*dtmcA^steps #using power operator
finalState
```

```
##           a      b      c
## [1,] 0.3125 0.375 0.3125
```

- ▶ As well as steady states distribution

```
steadyStates(dtmcA) #S4 method
```

```
##              a              b              c  
## [1,] 0.3333333 0.3333333 0.3333333
```

- ▶ The summary method shows the proprieties of the DTCM

```
summary(mcMathematica)
```

```
## Mathematica Markov chain that is composed by:  
## Closed classes:  
## a b c d  
## Transient classes:  
## NONE  
## The Markov chain is irreducible  
## The absorbing states are: NONE
```

#Estimation and simulation

- ▶ The package permits to fit a DTMC estimating the transition matrix from a sequence of data.
- ▶ `createSequenceMatrix` returns a function showing previous vs actual states from the pairs in a given sequence.

```
r #using Alofi rainfall dataset data(rain)
mysequence<-rain$rain
createSequenceMatrix(mysequence)

## 0 1-5 6+ ## 0 362 126 60 ## 1-5 136 90 68 ## 6+ 50
79 124
```

- ▶ markovchainFit function allows to obtain the estimated transition matrix and the confidence levels (using elliptic MLE hypothesis).

```
myFit<-markovchainFit(data=mysequence,confidencelevel = .9,  
myFit
```

```
## $estimate  
## MLE Fit  
## A 3 - dimensional discrete Markov Chain with following  
## 0 1-5 6+  
## The transition matrix (by rows) is defined as follow  
##           0           1-5           6+  
## 0    0.6605839 0.2299270 0.1094891  
## 1-5  0.4625850 0.3061224 0.2312925  
## 6+   0.1976285 0.3122530 0.4901186  
##  
##  
## $confidenceInterval  
## $confidenceInterval$confidenceLevel
```


- ▶ See the vignettes for further fitting methods as well as for functionalities targeted on non - homogeneous Markov chains.

```
alofiMc<-myFit$estimate  
alofiMc
```

```
## MLE Fit  
## A 3 - dimensional discrete Markov Chain with following  
## 0 1-5 6+  
## The transition matrix (by rows) is defined as follow  
##           0           1-5           6+  
## 0    0.6605839 0.2299270 0.1094891  
## 1-5  0.4625850 0.3061224 0.2312925  
## 6+   0.1976285 0.3122530 0.4901186
```

Bibliography I

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