

# The Mandelbrot Set and its Variations

Jean Weight

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## INCOMPLETE DOCUMENT - WIP

### Abstract

The Mandelbrot set is a set of complex numbers, numbers that are the sum of real and imaginary numbers. Complex numbers are shown on the complex plane which is the equivalent of a 2-dimensional real number line.

## 1 Imaginary Numbers

Imaginary numbers are all the numbers who have negative real squares. Examples of imaginary numbers include  $\sqrt{-1}$ ,  $\sqrt{-25}$ ,  $-\sqrt{-1}$ ,  $\sqrt{-\sqrt{2}}$  and  $\sqrt{-x}$  for any positive reals  $x$ .

We define  $i$  to be the imaginary number such that  $i^2 = -1$ . Notice that no real  $i$  could satisfy this property.

All imaginary numbers can be written as a real number multiplied by  $i$ . For example  $\sqrt{-1} = i$  as  $i^2 = -1$ ,  $\sqrt{-25} = 5i$  as  $(5i)^2 = 25i^2 = -25$ ,  $-\sqrt{-1} = -i$ ,  $\sqrt{-\sqrt{2}} = \sqrt{\sqrt{2}}i = \sqrt[4]{2}$  and  $\sqrt{-x} = \sqrt{x}i$  for any positive reals  $x$ .