## LAPORAN TUGAS KECIL 3

Mata Kuliah IF2211 Strategi Algoritma

```
Puzzle move 28:

1 2 3 4
5 6 7 8
9 10 11 16
13 14 15 12

Puzzle move 29:
1 2 3 4
5 6 7 8
9 10 11 12
13 14 15 16

1691990 nodes were created in the algorithm The elapsed time is 37.1458 seconds
```

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# PROGRAM STUDI TEKNIK INFORMATIKA SEKOLAH TEKNIK ELEKTRO DAN INFORMATIKA INSTITUT TEKNOLOGI BANDUNG

2022

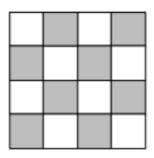
## **BABI**

## Algoritma Branch and Bound

Algoritma *Branch and Bound* adalah algoritma yang membagi suatu masalah menjadi masalah masalah yang lebih kecil (*Branch*) dengan sebuah batasan (*Bound*) untuk mencapai solusi optimal. Algoritma ini membentuk sebuah pohon ruang status, yang setiap simpul diberi nilai *cost*. Algoritma ini akan selalu mengolah simpul yang memiliki *cost* terendah agar mendapatkan solusi optimal.

Untuk mencari solusi optimal dari sebuah 15-puzzle akan digunaka algoritma Branch and Bound dengan langkah-langkah:

1. Sebelum masuk algoritma hitung  $\sum_{i=1}^{16} Kurang(i) + X$ , dengan Kurang(i) adalah banyaknya ubin bernomor j sedemikian sehingga j < i dan POSISI(j) > POSISI(i). POSISI(i) = posisi ubin bernomor i pada susunan yang diperiksa. Sedangkan X akan bernilai 1 jika tile kosong (di dalam program adalah tile bernomor 16) berada di tile yang diarsir, dan 0 jika tidak.



Jika  $\sum_{i=1}^{16} Kurang(i) + X$  bernilai ganjil, maka puzzle tidak bisa diselesaikan. Sedangkan jika bernilai genap, maka puzzle bisa diselesaikan. Jika tidak bisa diselesaikan, maka berhenti.

- 2. Masukkan simpul akar ke dalam antrian Q. Q adalah sebuah *priority queue*. Jika simpul akar adalah memiliki *current puzzle state* yang merupakan solusi *puzzle* (*goal node*), maka solusi telah ditemukan. Setiap simpul akan berisi *cost*, *level*, *address to parent node*, *current puzzle state*, dan *move* yang dilakukan. *cost* di node adalah jumlah tile yang tidak seperti di solusi *puzzle*, sehingga Q akan memiliki priority sesuai dengan *cost* + *level*.
- 3. Jika Q kosong, Stop.
- 4. Jika Q tidak kosong, pilih dari antrian Q simpul i yang mempunyai nilai 'cost' ĉ(i) paling kecil. Jika terdapat beberapa simpul i yang memenuhi, pilih satu.
- 5. Jika simpul i memiliki *current puzzle state* yang memiliki solusi *puzzle*, berarti solusi sudah ditemukan.
- 6. Jika simpul i bukan simpul solusi, maka bangkitkan semua anak-anaknya. Anaknya adalah semua gerakan yang mungkin dan bukan kebalikan dari gerakan sebelumnya.
- 7. Untuk setiap anak j dari simpul i, hitung ĉ(j), dan masukkan semua anak-anak tersebut ke dalam Q.
- 8. Kembali ke langkah 3.

## BAB 2

## Source Program

Program ini ditulis dalam bahasa Python. Terdapat 2 file, main.py dan BnB.py. File main.py akan menerima input dan mengirimkan informasi untuk diolah, sedangkan BnB.py berisi fungsi dan prosedur untuk algoritma *Branch and Bound* tersebut.

#### File main.py

```
import BnB
import os.path
loop = True
while (loop):
    puzzle = []
   kurang = 1
    option = input("Read File or Randomized?\n(1) Read File\n(2)
Randomized\nInput: ")
   print("")
    while (option != "1" and option != "2"):
        option = input("Input error, Read File or Randomized?\n(1) Read
File\n(2) Randomized\nInput: ")
        print("")
    if (int(option) == 1):
        puzzle = BnB.readFile()
        kurang = BnB.printPuzzleKurang(puzzle)
    elif (int(option) == 2):
        repeat = True
        puzzle = BnB.randomPuzzle()
        kurang = BnB.printPuzzleKurang(puzzle)
        while (repeat):
            option2 = input("Is this okay? (Y/N): ")
            if (option2 == "Y" or option2 == "y"):
                repeat = False
            elif (option2 == "N" or option2 == "n"):
                puzzle = BnB.randomPuzzle()
                kurang = BnB.printPuzzleKurang(puzzle)
            else:
                print("\nInput error")
        print("")
    if (kurang%2 == 0):
```

```
print("Loading...\n")
    BnB.solve(puzzle)
else:
    print("\nPuzzle cannot be solved\n")

option3 = input("Want to do another? (Y/N): ")
    repeat = True
while (repeat):
    if (option3 == "Y" or option3 == "y"):
        repeat = False
    elif (option3 == "N" or option3 == "n"):
        loop = False
        repeat = False
    else:
        option3 = input("Input error. Want to do another? (Y/N): ")
print("")
```

## File BnB.py

```
import os
import random
import time
from heapq import heappush, heappop
from tokenize import Token
# Class for priority queue
class PQueue:
   # Initiate a Priority Queue
    def __init__(self):
        self.heap = []
   # Push into the queue
    def push(self, k):
        heappush(self.heap, k)
    # Pop from the queue
    def pop(self):
        return heappop(self.heap)
    # Check if the queue is empty
    def empty(self):
        if not self.heap:
            return True
        else:
           return False
```

```
# Class for nodes
class Node:
   # Initiate a node
    def __init__(self, cost, level, parent, puzzle, move):
        self.cost = cost
        self.level = level
        self.parent = parent
        self.puzzle = puzzle
        self.move = move
    def __lt__(self, nxt):
        return self.cost + self.level < nxt.cost + nxt.level</pre>
# Function for reading files
def readFile():
    puzzle = []
    puzzleRow = []
    filename = input("Please input filename: ")
    path = os.path.join((os.path.abspath(os.path.join(os.getcwd(),
os.pardir))), "test", filename)
    while (not os.path.exists(path)):
        filename = input("\nFilename not found. Please reinput filename: ")
        path = os.path.join((os.path.abspath(os.path.join(os.getcwd(),
os.pardir))), "test", filename)
    file = open(path).read()
    array = file.split('\n')
    for i in range (len(array)):
        elements = array[i].split(" ")
        puzzleRow = []
        for j in range (len(elements)):
            puzzleRow.append(int(elements[j]))
        puzzle.append(puzzleRow)
    return (puzzle)
# Function to randomized a puzzle
def randomPuzzle():
   puzzle = []
   puzzleRow = []
    check = [False for i in range (16)]
    for i in range (4):
        puzzleRow = []
```

```
for j in range(4):
            n = random.randint(1,16)
            while (check[n-1]):
                 n = random.randint(1,16)
            check[n-1] = True
            puzzleRow.append(n)
        puzzle.append(puzzleRow)
    return (puzzle)
# Function that counts KURANG(i) + X
def kurang(puzzle) :
    kurang = 0
    before = 0
    print("KURANG(i):")
    for e in range(1, len(puzzle) * len(puzzle[0]) + 1):
        found = False
        grid = False
        ii = 0
        jj = 0
        while (ii < len(puzzle) and not found):</pre>
            jj=0
            while (jj < len(puzzle[0]) and not found):</pre>
                if (puzzle[ii][jj] == e):
                    found = True
                else:
                    jj += 1
            if (not found):
                ii += 1
        for i in range (len(puzzle)):
            for j in range (len(puzzle[i])):
                if (puzzle[i][j] < e and ((i > ii) or (i == ii and <math>j > jj))):
                     kurang += 1
                if (e == 16 and puzzle[i][j] == 16 and ((i\%2 == 1 and j\%2 ==
0) or (i\%2 == 0 \text{ and } j\%2 == 1))):
                     kurang += 1
                    grid = True
        if (grid):
            print("Tile " + str(e) + ": " + str(kurang - before - 1))
            before = kurang
        else:
            print("Tile " + str(e) + ": " + str(kurang - before))
            before = kurang
    return kurang
# Function that prints out the puzzle and KURANG(i) + X
def printPuzzleKurang(puzzle):
```

```
print("Puzzle:")
    x = '\n'.join([''.join(['{:4}'.format(element) for element in row]) for
row in puzzle])
    print(x)
    print("")
    nkurang = kurang(puzzle)
    print("\nKURANG(i) + X =", nkurang,"\n")
    return nkurang
# Function that counts how many tiles are not in the correct places
def countWrong(puzzle):
    cost = 0
    for i in range (len(puzzle)):
        for j in range (len(puzzle[0])):
            if (puzzle[i][j] != (i*len(puzzle[0]) + j + 1)):
                cost += 1
    return (cost)
# Function that search the location of the empty tile (16 tile)
def search16(puzzle):
   i = 0
    i = 0
    found = False
    while (i < len(puzzle) and not found):</pre>
        while (j < len(puzzle[0]) and not found):</pre>
            if (puzzle[i][j] == 16):
                found = True
            else:
                j += 1
        if (not found):
            i += 1
    return ([i, j])
# Function that switch a tile with an empty tile
def switchEmpty(puzzle, i, j):
    empty = search16(puzzle)
    tileSwitched = [empty[0] + i, empty[1] + j]
    temp = puzzle[empty[0]][empty[1]]
    puzzle[empty[0]][empty[1]] = puzzle[tileSwitched[0]][tileSwitched[1]]
    puzzle[tileSwitched[0]][tileSwitched[1]] = temp
```

```
return (puzzle)
# Function that prints out the puzzle movements from start to finish
def printFinal(node):
    i = 0
    if (node.parent != None):
        i = printFinal(node.parent)
        i += 1
    print("Puzzle move " + str(i) + ": " )
    x = '\n'.join([''.join(['{:4}'.format(element) for element in row]) for
row in node.puzzle])
    print(x, "\n")
    return (i)
# Function that checks if a move is the reverse of the move before that
def notReverse(i, j):
   return (not((i == 0 and j == 2) or (i == 2 and j == 0) or (i == 1 and j == 0
3) or (i == 3 \text{ and } j == 1)))
# Procedure that solves the puzzle with Branch and Bound
def solve(puzzle):
    startTimer = time.perf_counter()
    finalPuzzle = [[1, 2, 3, 4], [5, 6, 7, 8], [9, 10, 11, 12], [13, 14, 15,
16]]
    rowMove = [ 1, 0, -1, 0 ] # Empty slot move 0 = down, 1 = left, 2 = up, 3
= right
    colMove = [ 0, -1, 0, 1 ]
    pqueue = PQueue()
    totalNodes = 1
    # Make root node
    root = Node(countWrong(puzzle), 0, None, puzzle, None)
    pqueue.push(root)
    # Gets node with the lowest cost
   while (not pqueue.empty()):
        pnode = pqueue.pop()
        current = pnode.puzzle
        if (current == finalPuzzle):
            break
        else:
            # Move the empty tile to 4 different ways
            for i in range (4):
                empty = search16(current)
```

```
# Check if move is valid
                if (empty[0] + rowMove[i] >= 0 and empty[0] + rowMove[i] <</pre>
len(current) and empty[1] + colMove[i] >= 0 and empty[1] + colMove[i] <</pre>
len(current[0]) and notReverse(i, pnode.move)):
                    # Make the moved puzzle
                    switchedPuzzle = [[1, 2, 3, 4], [5, 6, 7, 8], [9, 10, 11,
12], [13, 14, 15, 16]]
                    for ii in range (len(current)):
                        for jj in range (len(current[0])):
                            switchedPuzzle[ii][jj] = current[ii][jj]
                    switchedPuzzle = switchEmpty(switchedPuzzle, rowMove[i],
colMove[i])
                    # Make the node and push it to priority queue
                    child = Node(countWrong(switchedPuzzle), pnode.level + 1,
pnode, switchedPuzzle, i)
                    pqueue.push(child)
                    totalNodes += 1
    endTimer = time.perf_counter()
    printFinal(pnode)
    print(totalNodes, "nodes were created in the algorithm")
    print(f"The elapsed time is {endTimer - startTimer:0.4f} seconds")
    print("")
```

## BAB 3

## Screenshot input dan output

#### 1. failed1.txt

Read File or Randomized?

input:

```
    Read File
    Randomized

Input: 1
Please input filename: failed1.txt
output:
Puzzle:
    3
       6
           12 13
    1 11
           14 16
    9 8
            7 10
    2 15
            4
               5
KURANG(i):
Tile 1: 0
 Tile 2: 0
 Tile 3: 2
 Tile 4: 0
 Tile 5: 0
 Tile 6: 4
 Tile 7: 3
 Tile 8: 4
 Tile 9: 5
 Tile 10: 3
 Tile 11: 7
 Tile 12: 9
Tile 13: 9
 Tile 14: 7
 Tile 15: 2
 Tile 16: 8
KURANG(i) + X = 63
 Puzzle cannot be solved
Want to do another? (Y/N):
```

## 2. failed2.txt

## input:

```
Read File or Randomized?
(1) Read File
(2) Randomized
Input: 1
Please input filename: failed2.txt
```

```
Puzzle:
  12
      5
          1
  16
       2
           6 11
       7
  10
          4
              15
  14
      8 13
              9
KURANG(i):
Tile 1: 0
Tile 2: 0
Tile 3: 1
Tile 4: 0
Tile 5: 4
Tile 6: 1
Tile 7: 1
Tile 8: 0
Tile 9: 0
Tile 10: 4
Tile 11: 5
Tile 12: 11
Tile 13: 1
Tile 14: 3
Tile 15: 4
Tile 16: 11
KURANG(i) + X = 47
Puzzle cannot be solved
Want to do another? (Y/N):
```

#### 3. success1.txt

#### input:

```
Read File or Randomized?
(1) Read File
(2) Randomized
Input: 1
Please input filename: success1.txt
```

```
Puzzle:
  16
          4
              8
  1
      5
          2
              6
   7 10 15 11
  9 13 14 12
KURANG(i):
Tile 1: 0
Tile 2: 0
Tile 3: 2
Tile 4: 2
Tile 5: 1
Tile 6: 0
Tile 7: 0
Tile 8: 5
Tile 9: 0
Tile 10: 1
Tile 11: 1
Tile 12: 0
Tile 13: 1
Tile 14: 1
Tile 15: 5
Tile 16: 15
KURANG(i) + X = 34
Loading...
```

## Puzzle move 0: 3 4 8 16 2 6 1 7 10 15 11 9 13 14 12 Puzzle move 1: 1 3 4 8 2 6 16 7 10 15 11 9 13 14 12 Puzzle move 2: 1 3 4 8 5 16 2 6 7 10 15 11 9 13 14 12 Puzzle move 3: 1 3 4 8 5 10 2 6 7 16 15 11 9 13 14 12 Puzzle move 4: 1 3 4 8 5 10 2 6 16 7 15 11 9 13 14 12 Puzzle move 5: 1 3 4 8 5 10 2 6 9 7 15 11 16 13 14 12 Puzzle move 6: 1 3 4 8 5 10 2 6 9 7 15 11 13 16 14 12

## Puzzle move 7: 1 3 4 8 5 10 2 6 9 7 15 11 13 14 16 12 Puzzle move 8: 1 3 4 8 5 10 2 6 9 7 16 11 13 14 15 12 Puzzle move 9: 1 3 4 8 5 10 2 6 9 16 7 11 13 14 15 12 Puzzle move 10: 1 3 4 8 5 16 2 6 9 10 7 11 13 14 15 12 Puzzle move 11: 1 3 4 8 5 2 16 6 9 10 7 11 13 14 15 12 Puzzle move 12: 1 3 4 8 5 2 6 16 9 10 7 11 13 14 15 12 Puzzle move 13: 1 3 4 16 5 2 6 8 9 10 7 11 13 14 15 12

```
Puzzle move 14:
    3 16 4
  1
  5
     2
       6
            8
  9 10
       7 11
 13 14 15
          12
Puzzle move 15:
  1 16
        3 4
  5 2
  9 10
        7 11
 13 14 15 12
Puzzle move 16:
     2
        3 4
  1
  5 16
       6
           8
  9 10
       7 11
 13 14 15
          12
Puzzle move 17:
  1
     2 3 4
  5 6 16
            8
       7 11
  9 10
 13 14 15
           12
Puzzle move 18:
  1
     2
        3 4
  5 6
        7 8
  9 10 16 11
 13 14 15
          12
Puzzle move 19:
  1
     2 3 4
  5
    6
        7
            8
  9 10 11 16
 13 14 15
          12
Puzzle move 20:
  1 2
       3 4
  5
     6
        7
          8
  9 10 11 12
 13 14 15
1776 nodes were created in the algorithm
The elapsed time is 0.0264 seconds
```

Want to do another? (Y/N):

## 4. success2.txt

## input:

```
Read File or Randomized?

(1) Read File
(2) Randomized
Input: 1

Please input filename: success2.txt
```

```
Puzzle:
  1 16
        2 3
  5 9 8 11
  6 13 4 10
 14 15 12
             7
KURANG(i):
Tile 1: 0
Tile 2: 0
Tile 3: 0
Tile 4: 0
Tile 5: 1
Tile 6: 1
Tile 7: 0
Tile 8: 3
Tile 9: 4
Tile 10: 1
Tile 11: 4
Tile 12: 1
Tile 13: 4
Tile 14: 2
Tile 15: 2
Tile 16: 14
KURANG(i) + X = 38
Loading...
```

```
Puzzle move 0:
 1 16
      2 3
 5 9
       8 11
 6 13 4 10
14 15 12 7
Puzzle move 1:
 16 1 2 3
 5 9
      8 11
 6 13
      4 10
14 15 12 7
Puzzle move 2:
 5 1 2 3
16 9
      8 11
 6 13
      4 10
14 15 12 7
Puzzle move 3:
 5 1 2 3
 6 9
      8 11
16 13
      4 10
 14 15 12 7
Puzzle move 4:
 5 1 2 3
 6 9
      8 11
13 16
       4 10
 14 15 12 7
Puzzle move 5:
 5 1 2 3
 6 16
      8 11
 13 9
       4 10
 14 15 12 7
Puzzle move 6:
 5
    1
       2 3
      16 11
 6
   8
   9
      4 10
 13
 14 15 12 7
```

```
Puzzle move 7:
  5
     1 2 3
 6
    8
       4 11
 13 9 16 10
 14 15 12 7
Puzzle move 8:
 5
    1 2 3
 6
   8
       4 11
 13 9 10 16
 14 15
       12 7
Puzzle move 9:
 5
    1 2 3
 6
   8
       4 11
 13 9 10 7
 14 15
       12 16
Puzzle move 10:
 5
    1 2 3
 6
   8
       4 11
 13 9 10 7
 14 15
       16 12
Puzzle move 11:
 5
    1 2 3
       4 11
 6
    8
 13 9 10 7
 14 16
       15 12
Puzzle move 12:
 5
    1 2 3
 6
    8
       4 11
 13 9 10 7
 16 14
       15 12
Puzzle move 13:
 5
    1 2 3
 6
    8
       4 11
 16 9 10 7
 13 14 15 12
```

## Puzzle move 14: 5 1 2 3 6 8 4 11 9 16 10 7 13 14 15 12 Puzzle move 15: 5 1 2 3 6 8 4 11 9 10 16 7 13 14 15 12 Puzzle move 16: 5 1 2 3 6 8 4 11 9 10 7 16 13 14 15 12 Puzzle move 17: 5 1 2 3 6 8 4 16 9 10 7 11 13 14 15 12 Puzzle move 18: 5 1 2 3 6 8 16 4 9 10 7 11 13 14 15 12 Puzzle move 19: 5 1 2 3 6 16 8 4 7 11 9 10 13 14 15 12 Puzzle move 20: 5 1 2 3 16 6 8 4 7 11 9 10 13 14 15 12

```
Puzzle move 21:
 16 1 2 3
 5 6
       8 4
 9 10 7 11
 13 14 15 12
Puzzle move 22:
 1 16
       2 3
 5 6
       8 4
 9 10 7 11
 13 14 15 12
Puzzle move 23:
 1 2 16 3
 5 6 8
          4
 9 10 7 11
 13 14 15 12
Puzzle move 24:
 1 2 3 16
 5 6
       8 4
 9 10 7 11
 13 14 15 12
Puzzle move 25:
 1 2 3 4
 5 6
       8 16
 9 10 7 11
 13 14 15 12
Puzzle move 26:
 1 2 3 4
  5 6 16
          8
       7 11
 9 10
 13 14 15 12
Puzzle move 27:
  1 2
       3 4
  5 6
       7 8
  9 10 16 11
 13 14 15 12
```

```
Puzzle move 28:

1 2 3 4
5 6 7 8
9 10 11 16
13 14 15 12

Puzzle move 29:
1 2 3 4
5 6 7 8
9 10 11 12
13 14 15 16

1691990 nodes were created in the algorithm The elapsed time is 37.3939 seconds

Want to do another? (Y/N):
```

#### 5. success3.txt

input:

```
Read File or Randomized?
(1) Read File
(2) Randomized
Input: 1
Please input filename: success3.txt
```

```
Puzzle:
 13 9
              1
 14 6 7
 15 10 11
 16 12 8
KURANG(i):
Tile 1: 0
Tile 2: 0
Tile 3: 0
Tile 4: 0
Tile 5: 4
Tile 6: 3
Tile 7: 3
Tile 8: 1
Tile 9: 8
Tile 10: 3
Tile 11: 3
Tile 12: 2
Tile 13: 12
Tile 14: 9
Tile 15: 6
Tile 16: 3
KURANG(i) + X = 58
Loading...
```

```
Puzzle move 0:
    9 5 1
 13
 14
    6
       7
           2
 15 10 11
           3
 16 12
        8
           4
Puzzle move 1:
 13 9 5
          1
 14 6
        7
           2
           3
 16 10 11
 15 12
        8
           4
Puzzle move 2:
 13 9 5 1
 16
    6
       7
           2
           3
 14 10 11
 15 12
       8
           4
Puzzle move 3:
 16 9 5 1
 13
    6
       7
           2
 14 10 11
 15 12
       8
           4
Puzzle move 4:
 9 16
       5 1
 13 6
       7
           2
 14 10 11
 15 12
       8
           4
Puzzle move 5:
 9 5 16
          1
 13
    6
       7
           2
 14 10 11
           3
 15 12 8
           4
```

```
Puzzle move 6:
 9 5 1 16
 13 6
       7
           2
 14 10
       11
           3
 15 12
       8
           4
Puzzle move 7:
 9 5
       1 2
 13 6
       7 16
 14 10
       11
           3
15 12
       8
           4
Puzzle move 8:
 9 5 1 2
 13 6 7
           3
 14 10 11 16
15 12
       8 4
Puzzle move 9:
 9 5
       1 2
 13 6
       7
           3
 14 10 11
           4
 15 12 8 16
Puzzle move 10:
 9 5
       1
           2
 13 6
       7
           3
 14 10 11
           4
 15 12 16
           8
Puzzle move 11:
 9 5
       1
           2
 13 6
       7
           3
 14 10 11
           4
 15 16 12
           8
Puzzle move 12:
 9
    5
       1
           2
 13 6
       7
           3
 14 10 11
           4
 16 15 12
           8
```

```
Puzzle move 13:
 9 5 1 2
    6
        7
 13
 16 10 11
           4
 14 15 12
            8
Puzzle move 14:
 9 5 1
           2
 16
    6
       7
           3
 13 10 11
           4
14 15 12
            8
Puzzle move 15:
 16 5 1
           2
 9
        7
    6
           3
 13 10 11
           4
14 15 12
            8
Puzzle move 16:
 5 16
       1
 9 6
       7
           3
 13 10 11
           4
 14 15 12
Puzzle move 17:
 5 1 16
    6
 9
       7
           3
 13 10 11
           4
 14 15 12
Puzzle move 18:
 5 1
       2 16
 9
       7
    6
           3
 13 10 11
           4
 14 15 12
Puzzle move 19:
  5 1
        2
           3
  9
    6
       7
          16
 13 10 11
           4
 14 15 12
           8
```

## Puzzle move 20:

5 1 2 3

9 6 7 4

13 10 11 16

14 15 12 8

## Puzzle move 21:

5 1 2 3

9 6 7 4

13 10 11 8

14 15 12 16

## Puzzle move 22:

5 1 2 3

9 6 7 4

13 10 11 8

14 15 16 12

## Puzzle move 23:

5 1 2 3

9 6 7 4

13 10 11 8

14 16 15 12

## Puzzle move 24:

5 1 2 3

9 6 7 4

13 10 11 8

16 14 15 12

## Puzzle move 25:

5 1 2 3

9 6 7 4

16 10 11 8

13 14 15 12

## Puzzle move 26:

5 1 2 3

16 6 7 4

9 10 11 8

13 14 15 12

```
Puzzle move 27:
 16
     1
         2
            3
         7
     6
  5
             4
  9 10
        11
             8
 13 14
        15 12
Puzzle move 28:
  1 16
        2
  5
     6
         7
             4
  9 10 11
             8
 13 14 15 12
Puzzle move 29:
  1
     2 16
            3
  5
        7
     6
             4
  9 10 11
             8
 13 14 15 12
Puzzle move 30:
     2
        3 16
  1
  5
     6
         7
            4
  9 10
       11
             8
 13 14 15 12
Puzzle move 31:
     2
  1
         3
  5
     6
         7
            16
  9 10
       11
            8
 13 14 15
           12
Puzzle move 32:
  1
     2
         3
            4
  5
     6
         7
             8
  9 10
        11
            16
 13 14 15
           12
Puzzle move 33:
  1
     2
        3
           4
  5
     6
             8
  9 10 11 12
 13 14 15
            16
```

7224480 nodes were created in the algorithm The elapsed time is 158.3336 seconds

Want to do another? (Y/N): n

## BAB 4

# GitHub Program dan Berkas Teks

Untuk program dan berkas teks saya, bisa dilihat di link berikut:

https://github.com/Enderageous/Tucil3\_13520012

# Lampiran

Poin	Ya	Tidak
1. Program berhasil		
dikompilasi	V	
2. Program berhasil running	$\sqrt{}$	
3. Program dapat menerima		
input dan menuliskan output	V	
4. Luaran sudah benar untuk		
semua data uji	V	
5. Bonus dibuat		$\sqrt{}$