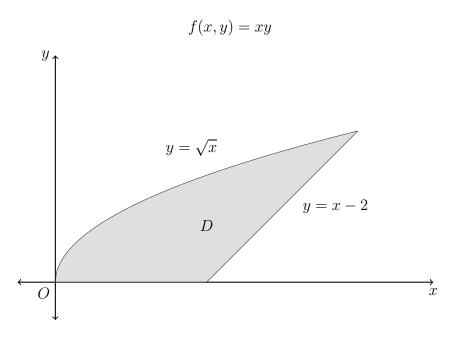
15.2.9. (pg. 1059)

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(a) Express the double integral $\iint_D f(x,y) dA$ as an iterated integral for the given function f and region D.

$$y = \sqrt{x}$$

$$x = y^2$$

$$y = x - 2$$

$$x = y + 2$$

$$y^{2} = y + 2$$

$$0 = y^{2} - y - 2$$

$$= (y - 2)(y + 1)$$

$$y = -1, 2$$

$$\iint\limits_D f(x,y) \, \mathrm{d}A = \int_0^2 \int_{y^2}^{y+2} xy \, \mathrm{d}x \, \mathrm{d}y$$

(b) Evaluate the iterated integral.

$$\int_{0}^{2} \int_{y^{2}}^{y+2} xy \, dx \, dy = \int_{0}^{2} \left[\frac{x^{2}y}{2} \right]_{y^{2}}^{y+2} \, dy$$

$$= \int_{0}^{2} \left[\frac{(y+2)^{2}y}{2} - \left(\frac{y^{5}}{2} \right) \right] \, dy$$

$$= \int_{0}^{2} \left[\frac{y^{3} + 4y^{2} + 4y - y^{5}}{2} \right] \, dy$$

$$= \left[-\frac{y^{6}}{12} + \frac{y^{4}}{8} + \frac{2y^{3}}{3} + y^{2} \right]_{0}^{2}$$

$$= -\frac{64}{12} + \frac{16}{8} + \frac{16}{3} + 4$$

$$= 6$$

I asdf

II

III

IV