

# Ex1 Separately excited dc motor (1)

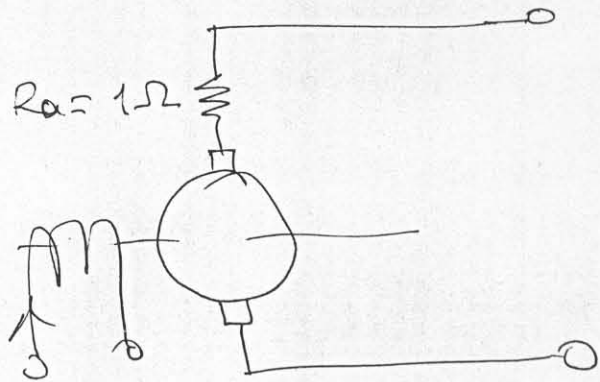
$$I_a(\text{rated}) = 100 \text{ A}$$

$$R_a = 1 \Omega$$

$$E_a \text{ vs } I_f \text{ at } 1000 \text{ RPM}$$

$$E_a = 200 I_f \quad I_f \leq 1.0 \text{ A}$$

$$E_a = 100 I_f + 100 \quad I_f > 1.0 \text{ A}$$



a) Obtain its magnetization ch at 500 rpm

$$\text{Since } E_a = K_a \phi_d \omega_r$$

$$\text{then } \left. \frac{E_{a1}}{E_{a2}} \right|_{\substack{I_f - \text{const} \\ \phi_d - \text{const}}} = \left. \frac{\omega_{r1}}{\omega_{r2}} \right|_{\substack{I_f - \text{const} \\ \phi_d - \text{const}}} = \frac{n_1}{n_2}$$

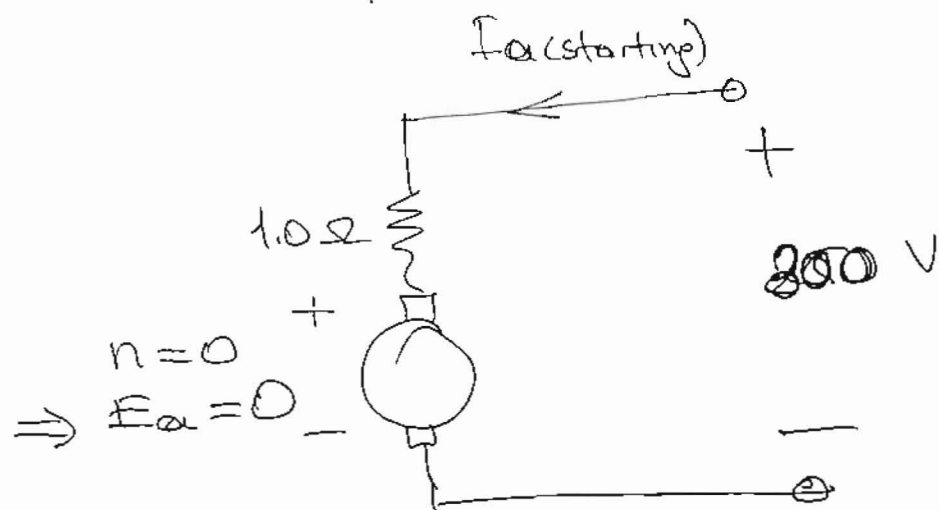
$$\Rightarrow E_{a2} = \frac{n_2}{n_1} E_{a1} = \frac{500}{1000} E_{a1} = 0.5 E_{a1} //$$

$$\text{New Ch: } E_a = 100 I_f \quad I_f \leq 1.0 \text{ A}$$

$$E_a = 50 I_f + 50 \quad I_f > 1.0 \text{ A} //$$

(2)

b) If it is started by direct on starting technique compute initial value of starting current by assuming that  $V_t(\text{rated}) = 300 \text{ V}$  and  $I_f = 1.0 \text{ A}$ .



$$V_t = E_a + I_a R_a \quad (\text{for Motoring Operation})$$

$$300 = 0 + I_a \times 1.0$$

$$\Rightarrow I_a = 300 \text{ A} \gg I_{a(\text{rated})} //$$

Compute  $I_a$  when the speed reaches 500 RPM.

at 500 rpm  $E_a$  is 100 V.

$$300 = 100 + I_a \times 1.0$$

$$I_a = \frac{300 - 100}{1.0} = 200 \text{ A} //$$

Compute  $I_a$  at 1000 rpm.  
at 1000 rpm  $E_a$  is 200 V

$$300 = 200 + I_a \times 1.0$$

$$I_a = \frac{300 - 200}{1.0} = 100 \text{ A} = I_{a(\text{rated})} //$$

(3)

c) Compute  $T_e$  at  $n=1000$  rpm and  $I_f=1.0$  A  
 at 1000 rpm :  $E_a = 200$  V  
 and  $I_f=1.0$  A

$$E_a = K_a \phi_d \omega_r$$

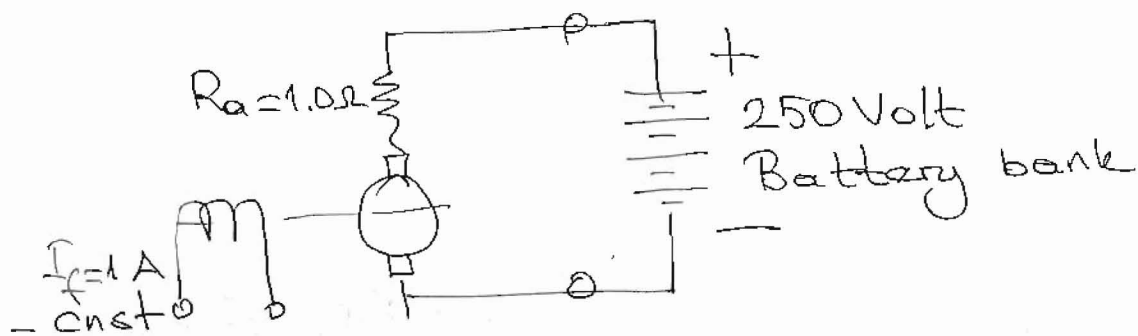
$$200 = K_a \phi_d \times 1000 \frac{2\pi}{60}$$

$$\therefore K_a \phi_d = 1.91$$

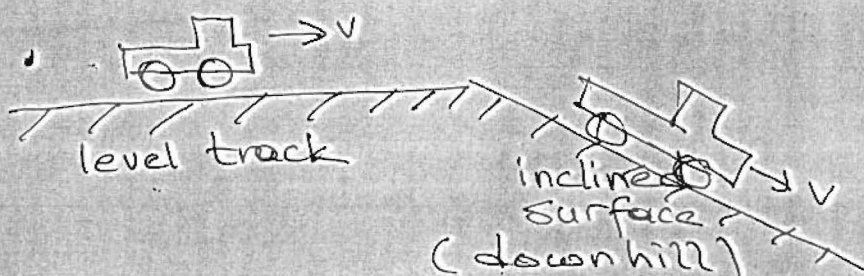
$$T_e = K_a \phi_d I_a$$

$$T_e = 1.91 \times 100 = 191 \text{ Nm} //$$

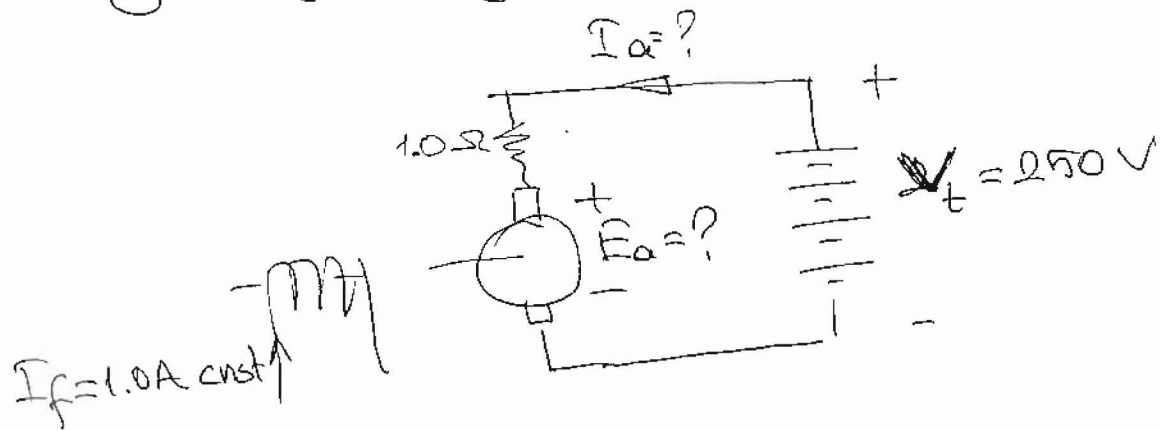
d) Let us drive an electric car  
 by using the separately excited  
 dc motor given above.



Consider the following track  
 on the ~~road~~ road.



Compute the maximum speed of the motor on the level track by neglecting friction and windage losses. (4)



Since  $T_L$  owing to gravitational force on a level track is zero and  $T_{few} = 0$  then  $T_e = T_L + T_{few} = 0 \text{ Nm}$

$$T_e = k_a \phi_d I_a \Rightarrow I_a = 0 //$$

$$V_t = E_a + I_a R_a$$

$$250 = E_a + 0$$

$$\therefore E_a = 250 \text{ V} //$$

at  $I_f = 1.0 \text{ A}$   $E_{a2} = \frac{N_2}{1000 \text{ rpm}} \times 200 \text{ volts}$

$$250 = \frac{N_2 \times 0.2}{1000}$$

$$\Rightarrow N_2 = 1250 \text{ rpm} //$$

max motor speed

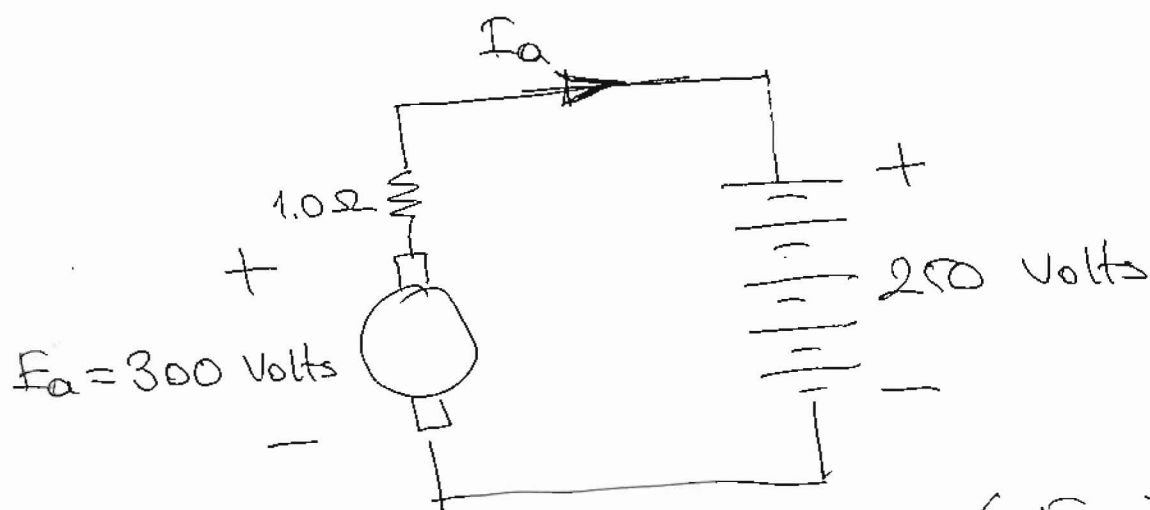


(5)

Assume now that the electric vehicle moves downhill at a constant speed (constant motor speed is 1500 rpm). Identify the operation mode of the dc machine. Compute electromechanical torque and <sup>electromechanical</sup> power. ~~converted~~.

At 1500 rpm and  $I_f = 10 \text{ A}$

$$E_a = \frac{1500}{1000} \times 200 = 300 \text{ Volts}$$



Armature current reverses ( $E_a > V_t$ )

$$I_a = \frac{V_t - E_a}{R_a} = \frac{250 - 300}{1.0} = -50 \text{ A} //$$

Electromechanical Power,  $P_e = E_a I_a = -300 \times 50 = -15000 \text{ W} //$

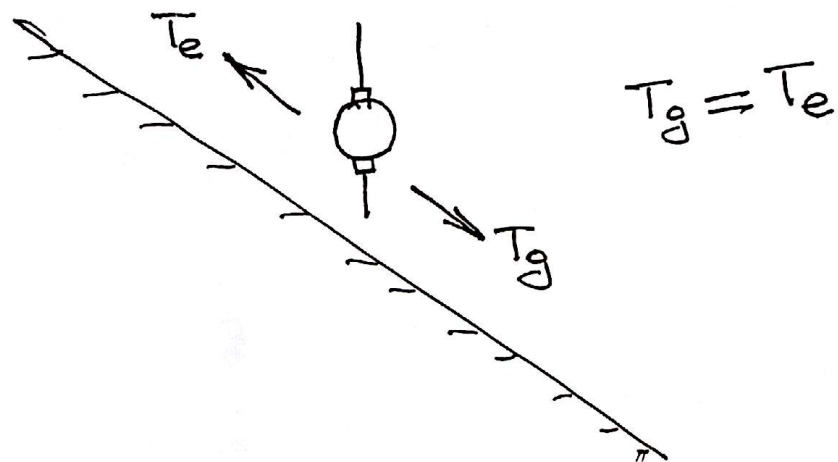
(-) sign: Mechanical Power Converted to Electrical Form.

DC M/C operates in GENERATING Mode.

$$T_e = K_a \phi_d I_a$$

$$T_e = 1.91 \times (-50) = -95.5 \text{ Nm} //$$

(6)



This technique is known as the **ELECTRIC BRAKING**. Since the electrical energy generated will then be stored in the battery bank, it is called **REGENERATIVE BRAKING** technique.

$T_g$  owing to gravitational force tends to move the electric vehicle downhill.

What will happen if the driver increases  $I_a$  from 1.0 A to 1.5 A?

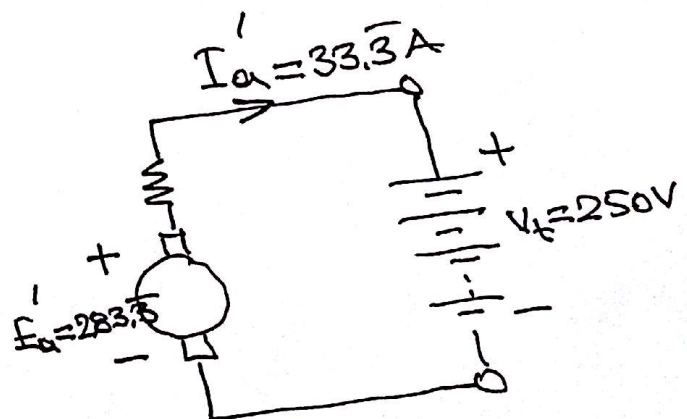
$T_g$  and hence  $T_e$  remains the same.

$T_e = K_a \phi_d' I_a'$   $\phi_d$  is increased from 1.0 pu to 1.5 pu

Therefore,

$$\text{New } I_a' = \frac{I_a}{1.5} = \frac{50}{1.5} = 33.3 \text{ A}$$

$$\begin{aligned} \text{New } E_a' &= V_t + R_a I_a' \\ &= 250 + 1.0 \times 33.3 \\ &= 283.3 \text{ V} \end{aligned}$$



If the shaft speed were 1000 rpm (7)  
then  $E_a$  would be  $E_a = 100 I_f + 100$   
 $= 100 \times 1.5 + 100$   
 $= 250 \text{ volts}$

However,  $E_a$  is  $283.3 \text{ V}$

Therefore,  $\frac{n_1}{n_2} = \frac{E_{a1}}{E_{a2}} \Big|_{I_f = 1.5 \text{ A}}$

New  $n = 1133 \text{ rpm} //$

If one increases  $I_f$  and hence  $\phi_d$ ,  
electric vehicle starts to move downhill  
at a lower speed.

Repeat the problem by assuming  
that  $I_f$  is reduced from  $1.0 \text{ A}$  to  $0.5 \text{ A}$ .