DC Link Capacitor Optimization for Integrated Modular Motor Drives

Mesut Uur
Department of Electrical and Electronics Engineering
Middle East Technical University
Ankara, Turkey
Email: ugurm@metu.edu.tr

Ozan Keysan

Department of Electrical and Electronics Engineering

Middle East Technical University

Ankara, Turkey

Email: keysan@metu.edu.tr

Abstract—In this paper, selection of optimum DC link capacitor for Integrated Modular Motor Drives (IMMD) is presented. First, a review of IMMD technologies is given and current research and future prospects are studied. Inverter topologies and gate drive techniques are evaluated in terms of DC link performance. The urge for volume reduction in IMMD poses a challenge for the selection of optimum DC link capacitor. DC Link capacitor types are discussed and critical aspects in selecting the DC links capacitor are listed. Analytical modeling of DC link capacitor parameters is performed and it is verified by simulations conducted using MATLAB/Simulink. Optimum selection of DC link capacitor is achieved based on the electrical, thermal and economical model.

I. INTRODUCTION

In conventional motor drive systems, drive units are placed in a cabinet and connected to the motor by means of long cables. Placing the motor and its drive separately increases the volume and weight of the system decreasing the system power density. In aerospace and electric traction applications, the motor drives are fundamental elements and power density plays an important role in the design [1]-[6]. In addition, due to the long connection cables, high voltage transients on the motor windings caused by PWM operation occurs on the motor terminals causing leakage currents through stator winding insulation, which cause aging of insulations and shorten the motor lifetime [7], [8]. One counter-measure for this effect is the utilization of filters between motor and drive, which are bulky and costly [1]. In recent years, a new concept called Integrated Modular Motor Drives (IMMDs) has emerged to overcome the aforementioned problems. This concept suggests that, the drive stage of a motor drive system including the power stage, control electronics, passive elements and heatsink can be integrated into the motor resulting in a single integrated unit [1], which brings several advantages. The power density of the motor drive system is significantly increased [4], [7]. A cost reduction of 20-40 with integration is possible due to the elimination of separate enclosures and cables [1]. Furthermore, the long cables are eliminated so that the lifetime of the motor is increased and EMI problems are minimized [2]. In addition, this concept aims to modularize the overall system, dividing it into several identical parts, which share the total power equally. This technique significantly increases the fault tolerance of the motor and the drive as the system can continue

its operation even if a fault occurs on one of the modules [3], [6], [7]. In [2], fault modes for both machine and power electronics are investigated and increase of fault tolerance for IMMDs has been shown. Moreover, the voltage stress on each module and motor winding group is reduced, which also enables the utilization of power semiconductor devices with low breakdown voltage ratings [9], [10]. The thermal performance of the drive is also improved as the heat sources in the system are now distributed on a larger surface area, and hot spot temperatures are reduced. In addition, fabrication, installation, maintenance and repair costs are also reduced thanks to the modular structure [1], [3], [5], [8].

Alongside of these benefits, integration of the motor and drive introduces several challenges [1], [10]. First of all, fitting all the drive components in such a small volume requires size optimization and optimum placement of components. Moreover, cooling of motor and drive together is very difficult and detailed thermal analysis is required as presented in [5]. In addition, the electronics is directly subjected to the physical vibration caused by the motor. In [3], influence of machine vibration and noise to the power electronics has been investigated for a 67 kW IMMD prototype with 5-phase switched reluctance motor. To demonstrate the thermal, vibrational and EMI effects to the electronics caused by the motor, a 10 pole permanent magnet machine prototype was developed with 6 stator phases in [8]. To reduce the size of passive elements, increasing the operation frequency by the utilization of new generation wide bandgap (WBG) power semiconductors is proposed [4], [10]. Efficiency of 99.3 has been achieved for a 900 W motor drive application with GaN power FETs [11]. By increasing frequency, parasitic inductances on both power stage and gate drive circuitry become more significant, which requires careful layout design [1].

Reduction of DC link capacitor volume is very critical in IMMD design. In motor drive systems, DC link capacitors constitute a significant portion of the overall volume and the limited converter space in IMMDs makes the optimization of DC links capacitors essential. In [12]–[14], methods such as DC link analytical modeling, evaluation of capacitor types and their comparison, application of interleaving technique for size reduction are presented. DC link capacitor selection procedure specific to IMMDs is presented in [1], [9], [10]. In this paper,

DC link modeling is studied for an IMMD and optimum capacitor selection for the DC link is achieved based on a selection algorithm. Commercial off-the-shelf capacitor types suitable for IMMD applications have been listed and compared in terms of current ripple, cost, power density, volume and thermal performance. Effect of interleaving on capacitor RMS current ripple is analyzed.

II. IMMD TECHNOLOGY REVIEW

A. The Concept of IMMD

There are several ways for integration of motor drive and motor proposed in the literature [1], [2]. For surface mount integrated motors, motor drive is mounted on the case of the motor, which is the most common integration type. High power integrated motor drives (IMDs) have been achieved commercially with this technique, whereas this type of integration lacks the benefits of modularity. Another technique is called end plate mount integration. The IMMD concept mentioned in this paper has the stator iron mount type integration, which add modularity to the system. In this configuration, the system is composed of three main parts, which constitute one module of the system: a segmented stator pole piece, a concentrated coil and the power converter and its controller dedicated to that pole piece. Two examples of this IMMD configuration are shown in Fig. 1 [1], [10].

Fig. 1: Integrated Modular Motor Drive Examples

B. Modular Motor with Split Windings

In a conventional motor, the stator coils in different poles are usually connected in series forming a single winding for each phase. In a modular motor design, these pole windings can be connected to separate drive inverters, which are called split winding machines [6], [7], [10]. Split winding machine configuration brings modularity to the system and increases redundancy and fault tolerance. It also increases the flexibility of the design since various connections of separate motor drive inverter modules are possible. Complex interconnections are not required so that end winding cost and losses will also reduce [10]. The segmented stator is usually formed with concentrated coils, which brings ease of manufacturing [4].

C. IMMD topologies

In IMMDs, connection of the inverters in parallel and/or series on the DC link in a variety of combinations is possible without the practical concerns related to circulating currents between inverters, since the load side is inherently isolated due to split winding machine configuration.

With modular machine, the voltage level on each segment will be small supposing that the total number of turns is preserved. Presence of a high voltage on DC link will require some sort of series connection of converters or power switches in a multileveled structure. In addition, keeping the voltage level of each inverter module small will lead to the possibility of utilizing low voltage power semiconductors, which will

surely enable using new generation high electron mobility transistors (HEMT) such as Gallium Nitride (GaN) [10]. Furthermore, reduction of the voltage rating of each power device yields a reduction on the switching losses of the overall system [1]. Utilization of such low voltage devices leads to a multilevel converter in case of using a passive rectifier where the available DC link voltage is fixed [7]. Many multilevel converter topologies have been proposed in the literature [9]. The most common ones are Neutral Point Clamped (NPC), Flying Capacitor (FLC), Cascaded H-Bridge (CHB) and Modular Multilevel Converter (MMC). These methods have been discussed and compared in [1], [9], [10].

The major limitation for topologies having series connection is reduced fault tolerance [6]. One of the main ideas behind modularity is to enhance the fault tolerance of the system, so it is not wise to use a fully series connected topology. On the other hand, fault tolerance on the motor drive is guaranteed for topologies with parallel connection [6]. Moreover, voltage balancing is required for series connected multilevel type converters.

It is also possible to construct a topology by just simply connecting several 3-phase 2-level modules, each of which is responsible for one armature winding module, in series and parallel according to the need for voltage and current sharing. This type of topology has the advantage of flexibility in the design, absolute symmetry, redundancy and better fault tolerance on motor drive stage. The simple structure also eliminates the need of any additional circuit components. The number of series connected modules can be determined by the relation between DC link voltage level and the breakdown voltage level of the power semiconductor. Once it is fixed, according to the determined pole number of the motor, number of parallel connected converters can be selected.

D. Wide Bandgap Power Semiconductor Devices

As mentioned previously, WBG power semiconductor devices are good candidates for IMMD applications thanks to their low on-state resistance, high switching speed and high maximum junction temperatures [11]. For traditional silicon devices such as Insulated Gate Bipolar Transistor (IGBT), switching frequency is usually limited to 20 kHz [4]. With Silicon Carbide (SiC) MOSFET and GaN, switching frequencies up to 100 kHz can be used in applications with tens of kWs [10, 13] [10], [11]. In IMMD prototype examples, GaN transistors have been widely utilized due to their very low on-state resistance, which reduces conduction loss drastically, very high switching speed, which enables size reduction for passive elements, and good thermal performance. Moreover, GaN devices do not need external free-wheeling diodes as their reverse conduction performance is good. Their efficiency in IMMD applications has been proven to be good, not only at rated power, but also in the whole output power range [11]. In [10], GaN transistors with 200 V breakdown voltage rating were utilized at 40 kHz switching frequency in an IMMD prototype where no heatsink was required. On the other hand, due to low voltage rating of a single device, series connected multilevel converter topology had to be utilized [7].

III. DC LINK MODELING

Reduction of DC link capacitor volume is very critical in IMMD design. As seen in Fig. 2, in a modern power electronics system, passive elements take a significant portion of overall volume and cost [1]. It was also stated in [12] that, in motor drive inverters, DC link capacitors constitute 20 of cost and weigh, and 30 of volume. The limited converter space in IMMDs makes the optimization of DC links capacitors essential. For this purpose, accurate modeling of DC link is required. Decreasing the volume of capacitors is not sufficient alone, the height of the capacitors should also be minimized as they are the tallest components in IMMDs [7], [10].

Fig. 2: Volume and cost sharing of different parts in a modern power electronics system [1]

A. Analytical Modeling

The fundamental parameters affecting the size of a DC link capacitor are DC voltage requirement, capacitance requirement due to DC link voltage ripple and RMS current rating requirement due to DC link capacitor current ripple. Temperature characteristics is also important as it affects the reliability and lifetime of a capacitor.

DC link voltage, which is a parameter directly related to capacitor height, highly depends on the selected inverter topology. For multilevel converters where several converter are connected in series, DC voltage rating of each capacitor can be reduced. Actually, same thing can be done for a topology with a single DC link by just simply connected capacitors with lower voltage ratings in series. In Section 4, effect of series connection of several DC link capacitors with lower DC voltage rating is discussed. RMS current rating is directly related to the power requirement and is not effected much by the switching frequency [7], [10], [12]. Therefore, for a given converter with a specific power output, this parameter is fixed. Capacitance requirement, on the other hand, is directly related with the switching frequency. In this section, each parameter will be analytically modeled to be used in the capacitor selection algorithm. The model of the DC link to be used in this paper is shown in Fig. 3. Rectifier side is considered to be an ideal DC source, denoted as $I_i n$. The inverter DC current $(i_d c)$ is the sum of the average current $(I_i n)$, and the ripple current which flows through the capacitor (i_c) . The average DC current can be expressed as in 1, where I(a, peak) is the peak value of any line current, m_a is modulation index, and is power factor angle.

Fig. 3: Model of the DC Link

$$I_{avg} = \frac{3}{4} I_{a,peak} m_a cos(\phi) \tag{1}$$

The capacitor current is composed of sideband harmonics around the switching frequency and its integer multiples. The RMS value of this current has been derived in [12], [13] as in 2, where $I_{(a,rms)}$ is the RMS value of any line current.

$$I_{avg} = \frac{3}{4} I_{a,peak} m_a cos(\phi) \tag{2}$$

The voltage ripple on the DC link has not been explicitly derived in the literature. Here, a method is developed to model the peak-to-peak ripple voltage by using the relation between the capacitor voltage and current, and the shape of the capacitor ripple current as shown in 3.

$$I_{avg} = \frac{3}{4} I_{a,peak} m_a cos(\phi)$$
 (3)

Finally, temperature characteristics and the power loss of capacitors are modeled. The core temperature (T_c) of a capacitor can be expressed as in 4, where T_a is the ambient temperature, $R_(th,c)$ is the thermal resistance of the capacitor, and R_c is the ESR of the capacitor, which is a parameter dependent on the core temperature of the capacitor as shown in 5 [13]. As seen from these equations, ESR of the capacitor R_c is a temperature dependent parameter so that the thermal model is an implicit equation and should be treated so.

$$I_{avg} = \frac{3}{4} I_{a,peak} m_a cos(\phi) \tag{4}$$

$$I_{avg} = \frac{3}{4} I_{a,peak} m_a cos(\phi) \tag{5}$$

B. Effect of Interleaving

Interleaving is widely used in power converters to decrease ripple currents and ripple voltages for passive component size reduction [14]. IMMD system is suitable for the application of interleaving as there are multiple converter modules, which can be connected in different configurations. It is a well-known fact that, phase shifting applied to the converters which are interleaved reduces the capacitor current ripple and DC link voltage ripple [1], [10], [12]. In [10], interleaving has been applied to an IMMD prototype switching frequency of which is 100 kHz. The effect of interleaving to the DC link current waveform and the RMS value of the capacitor current in motor drive inverters is obtained by simulation as shown in Fig 4. The rule of thumb phase shift angle to be applied to the converters is usually given as 360/n [1]. The percent RMS current is obtained with changing number of parallel connected modules to shown the optimum phase shift angle for each case as in Fig. 5. It has been shown that, minimum percent RMS current is obtained around 360/n angle for each case. It is also shown that, RMS current does not decrease significantly after a certain number of parallel connected modules, and a total number of 4 or 6 modules can be suggested.

Fig. 4: Effect of interleaving to motor drive inverters

Fig. 5: Capacitor percent RMS current characteristics

IV. DC LINK CAPACITOR EVALUATION

A. Types of Capacitors

Common capacitor types used in motor drive DC links are aluminum electrolytic capacitors, metal film capacitors and multilayer ceramic capacitors (MLCC). Comparison of these capacitors in terms of several aspects are shown in Table I [1], [4], [7], [10], [15].

Aluminum electrolytic capacitors are usually preferred due to their high capacitance and low cost. On the other hand, since their RMS current ratings are low, parallel connection of multiple capacitors may be required. Reliability of these capacitors is a major concern as their lifetime and failure rate highly depend on operating temperature, voltage and current magnitudes [12]. When an aluminum electrolytic capacitor is operated at 90 of its rated voltage, the failure rate reduces to 60 [13]. Temperature limitation is another major concern of electrolytic capacitors, which makes them unsuitable for IMMD applications [15].

Film capacitors, on the contrary, have low capacitance but high RMS current rating. Therefore, parallel connection of multiple film capacitors is required to meet the capacitance requirement. As the capacitance value can be optimized with switching frequency, which is not the case for RMS current, they are more preferable in IMMD applications. They are very reliable and durable capacitors, however they are more expensive than electrolytic capacitors.

MMLCs are low cost and high current rating capacitors, however they are not commercially available with the power rating of a DC link capacitor. Therefore, series and parallel connection of several capacitors is needed. The main problem for MLLC in IMMD applications is their sensitivity to mechanical effects such as vibration [15] due to being in close proximity to the motor.

TABLE I: COMPARISON OF CAPACITOR TYPES

Total output power	10 kW	Switching frequency	20 kHz
Motor fund. frequency	50 Hz	Supply frequency	50 Hz
Supply voltage	400 V	Motor voltage	400 V
Three-phase modules	4	Parallel connected modules	4
DC Bus filter inductance	1 mH	DC bus filter capacitance	100 uF
Some motor parameters	abc	Some other parameters	xyz

B. Capacitor Selection Aspects

In motor drives, DC link capacitors have the functions of taking on the power fluctuation on the DC link occurring at two or six times the supply frequency (depending on the number of phases), supplying the current ripples at the inverter switching frequency, to avoid the injection of high frequency ripples from one side to the other in the back-to-back structure (decoupling), to provide the drive system for a while in case

of power shutdown, to supply the transient powers etc. [13]. In this research work, rectifier side is considered as an ideal DC current source so that the only frequency components observed on the DC link will be composed only inverter side harmonics. Normally, superposition should be used considering both the harmonic contributions of both inverter side and rectifier side [13]. The basic parameters affecting the selection of DC link capacitor are: o Capacitance requirement due to DC link voltage ripple, o RMS current rating requirement due to DC link capacitor current ripple, o Voltage rating due to DC link voltage and topology. In addition, for an IMMD system, the major concerns for the DC link capacitor selection can be listed as follows: High power density due to size constraints Low height Low cost Low temperature sensitivity Mechanical durability due to being in close proximity to the motor Low reduction in lifetime due to operating conditions

C. Capacitor Selection Algorithm

Based on the analytical models developed so far, capacitor datasheets, capacitor selection aspects and simulation work, an algorithm for the optimization of DC link capacitor for an IMMD application is developed and implemented. The basic flowchart of the algorithm can be seen in Fig. 6. The algorithm takes the inputs which define the operating conditions and ratings of the motor drive, takes the limitations as constraints and use them in the calculation of critical variables. The capacitor RMS current requirement is calculated with modulation index being variable to cover the whole operating region. Switching frequency is also considered as a variable parameter to give the designer flexibility, which is then used in capacitance requirement calculation. Datasheet parameters are fed to the algorithm to check the performance of different capacitors with the given constraints. The number of capacitors to be connected in parallel is determined for each type. In addition to this procedure, capacitors with different voltage ratings are also considered to observe the effect of using multiple series connected capacitors.

Fig. 6: Flowchart of the optimum capacitor selection algorithm

V. RESULTS

The results obtained by using the algorithm and a set of film capacitors from [16] and presented in this section. The system parameters and constraints used in the algorithm are listed in Table II. In Fig. 7, RMS current requirement for different modulation index values are obtained. In Fig. 8, capacitance requirement for different switching frequencies are obtained considering the modulation index at the worst condition. It has been shown that increasing the switching frequency above 100 kHz does not have much effect on the capacitance requirement. Moreover, after this point, the RMS current requirement becomes more dominant for film capacitors. Moreover, the maximum RMS current requirement occurs around 0.8 modulation index, which has been taken as the actual requirement. Effect of frequency to the RMS current

is negligibly small, and it is not included in the analysis and results.

TABLE II: System parameters and constraints

				_
Total output power	10 kW	Switching frequency	20 kHz	Ť
Motor fund. frequency	50 Hz	Supply frequency	50 Hz	Ť
Supply voltage	400 V	Motor voltage	400 V]
Three-phase modules	4	Parallel connected modules	4	Ť
DC Bus filter inductance	1 mH	DC bus filter capacitance	100 uF	Ť
Some motor parameters	abc	Some other parameters	xyz	1

Fig. 7: RMS current requirement vs modulation index

Fig. 8: Capacitance requirement vs switching frequency

Two sets of capacitors, having 25 different capacitors each, were selected from the same datasheet [16], which have voltage rating of 300V and 450V. The algorithm was implemented on these sets and number of series and parallel connections needed for each type of capacitor is found. Some samples from the capacitors are selected and listed in III, and compared, which was achieved with 40 kHz switching frequency. The suitable capacitors according to the selected constraints are highlighted on Table III.

Using a single capacitor with large capacitance and large voltage rating (Cap no.12) seems to be a good choice at the first glance as it has a very good power density, low height and lowest cost; however, it has the highest temperature rise since its surface area is too small. On the other hand, using high number of capacitors having low capacitance and low voltage rating (Cap no.1, 2, and 3) gives best thermal performance and lowest height, but their power density is too small and cost increases with this configuration. It can also be deduced that using high number of series connections and low number of parallel connections (Cap no. 4, 5) yields the worst results in terms of all the constraints.

For 450V capacitors, selecting capacitors with low capacitance (Cap no. 6, 7) is not also the best choice as the cost increases due to multiple parallel connection. The best results have been obtained by capacitor no.9 which has 20 F capacitance and 450 V voltage rating and needs 4 parallel connection.

VI. CONCLUSION

IMMD applications is presented. Integration of the motor drive power electronics into the motor introduces several challenges for the DC link capacitor selection. On the other hand, modular structure of IMMD brings flexibility for the design and capacitor selection. Interleaving technique can be applied to reduce the DC link voltage and current ripple. Among several capacitor types, film capacitor is more suitable for IMMD DC links due to its good current ripple ratings,

TABLE III: Comparison of Selected Capacitors,(s: series, p: parallel)

	Total output power	10 kW	Switching frequency	20 kHz
	Motor fund. frequency	50 Hz	Supply frequency	50 Hz
z	Supply voltage	400 V	Motor voltage	400 V
	Three-phase modules	4	Parallel connected modules	4
7	DC Bus filter inductance	1 mH	DC bus filter capacitance	100 uF
	Some motor parameters	abc	Some other parameters	xyz
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reliability, good thermal performance and suitability for vibrational environments. Accurate models have been developed considering electrical, thermal and economical aspects. These models are used in an algorithm to determine the best choice among a set of selected commercial film capacitors. The alternative configurations include series connection of multiple low voltage capacitors to meet the DC link voltage requirement and parallel connection of multiple low capacitance capacitors to meet the voltage and current ripple requirements.

Considering the parameters such as power density, cost, height and temperature rise, it has been shown that, using 4 20 F, 450 V capacitors in parallel gives the best performance in all aspects for this specific application.

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