

$$S_a = \frac{1}{2} + \frac{M}{2} \cos(w_o + \theta_o) + \left(\frac{2}{\pi} \sum_{m=1}^{inf} J_o(m\pi \frac{M}{2}) \sin(m\frac{\pi}{2}) \cos(m(w_c + \theta_c)) \right) + \left(\frac{2}{\pi i} \sum_{m=1}^{inf} \sum_{n=-inf}^{inf} \left(\frac{1}{m} \right) J_n\left(\frac{mM\pi}{2}\right) \sin\left(\frac{(m+n)\pi}{2}\right) \cos(m(w_c + \theta_c) + n(\theta_o + w_o)) \right)$$

Diagram illustrating the components of the switching function S_a :

- Fundamental Component**: Indicated by a green arrow pointing to the term $\frac{M}{2} \cos(w_o + \theta_o)$.
- Bessel function (0 order)**: Indicated by a black arrow pointing to the term $J_o(m\pi \frac{M}{2})$.
- Switching Harmonics**: Indicated by a red arrow pointing to the term $\sin(m\frac{\pi}{2})$.
- Side Band harmonics**: Indicated by a blue arrow pointing to the double summation term.
- Bessel function (n^{th} order)**: Indicated by a black arrow pointing to the term $J_n(\frac{mM\pi}{2})$.

Parameters:

$M \Rightarrow$ modulation index

$\omega_o \Rightarrow$ output(fundamental) frequency

$\omega_c \Rightarrow$ carrier(switching) frequency

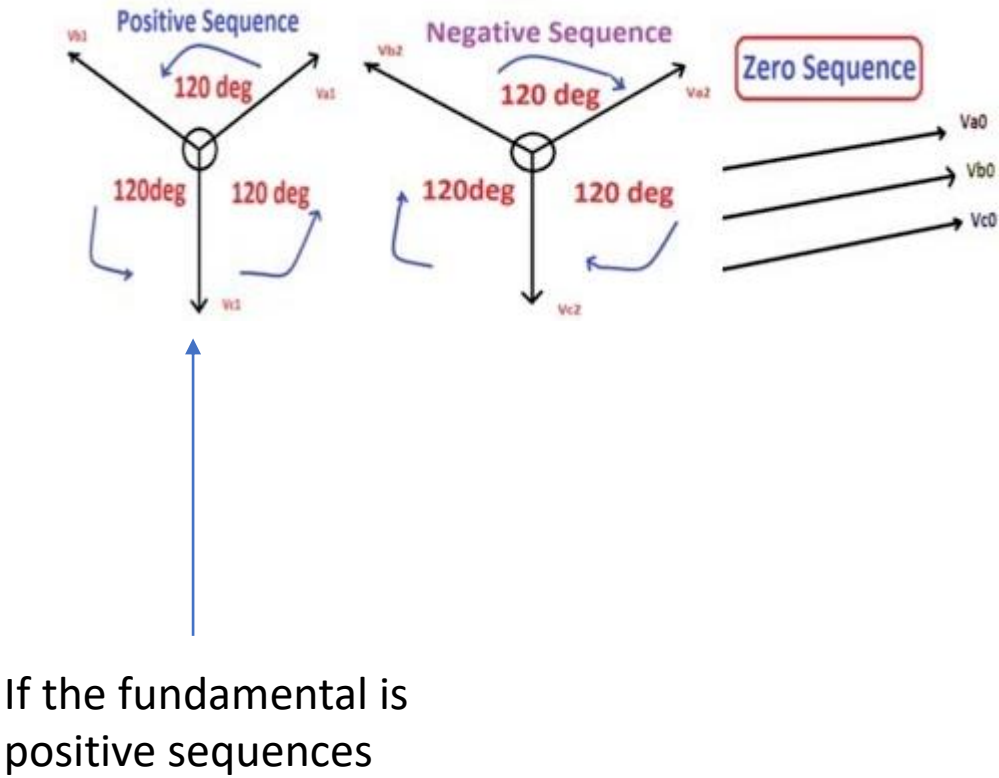
$\theta_o \Rightarrow$ output phase

$\theta_c \Rightarrow$ carrier phase

Deductions

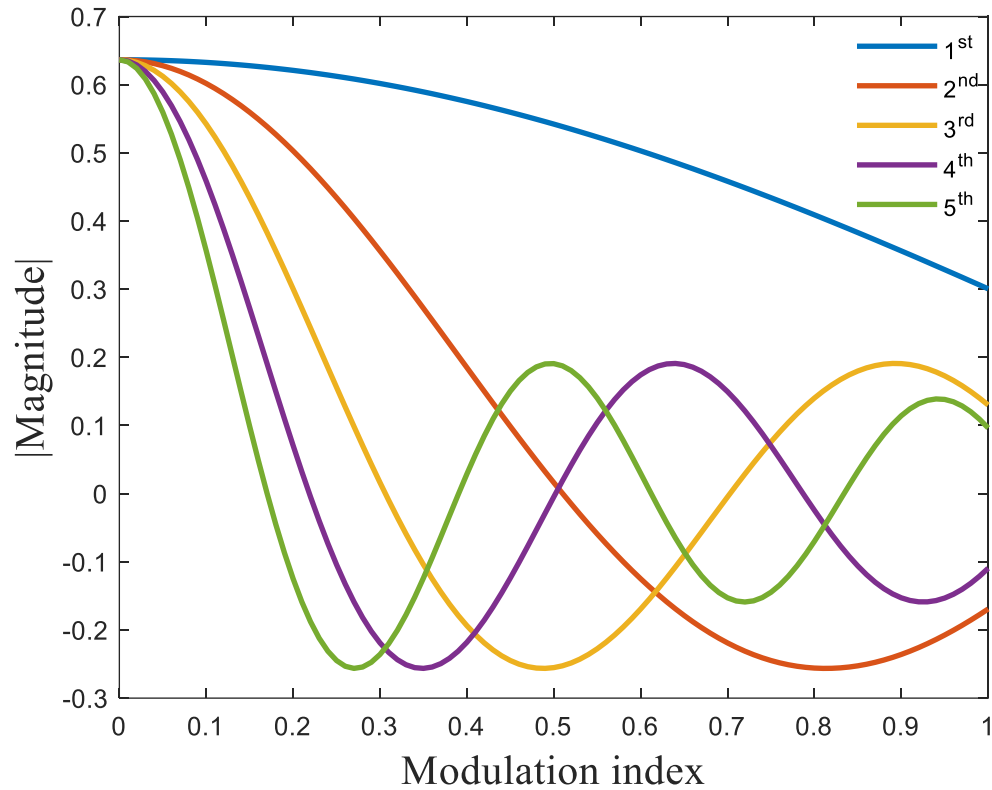
- Fundamental component is independent from carrier(switching) frequency and phase
- There is no even harmonics of the switching and the sign of the odd harmonics is alternated.
- The switching harmonics are independent from fundamental frequency and phase.
- The side band harmonics are affected by all fundamental and carrier frequency and phases.

Sequences of the Switching Harmonics and Side Bands



Frequency	Phase A	Phase B	Phase C
f_o	$\theta_o = 0^\circ$	$\theta_o = 120^\circ$	$\theta_o = -120^\circ$
$f_s - 4f_o$	0°	240°	120°
$f_s - 2f_o$	180°	300°	60°
f_s	0°	0°	0°
$f_s + 2f_o$	180°	60°	300°
$f_s + 4f_o$	0°	120°	240°

Switching Harmonics



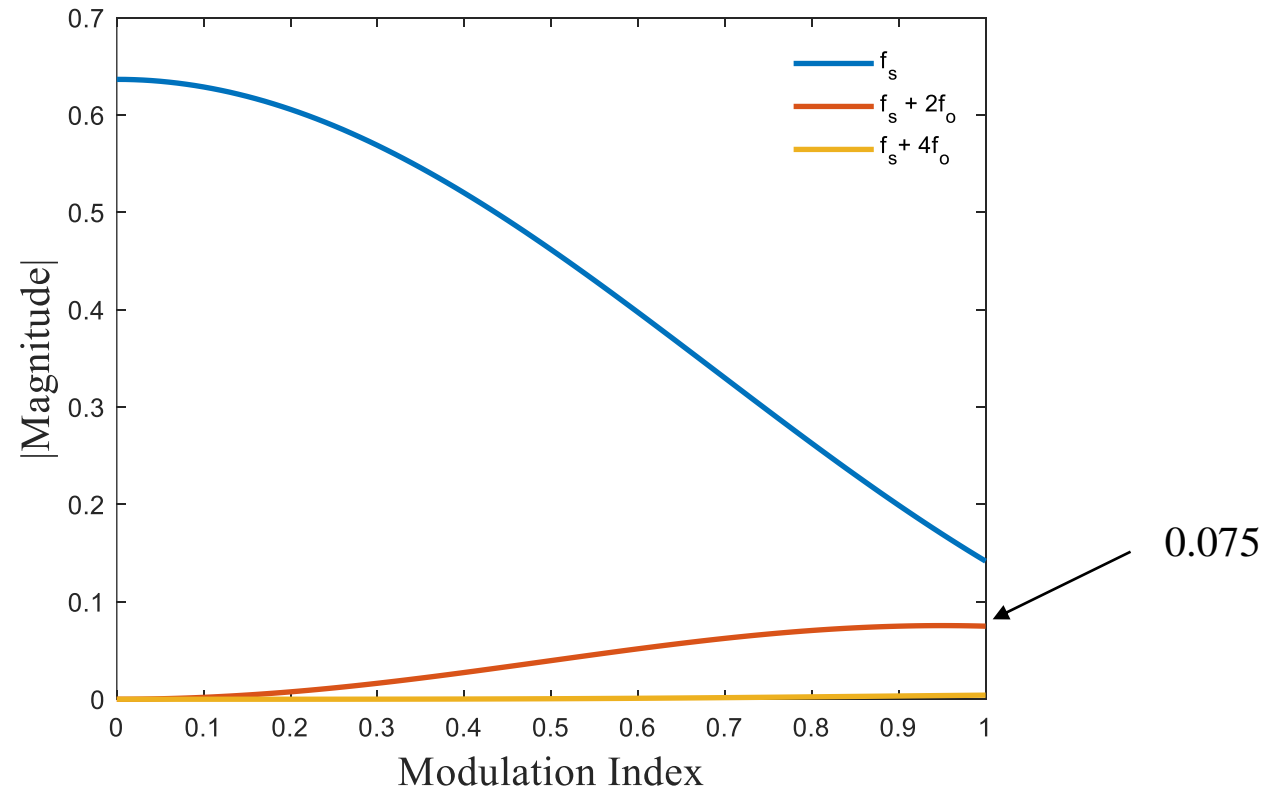
Max = 0.6366 (ma=0 for 1st)

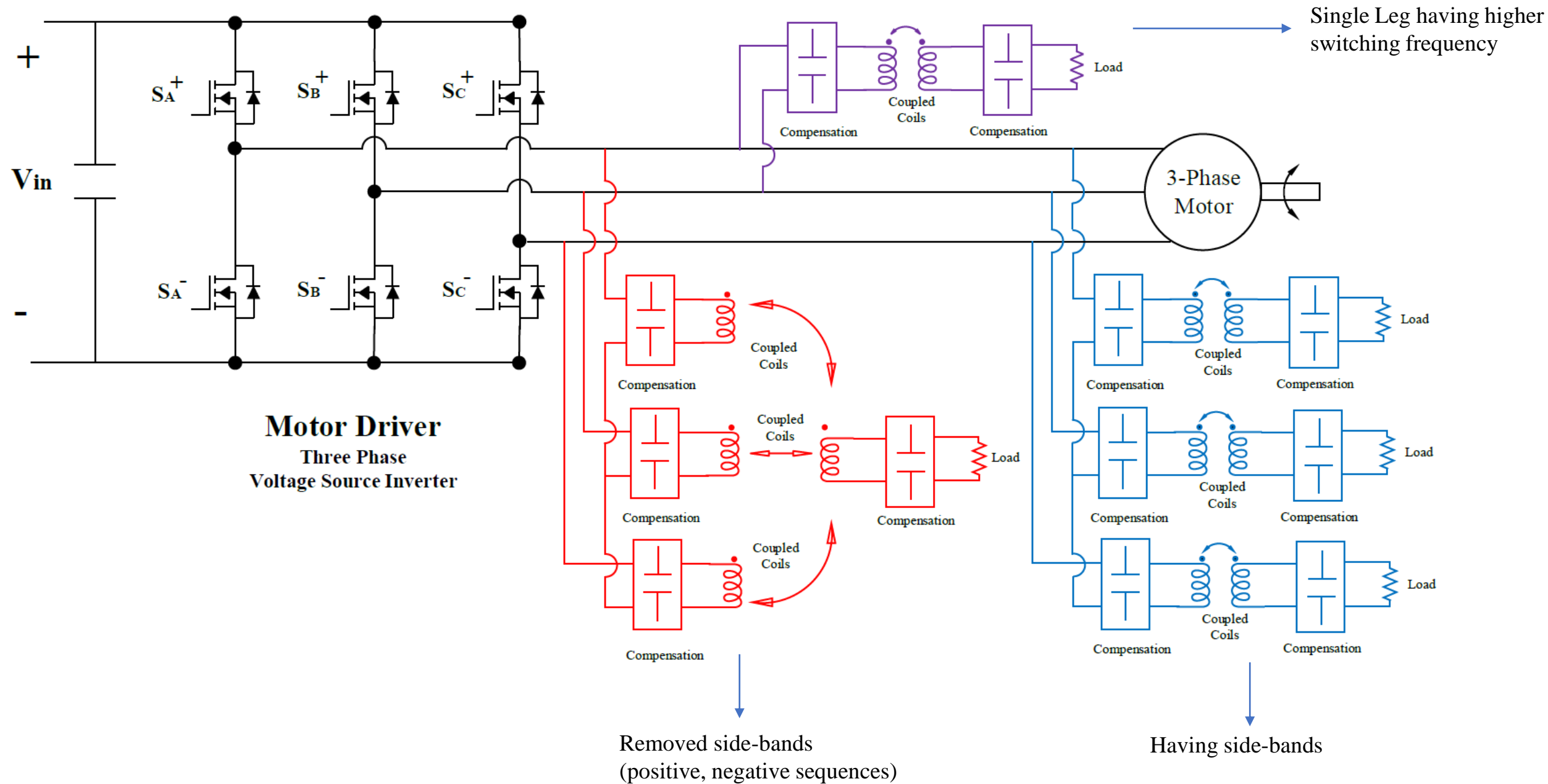
Min = 0.3005 (ma=1 for 1st)



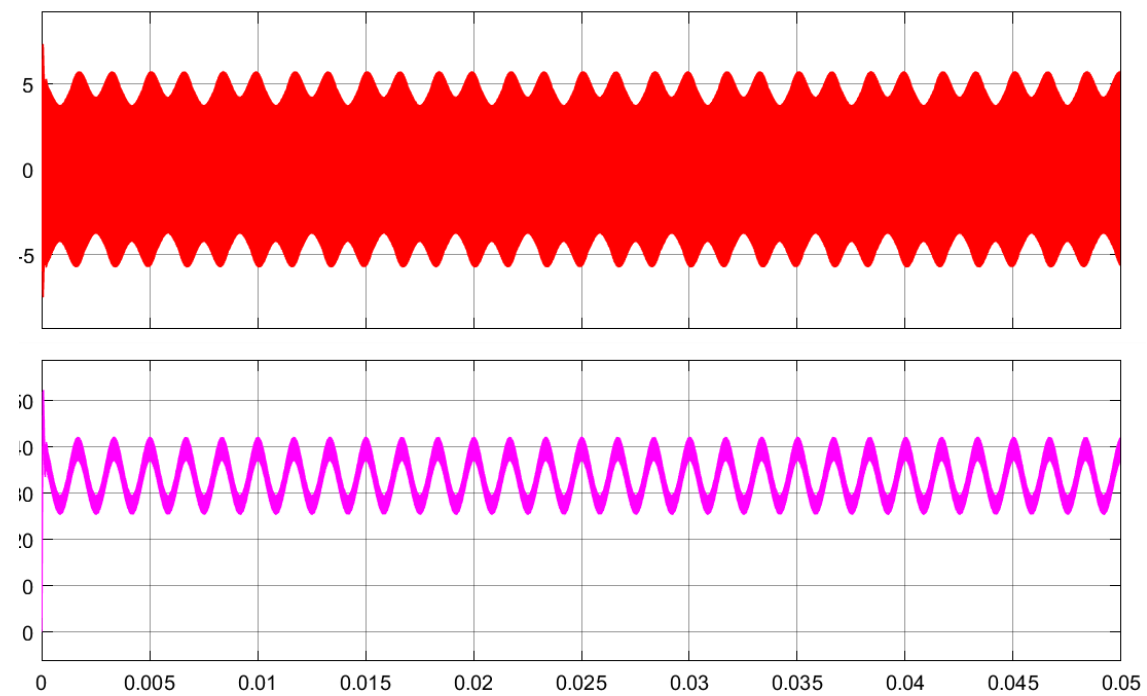
It is very promising if we think the duty cycle control of DC motor

Side Band Harmonics

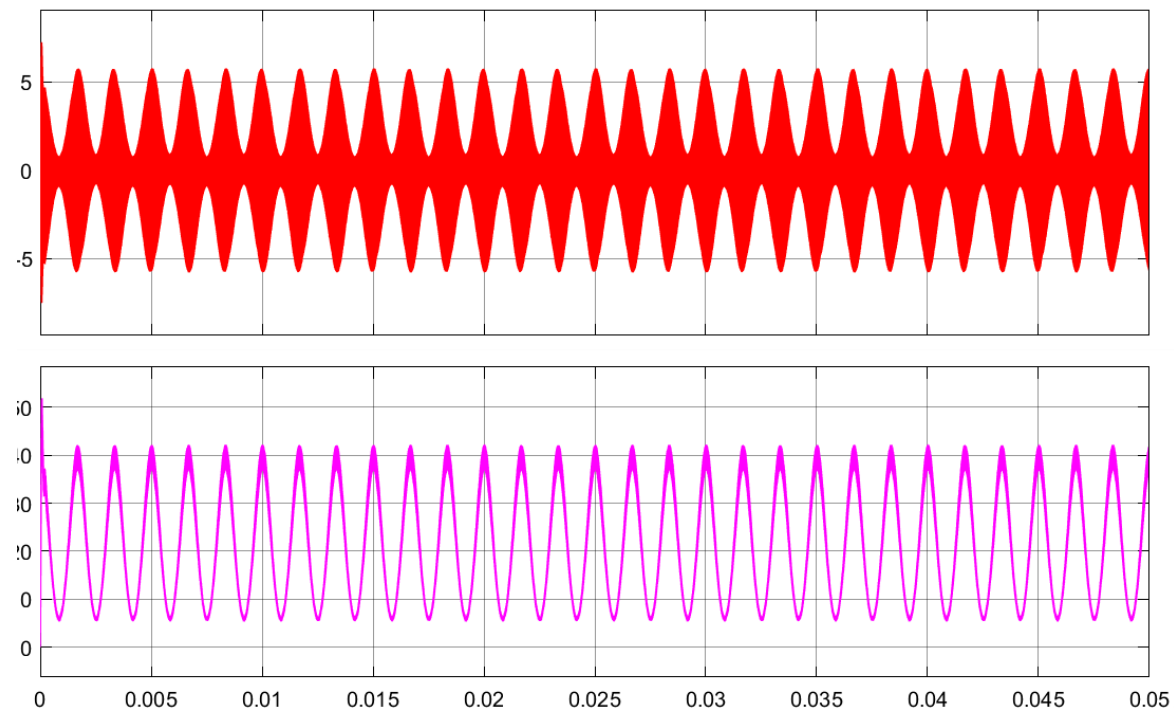




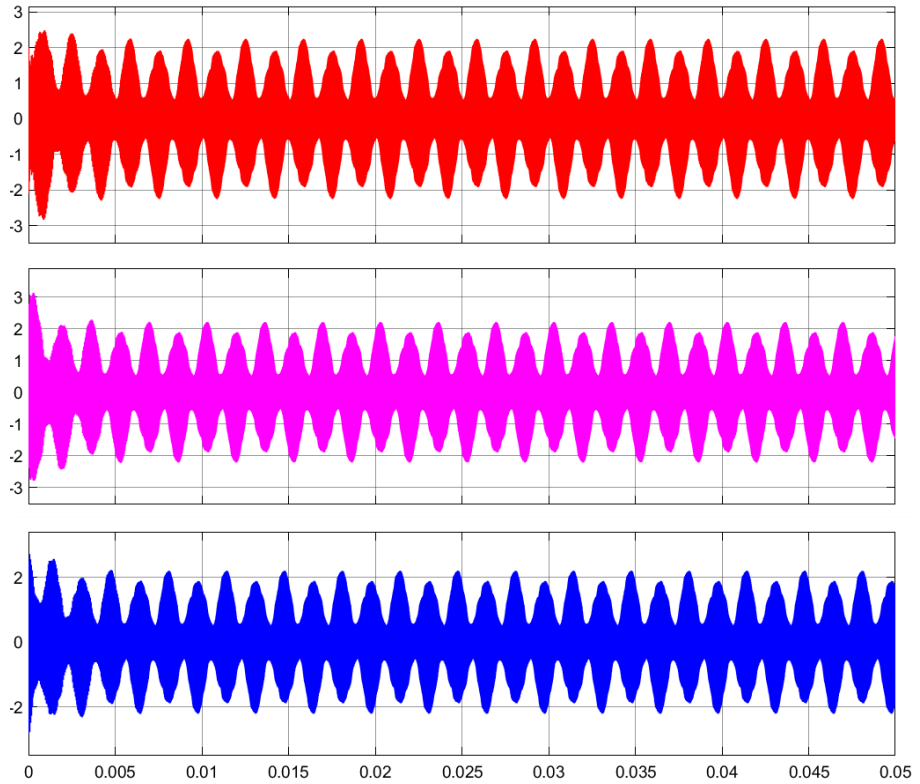
ma=0.5



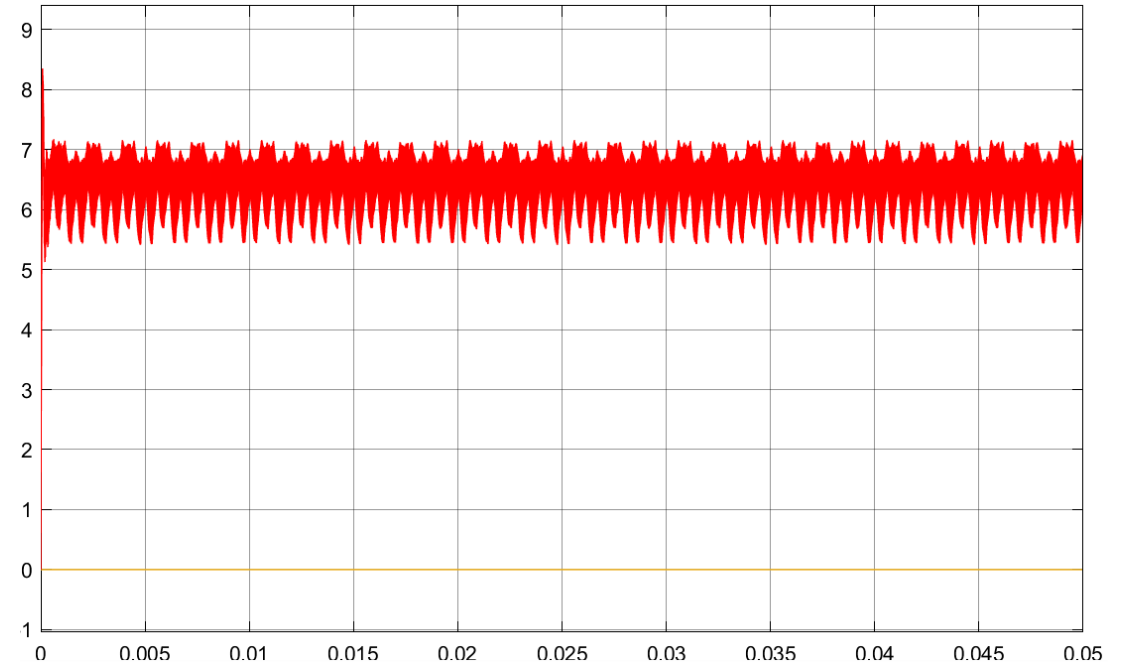
ma=0.9



Side-Bands create the envelopes



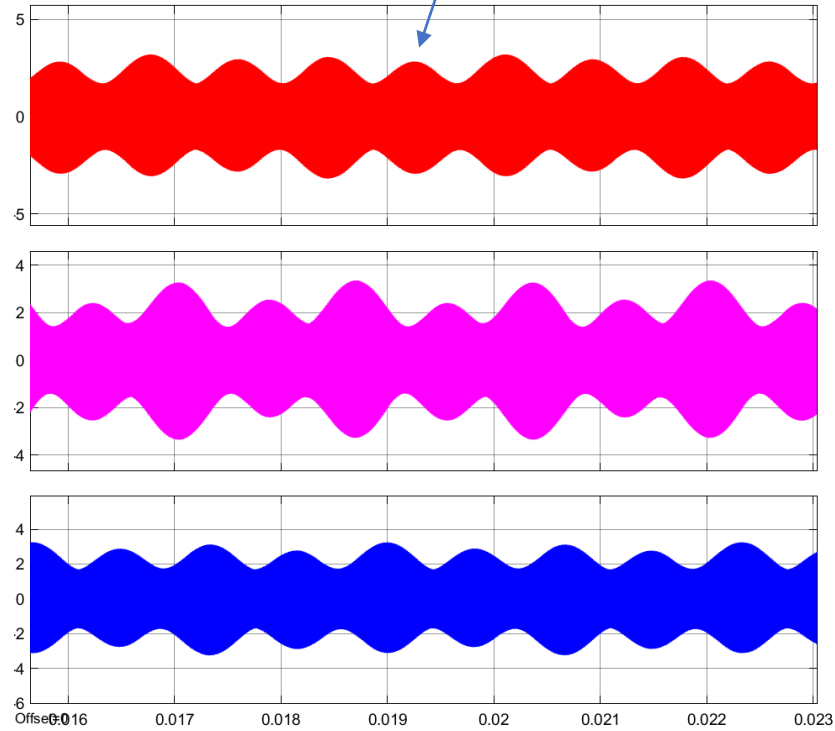
Tx Currents



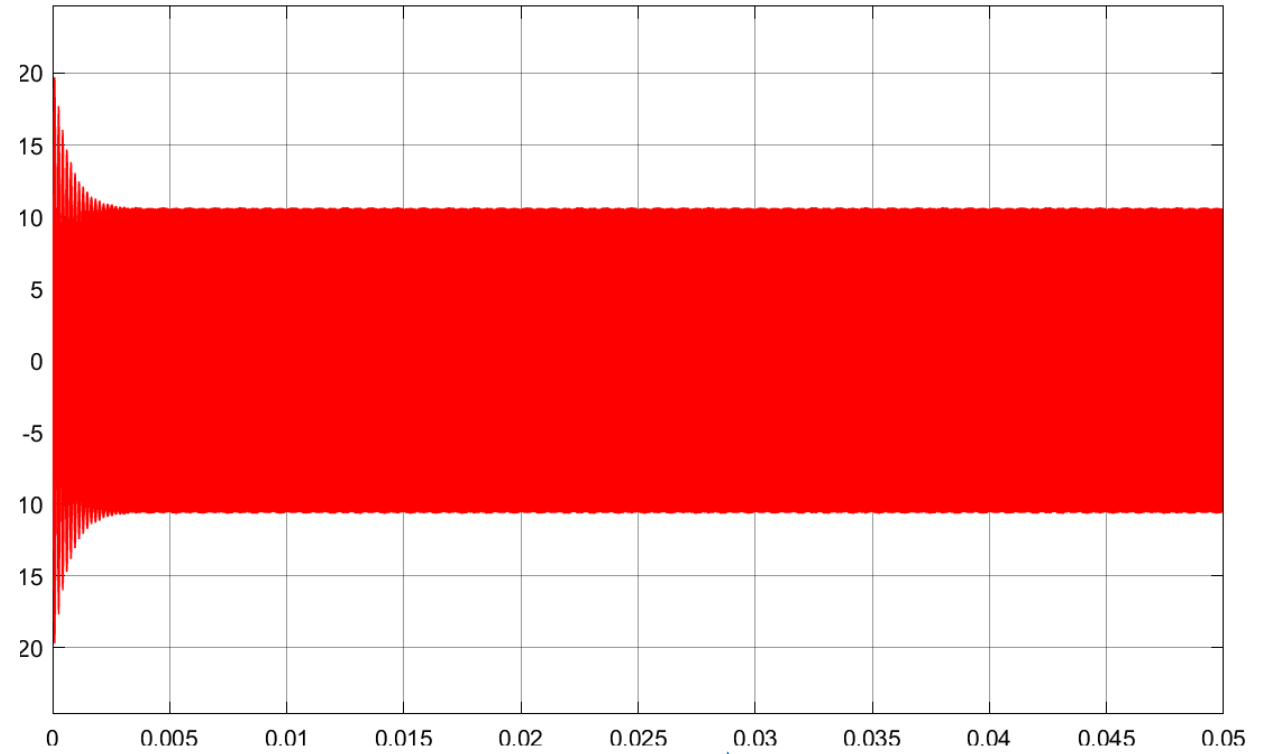
Output has only switching harmonics



Side-Bands create the envelopes



Tx Currents



Output has only switching harmonics