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## Bcd synchronous counters

The BCD counter is just a special case of the MOD-N counter ( $N = 10$ ). BCD counters are very commonly used because most human beings count in decimal. It is by default an up counter.

We prefer synchronous counter because there is not a regular pattern in the state table as it is in straight binary counter. So, we use a universal clock pulse which triggers all the flip flops simultaneously.

### ➤ BCD SYNCHRONOUS COUNTER USING T FLIP-FLOPS

#### State table for BCD counters

*State Table for BCD Counter*

Present State				Next State				Output	Flip-Flop Inputs			
$Q_8$	$Q_4$	$Q_2$	$Q_1$	$Q_8$	$Q_4$	$Q_2$	$Q_1$	$y$	$TQ_8$	$TQ_4$	$TQ_2$	$TQ_1$
0	0	0	0	0	0	0	1	0	0	0	0	1
0	0	0	1	0	0	1	0	0	0	0	1	1
0	0	1	0	0	0	1	1	0	0	0	0	1
0	0	1	1	0	1	0	0	0	0	1	1	1
0	1	0	0	0	1	0	1	0	0	0	0	1
0	1	0	1	0	1	1	0	0	0	0	1	1
0	1	1	0	0	1	1	1	0	0	0	0	1
0	1	1	1	1	0	0	0	0	1	1	1	1
1	0	0	0	1	0	0	1	0	0	0	0	1
1	0	0	1	0	0	0	0	1	1	0	0	1

Using k-map we can find the input functions to T flip-flops as

$$Tq_1=1, Tq_2=Q_8'Q_1, Tq_4=Q_2Q_1, Tq_8=Q_1Q_8+Q_4Q_2Q_1$$

k-map illustration is mentioned under:-

<b>Q2Q1</b> <b>Q8Q4</b>	00	01	11	10
00		1	1	
01		1	1	
11	X	X	X	X
10			X	X

k-map for  $Tq2 = Q1Q8'$

<b>Q2Q1</b> <b>Q8Q4</b>	00	01	11	10
00			1	
01			1	
11	X	X	X	X
10			X	X

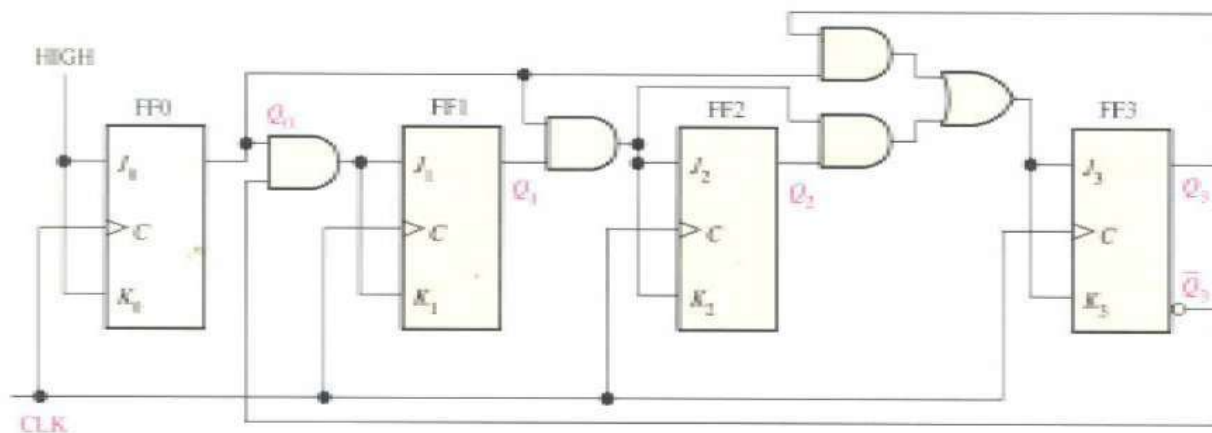
K-map for  $Tq4 = Q2Q1$

<b>Q2Q1</b>	00	01	11	10

$Q_8Q_4$				
00				
01			1	
11	X	X	X	X
10		1	X	X

*k-map for Tq8 is mentioned under :  $Q_1Q_8+Q_1Q_2Q_4$*

## Circuit diagram for synchronous BCD counters using jk flip flops:



## Advantages of synchronous bcd counters:

- Synchronous counters are easy to design.
- With all inputs wired together there is no inherent propagation delay.
- Overall faster operation may be achieved as compared to asynchronous counters

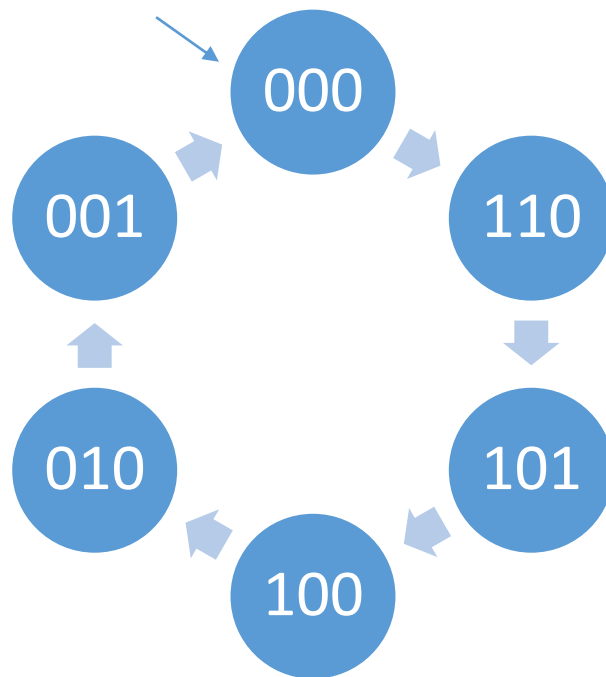
## COUNTERS WITH UNUSED STATES

Counters with  $n$  flip-flops have  $2^n$  states. For all the examples we have shown so far, we had  $2^n$  states and used  $n$  flip-flops. But sometimes we may have unused, leftover states. This happens because in

certain occasions, the sequential circuit uses fewer than its maximum number of states. The unused states do not play any role in specifying the sequential circuit and hence, are not listed in the stable table.

For example:

Here is a stable table that repeatedly counts 000, 001, 011, 100, 101, 110 .



PRESENT STATE			NEXT STATE		
$Q_2$	$Q_1$	$Q_0$	$Q_2$	$Q_1$	$Q_0$
0	0	0	0	0	1
0	0	1	0	1	0
0	1	0	1	0	0
1	0	0	1	0	1
1	0	1	1	1	1
1	1	0	0	0	0
1	1	0	X	X	X
0	1	1	X	X	X

The unused states can be treated as DON'T CARE.

Using a J/K flip-flop:

PS $Q_2 Q_1 Q_0$	NS $Q_2 Q_1 Q_0$	$J_C K_C$	$J_B K_B$	$J_A K_A$
000	001	0X	0X	1X
001	010	0X	1X	X1
010	100	1X	X1	0X
100	101	X0	0X	1X
101	110	X0	1X	X1
110	000	X1	X1	0X

Now by K-map method:

$$J_C = Q_B$$

$$K_C = Q_B$$

$$J_B = Q_A$$

$$K_B = 1$$

$$J_A = \text{complement of } Q_B$$

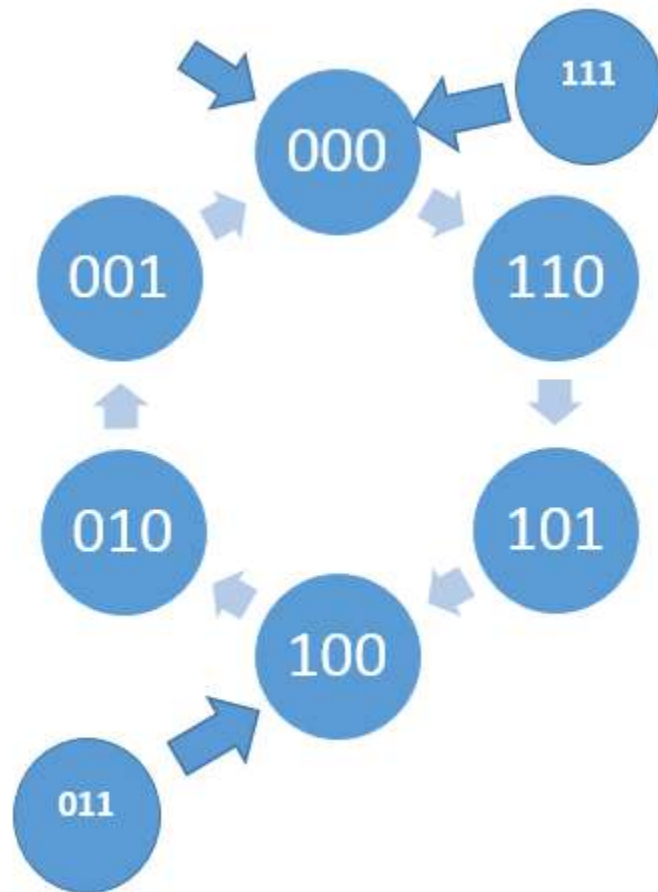
$$K_A = 1$$

It is possible that sometimes, outside noise can cause the counter to enter unused state. We must ensure that the counter eventually reaches valid state.

To avoid this and guarantee a safe circuit, we assign the next state to the unused states. This way, even if the circuit somehow enters an unused state, it will eventually end up in a used state.

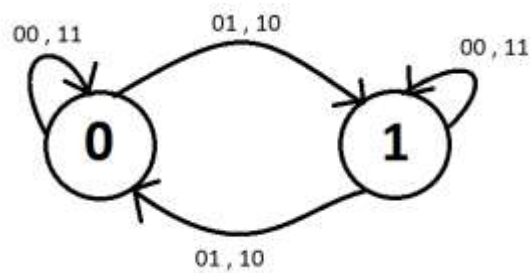
In the example given above, it is possible that the unused states 011 and 111 enter into the counter. So, we need to force one unused state to go to the used state.

PS	NS
011	100
111	000



## Example 1

2 bit counter using D flip flop (2 states)



Present State Q	Input		Next State Q+	D f/f
	x	Y		
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	0
1	0	0	1	1
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

D = N.S.

K-Map for D

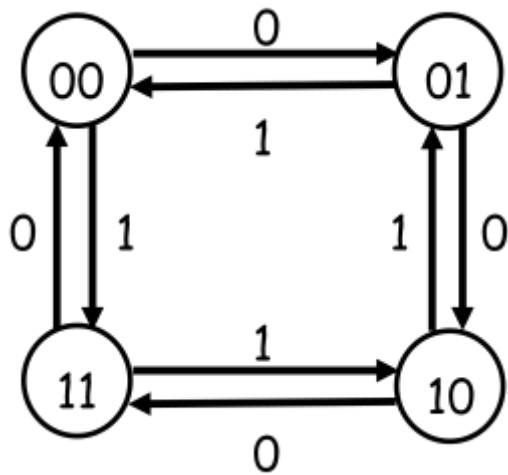
		00		01		11		10	
xy	q \								
	0	0	1	0	1	0	1	0	1
1	1	1	0	1	0	1	0	0	1

$$D = Q \oplus x \oplus y$$

## Example 2

1 bit counter using JK flip flop (4 states)





K-MAP

Present State		Inputs X	Next State		Flip flop inputs			
$Q_1$	$Q_0$		$Q_1$	$Q_0$	$J_1$	$K_1$	$J_0$	$K_0$
0	0	0	0	1	0	x	1	x
0	0	1	1	1	1	x	1	x
0	1	0	1	0	1	x	x	1
0	1	1	0	0	0	x	x	1
1	0	0	1	1	x	0	1	x
1	0	1	0	1	x	1	1	x
1	1	0	0	0	x	1	x	1
1	1	1	1	0	x	0	x	1

$$J_1 = K_1 = Q_0' X + Q_0 X' = Q_0 \oplus X$$

$$J_0 = K_0 = 1$$

