

$$\vec{v} = \frac{\vec{Q}}{\phi}$$

$$\frac{\partial(\rho\phi)}{\partial t} + \nabla \cdot (\rho \vec{Q}) = 0$$

$$\underbrace{\phi \frac{\partial \rho}{\partial t} + \rho \frac{\partial \phi}{\partial t}}_{\text{red bracket}} + \underbrace{\nabla \rho \cdot \vec{Q}}_{\text{blue bracket}} + \rho \nabla \cdot \vec{Q} = 0$$

$$\rho = \rho(p(\vec{x})), \quad \phi = \phi(p(\vec{x}))$$

$$\left[\phi \rho \left[\underbrace{\frac{1}{\phi} \frac{\partial \phi}{\partial p} \frac{\partial \rho}{\partial t}}_{C_R} + \underbrace{\frac{1}{\rho} \frac{\partial \rho}{\partial p} \frac{\partial \phi}{\partial t}}_C \right] + \frac{\partial \rho}{\partial p} \nabla \rho \cdot \vec{Q} + \rho \nabla \cdot \vec{Q} = 0 \right] \frac{1}{\rho}$$

$$\phi \underbrace{\left[C_R + C \right]}_{C_t} \frac{\partial \rho}{\partial t} + \underbrace{\frac{1}{\rho} \frac{\partial \rho}{\partial p}}_c \nabla \rho \cdot \vec{Q} + \nabla \cdot \vec{Q} = 0$$

$$\vec{Q} = -\frac{k}{\mu} (\nabla p - \cancel{\rho \vec{g}})$$

homo, iso, no gravity

$$\phi c_t \frac{\partial p}{\partial t} - c \nabla p \cdot \left(\frac{k}{\mu} \nabla p \right) - \nabla \cdot \left(\frac{k}{\mu} \nabla p \right) = 0$$

$$\frac{\mu \phi c_t}{k} \frac{\partial p}{\partial t} = \nabla \cdot (\nabla p) + c (\nabla p \cdot \nabla p)$$

small & constant
compressibility

$$\boxed{\frac{\partial p}{\partial t} = \frac{1}{\alpha} \nabla \cdot (\nabla p)}$$

Heat equation

"Pressure diffusivity eqn"

$$\alpha = \frac{\mu \phi c_t}{k}$$