

## 1 Nelson Rules for Interpreting Control Charts

- The eight tests used in statistical process control were developed by Lloyd S. Nelson, a process control expert. They are based on his determination that the identified patterns are very unlikely to occur in stable processes.
- Thus the existence of any of these patterns in an  $\bar{X}$  chart indicates that the process may be unstable, and that one or more assignable causes may exist.
- The table on the next page contains examples of test failure for each of the eight tests, with a description for each graph as to what is required for the illustrated test failure.
- In practice, tests 1,2 and 7 are considered the three most useful.

### 1.1 Descriptions of Tests

**Test 1 - 3 sigma rule** Identifies points outside of the control limits  
Test 1 identifies points that are more standard deviations from the center line. Test 1 is universally recognized as necessary for detecting out-of-control situations. It has a false alarm rate of only 0.27%.

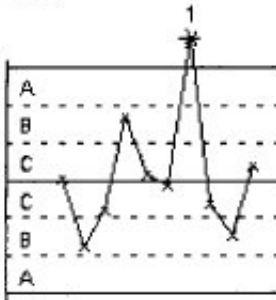
**Test 2** Identifies shifts in the means

Test 2 signals when 9 points in a row fall on the same side of the center line. The use of Test 2 significantly increases the sensitivity of the chart to detect small shifts in the mean.

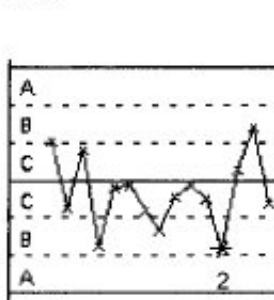
When test 1 and test 2 are used together, significantly fewer subgroups are needed to detect a small shift in the mean than are needed when test 1 is used alone. Therefore, adding test 2 helps to detect common out-of-control situations and increases sensitivity enough to warrant a slight increase in the false alarm rate.

**Test 1**

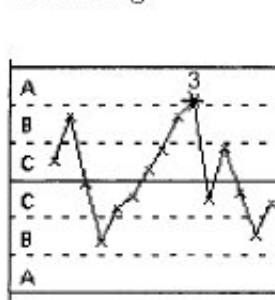
One point more than 3 sigmas from center line

**Test 2**

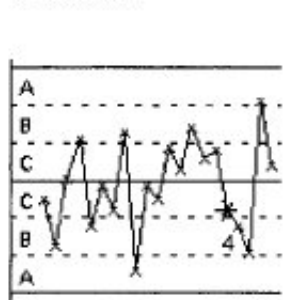
Nine points in a row on same side of center line

**Test 3**

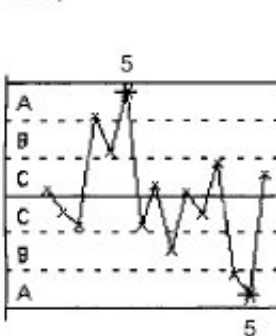
Six points in a row, all increasing or all decreasing

**Test 4**

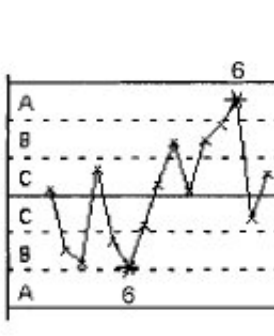
Fourteen points in a row, alternating up and down

**Test 5**

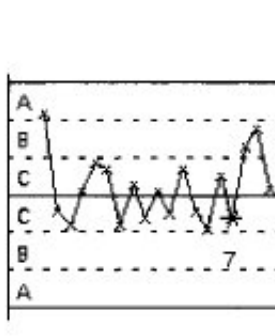
Two out of three points in a row more than 2 sigmas from center line (same side)

**Test 6**

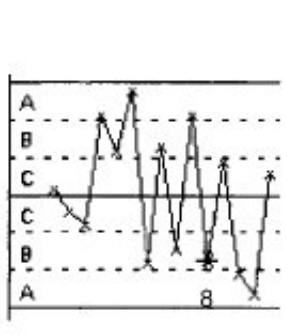
Four out of five points in a row more than 1 sigma from center line (same side)

**Test 7**

Fifteen points in a row within 1 sigma of center line (either side)

**Test 8**

Eight points in a row more than 1 sigma from center line (either side)



**Test 3**  $k$  points in a row, all increasing or all decreasing

Test 3 is designed to detect drifts in the process mean.

However, when test 3 is used in addition to test 1 and test 2, it does not significantly increase the sensitivity of the chart to detect drifts in the process mean.

**Test 4**  $k$  points in a row, alternating up and down

Although this pattern can occur in practice, it is recommended to search for any unusual trends or patterns rather than test for one specific pattern.

**Test 5**  $k$  out of  $k+1$  points  $> 2$  standard deviations from center line

This test is not quite as informative because it did not uniquely identify special cause situations that are common in practice.

**Test 6**  $k$  out of  $k+1$  points  $> 1$  standard deviation from the center line

This test is not quite as informative because it did not uniquely identify special cause situations that are common in practice.

**Test 7** Identifies control limits that are too wide

Test 7 signals when 12 or 15 points in a row fall within 1 standard deviation of the center line.

Test 7 is used only for the  $\bar{X}$  chart when the control limits are estimated from the data. When this test fails, the cause is usually a systemic source of variation (stratification) within a subgroup, which is often the result of not forming rational subgroups.

**Test 8**  $k$  points in a row  $> 1$  standard deviation from center line (either side)

This test is not quite as informative because it did not uniquely identify special cause situations that are common in practice.